



Dynamique des plages sableuses soumises à l'action des vagues, de la marée et des rechargements artificiels

David MORELLATO

18 décembre 2008

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

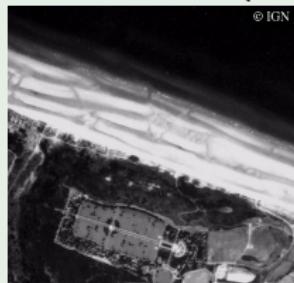
Examples of bar systems

3D Sandbars

Truc Vert beach (FR)



Omaha beach (FR)



Longshore Sandbars

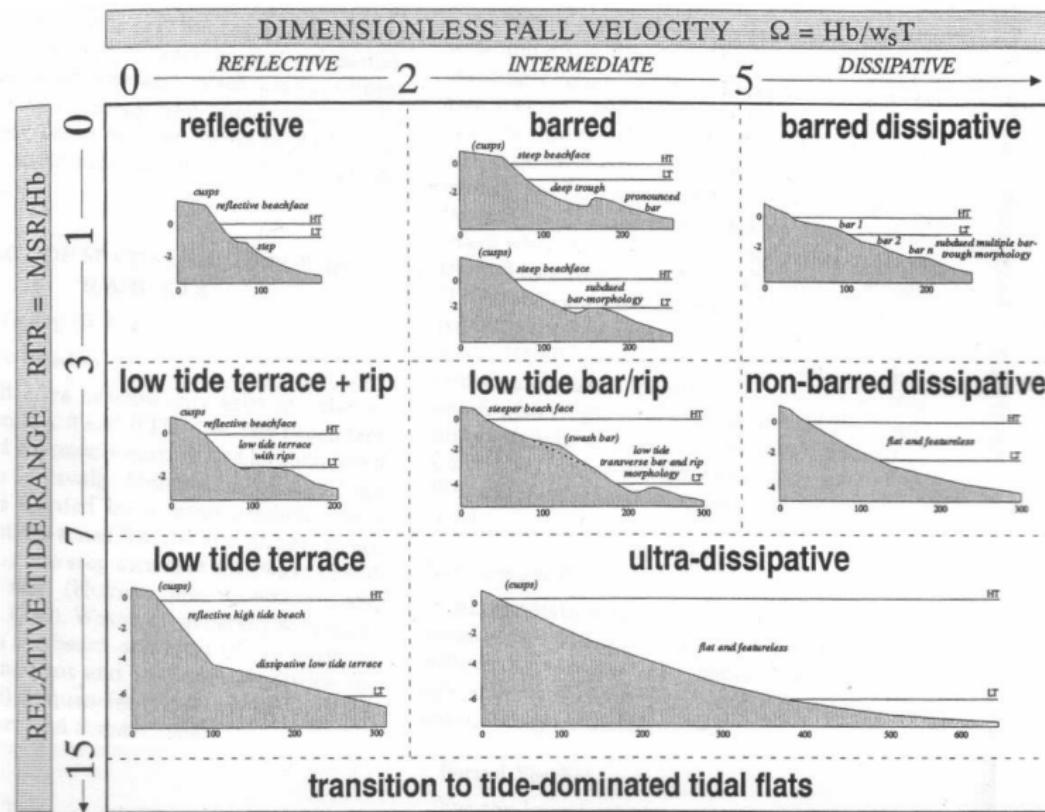
Wessex Coast (UK)



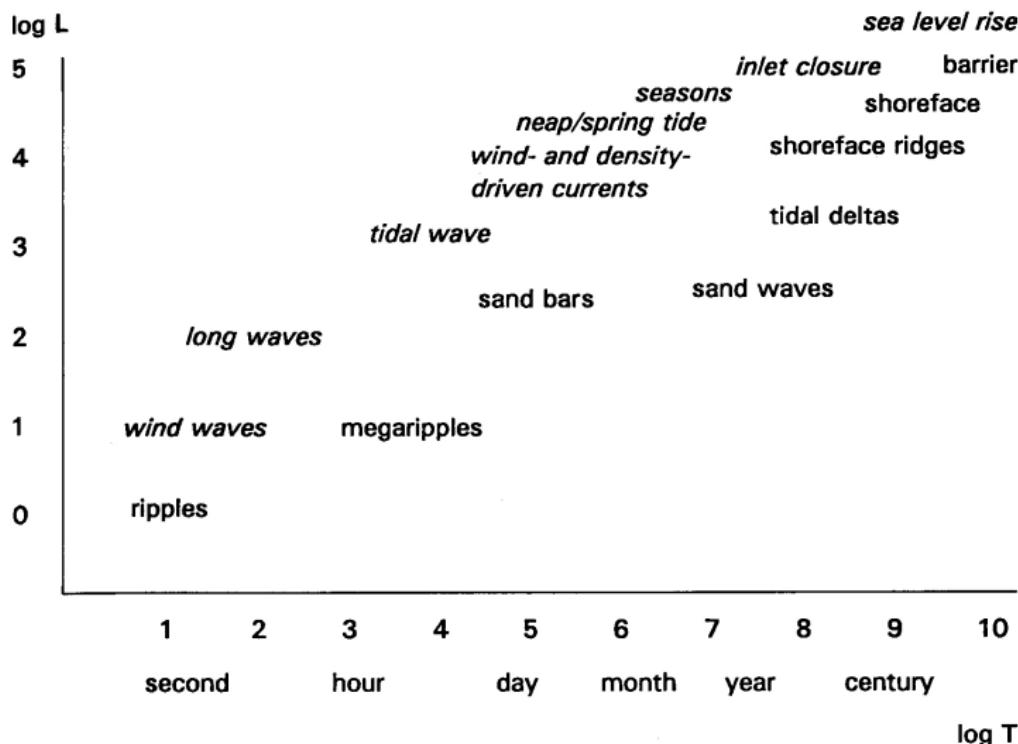
Egmond aan Zee (NL)



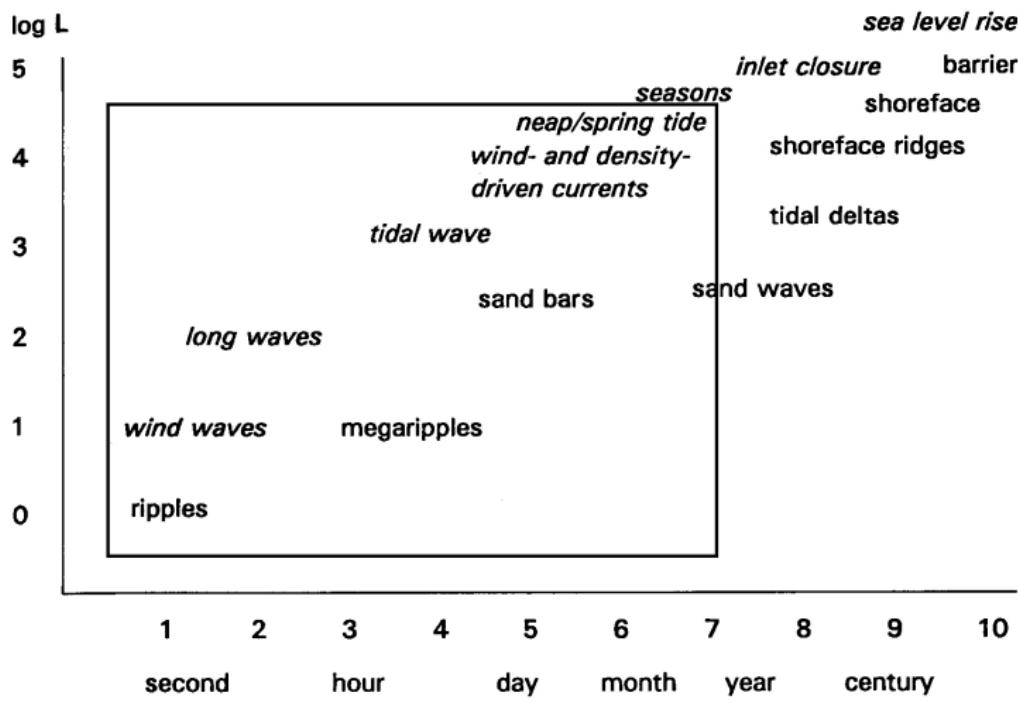
Masselink and Short (1993) conceptual beach model



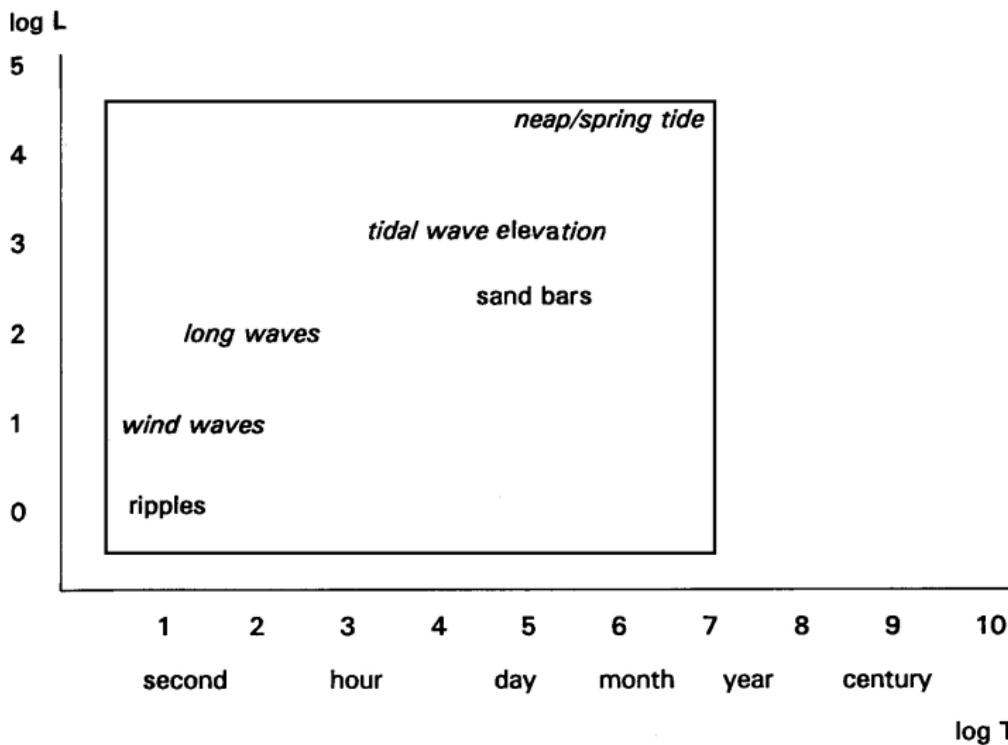
Time and space scales of the inner-shelf morphodynamic system



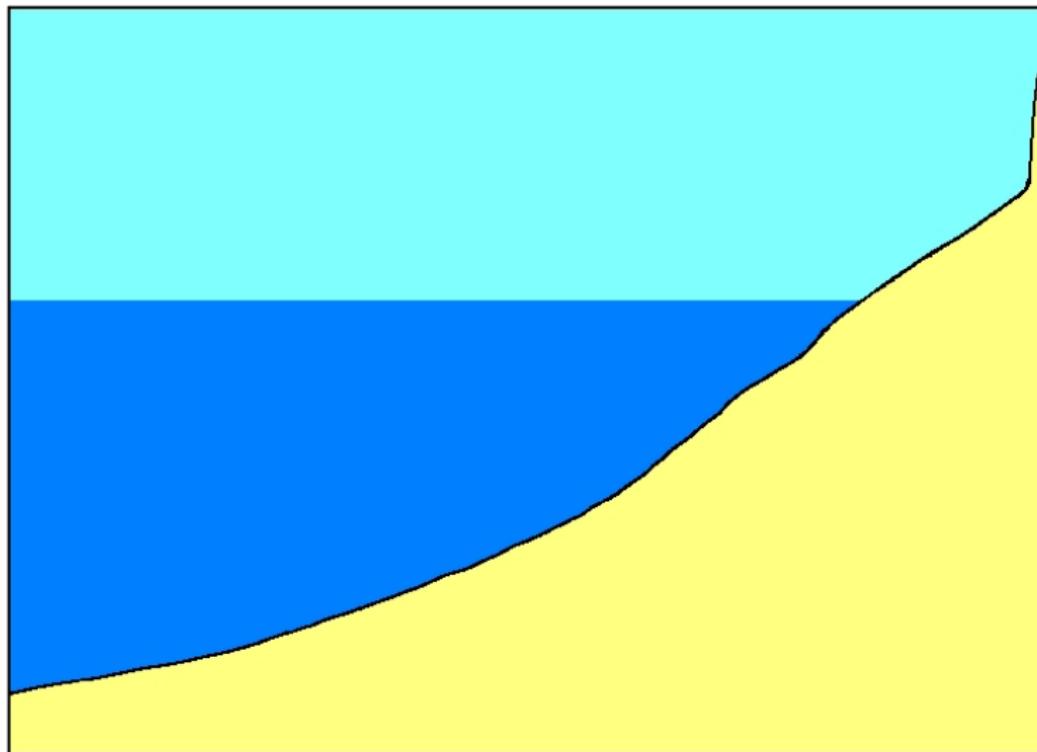
Time and space scales of the inner-shelf morphodynamic system



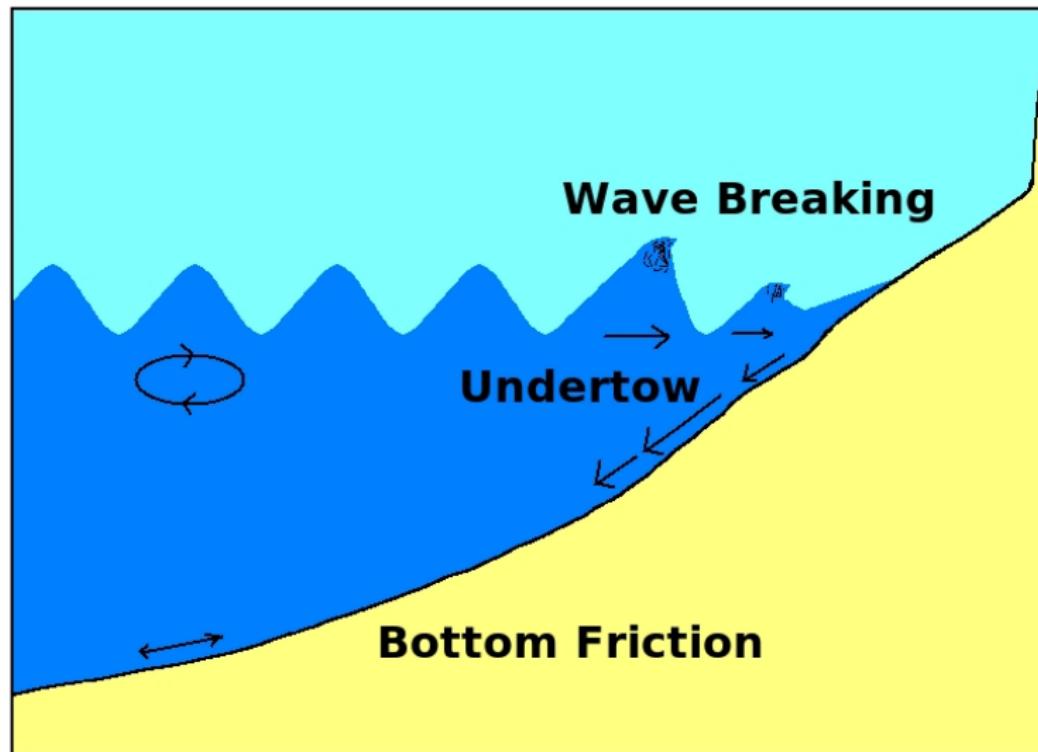
Time and space scales of the inner-shelf morphodynamic system



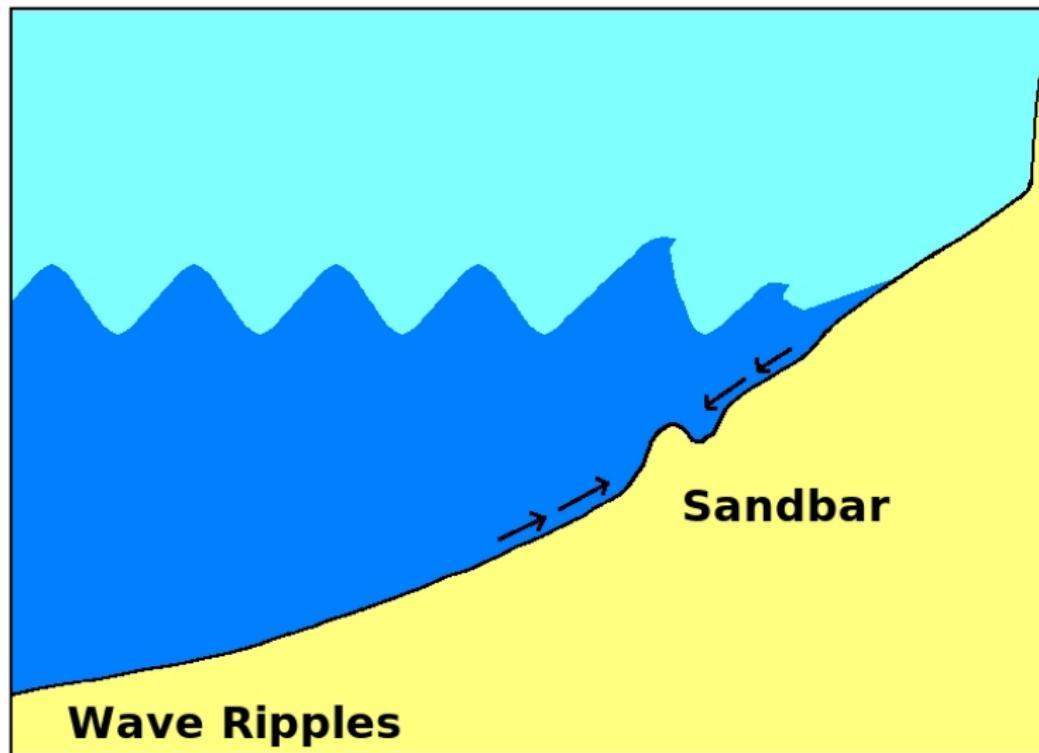
Cross-shore processes on sandy beaches



Cross-shore processes on sandy beaches



Cross-shore processes on sandy beaches



Topic : dynamic of sandy beaches under waves, tide and artificial nourishments

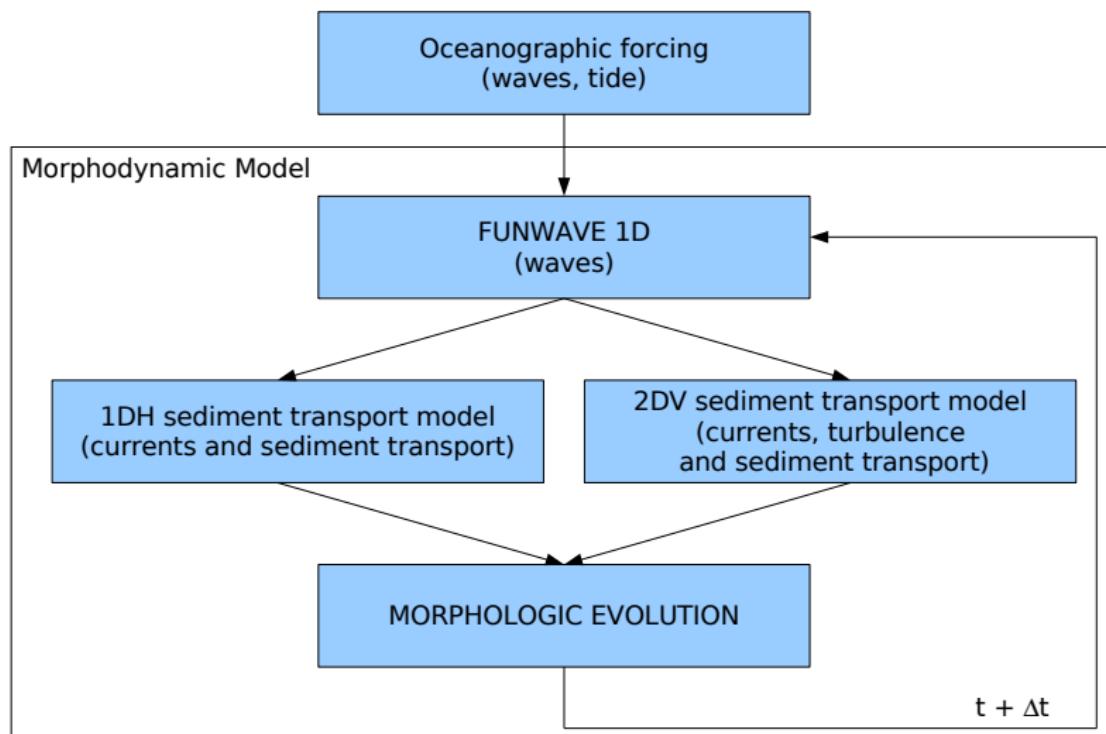
Questions

- How to model cross-shore processes ?
- What is the fastest-most accurate way to model beach evolutions ?
- What are the effects of waves and tide on beach morphology ?
- What is the best way to nourish a beach ?

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Morphodynamic model



Wave model

Wave model FUNWAVE (Kirby *et al.*, 1998)

Based on Wei *et al.* (1995)'s equations :

$$\eta_t + M_x = 0$$

$$u_{\alpha t} + u_{\alpha} u_{\alpha x} + g \eta_x + V = 0$$

$$\begin{aligned} M &= (h + \eta) \left[u_{\alpha} + \left(z_{\alpha} + \frac{1}{2} (h - \eta) \right) (h u_{\alpha})_{xx} \right. \\ &\quad \left. + \left(\frac{1}{2} z_{\alpha}^2 - \frac{1}{6} (h^2 - h\eta + \eta^2) \right) u_{\alpha xx} \right] \end{aligned}$$

$$\begin{aligned} V &= z_{\alpha} \left\{ \frac{1}{2} z_{\alpha} u_{\alpha txx} + (h u_{\alpha t})_{xx} \right\} + \left\{ \frac{1}{2} (z_{\alpha}^2 - \eta^2) u_{\alpha} u_{\alpha xx} + \frac{1}{2} [(h u_{\alpha})_x + \eta u_{\alpha x}]^2 \right\}_x \\ &\quad + \left\{ (z_{\alpha} - \eta) u_{\alpha} (h u_{\alpha})_{xx} - \eta \left[\frac{1}{2} \eta u_{\alpha t x} + (h u_{\alpha t})_x \right] \right\}_x \end{aligned}$$

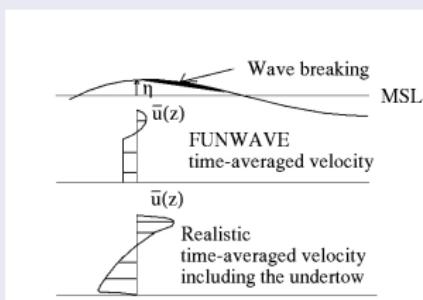
with η the free surface, h the water depth and u_{α} the horizontal velocity at $z_{\alpha} = 0.531h$

$$u_{\text{FUNWAVE}}(z) = u_{\alpha} + \frac{z_{\alpha}^2 - z^2}{2} u_{\alpha xx} + (z_{\alpha} - z) (h u_{\alpha})_{xx}$$

Wave model

Wave processes and FUNWAVE (Kirby *et al.*, 1998)

- **Bottom friction** $F_b = \frac{Kg}{h+\eta} u_\alpha |u_\alpha|$ including **wave-ripples** predictors of Nielsen (1992),
- **Streaming** neglected,
- **Wave breaking** from Kennedy *et al.* (2000) : eddy viscosity of Zelt (1991) and realistic description of the initiation/cessation of wave breaking of Schäffer *et al.* (1993) on free surface slope,
- **Undertow** not well reproduced in $u_{\text{FUNWAVE}}(z)$. Needs a correction :
 - 1st option : Post-treatment of Lynett (2006)
 - 2nd option : Turbulence closure vertical model



1DH sediment transport model

Bailard's total transport formula (1981) : bedload and suspension

$$q_{1DH}(x) = q_{c0}(x) + q_{c\beta}(x) \quad + \quad q_{s0}(x) + q_{s\beta}(x)$$

$$q_{c0}(x) = \frac{C_f \varepsilon_c}{2g(s-1)\tan\phi} \overline{|u(x, -h, t)|^2 u(x, -h, t)}$$

$$q_{c\beta}(x) = -\frac{C_f \varepsilon_c}{2g(s-1)\tan^2\phi} \overline{|u(x, -h, t)|^3} \beta(x)$$

$$q_{s0}(x) = \frac{C_f \varepsilon_s}{2g(s-1)w_f} \overline{|u(x, -h, t)|^3}$$

$$q_{s\beta}(x) = -\frac{C_f \varepsilon_s^2}{2g(s-1)w_f^2} \overline{|u(x, -h, t)|^5} \beta(x)$$

Lynett's model (2006)

$$u_{LYNETT}(z) = u_{FUNWAVE}(z) + u_B(z)$$

with

$$u_B(z) = \delta_{\text{breaking switch}} (C_{\text{roller}} - u_{\text{FUNWAVE}}(\eta)) \frac{\exp(k(z-\eta)) - \exp(k(z_B-\eta))}{1 - \exp(k(z_B-\eta))}$$

$$\delta_{\text{breaking switch}} = 0 \text{ ou } 1$$

2DV sediment transport model

Turbulence closure vertical model

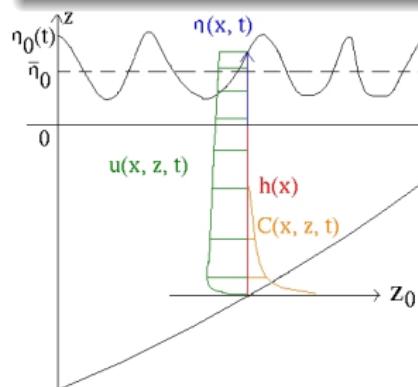
$$\frac{\partial \mathbf{u}}{\partial t} - \frac{\sigma}{H} \frac{\partial \eta}{\partial t} \frac{\partial \mathbf{u}}{\partial \sigma} = \frac{\partial \bar{\mathbf{u}}_0}{\partial t} + \frac{\partial}{\partial \sigma} \left(\nu_t \frac{\partial \mathbf{u}}{\partial \sigma} \right) \frac{1}{H^2} - \frac{1}{\rho_w} \frac{\partial \bar{\tau}_{zx}}{\partial z}$$

$$\frac{\partial k}{\partial t} - \frac{\sigma}{H} \frac{\partial \eta}{\partial t} \frac{\partial k}{\partial \sigma} = \frac{1}{H^2} \frac{\partial}{\partial \sigma} \left(\frac{\nu_t}{\sigma_k} \frac{\partial k}{\partial \sigma} \right) + \frac{\nu_t}{H^2} \left(\frac{\partial \mathbf{u}}{\partial \sigma} \right)^2 - C_\nu \frac{k^{3/2}}{l} \text{ with } \nu_t = l \sqrt{k}$$

$$\frac{\partial C}{\partial t} - \frac{\sigma}{H} \frac{\partial \eta}{\partial t} \frac{\partial C}{\partial \sigma} = \frac{1}{H} \frac{\partial}{\partial \sigma} [(w_f - w_\sigma) C] + \frac{1}{H^2} \frac{\partial}{\partial \sigma} \left(\varepsilon_{sd} \frac{\partial C}{\partial \sigma} \right) \text{ with } \varepsilon_{sd} = \nu_t$$

$$q_{2DV}(x) = \bar{q}_{su}(x) + \bar{q}_{sw}(x) + \bar{q}_{sl}(x) + \bar{q}_c(x)$$

$$q_{2DV}(x) = \int_{z_0}^H C(z) \bar{u}(z) dz + \int_{z_0}^H C(z) u_w(z, t) dz + \int_{z_0}^H C(z) U_I(z) dz + q_{co} + q_{cb}$$



$$\sigma = 1 \quad u(1) = u_{\text{FUNWAVE}} + \delta_{\text{breaker}} \gamma \sqrt{(gH)}$$

$$\begin{aligned} H &= \eta + h - z_0 \\ z &= z_0 + H \sigma \end{aligned}$$

$$\sigma = 0 \quad u(0) = 0$$

$p(0) = wf$ Co for sheetflow (Zyserman and Fredsoe, 1984)
Nielsen's pick-up function (1992) for rippled bed

Morphologic evolution

Sediment conservation law

$$\frac{\partial h}{\partial t} = \frac{1}{1-\varepsilon} \frac{\partial q}{\partial x}$$

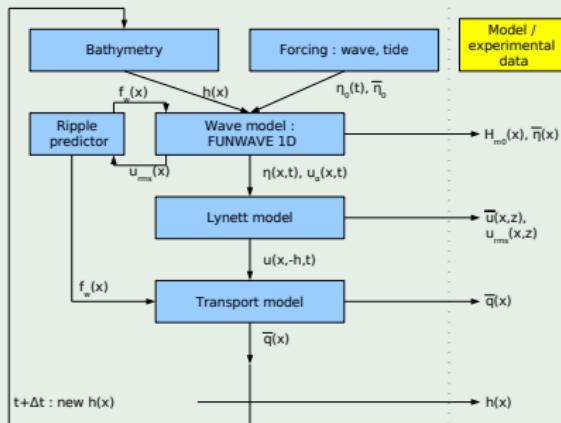
resolved with a modified-Lax scheme (idem Rakha *et al.*, 1997)

Tide effects

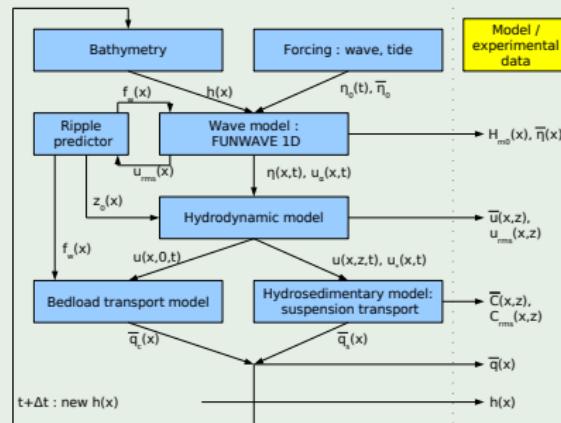
- Water level constant during a morphodynamic step Δt (typically 10 minutes)
- No tidal currents
- Tidal signal :
 - Sinusoidal ($T_{M2}=12H25mn$)
 - Spring-to-spring tidal cycle ($T_{M2}=12H25mn$, $T_{S2}=12H00mn$)
 - Experimental data

Two morphodynamic models

FUNBEACH 1DH



FUNBEACH 2DV



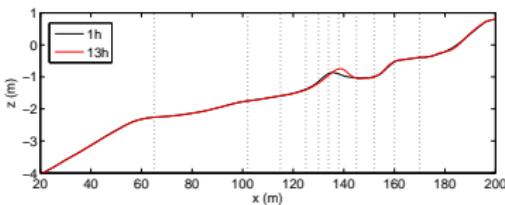
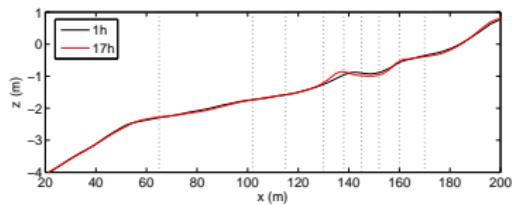
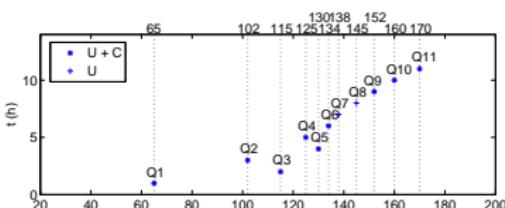
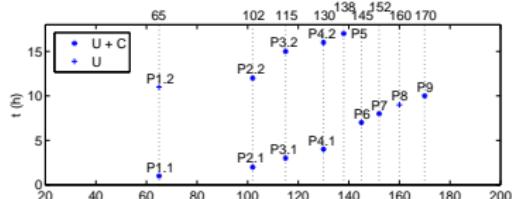
Validation

- Large wave tank experiments : Delta flume'93
- Field measurements : Pentrez beach

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Delta Flume'93 data description



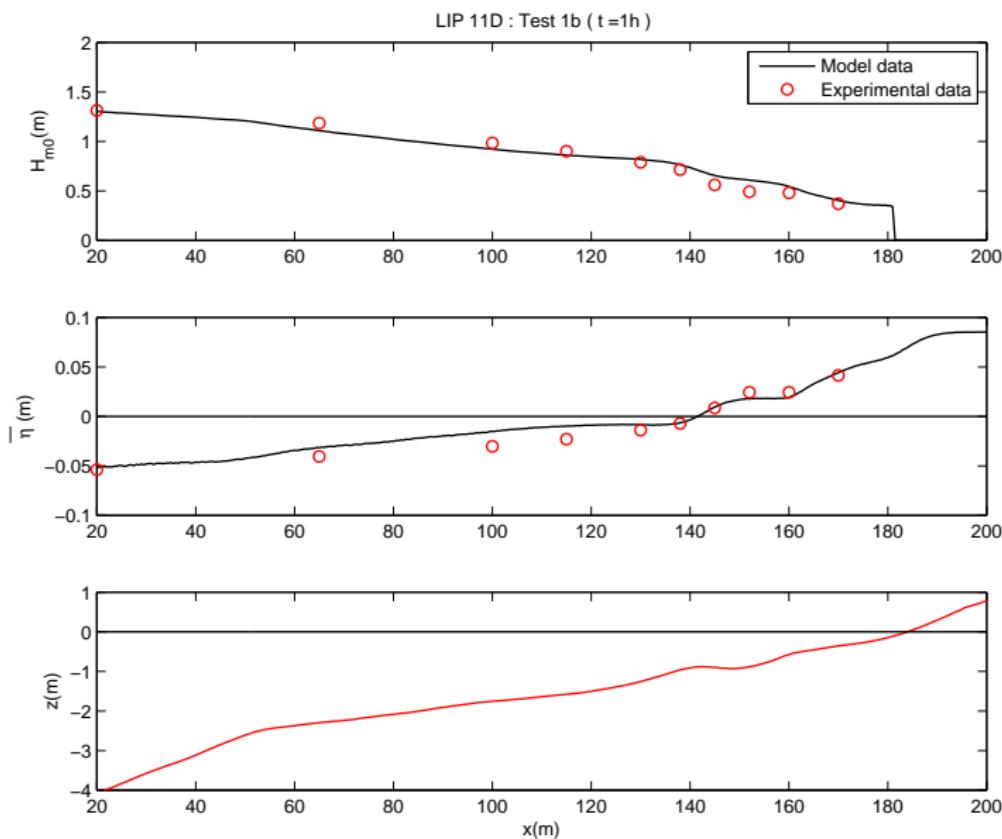
Test 1b

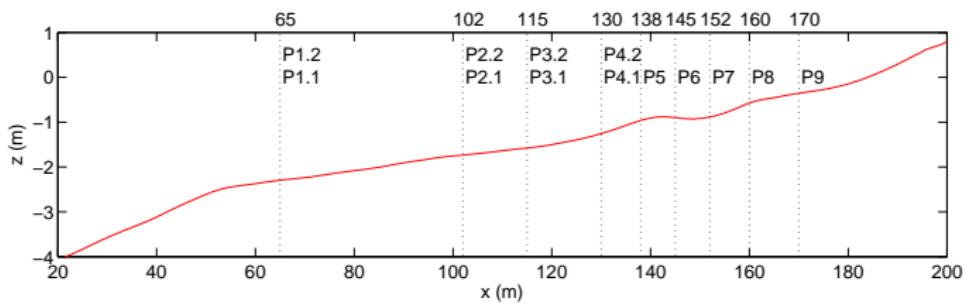
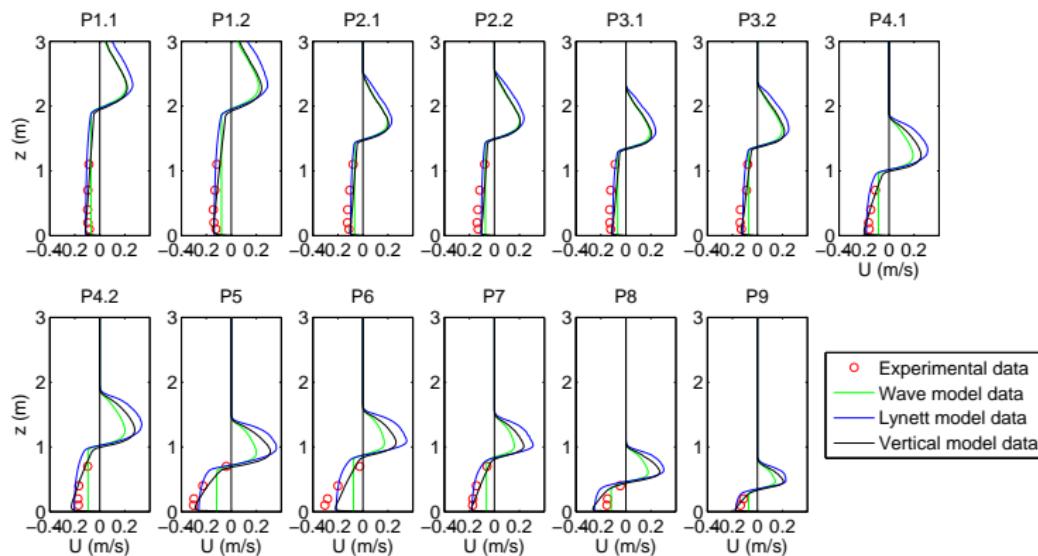
- $H_{m_0} \simeq 1.40$ m, $T_p \simeq 5$ s
- Duration : 17 H
- Offshore bar migration

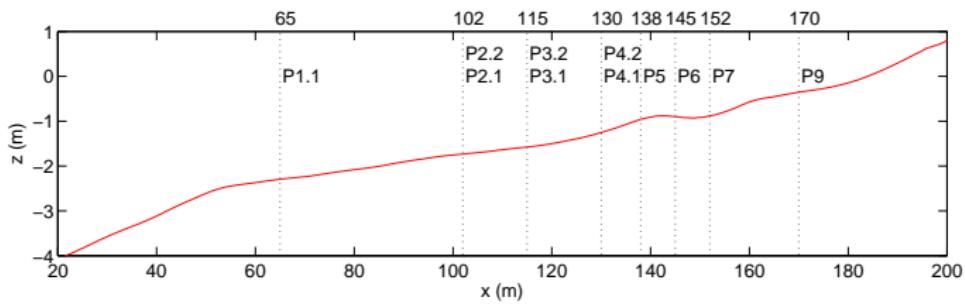
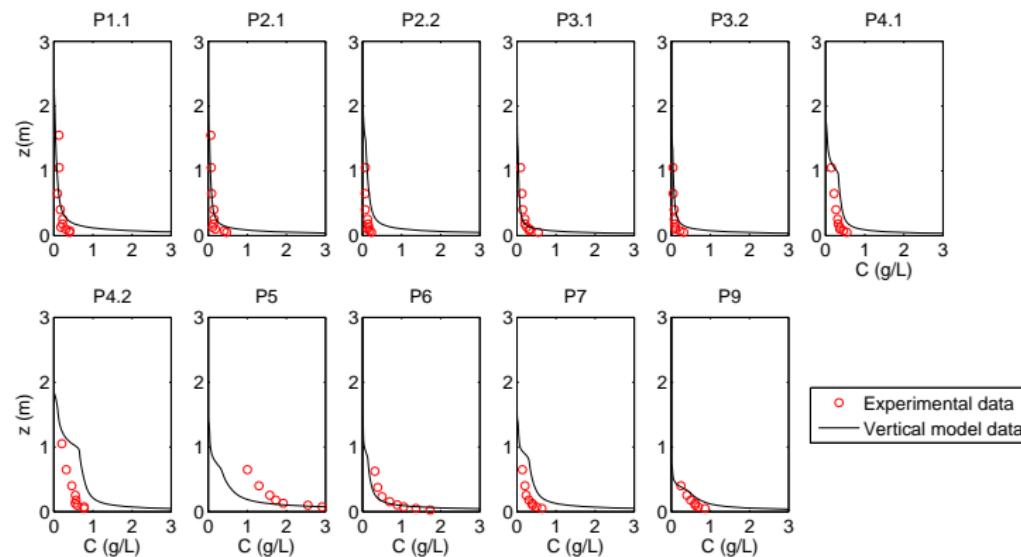
Test 1c

- $H_{m_0} \simeq 0.60$ m, $T_p \simeq 8$ s
- Duration : 13 H
- Onshore bar migration

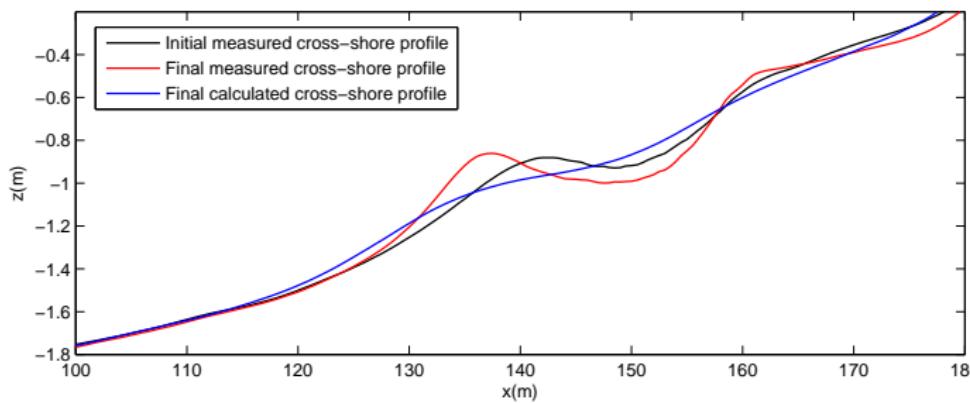
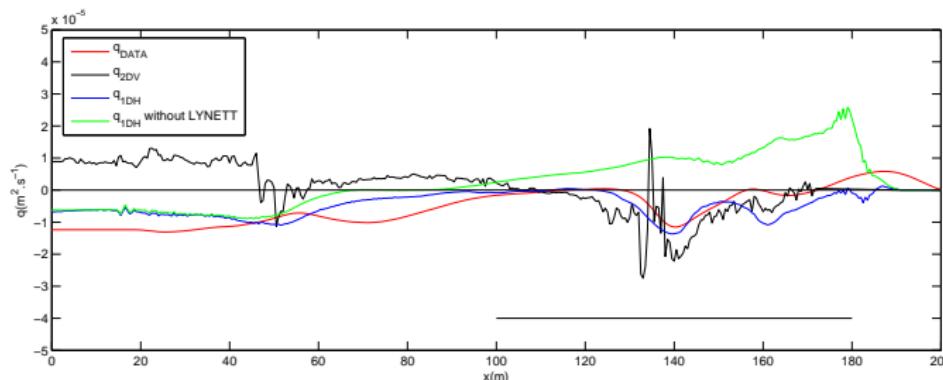
Test 1b : H_{m_0} and $\bar{\eta}$



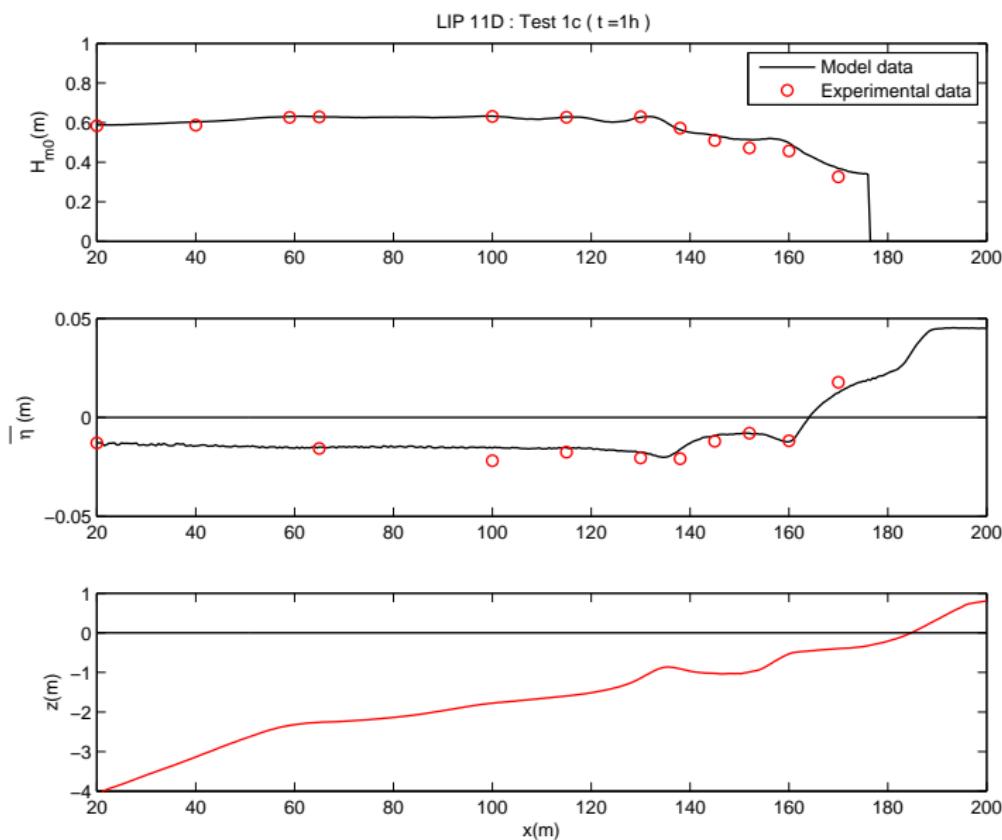
Test 1b : \overline{U} 

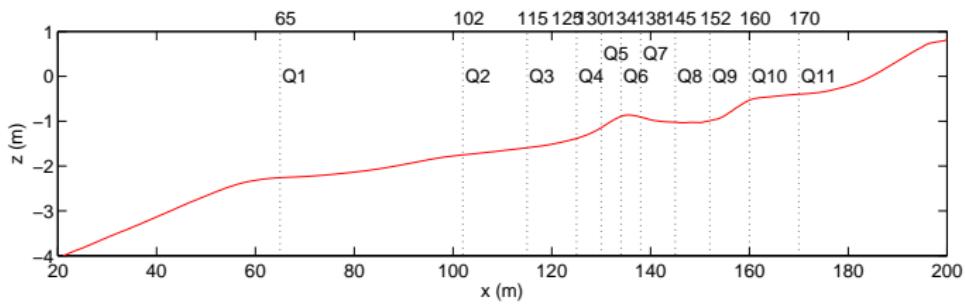
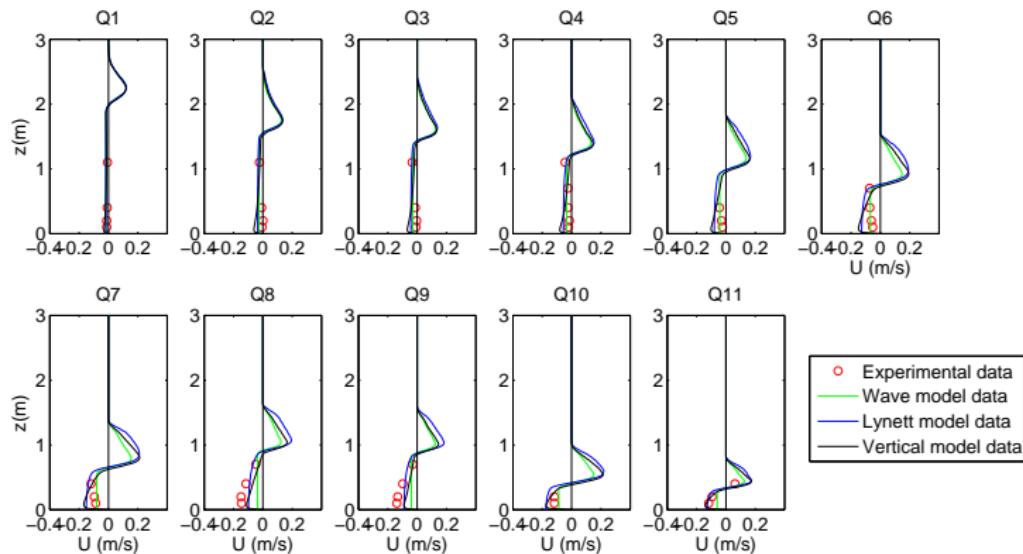
Test 1b : \bar{C} 

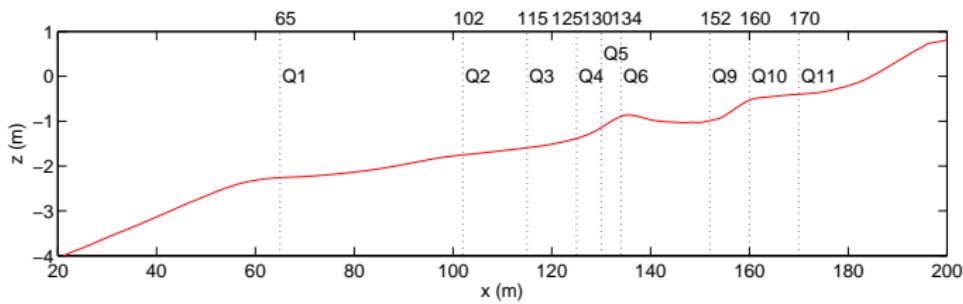
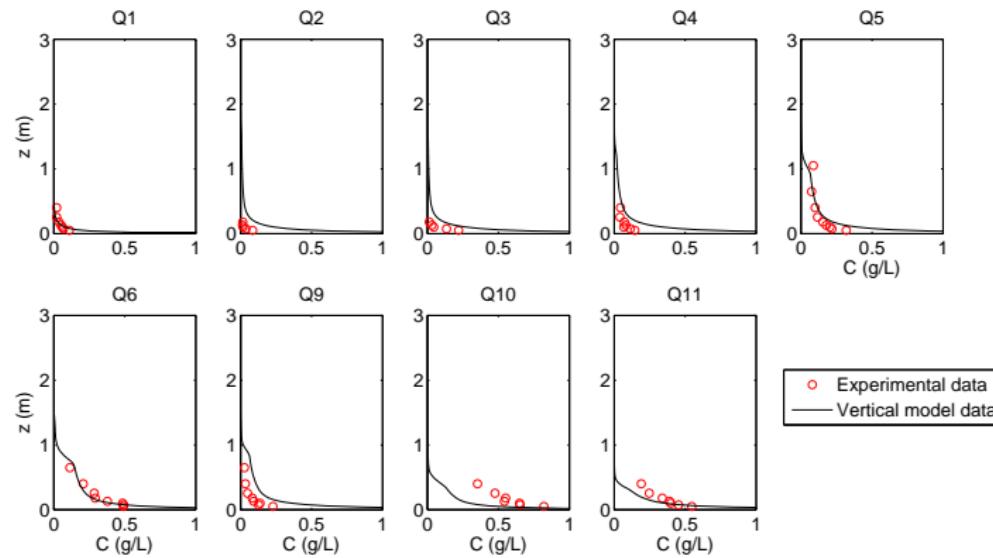
Test 1b : transport rates (first time step) and cross-shore profile evolution



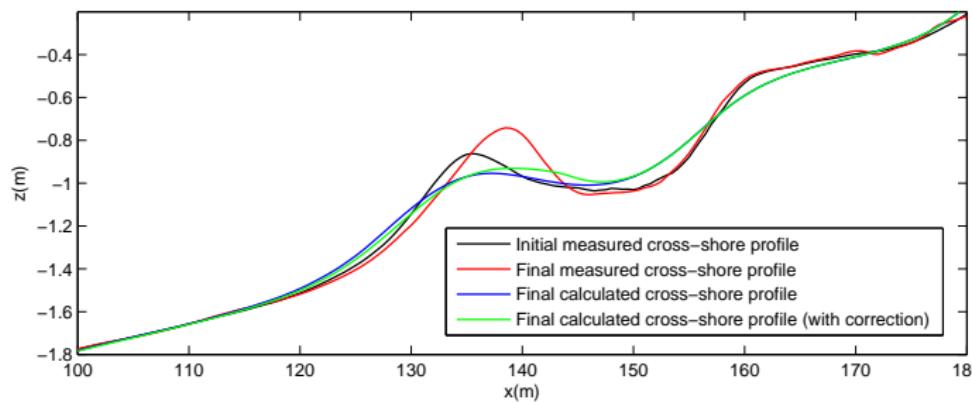
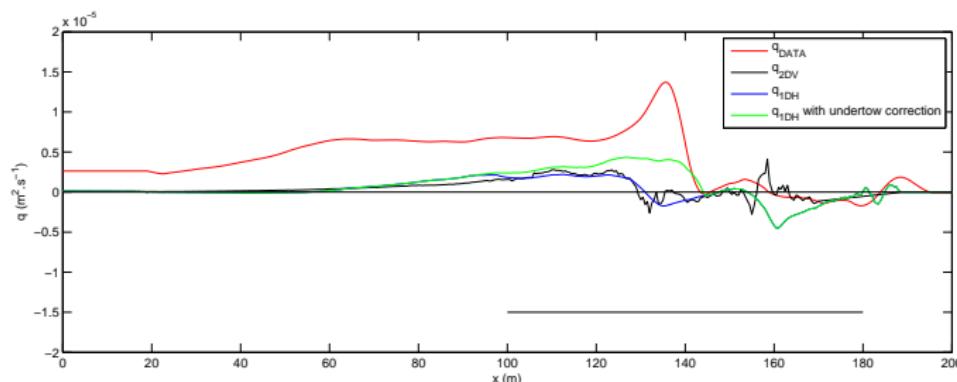
Test 1c : H_{m_0} and $\bar{\eta}$



Test 1c : \overline{U} 

Test 1c : \bar{C} 

Test 1c : transport rates (first time step) and cross-shore profile evolution



To conclude with Delta Flume experiments :

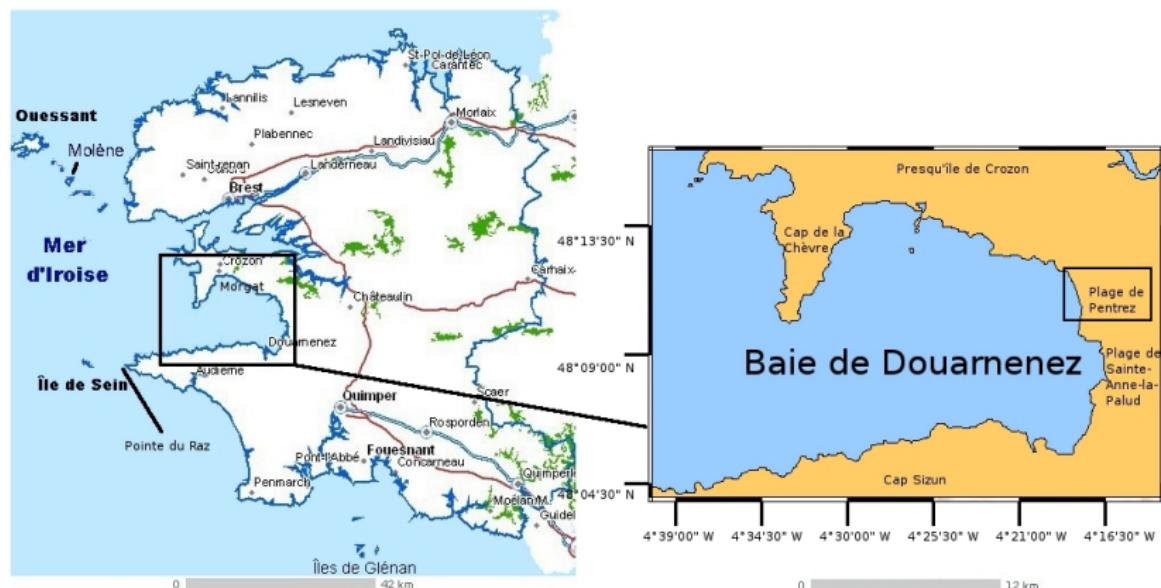
Synthesis

- Good estimation of wave heights, water level, mean velocities and mean concentrations of sediment by FUNBEACH,
- Good estimation of bar movement for test 1b,
- Poor estimation of bar evolutions for test 1c which highlights the interest of estimating correctly the bottom velocities (undertow) to get better morphologic predictions,
- Due to long computational time and numerical instabilities for FUNBEACH 2DV, establishing of a method of computation :
 - Calibration of the 2DV transport model on velocity and concentrations experimental data,
 - Calibration of the 1DH transport model on the 2DV transport model in terms of transport rates,
 - Morphologic evolution calculated with FUNBEACH 1DH.

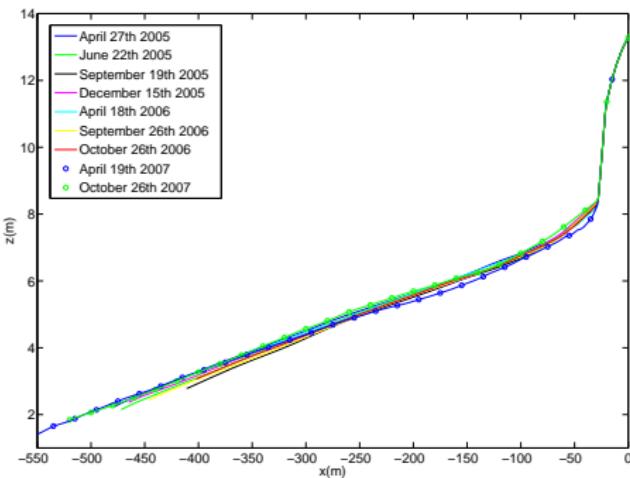
Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Pentrez beach in the bay of Douarnenez

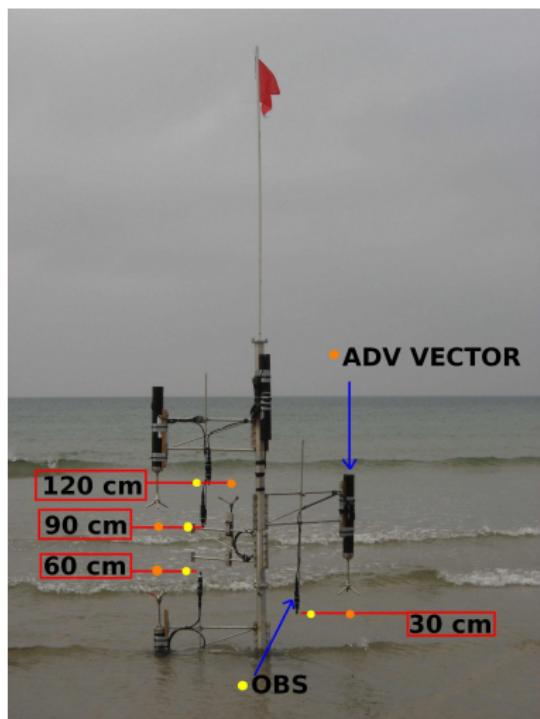


Pentrez beach and topographic survey



- Macrotidal beach ($TR > 4\text{m}$) with weak tidal currents,
- Cross-shore configuration (longshore currents neglected),
- Swell with spilling breakers,
- Weak morphologic evolution (maximum of 40 cm in the intertidal zone during 30 months).

MII : « Mât Instrumenté en zone Intertidale »



- 3 or 4 Acoustic Doppler Velocimeters VECTOR,
- 3 or 4 OBS turbidimeters.

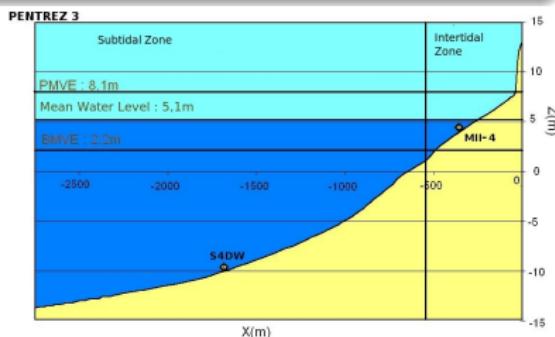
at 30, 60, 90 (and 120 cm)
over the bottom.

in addition to an offshore
($z=-10m$) wave sensor.

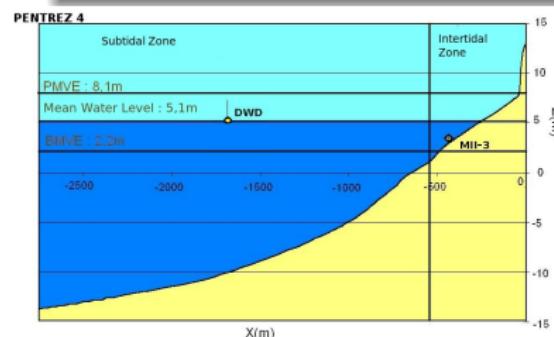
Pentrez beach Campains

Campains	offshore sensor	intertidal sensors	Tidal coefficients
PENTREZ#1	Wave rider	S4DW velocimeter	42 to 62
PENTREZ#2	Wave rider	2 ADV VECTOR	86 to 105
PENTREZ#3	S4DW	MII#4	56 to 74
PENTREZ#4	Wave rider	MII#3	62 to 96

PENTREZ#3 :
18-20 october 2006



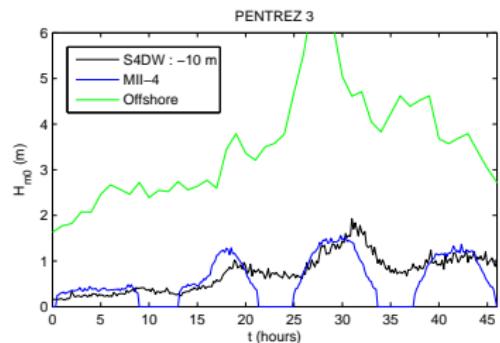
PENTREZ#4 :
14-16 april 2007



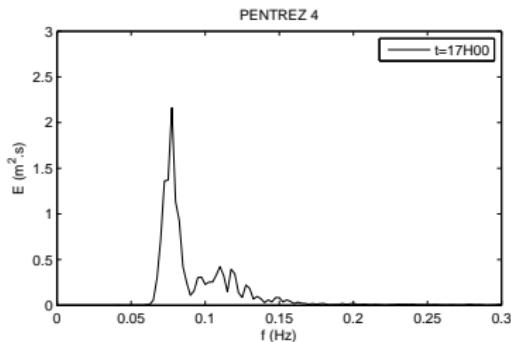
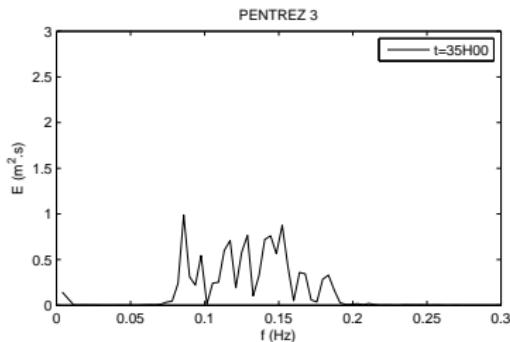
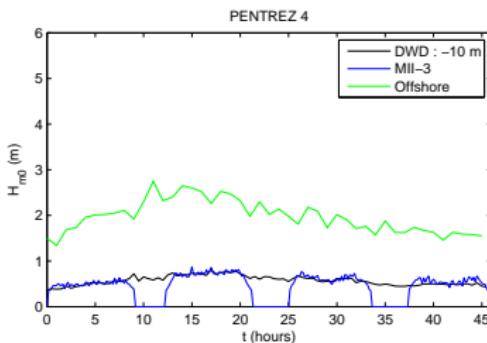
Continuous data acquisition during 46 hours.

Spectral wave heights and wave spectrum

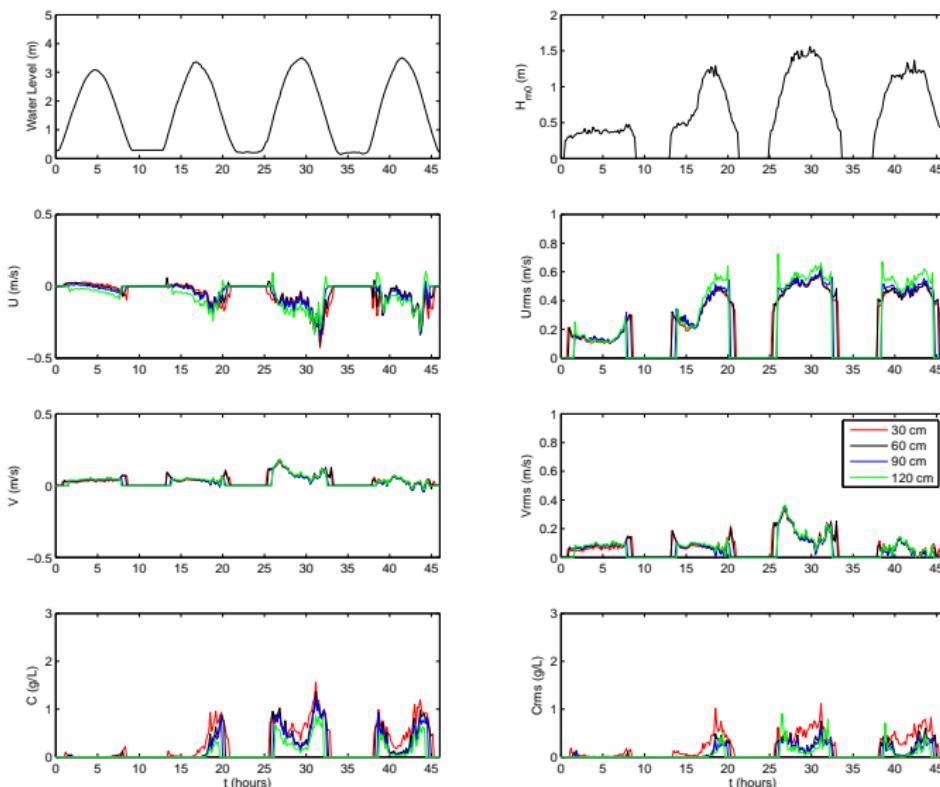
PENTREZ#3 : Wind Waves



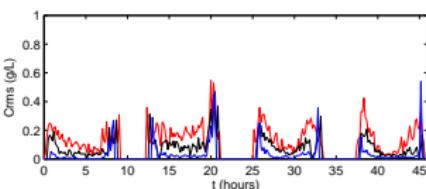
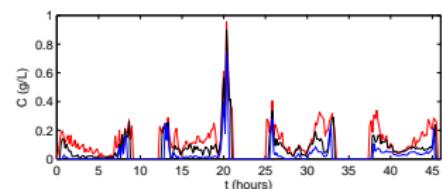
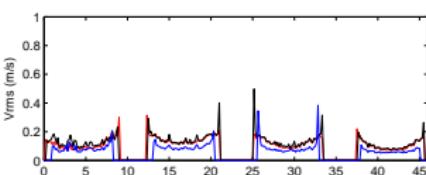
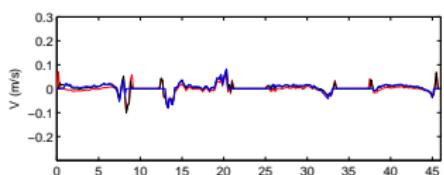
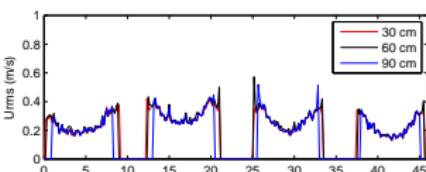
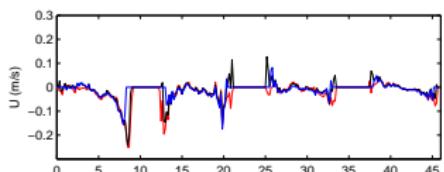
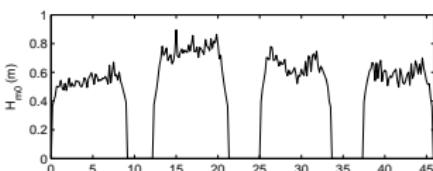
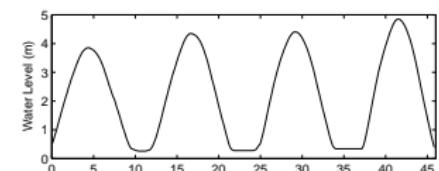
PENTREZ#4 : Swell



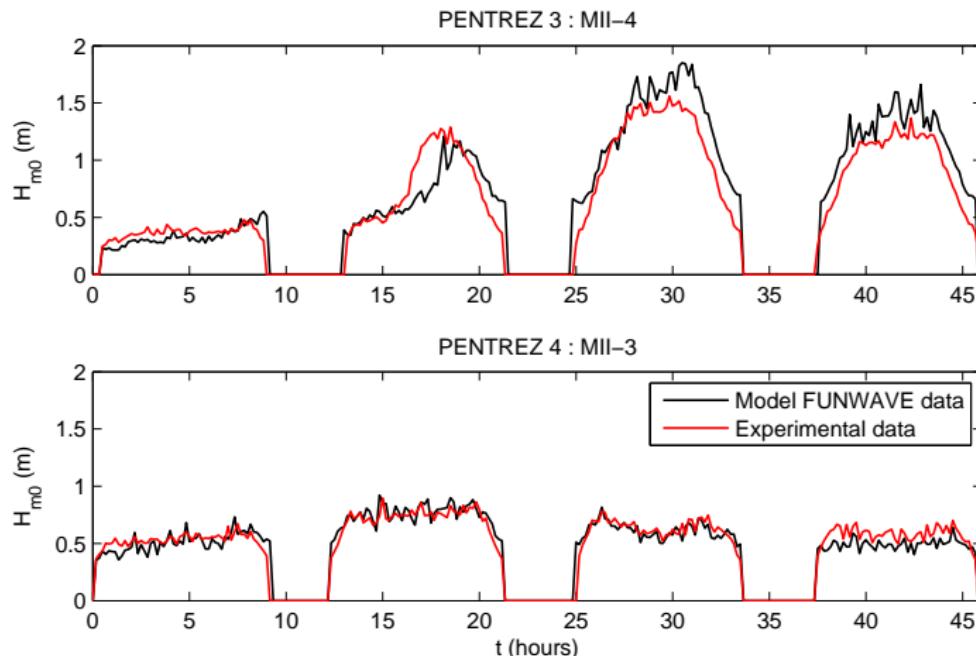
Experimental data analysis : PENTREZ#3



Experimental data analysis : PENTREZ#4

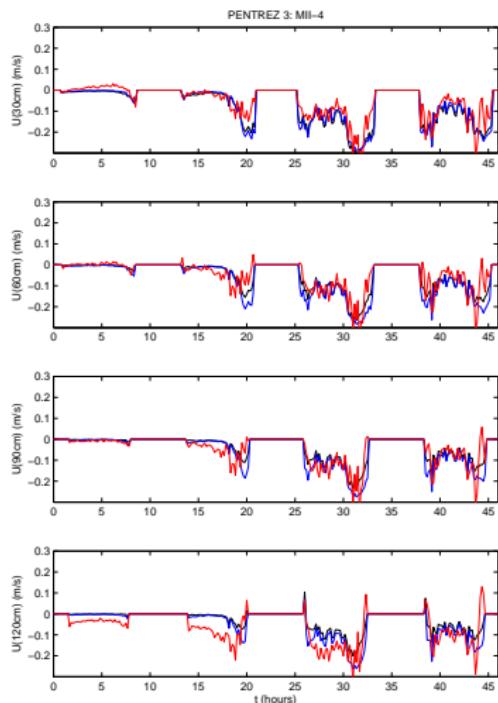


Experimental vs. FUNWAVE : wave heights

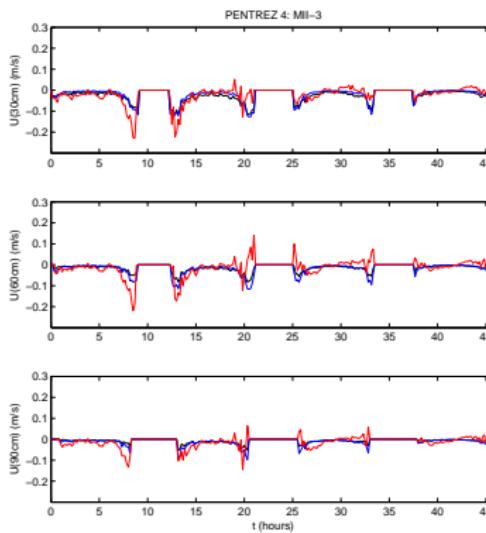


Experimental vs. models : mean velocities

PENTREZ#3



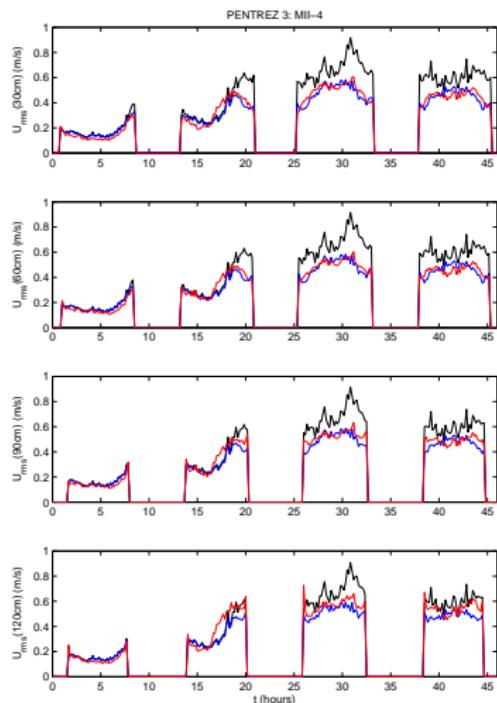
PENTREZ#4



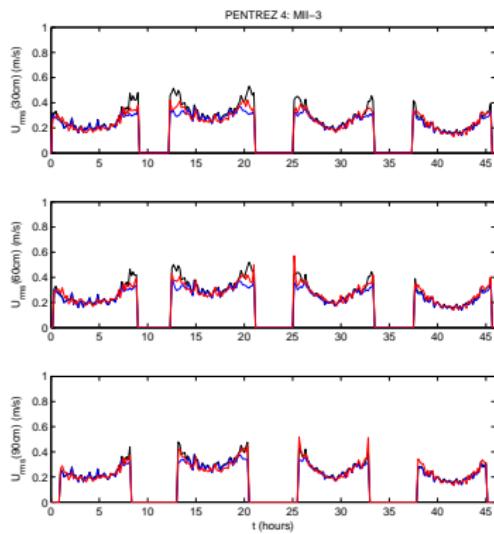
Vertical model data
Lynett model data
Tidal-corrected experimental data

Experimental vs. models : RMS velocities

PENTREZ#3



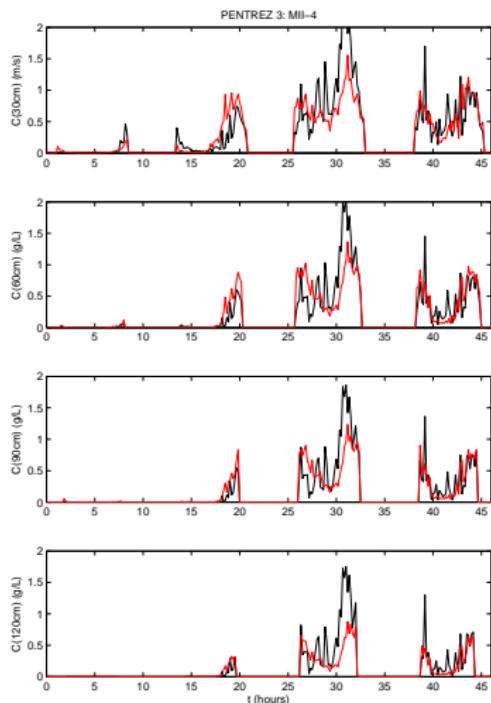
PENTREZ#4



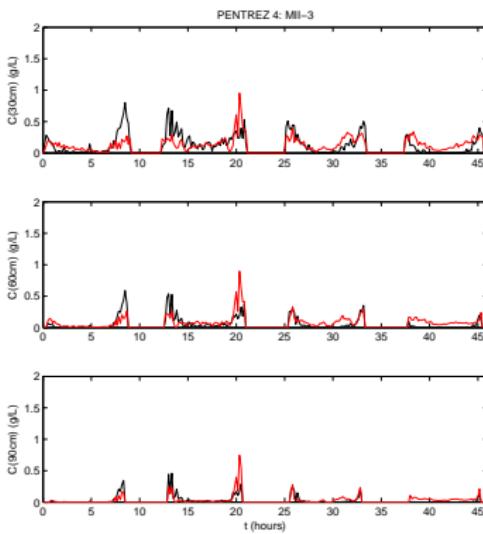
— Vertical Model data
— Lynett Model data
— Experimental data

Experimental vs. 2DV model : mean concentrations

PENTREZ#3



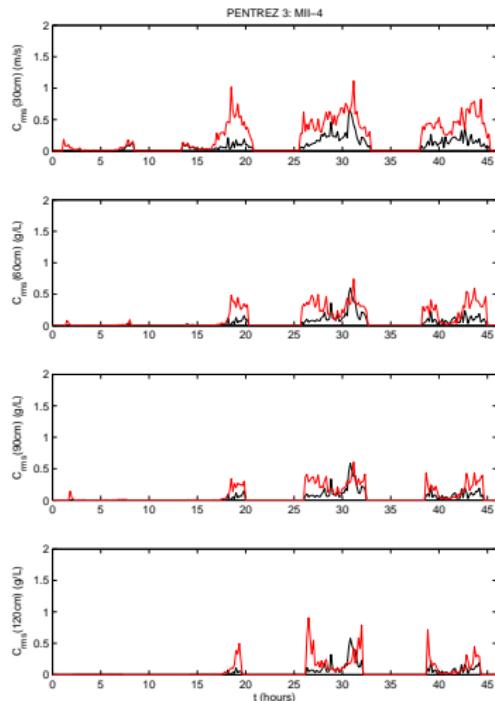
PENTREZ#4



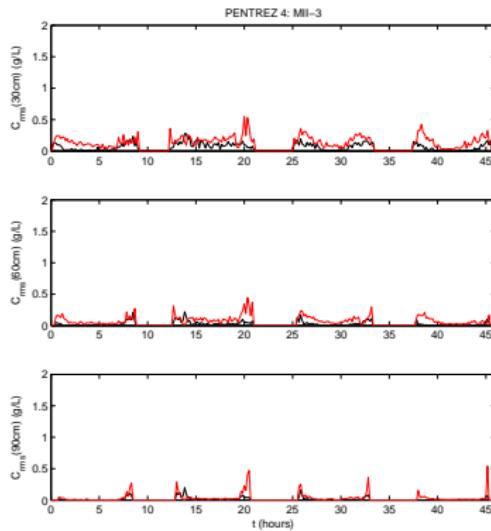
Vertical Model data
Experimental data

Experimental vs. 2DV model : RMS concentrations

PENTREZ#3

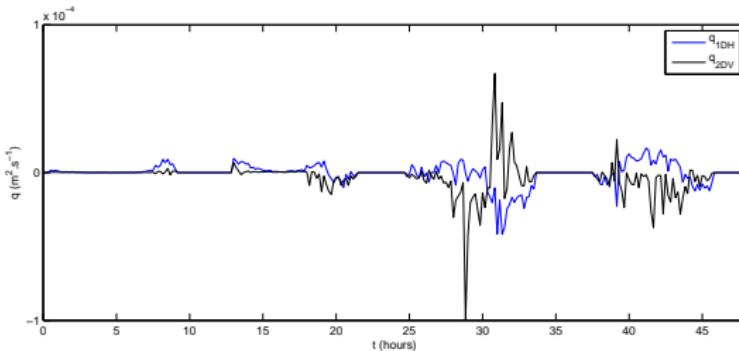


PENTREZ#4

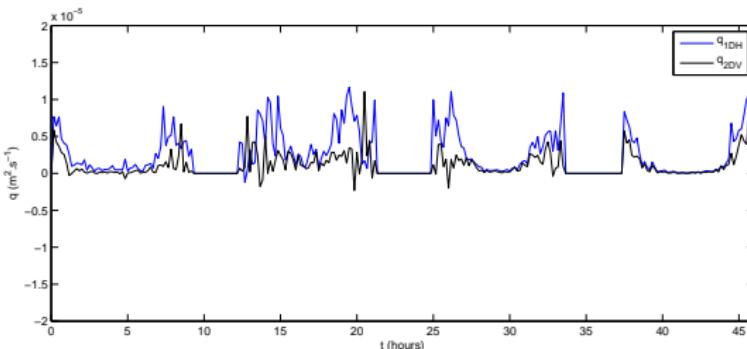


Predicted transport rates

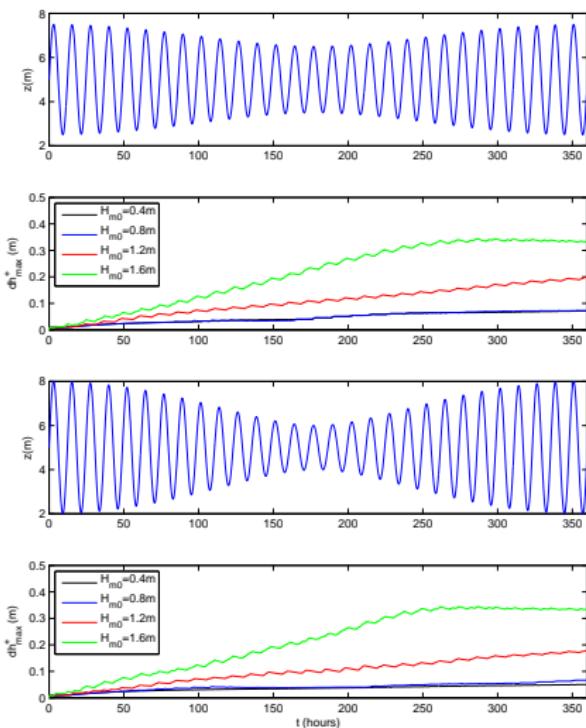
PENTREZ#3



PENTREZ#4



Predicted Spring-to-Spring morphologic evolution on Pentrez beach



To conclude with Pentrez beach measurements :

Synthesis

- Good estimation of wave heights by FUNWAVE 1D,
- Good estimation of mean and RMS velocities by FUNBEACH 2DV and FUNBEACH 1DH,
- Good estimation of mean concentration of sediment and worse estimation of RMS concentration of sediment by FUNBEACH 2DV,
- FUNBEACH 2DV predicted transport rates for wind waves in PENTREZ#3 worse than swell in PENTREZ#4,
- FUNBEACH 1DH cheaper in computer time and more stable than FUNBEACH 2DV.

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Numerical study

Objective

Effects of various parameters on beach morphodynamic with FUNBEACH 1DH :

- Wave height,
- Tide range,
- Wave spectrum,
- Beach slope,
- Grain size.

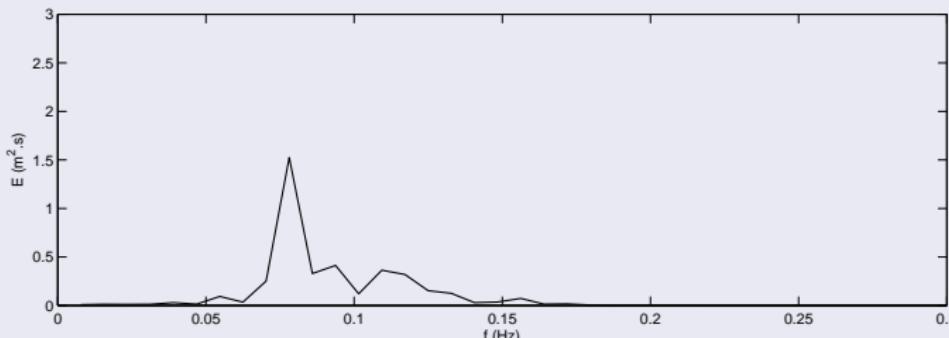
General conditions of test-cases

- Plane sloping beach,
- 14 tidal cycles of constant wave forcing,
- Constant tide range.

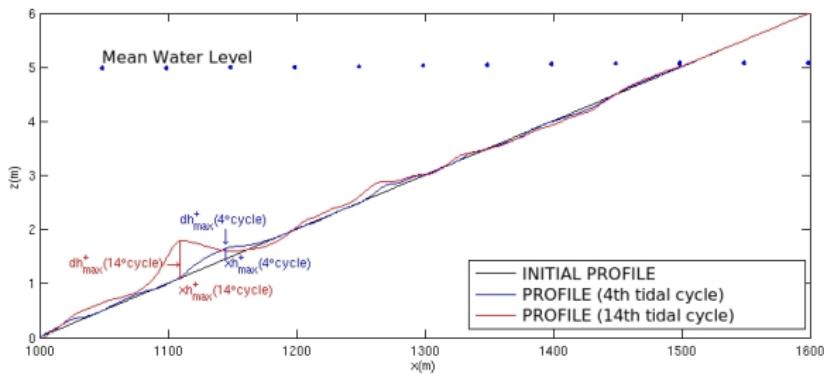
First test-case : Sensivity of bar formation to Wave Height and Tide Range

Conditions

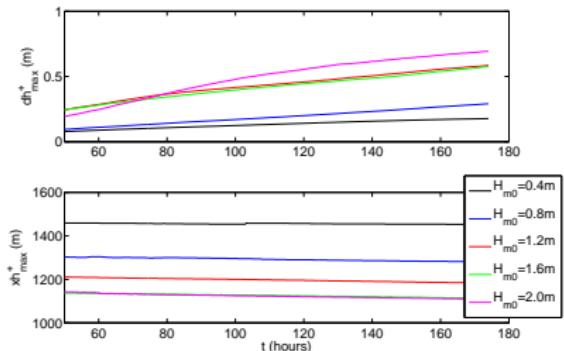
- Wave height : 0.4m, 0.8m, 1.2m, 1.6m and 2 m,
- Tide range : 0m, 1m, 2m, 3m, 4m, 5m and 6m,
- Beach slope : $\beta_p = 1\%$,
- Grain size : $d_{50} = 0.144\text{mm}$,
- Swell conditions : $T_p = 14.3\text{s}$,



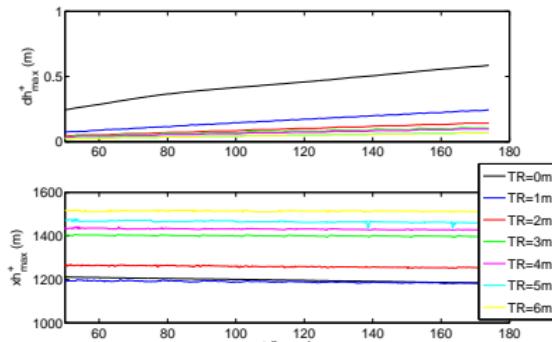
Bar evolution



H_{m_0} variable and TR=0m



$H_{m_0}=1.2m$ and TR variable

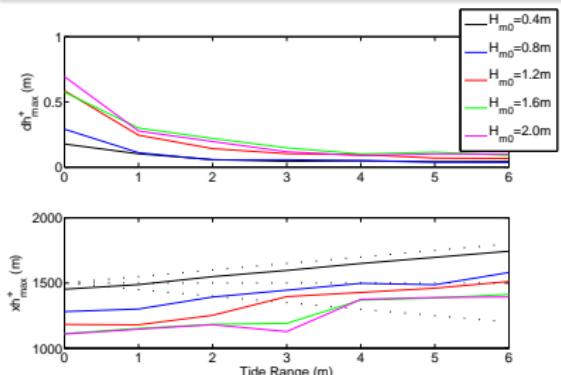


Morphologic evolution after 14 tidal cycles

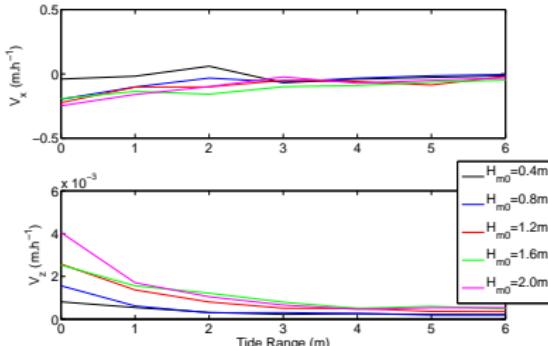
H_{m_0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	BS	BI	-	-	-	-	-
0.8m	BS	BS	-	-	-	-	-
1.2m	3BS	2BS	BS	BI	BI	-	-
1.6m	3BS	2BS	BS	BS	BI	BI	BI
2.0m	5BS	2BS	2BS	BS	BI	BI	BI

n BS : n Subtidal Bar; n BI : n Intertidal Bar; Bold Form : Big Bar.

Bar elevation and position



Bar migration and accretion velocities



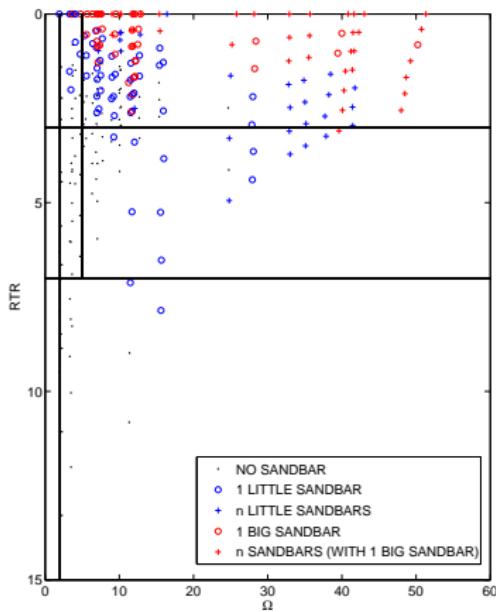
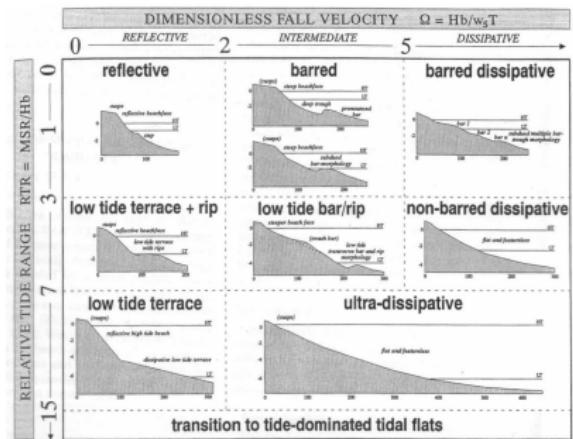
To conclude with this numerical study :

Synthesis

- The number, the volume, the distance to coastline and the velocities of bars increase with the wave height.
- This response decreases when :
 - the tide range increases,
 - the wave spectrum width increases,
 - the median grain size increases,
 - the beach slope decreases,
 - the wave period decreases.
- Spring-to-spring tidal cycle : morphology is more influenced by spring tide period.

To conclude with this numerical study :

Masselink and Short (1993) beach model vs. numerical model

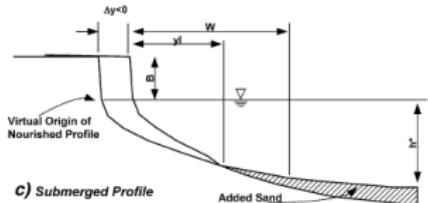
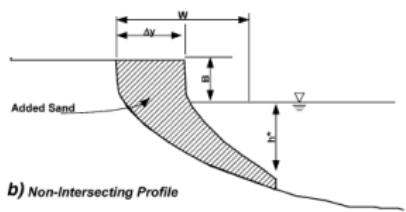
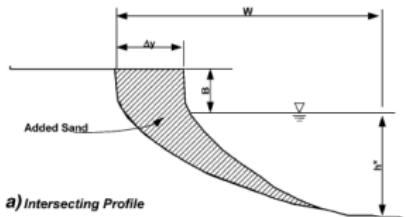


Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Beach nourishment with a native sand deposit

Dean's (1998) method
(equilibrium concept)

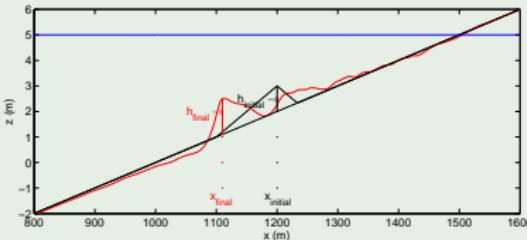


Questions

- What is the best place to nourish a beach ?
- Which profile is the most stable ?

Method

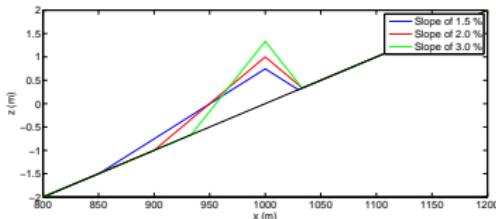
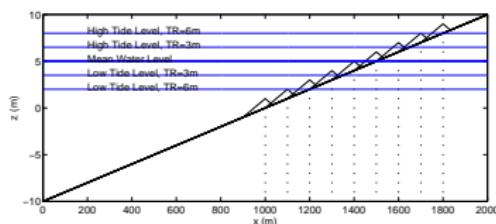
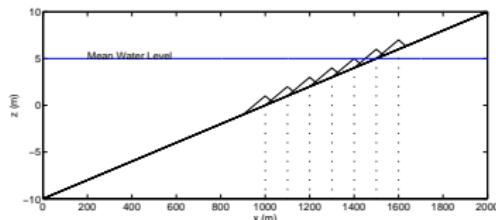
Evolution with FUNBEACH 1DH of an artificial nourishment after 15 days of swell on a plane sloping beach.



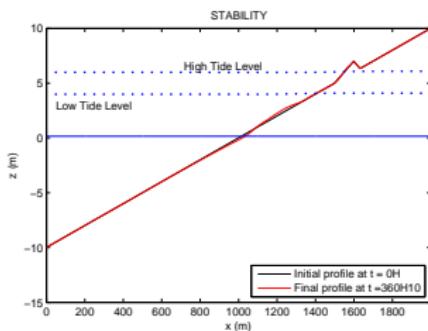
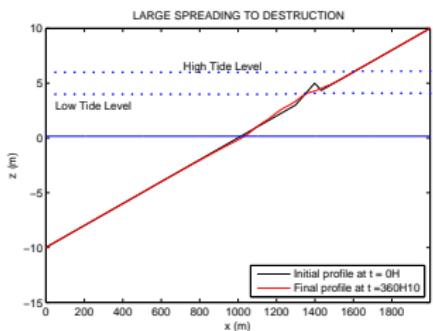
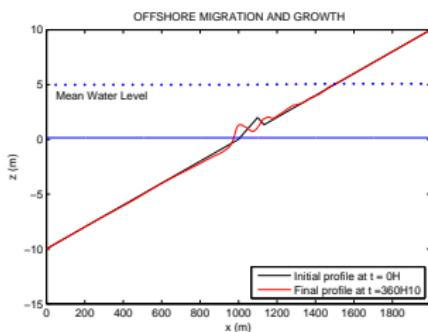
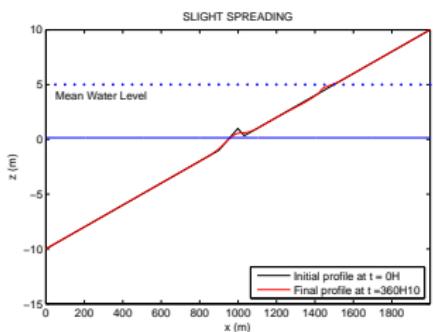
Numerical study

Test-cases

- Plane sloping beach ($\beta=1\%$, $d_{50} = 0.144$).
- Artificial nourishment of $66,7 \text{ m}^3/\text{ml}$.
- Without tide : 5 wave heights from 0.4m to 2m and 7 positions across the profile from $z_{MWL}=-5\text{m}$ to $z_{MWL}= +1\text{m}$.
- With tide : $H_{m0}=1.2\text{m}$ with 6 tide ranges from 1m to 6m and 9 positions across the profile from $z_{MWL}=-5\text{m}$ to $z_{MWL}= +3\text{m}$.
- 3 slopes : 1.5%, 2% et 3%.



Different types of morphologic response



Synthesis of simulated evolutions

- On microtidal beaches :
 - Before the breaking zone : slight spreading,
 - In the breaking zone : growth,
 - After the breaking zone : large spreading to destruction,
 - Near the shoreline : stability.
- On mesotidal and macrotidal beaches :
 - Before the low-tide breaking zone : slight spreading,
 - In the lower intertidal zone : large spreading to destruction,
 - In the upper intertidal zone : stability.
- Influence of the slope of the artificial nourishment :
 - An artificial nourishment with highest slope moves slowest,
 - The wave height is most reduced with artificial nourishment with highest slope.

Practical recommendations of beach nourishments

- Bars and berms are the best locations to nourish microtidal beaches,
- The upper intertidal zone is the best location to nourish mesotidal and macrotidal beaches,
- Steep nourishments are recommended.

need to be confirmed by further studies.

Content

- 1 Introduction
- 2 Models description
- 3 Model validation on Deltaflume
- 4 Model validation on Pentrez beach
- 5 Influences of waves and tide on a plane sloping beach
- 6 Artificial nourishment study
- 7 Conclusions

Conclusions

- Development of a new morphodynamic model able to reproduce beach processes :
 - Wave propagation, wave breaker and bottom friction including wave ripples, thanks to FUNWAVE model,
 - Undertow and near-bed velocities, thanks to Lynett (2006) and turbulence closure vertical model,
 - Beach evolution and bar movement.
- Lynett-Bailard approach (1DH) faster and more accurate than the turbulence closure vertical approach (pseudo-2DV).
- Influence of several parameters on beach morphology :
 - The number, the volume, the distance to coastline and the velocities of bars increase with the wave height.
 - This response decreases when the tide range, the wave spectrum width and the median grain size increase, and when the beach slope and the wave period decrease.
- Appropriated locations and forms for beach nourishments have been identified.

Prospects

- FUNBEACH 1DH and FUNBEACH 2DV + MII to study other field sites,
- Multi-class approach to study grain size evolution of the beach,
- Effective 2DV approach : see Lynett and Liu's (2004) multi-layer model,
- Account for the longshore component : FUNWAVE 2D \Rightarrow FUNBEACH 2DH and FUNBEACH 3D with a potential alternative for long term simulations given by a phase-averaged model like XBEACH (Roelvink *et al.*, 2008).

Second test-case : Wave spectrum

Wind waves

H_{m0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	BS	BI	-	-	-	-	-
0.8m	BS	2BS	-	-	-	-	-
1.2m	3BS	2BS	-	-	-	-	-
1.6m	2BS	2BS	BS	BS	-	-	-
2.0m	2BS	2BS	BS	BS	-	-	-

Monochromatic wave

H_{m0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	2BS	BI	BI	BI	BI	BI	BI
0.8m	BS	2BS	BI BS	BI BS	BI	BI	BI
1.2m	5BS	BS BI	2BS	BI BS	BI BS	BI BS	BI BS
1.6m	3BS	2BS	2BS	2BS	BI BS	BI BS	BI BS
2.0m	2BS	2BS	2BS	3BS	2BS	BI BS	BI

⇒ Narrower wave spectrum increases bar dynamics.

Third test-case : beach slope

Beach slope $\beta_p = 0.5\%$

H_{m0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	-	-	-	-	-	-	-
0.8m	BS	BI	-	-	-	-	-
1.2m	6BS	BS	-	-	-	-	-
1.6m	9BS	3BS	2BS	-	-	-	-
2.0m	4BS	3BS	-	-	-	-	-

Beach slope $\beta_p = 2.0\%$

H_{m0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	-	-	-	-	-	-	-
0.8m	BS	BS	BS	-	-	-	-
1.2m	BS	BS	BS	BS	BS	BS	BS
1.6m	BS						
2.0m	BS	BS	BS	BS	BS	BS	BI BS

⇒ Steeper beach increases bar dynamics.

Fourth test-case : grain size

Median grain size $d_{50} = 0.063\text{mm}$

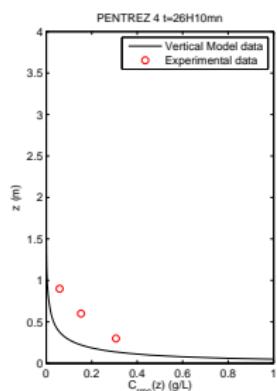
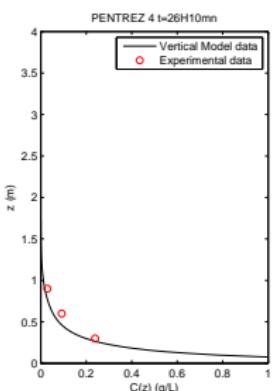
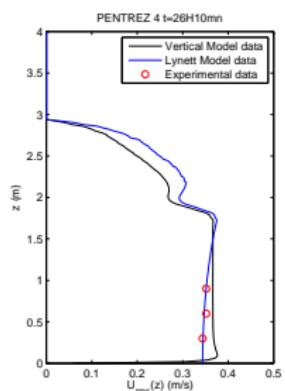
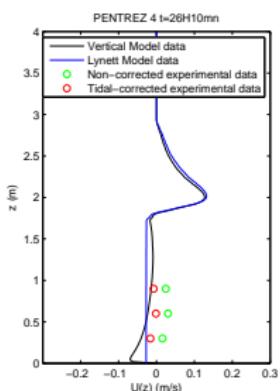
H_{m_0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	2BS	BI	BI	BI	BI	BI	BI
0.8m	4BS	BS	BS	BI	BI	BI	BI
1.2m	3BS	BS	BS	BS BI	BI BS	BI BS	BI BS
1.6m	5BS	BS BI	BS BI	BS BI	BI BS	2BI BS	2BI BS
2.0m	3BS	3BS BI	BS	BS BI	BI BS	2BI BS	2BI BS

Median grain size $d_{50} = 0.200\text{mm}$

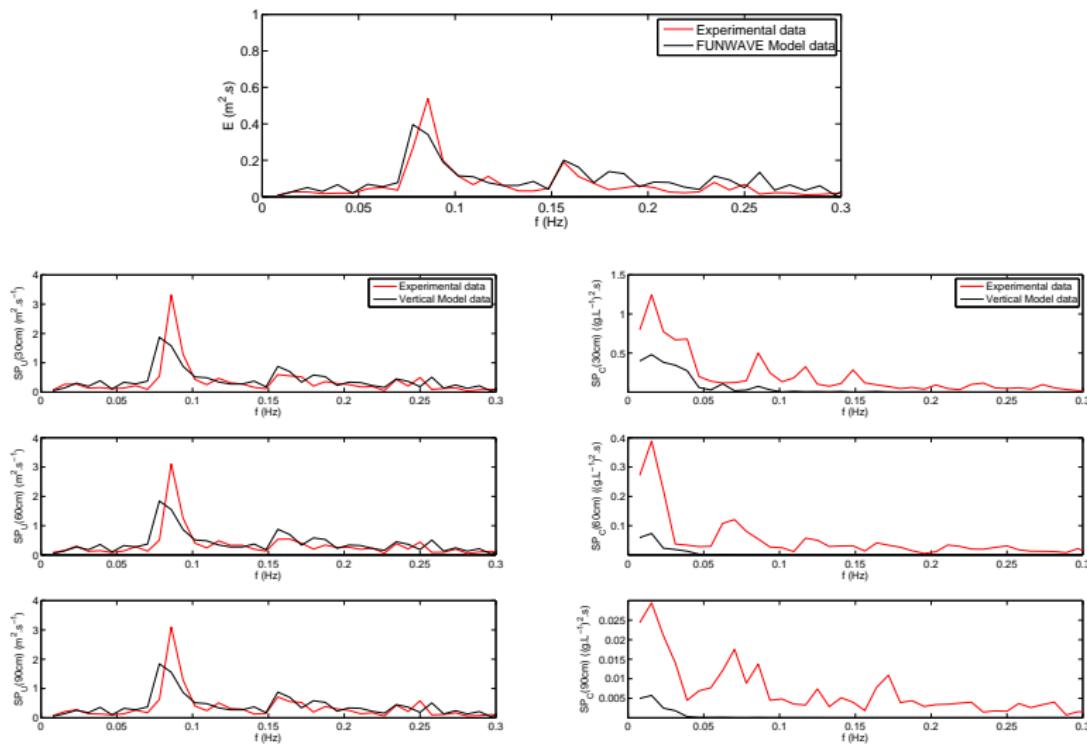
H_{m_0} / TR	0m	1m	2m	3m	4m	5m	6m
0.4m	BS	-	-	-	-	-	-
0.8m	BS	-	-	-	-	-	-
1.2m	3BS	BS	-	-	-	-	-
1.6m	3BS	BS	BS	-	-	-	-
2.0m	3BS	2BS	BS	-	-	-	-

⇒ Finer sand beach increases bar dynamics.

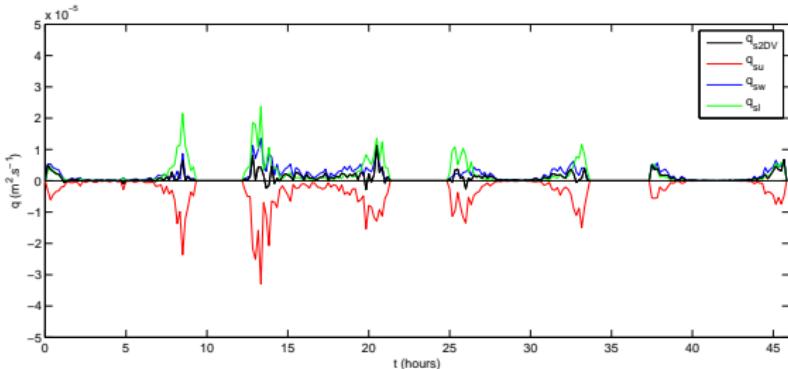
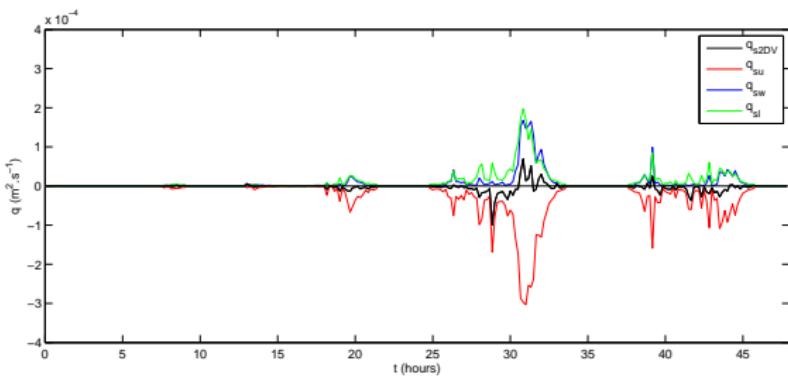
Vertical profiles example ($t=26H10mn$ PENTREZ#4)



Wave, Velocity and Sediment concentration spectra (t=26H10mn PENTREZ#4)



Transport rates components



Long simulations on a plane sloping beach

