

# Specification and Verification of Multithreaded Object-Oriented Programs with Separation Logic

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Soutenance de thèse

Thèse dirigée par Marieke Huisman  
Thèse effectuée au sein des équipes Everest et FMT

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# Un programme, qu'est ce que c'est ?

- Un programme est une **suite d'instructions**.

Exemple de programme calculant la valeur d'une fraction:

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lire n;  
lire d;  
affiche n / d;
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- S'assurer que les programmes fonctionnent correctement.
  - ↳ Par exemple, le programme ci-dessus est-il correct ?
  - ↳ Hum, pas vraiment, on peut effectuer une division par zéro. . .
  - ↳ C.à.d. que ce programme peut *planter*.

# Un programme, qu'est ce que c'est ?

- Un programme est une **suite d'instructions**.

Exemple de programme calculant la valeur d'une fraction:

```
lire n;  
lire d;  
si d  $\neq$  0 alors affiche (n / d);  
sinon affiche "Erreur : d doit etre different de zero.";
```

Le but de cette thèse:

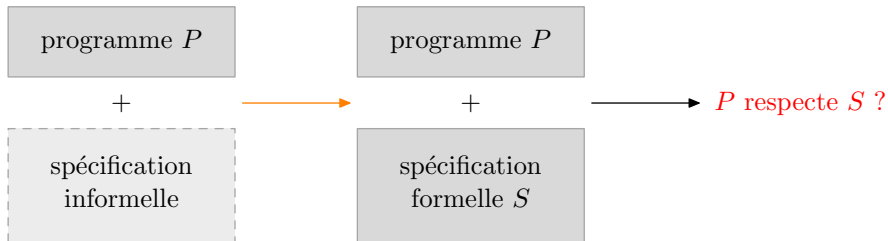
- S'assurer que les programmes fonctionnent correctement.
- ↳ Par exemple, le programme ci-dessus est-il correct ?
- ↳ Oui!

# Vérifier des programmes

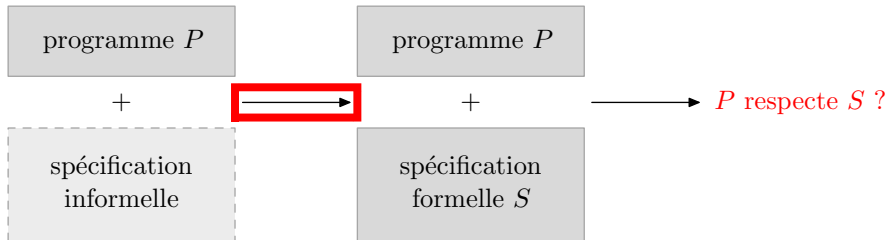
Pour s'assurer du bon fonctionnement des programmes, on les *vérifie*.

Vérifier un programme  $P$ , ça consiste à:

- **Spécifier formellement  $P$** , c.à.d. exprimer ce que  $P$  est censé faire.
- **Vérifier que  $P$  satisfait sa spécification.**

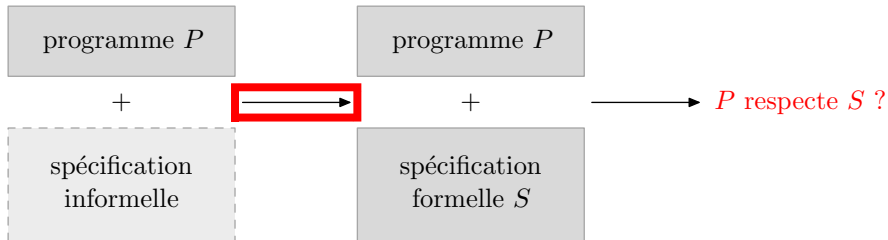


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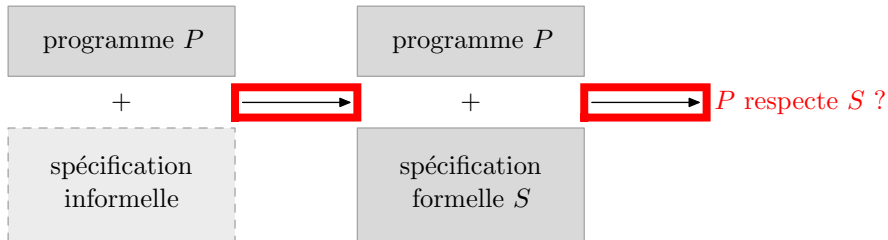
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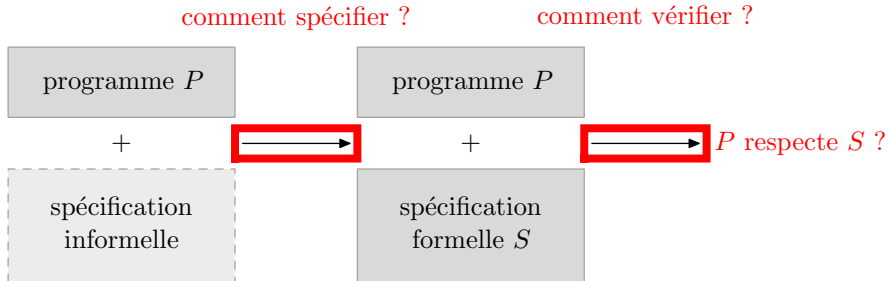


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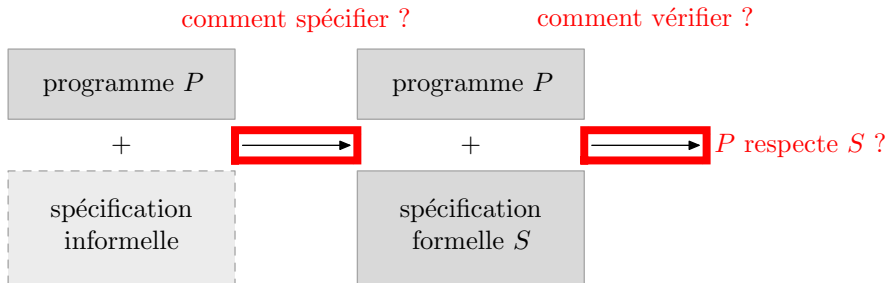
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Pour des programmes *objets* et *multi-processeurs*.

# Objectives of the thesis

To adapt separation logic to multithreaded Java

↳ I.e. to support Java's primitives for multithreading:

- (1) fork/join
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By using variants of separation logic [Reynolds'02]:

- Separation logic for while programs with a parallel operator  $\parallel$  [O'Hearn'07]
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Side effects of the thesis:

- Three analyses based on separation logic

# Our tool for reasoning: Separation Logic

Our assertion language is *permission accounting separation logic*

[Reynolds'02, Bornat et al.'05].

- Formulas represent permissions to access the heap.
- Formula  $x.f \overset{\pi}{\dashv} v$  has a dual meaning:
  - $x.f$  contains value  $v$ .
  - Permission  $\pi$  to access field  $x.f$ .
- Permissions  $\pi$  are fractions in  $(0, 1]$  [Boyland'03].
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Compared to the literature:

- We mix object-orientation and permissions.
- Classes can be parameterized by specification values.

# Objective 1: fork/join [AMAST'08]

fork and join are the two primitives used to create and wait threads

(in Java, C++, C, python, etc.):

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- ↳ fork and join are more general than `||`.

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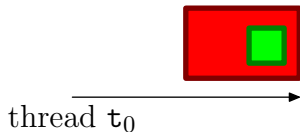
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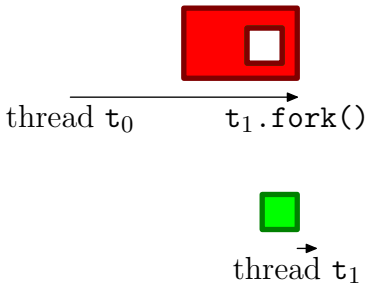
In terms of resources (i.e. the heap), fork and join behave as follows:

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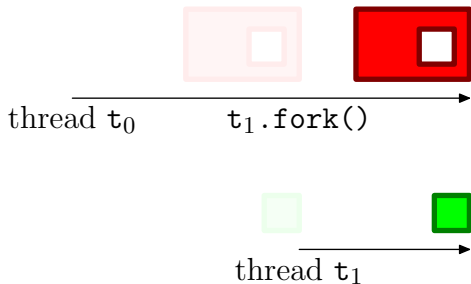
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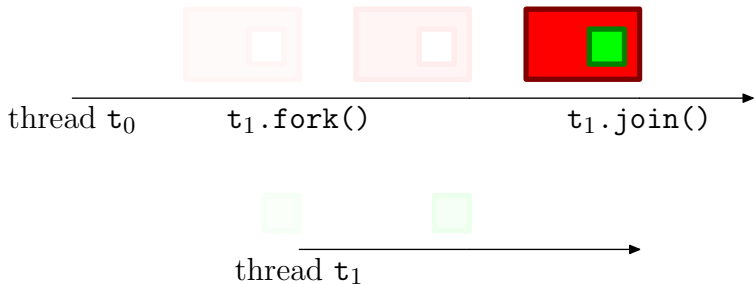
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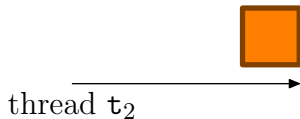
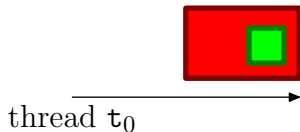


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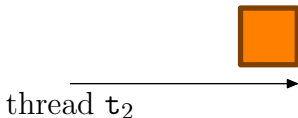
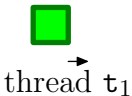
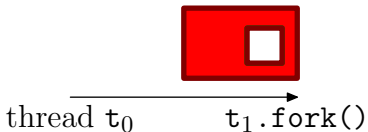




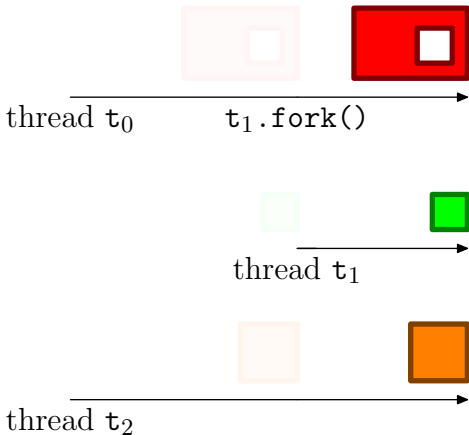
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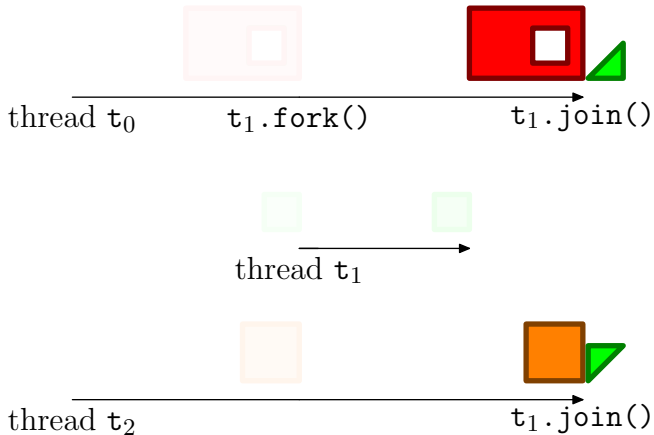
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# Hoare rules for fork and join

```
class Thread extends Object{
```

```
void fork();
```

```
void join();
```

```
void run() { null }
```

```
}
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- When `t.fork()` is called, `t.run()` is executed in parallel.

# Hoare rules for fork and join

```
class Thread extends Object{  
  pred preFork = true; // to be extended in subclasses  
  
  requires preFork; ensures true;  
  void fork();  
  
  void join();  
  
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```

- When `t.fork()` is called, `t.run()` is executed in parallel.

# Hoare rules for fork and join

```
class Thread extends Object{
  pred preFork = true;
  pred postJoin = true; // to be extended in subclasses

  requires preFork; ensures true;
  void fork();

  requires Join(this); ensures postJoin;
  void join();

  requires preFork; ensures postJoin;
  void run() { null }
}
```

- `t.join()` resumes when `t` terminates.
- `Join(t)`: the thread in which this formula appears can get back `t`'s postcondition when `t` terminates.



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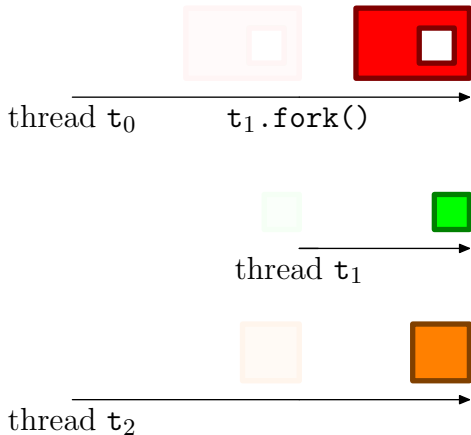
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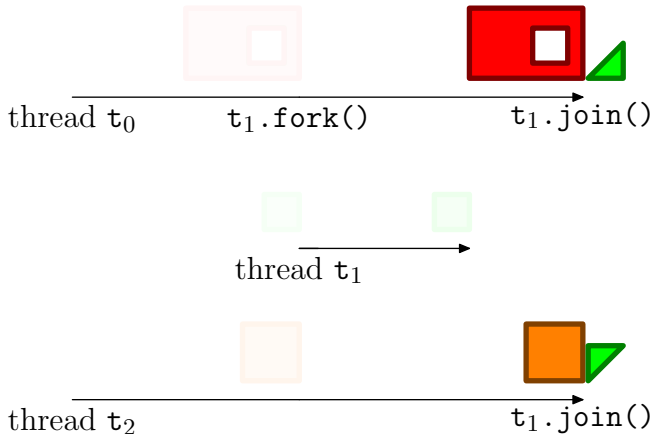
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- `t.join()` resumes when `t` terminates.
  - `Join(t)`: the thread in which this formula appears can get back `t`'s postcondition when `t` terminates.
- ↳ But this does not allow concurrent joiners.

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# Hoare rules for fork and join

```
class Thread extends Object{
  pred preFork = true;
  pred postJoin<perm p> = true;

  requires preFork; ensures true;
  void fork();

  requires Join(this,p); ensures postJoin<p>;
  void join();

  requires preFork; ensures postJoin<1>;
  void run() { null }
}
```

↳ We parameterize Join and postJoin by a permission.

- Join( $t, p$ ) give access to fraction  $p$  of thread  $t$ 's postcondition.

# Hoare rules for fork and join

```
class Thread extends Object{
  pred preFork = true;
  group postJoin = true;

  requires preFork; ensures true;
  void fork();

  requires Join(this,p); ensures postJoin<p>;
  void join();

  requires preFork; ensures postJoin<1>;
  void run() { null }
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```

- For soundness:
- postJoin is a special predicate: a **group**.
- ↳ It satisfies  $\forall \text{perm } p. \text{postJoin}\langle p \rangle *-* (\text{postJoin}\langle p/2 \rangle * \text{postJoin}\langle p/2 \rangle)$ .

## Objective 2: reentrant locks [APLAS'08]

Reentrant locks are the main primitive to acquire/release locks in Java.

- They can be acquired more than once (and released accordingly)
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```
class Set{
    int size() { // client and helper method

}
    bool has(Element e) { // client method

}
}
```

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class Set{
    int size(){
        lock(this);
        ...
        unlock(this);
        return ...;
    }
    bool has(Element e){
        lock(this);
        bool result;
        if(size()==0) unlock(this); return false;
        else ...;    unlock(this); return ...;
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In separation logic [O'Hearn'07]:

- Each lock guards a part of the heap called the lock's **resource invariant**.
- Resource invariants are exchanged between locks and threads:
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Resource invariants are represented by the distinguished *abstract predicate* **inv**:

```
class Object{  
  pred inv = true;  
}
```

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  - But this is unsound for reentrant locks!
- ↳ We need to distinguish between initial acquisitions and reentrant acquisitions.

# Separation Logic for Reentrant Locks

4 formulas to speak about locks (where  $S$  is a *multiset*):

`Lockset(S) | S contains x | x.fresh | x.initialized`

For each thread, we track the set of currently held locks:

- `Lockset(S)`:  $S$  is the **multiset** of currently held locks.
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For each lock, we track its abstract lock state:

- `x.fresh`:  $x$ 's resource invariant is not initialized
- `x.initialized`:  $x$ 's resource invariant is initialized.

# Initializing Locks

$$\frac{C\langle\bar{\pi}\rangle <: \Gamma(x)}{\Gamma \vdash \{ \text{true} \} \quad x = \text{new } C\langle\bar{\pi}\rangle \quad \{x.\text{init} * C \text{ classof } x * \textcircled{*}_{\Gamma(u)} <: \text{Object } x != u * \text{x.fresh}\}} \text{(New)}$$

- ↳ After creation a lock cannot be acquired: `x.initialized` fails to match `(Lock)`'s precondition.



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$$\frac{\Gamma \vdash \begin{array}{l} \{\text{Lockset}(S) * x.\text{inv} * x.\text{fresh}\} \\ x.\text{commit} \\ \{\text{Lockset}(S) * \neg(S \text{ contains } x) * x.\text{initialized}\} \end{array}}{\text{(Commit)}}$$

- ↳ `x.commit` is a no-op.
- ↳ After being committed a lock can be acquired: (Commit)'s postcondition entails `x.initialized`.

# Acquiring Locks

$$\frac{}{\Gamma \vdash \text{lock}(x) \{ \text{Lockset}(x \cdot S) * x.\text{inv} \}} \text{ (Lock)}$$

$\{ \text{Lockset}(S) * (\neg S \text{ contains } x) * x.\text{initialized} \}$

- ↳ **First acquirement:** resource invariants obtained.
- ↳ Nothing special to handle subclassing.

$$\frac{}{\Gamma \vdash \text{lock}(x) \{ \text{Lockset}(x \cdot x \cdot S) \}} \text{ (Re-Lock)}$$

- ↳ **Reentrant acquirement:** x's resource invariant not obtained.

# Releasing Locks

- The 2 rules for releasing locks are dual to the rules for acquirement.
- ↳ Hence, we do not discuss them.

# Objectives 1 and 2: Achievements

- A **sound** verification system for realistic multithreaded Java programs.
- Usability tested against challenging case studies:
  - Concurrent iterator
  - Lock coupling algorithm (still some limitations)
- Algorithmic verification still to be developed

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After that:

- 3 new analyses based on separation logic
- ↳ 2 of these analyses are sketched in the next slides

# 1<sup>st</sup> Analysis: Fast Disproving of Entailment [IWACO'09]

Goal:

- Disprove entailment between **separation logic** formulas
- ↳ I.e. to prove  $A \not\vdash B$

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## Usefulness:

- Program verifiers spend their time checking entailment.
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- ↳ program verifiers have to find a  $F$  such that  $A \vdash B \star F$ .
  
- In full separation logic,  $\vdash$  is undecidable.
- If we can prove that  $A \not\vdash B$ , then we know that  $F$  cannot be found.
- ↳ This avoids trying to prove unprovable programs.



# Disproving Technique

Soundness of the proof system:

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Contraposition:

$$(\exists h, h \models A \wedge \neg h \models B) \text{ implies } A \not\vdash B$$

Goal of this work:

- Take  $A$  and  $B$  and prove that  $A \not\vdash B$
- By **discriminating** models of  $A$  and  $B$

# Disproving Technique (classical semantics)

Objective:

Find  $h$  such that  $h \models A$  and  $\neg h \models B$

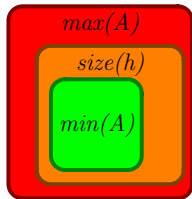
- We compute bounds on the size of models.
- $max : \text{Formula} \rightarrow \text{Size}$
- $min : \text{Formula} \rightarrow \text{Size}$
- $size : \text{Model} \rightarrow \text{Size}$

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- We compute bounds on the size of models.
- $max$  : Formula  $\rightarrow$  Size
- $min$  : Formula  $\rightarrow$  Size
- $size$  : Model  $\rightarrow$  Size



Properties of  $max$  and  $min$  (classical semantics):

$\forall h, h \models A$  implies  $min(A) \leq size(h) \leq max(A)$

# Disproving Technique (classical semantics)

$(\exists h, h \models A \wedge \neg h \models B)$  implies  $A \not\models B$

$\forall h, h \models A$  implies  $\min(A) \leq \text{size}(h) \leq \max(A)$

↓

$\max(A) < \min(B)$  implies  $A \not\models B$

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- Two different trade offs between speed and precision  
(two ways to define Size)
- **Proven correct** in Coq
- **License-left proof scripts**



## 2<sup>nd</sup> Analysis: Optimizations by Proof Rewriting [SAS'09]

- We parallelize and optimize **proven** programs.

To parallelize programs, you need to know:

- What data is accessed by programs.
- What data is **not** accessed by programs.

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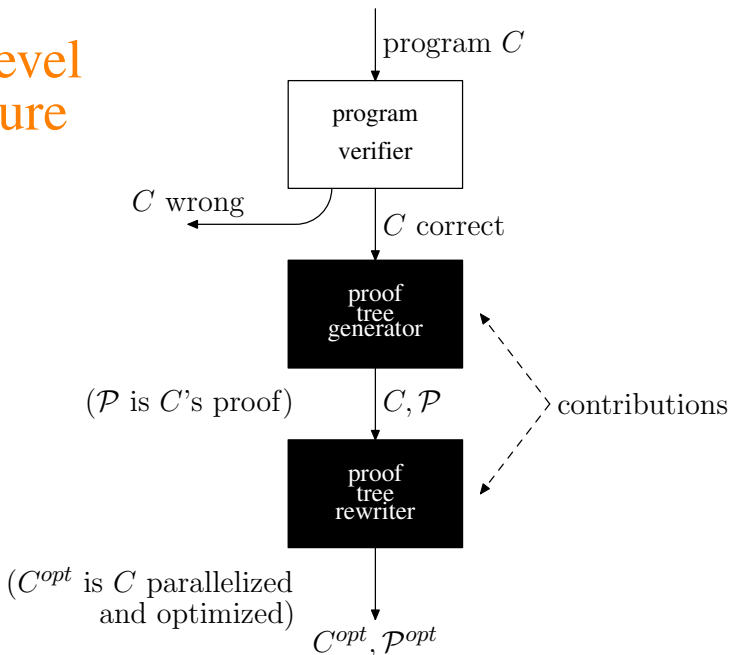
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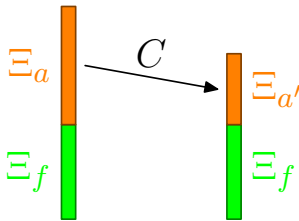
- Separation logic proofs exhibit how data is accessed (or not):
  - **Antiframes** exhibit data that is accessed. (explained next)
  - The **(Frame)** rule exhibits data that is **not** accessed. (explained next)
- Optimizations are expressed with a **rewrite system** between proof trees.
- Proof trees are derivations of Hoare triplets.

# High-Level Procedure



# Separation Logic: (Frame) rule

$$\frac{\{\Xi_a\} C \{\Xi_{a'}\}}{\{\Xi_a \star \Xi_f\} C \{\Xi_{a'} \star \Xi_f\}} \text{ (Frame } \Xi_f \text{)}$$



- $\Xi_a$  is the *antiframe* ← accessed data
- $\Xi_f$  is the *frame* ← not-accessed data
- Later, (Fr) sometimes abbreviates (Frame).

# With Frames: Parallelization Is Easy

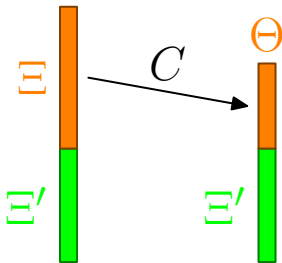
$$\frac{\frac{\{\Xi\}C\{\Theta\}}{\{\Xi \star \Xi'\}C\{\Theta \star \Xi'\}} \text{ (Fr } \Xi') \quad \frac{\{\Xi'\}C'\{\Theta'\}}{\{\Theta \star \Xi'\}C'\{\Theta \star \Theta'\}} \text{ (Fr } \Theta)}{\{\Xi \star \Xi'\}C; C'\{\Theta \star \Theta'\}} \text{ (Seq)}$$

$$\downarrow \text{Parallelize}$$

$$\frac{\{\Xi\}C\{\Theta\} \quad \{\Xi'\}C'\{\Theta'\}}{\{\Xi \star \Xi'\}C \parallel C'\{\Theta \star \Theta'\}} \text{ (Parallel)}$$

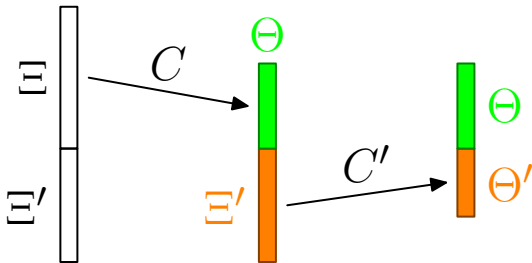
# Parallelize's left hand side

$$\frac{\frac{\{E\}C\{O\}}{\{E \star E'\}C\{O \star E'\}} \text{ (Fr } E') \quad \frac{\{E'\}C'\{O'\}}{\{O \star E'\}C'\{O \star O'\}} \text{ (Fr } O')}{\{E \star E'\}C; C'\{O \star O'\}} \text{ (Seq)}$$



# Parallelize's left hand side

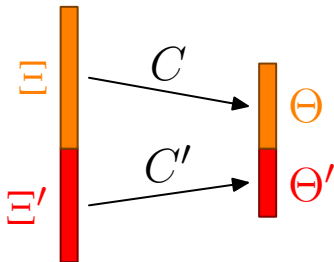
$$\frac{\frac{\{E\}C\{\Theta\}}{\{E \star E'\}C\{\Theta \star E'\}} \text{ (Fr } E') \quad \frac{\{E'\}C'\{\Theta'\}}{\{\Theta \star E'\}C'\{\Theta \star \Theta'\}} \text{ (Fr } \Theta)}{\{E \star E'\}C; C'\{\Theta \star \Theta'\}} \text{ (Seq)}$$





## Parallelize's right hand side

$$\frac{\{\mathbb{E}\}C\{\Theta\} \quad \{\mathbb{E}'\}C'\{\Theta'\}}{\{\mathbb{E} \star \mathbb{E}'\}C \parallel C'\{\Theta \star \Theta'\}} \text{ (Parallel)}$$

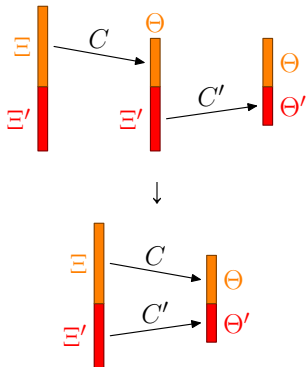


# Parallelize

$$\frac{\frac{\{E\}C\{\Theta\}}{\{E * E'\}C\{\Theta * E'\}} \text{ (Fr } E') \quad \frac{\{E'\}C'\{\Theta'\}}{\{\Theta * E'\}C'\{\Theta * \Theta'\}} \text{ (Fr } \Theta)}{\{E * E'\}C; C'\{\Theta * \Theta'\}} \text{ (Seq)}$$

↓ Parallelize

$$\frac{\{E\}C\{\Theta\} \quad \{E'\}C'\{\Theta'\}}{\{E * E'\}C \parallel C'\{\Theta * \Theta'\}} \text{ (Parallel)}$$



## 2<sup>nd</sup> Analysis: Achievements

- An **entirely new technique** to parallelize and optimize programs.
  - ↳ Other optimizations than parallelization have been studied.
- **No ad-hoc analyses**: separation logic proofs are taken as analyses.
- Can parallelize any code (i.e. not focused on loops).
- Soundness is easier to prove than for classical approaches.
- **License-left prototype implementation.**

# Related Work

## Program verification:

- Separation logic for sequential Java [Parkinson'05,Distefano et al.'08,Chin et al.'08]
- Separation logic for multithreaded C [Gotsman et al.'07,Appel et al.'07]
- Boogie for multithreaded C# [Barnett et al.'04,Jacobs et al.'06]
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## Automatic parallelization:

- Many “classical” approaches
- By using separation logic [Raza et al.'09]

# Main Publications

- Separation Logic Contracts for a Java-like Language with Fork/Join; Haack and Hurlin; AMAST'08
- Reasoning about Java's Reentrant Locks; Haack, Huisman, and Hurlin; APLAS'08
- Specifying and Checking Protocols of Multithreaded Classes; Hurlin; SAC'09
- Resource Usage Protocols for Iterators; Haack and Hurlin; Journal of Object Technology'09
- Size Does Matter: Two Certified Abstractions to Disprove Entailment in Intuitionistic and Classical Separation Logic; Hurlin, Bobot, and Summers; IWACO'09
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## Developments:

- 1 Some Coq proofs for the AMAST and APLAS papers.
- 2 ocaml implementation of some of the techniques described in the SAC paper.
- 3 Full Coq proofs for the IWACO paper.
- 4 ocaml and Java+tom prototype implementation of the SAS paper.



# Conclusion

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  - ↳ that uses realistic primitives,
  - ↳ and that handles challenging examples (iterator, lock-coupling).

Second:

- We extended previous work on protocols. (omitted in this talk)
- We discovered a fast algorithm to disprove entailment.
- We showed how to parallelize and optimize programs by rewriting their proofs.

# Future Work

For the verification system:

- Implementing it!
- Doing a large case study

For the disproving algorithm:

- Extension to object-orientation
- ↳ By keeping its simplicity and its usefulness (not straightforward)

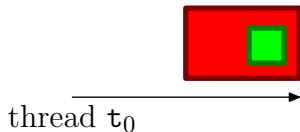
For the parallelizing analysis:

- Extension to object-oriented programs (easy)
- Extension to loops → to battle it out with classical parallelizers!

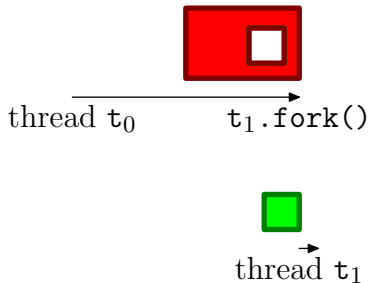
Thank you



## Fork and join in terms of resources (2)

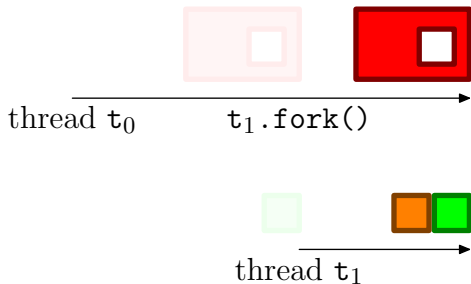


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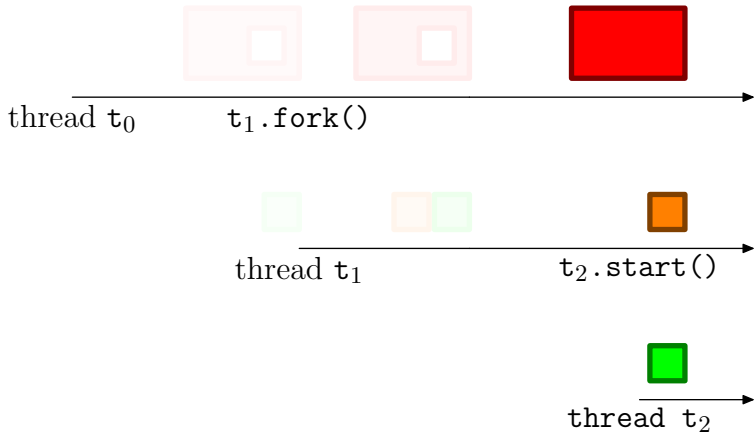




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# Releasing Locks

$$\frac{}{\Gamma \vdash \{\text{Lockset}(x \cdot x \cdot S)\} \text{unlock}(x) \{\text{Lockset}(x \cdot S)\}} \text{ (Re-Unlock)}$$

↳ Releasing  $x$  but  $x$ 's reentrancy level  $> 1$ : invariant not abandoned.

$$\frac{}{\Gamma \vdash \{\text{Lockset}(x \cdot S) * x.\text{inv}\} \text{unlock}(x) \{\text{Lockset}(S)\}} \text{ (Unlock)}$$

↳  $x$ 's reentrancy level not known to be  $> 1$ ,  $x$ 's resource invariant abandoned.

# Disproving Technique (classical semantics)

$(\exists h, h \models A \wedge \neg h \models B)$  implies  $A \not\models B$

$\forall h, h \models A$  implies  $\min(A) \leq \text{size}(h) \leq \max(A)$

↓

$\max(A) < \min(B)$  implies  $A \not\models B$

# Defining *size*

- $size(h) \triangleq$  sum of  $h$ 's permissions
- $size: Model \rightarrow Perm$

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- $size(h) \triangleq$  sum of  $h$ 's permissions
- $size: Model \rightarrow Perm$
  
- Models  $h$  are lists of triples of an **address**, a **permission**, and a value.
- ↳ An example model is  $(42, \pi, 3) :: (47, \pi', -5) :: (42, \pi'', 0) :: []$ .

$$size((42, \pi, 3) :: (47, \pi', -5) :: (42, \pi'', 0) :: []) = \pi + \pi' + \pi''$$

# Defining *max/min* (classical semantics)(excerpt)

$$\max(- \overset{\pi}{\mapsto} -) = \pi$$

$$\max(A \star B) = \max(A) +_{\pi} \max(B)$$

$$\min(- \overset{\pi}{\mapsto} -) = \pi$$

$$\min(A \star B) = \min(A) +_{\pi} \min(B)$$

$$h \models a \overset{\pi}{\mapsto} v \quad \text{iff} \quad h = (a, \pi, v)$$

$$h \models A \star B \quad \text{iff} \quad \exists h_A, h_B, h = h_A \uplus h_B, h_A \models A \text{ and } h_B \models B$$

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$$h \models A \vee B \quad \text{iff} \quad h \models A \text{ or } h \models B$$



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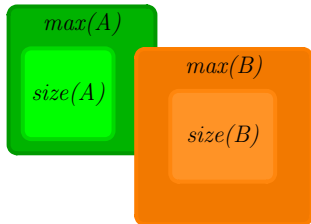
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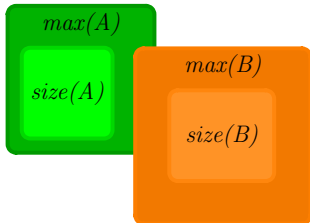
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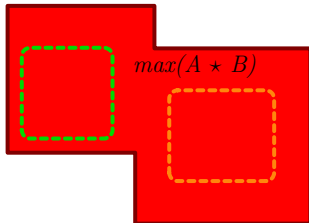
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$$h \models A \multimap B \quad \text{iff} \quad \forall h_A, h_A \models A \text{ and } h_A \text{ and } h \text{ are compatible} \\ \text{implies } h_A \uplus h \models A \star B$$

# Defining *max/min* (classical semantics)

$$\max(\forall\pi.A) = \max(A[\pi_w/\pi])$$

$$\max(\exists\pi.A) = \max(A[\pi_w/\pi])$$

$$\max(\forall v.A) = \max(\exists v.A) = \max(A)$$

$$\min(\forall\pi.A) = \min(A[\pi_w/\pi])$$

$$\min(\exists\pi.A) = \min(A[\varepsilon/\pi])$$

$$\min(\forall v.A) = \min(\exists v.A) = \min(A)$$

↳ Standard semantics of quantifiers (omitted)

- $\varepsilon$  is an infinitely **small** permission

# Defining *max/min* (classical semantics)

$$\max(b) = \infty$$

$$\min(b) = \pi_0$$

$$h \models b \quad \text{iff} \quad \text{oracle}(b)$$

- $b$  is a pure formula, i.e., it does not depend on the heap  $h$ .
- $\pi_0$  is the minimal permission.

# Toy Example

$$\Lambda_{x,y,z}^{n,m,k} \triangleq x \mapsto [f : n] \star y \mapsto [f : m] \star z \mapsto [f : k]$$

$$\frac{\frac{\frac{\frac{\{\Lambda_x^-\}x \rightarrow f = n\{\Lambda_x^n\}}{\{\Lambda_{x,y,z}^{n,m,-}\}x \rightarrow f = n\{\Lambda_{x,y,z}^{n,m,-}\}} \text{(Fr } \Lambda_{y,z}^{n,-}) \text{ (Mutate)}}{\{\Lambda_{x,y,z}^{n,m,-}\}x \rightarrow f = n\{\Lambda_{x,y,z}^{n,m,-}\}} \text{ (Fr } \Lambda_{y,z}^{n,-}) \text{ (Mutate)}}{\frac{\frac{\frac{\{\Lambda_y^-\}y \rightarrow f = m\{\Lambda_y^m\}}{\{\Lambda_{x,y,z}^{n,m,-}\}y \rightarrow f = m\{\Lambda_{x,y,z}^{n,m,-}\}} \text{(Fr } \Lambda_{x,z}^{n,-}) \text{ (Mutate)}}{\{\Lambda_{x,y,z}^{n,m,-}\}y \rightarrow f = m; z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{ (Seq)}}{\{\Lambda_{x,y,z}^{n,m,-}\}y \rightarrow f = m; z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{ (Seq)}}{\frac{\frac{\frac{\{\Lambda_z^-\}z \rightarrow f = k\{\Lambda_z^k\}}{\{\Lambda_{x,y,z}^{n,m,-}\}z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{(Fr } \Lambda_{x,y}^{n,m}) \text{ (Mutate)}}{\{\Lambda_{x,y,z}^{n,m,-}\}z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{ (Seq)}}{\{\Lambda_{x,y,z}^{n,m,-}\}z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{ (Seq)}}{\{\Lambda_{x,y,z}^{n,m,-}\}x \rightarrow f = n; y \rightarrow f = m; z \rightarrow f = k\{\Lambda_{x,y,z}^{n,m,k}\}} \text{ (Seq)}$$

↓

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# Guarantees of the Rewrite System

The rewrite system modifies programs but preserves specifications:

$$\frac{\mathcal{P}}{\{\Xi\}C\{\Theta\}} \downarrow \frac{\mathcal{Q}}{\{\Xi\}C'\{\Theta\}}$$

■ The program and the proof are modified:  $\mathcal{P}, C \rightarrow \mathcal{Q}, C'$ ,

↳ but specifications are preserved:  $\Xi, \Theta \rightarrow \Xi, \Theta$ .

Conjecture:

■ Programs related with  $\rightarrow$  are equivalent from a big step p.o.v.

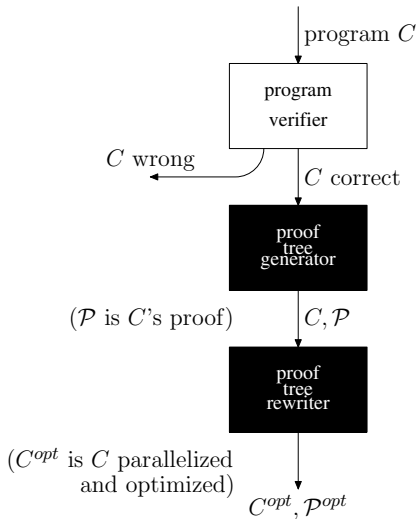
# We Want the Frames $\text{♪}$

- The **(Frame)** rule is the central ingredient of our procedure.
- Problem: Existing program verifiers (e.g. smallfoot) do not make frames explicit.

$$\frac{\Pi \vdash F = E \quad \dots}{\{\Pi \mid F \mapsto [\rho]\} E \rightarrow f = G\{\Pi \mid F \mapsto [\rho']\}} \text{ (Mutate)}$$

$\hookrightarrow$   $\Pi$  is “too big”: there exists a “smaller” antiframe  $\Pi_a$  such that  $\Pi_a \vdash F = E$ .

# Recall the big picture ?



In the proof tree generator:

- Proof rules with explicit frames.
- But still usage of the program's verifier **normal rules** for verification.

Next slides:

Proof rules with explicit {anti-,} frames

# We Want the Frames

Berdine, Calcagno, and O'Hearn "Symbolic Execution with Separation Logic"

$$\frac{\Pi \vdash F = E \quad \dots}{\{\Pi \mid F \mapsto [\rho]\} E \rightarrow f = G\{\Pi \mid F \mapsto [\rho']\}} \text{ (Mutate)}$$

With explicit frames and antiframes

$$\frac{\frac{\Pi_a \vdash F = E \quad \dots}{\{\Pi_a \mid F \mapsto [\rho]\} E \rightarrow f = G\{\Pi_a \mid F \mapsto [\rho']\}} \text{ (Mutate)}}{\{(\Pi_a \mid F \mapsto [\rho]) \star \Xi_f\} E \rightarrow f = G\{(\Pi_a \mid F \mapsto [\rho']) \star \Xi_f\}} \text{ (Frame } \Xi_f)$$

# We Want the Frames

Berdine, Calcagno, and O'Hearn "Symbolic Execution with Separation Logic"

$$\frac{\dots \quad x' \text{ fresh} \quad \Pi \vdash F = E}{\{\Pi \mid \Sigma \star F \mapsto [\rho]\} x := E \rightarrow f \{ \dots \wedge \Pi[x'/x] \mid (\Sigma \star F \mapsto [\rho])[x'/x] \}} \text{ (Lookup)}$$

With explicit frames and antiframes

$$\frac{\begin{array}{l} x' \text{ fresh} \quad \dots \\ \Pi_a \vdash F = E \\ \Xi = \Pi_a[x'/x] \wedge \dots \mid (\Sigma_a \star F \mapsto [\rho])[x'/x] \end{array}}{\{\Pi_a \mid \Sigma_a \star F \mapsto [\rho]\} x := E \rightarrow f \{ \Xi \} \quad x \notin \Xi_f} \text{ (Lookup)}$$

$$\frac{\{ \underbrace{(\Pi_a \mid \Sigma_a \star F \mapsto [\rho])}_{\text{antiframe needed to prove } E \mapsto [\rho] \text{ and affected by } [x'/x]} \star \underbrace{\Xi_f}_{\text{frame unaffected by } [x'/x]} \} x := E \rightarrow f \{ \Xi \star \Xi_f \}}{\text{ (Frame } \Xi_f \text{)}}$$

# We Want the Frames

Berdine, Calcagno, and O'Hearn "Symbolic Execution with Separation Logic"

$$\frac{\Pi \vdash \perp}{\{\Pi \mid \Sigma\} C \{\Theta\}} \text{ (Inconsistent)}$$

With explicit frames and antiframes

$$\frac{\frac{\Pi_a \vdash \perp}{\{\Pi_a \mid \text{emp}\} C \{\Theta\}} \text{ (Inconsistent)}}{\left\{ \underbrace{\Pi_a \mid \text{emp}}_{\text{sufficient antiframe to prove } \perp} \star \underbrace{\Pi_f \mid \Sigma_f}_{\text{frame}} \right\} C \{\Theta\}} \text{ (Frame } \Pi_f \mid \Sigma_f)$$

- $\text{emp} \stackrel{\Delta}{=} \text{the heap is empty.}$

# Shape of Generated Trees

- Because of the algorithm used in program verifiers,  
↳ proof trees have a special shape.

For successive commands  $C_0, C_1, C_2, \dots$ , proof trees have this shape:

$$\frac{\frac{\frac{\dots}{\{\dots\}C_0\{\dots\}} \text{(Fr } \boxed{E})}{\{\dots\}C_1\{\dots\}} \text{(Fr } \boxed{E'})}{\{\dots\}C_2\{\dots\}} \text{(Fr } \boxed{E'})}{\{\dots\}C_1; C_2; \dots\{\dots\}} \text{(Seq)} \text{(Seq)}$$

- A (Frame) at each command.
- ↳ Problem: Frames are **redundant** (i.e.,  $\boxed{E} \cup \boxed{E'} \neq \emptyset$ ).
- ↳ In practice, this must be avoided for optimizations to fire.



## We Want the Frames ♪

- We rewrite proof trees to frame multiple commands,

↳ i.e., we *factorize frames*.

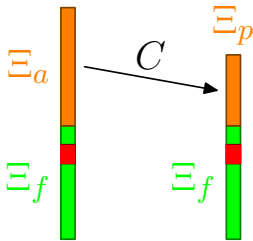
- Below,  $\Xi_c$  is the factorized frame.

Guard:  $\Xi_f \Leftrightarrow \Xi_{f_0} \star \Xi_c$  and  $\Theta_f \Leftrightarrow \Theta_{f_0} \star \Xi_c$

$$\begin{array}{c}
 \frac{\frac{\{ \Xi_a \} C \{ \Xi_p \}}{\{ \Xi_a \star \Xi_f \} C \{ \Xi_p \star \Xi_f \}} \text{ (Frame } \Xi_f)}{\{ \Xi_a \star \Xi_f \} C; C' \{ \Theta_p \star \Theta_f \}} \text{ (Seq)} \quad \frac{\frac{\{ \Theta_a \} C' \{ \Theta_p \}}{\{ \Theta_a \star \Theta_f \} C' \{ \Theta_p \star \Theta_f \}} \text{ (Frame } \Theta_f)}{\{ \Theta_a \star \Theta_f \} C' \{ \Theta_p \star \Theta_f \}} \text{ (Seq)} \\
 \downarrow \text{FactorizeFrames} \\
 \frac{\frac{\frac{\{ \Xi_a \} C \{ \Xi_p \}}{\{ \Xi_a \star \Xi_{f_0} \} C \{ \Xi_p \star \Xi_{f_0} \}} \text{ (Fr } \Xi_{f_0})} \quad \frac{\frac{\{ \Theta_a \} C' \{ \Theta_p \}}{\{ \Theta_a \star \Theta_{f_0} \} C' \{ \Theta_p \star \Theta_{f_0} \}} \text{ (Fr } \Theta_{f_0})}}{\{ \Xi_a \star \Xi_{f_0} \} C; C' \{ \Theta_p \star \Theta_{f_0} \}} \text{ (Seq)} \\
 \frac{\{ \Xi_a \star \Xi_{f_0} \} C; C' \{ \Theta_p \star \Theta_{f_0} \}}{\{ \Xi_a \star \Xi_f \} C; C' \{ \Theta_p \star \Theta_f \}} \text{ (Frame } \Xi_c)
 \end{array}$$

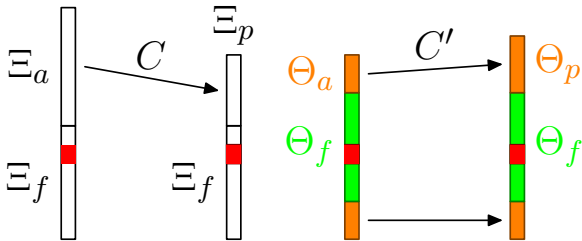
# FactorizeFrames's left hand side

$$\frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_f\}C\{\Xi_p \star \Xi_f\}} \text{ (Fr } \Xi_f)}{\{\Xi_a \star \Xi_f\}C; C'\{\Theta_p \star \Theta_f\}} \frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Fr } \Theta_f) \text{ (Seq)}$$



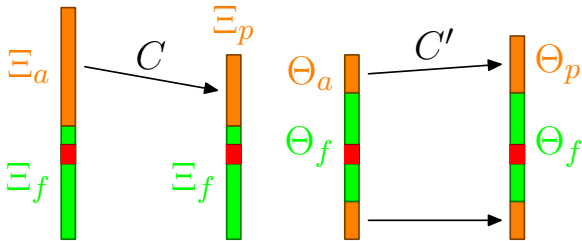
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# FactorizeFrames's left hand side

$$\frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_f\}C\{\Xi_p \star \Xi_f\}} \text{ (Fr } \Xi_f)}{\{\Xi_a \star \Xi_f\}C; C'\{\Theta_p \star \Theta_f\}} \frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Fr } \Theta_f) \text{ (Seq)}$$



- Guard:  $\Xi_f \Leftrightarrow \Xi_{f_0} \star \Xi_c$  and  $\Theta_f \Leftrightarrow \Theta_{f_0} \star \Xi_c$
- The part of the heap framed twice (in red) is the common frame  $\Xi_c$ .

# We Want the Frames ♪

Guard:  $\Xi_f \Leftrightarrow \Xi_{f_0} \star \Xi_c$  and  $\Theta_f \Leftrightarrow \Theta_{f_0} \star \Xi_c$

$$\begin{array}{c}
 \frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_f\}C\{\Xi_p \star \Xi_f\}} \text{ (Frame } \Xi_f)}{\{\Xi_a \star \Xi_f\}C; C'\{\Theta_p \star \Theta_f\}} \text{ (Frame } \Theta_f)}{\{\Xi_a \star \Xi_f\}C; C'\{\Theta_p \star \Theta_f\}} \text{ (Seq)} \\
 \downarrow \text{FactorizeFrames} \\
 \frac{\frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_{f_0}\}C\{\Xi_p \star \Xi_{f_0}\}} \text{ (Fr } \Xi_{f_0})} \quad \frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Theta_{f_0}\}C'\{\Theta_p \star \Theta_{f_0}\}} \text{ (Fr } \Theta_{f_0})}}{\{\Xi_a \star \Xi_{f_0}\}C; C'\{\Theta_p \star \Theta_{f_0}\}} \text{ (Seq)}}{\{\Xi_a \star \Xi_f\}C; C'\{\Theta_p \star \Theta_f\}} \text{ (Frame } \Xi_c)
 \end{array}$$

- ↳ The common part of  $\Xi_f$  and  $\Theta_f$  (i.e.,  $\Xi_c$ ) is framed separately.
- ↳ The new application of (Frame) is on a longer command ( $C; C'$ ) than before.

# Example

```
requires tree(x);
ensures tree(x);
rotate_tree(x){
  local x1,x2;
  if(x = nil){}
  else{
    x1 := x → l;
    x2 := x → r;
    x → l = x2;
    x → r = x1;
    rotate_tree(x1);
    rotate_tree(x2); }}}
```

→

```
requires tree(x);
ensures tree(x);
rotate_tree(x){
  local x1,x2;
  if(x = nil){}
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    x1 := x → l;
    x2 := x → r;
    (x → l = x2; x → r = x1) ||
    rotate_tree(x1); ||
    rotate_tree(x2); }}}
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    rotate_tree(x1); ||
    rotate_tree(x2); } }
```

## Implementation:

- The rewrite rules have been implemented in Java+**tom**.
- tom extends Java to pattern match against tom/user-defined Java objects.
- Each rewrite rule is less than 75 lines of code (i.e. manageable).
- Use of tom's strategies to fine tune optimizations.

# List of Optimizations

Optimizations include:

- parallelization (previous slides)
- Improvement of temporal locality (omitted in this talk)
- A generic optimization with 4 concrete applications: (omitted in this talk)
  - Early lock releasing
  - Late lock acquirement
  - Early disposal
  - Late allocation



# GenericOptimization

$$\frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_f\}C\{\Xi_p \star \Xi_f\}} \text{ (Frame } \Xi_f)}{\{\Xi_a \star \Xi_f\}C; C'\{\Xi'\}} \quad \frac{\frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Frame } \Theta_f)}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Seq)}$$

↓ GenericOptimization

$$\frac{\frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Xi_a \star \Theta_a \star \Xi_r\}C'\{\Xi_a \star \Theta_p \star \Xi_r\}} \text{ (Fr ...)}}{\{\Xi_a \star \Xi_f\}C'; C\{\Xi'\}} \quad \frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\dots\}C\{\Xi_p \star \Theta_p \star \Xi_r\}} \text{ (Fr ...)}}{\{\dots\}C\{\Xi_p \star \Theta_p \star \Xi_r\}} \text{ (Seq)}$$

Guard:  $\Theta_f \Leftrightarrow \Xi_p \star \Xi_r$

- This optimization changes the program order.
- ↳ The guard requires that  $C'$  frames the postcondition of  $C$  ( $\Xi_p$ ).

# Locks in Separation Logic

- Each lock guards a part of the heap called the lock's **resource invariant**.
- Resource invariants are exchanged between locks and threads:
  - 1 When a lock is acquired, it **lends** its resource invariant to the acquiring thread.
  - 2 When a lock is released, it **claims back** its resource invariant from the releasing thread.

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Formally:

$$\frac{\boxed{\mathbb{E}} \text{ is } x\text{'s resource invariant}}{\{\text{emp}\} \text{lock}(x) \{\boxed{\mathbb{E}}\}} \text{ (Lock)}$$

$$\frac{\boxed{\mathbb{E}} \text{ is } x\text{'s resource invariant}}{\{\boxed{\mathbb{E}}\} \text{unlock}(x) \{\text{emp}\}} \text{ (Unlock)}$$

(emp represents the empty heap)

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(emp represents the empty heap)

Next slide:

↳ Instantiation of the generic optimization to optimize usage of locks

# Instantiating GenericOpt.: EarlyUnlocking

$$\begin{array}{c}
 \frac{\frac{\{\Xi_a\}C\{\Xi_p\}}{\{\Xi_a \star \Xi_f\}C\{\Xi_p \star \Xi_f\}} \text{ (Fr } \Xi_f)}{\{\Xi_a \star \Xi_f\}C; \text{unlock}(x)\{\Theta_f\}} \text{ (Fr } \Theta_f)}{\{\Xi_a \star \Xi_f\}C; \text{unlock}(x)\{\Theta_f\}} \text{ (Seq)} \\
 \frac{\Theta_a \text{ is } x\text{'s resource invariant}}{\{\Theta_a\}\text{unlock}(x)\{\text{emp}\}} \text{ (Unlock)} \\
 \frac{\frac{\{\Theta_a\}\text{unlock}(x)\{\text{emp}\}}{\{\Xi_a \star \Theta_a \star \Xi_r\}\text{unlock}(x)\{\Xi_a \star \Xi_r\}} \text{ (Fr ...)}}{\{\Xi_a \star \Xi_f\}\text{unlock}(x); C\{\Xi_p \star \Xi_r\}} \text{ (Fr } \Xi_r)}{\{\Xi_a \star \Xi_f\}\text{unlock}(x); C\{\Xi_p \star \Xi_r\}} \text{ (Seq)}
 \end{array}$$

Guard:  $\Theta_f \Leftrightarrow \Xi_p \star \Xi_r$

- $(\Xi_p \star \Xi_f \Leftrightarrow \Theta_a \star \Theta_f + \text{guard})$  implies  $\Xi_f \Leftrightarrow \Theta_a \star \Xi_r$ .
- ↳ Command  $C$  does not access  $x$ 's resource invariant:
- Better unlock  $x$  before executing  $C$ !

## Example (2)

<pre>requires <math>x \mapsto [val : \_]</math>; ensures emp; copy_and_dispose(x){   local v;   lock(<math>r_{c \mapsto [val : \_]}</math>);   <math>v := x \rightarrow val</math>;   <math>c \rightarrow val = v</math>;   dispose(x);   unlock(<math>r_{c \mapsto [val : \_]}</math>); }</pre>	→	<pre>requires <math>x \mapsto [val : \_]</math>; ensures emp; copy_and_dispose(x){   local v;   <math>v := x \rightarrow val</math>;   dispose(x);   lock(<math>r_{c \mapsto [val : \_]}</math>);   <math>c \rightarrow val = v</math>;   unlock(<math>r_{c \mapsto [val : \_]}</math>); }</pre>
--	---	--

- $r$  is a lock with resource invariant  $c \mapsto [val : \_]$ , i.e., one cell  $c$  with field  $val$ .

Optimizations:

- The critical region is shortened.
- Memory is disposed as soon as possible.

# TemporalLocality

- temporal locality  $\triangleq$  time between two accesses to the same heap cell
- ↳ the smaller the better (no need to free/load processors's caches)

# TemporalLocality

- Intuition below:  $C$  and  $C''$  access the same part of the heap
- ↳ Execute them successively

$$\frac{\frac{\frac{\{\Xi\}C\{\Xi'\}}{\{\Xi \star \Theta\}C\{\Xi' \star \Theta\}} \text{ (Fr } \Theta)}{\{\Xi \star \Theta\}C; C'\{\Xi' \star \Theta'\}} \text{ (Seq)} \quad \frac{\frac{\{\Theta\}C'\{\Theta'\}}{\{\Xi' \star \Theta\}C'\{\Xi' \star \Theta'\}} \text{ (Fr } \Xi')}{\{\Xi' \star \Theta'\}C''\{\Xi'' \star \Theta''\}} \text{ (Fr } \Theta')}
 {\frac{\{\Xi \star \Theta\}C; C'; C''\{\Xi'' \star \Theta''\}}{\{\Xi \star \Theta\}C; C'; C''\{\Xi'' \star \Theta''\}} \text{ (Seq)}}$$

↓ TemporalLocality

$$\frac{\frac{\frac{\{\Xi\}C\{\Xi'\}}{\{\Xi \star \Theta\}C; C''\{\Xi'' \star \Theta''\}} \text{ (Seq)} \quad \frac{\{\Xi'\}C''\{\Xi''\}}{\{\Xi'' \star \Theta\}C'\{\Xi'' \star \Theta'\}} \text{ (Fr } \Xi')}
 {\frac{\{\Xi \star \Theta\}C; C''\{\Xi'' \star \Theta''\}}{\{\Xi \star \Theta\}C; C''; C'\{\Xi'' \star \Theta'\}} \text{ (Seq)}}$$



# Instantiating GenericOpt.: LateLocking

$$\begin{array}{c}
 \frac{\frac{\frac{\Xi_p \text{ is } x\text{'s resource invariant}}{\{\text{emp}\}\text{lock}(x)\{\Xi_p\}} \text{ (Lock)}}{\{\Xi_f\}\text{lock}(x)\{\Xi_p \star \Xi_f\}} \text{ (Frame } \Xi_f)}{\{\Xi_f\}\text{lock}(x); C'\{\Theta_p \star \Theta_f\}} \text{ (Seq)} \quad \frac{\frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Frame } \Theta_f)}{\{\Theta_a \star \Theta_f\}C'\{\Theta_p \star \Theta_f\}} \text{ (Seq)} \\
 \downarrow \text{LateLocking} \\
 \frac{\frac{\{\Theta_a\}C'\{\Theta_p\}}{\{\Theta_a \star \Xi_r\}C'\{\Theta_p \star \Xi_r\}} \text{ (Frame } \Xi_r)}{\{\Xi_f\}C'; \text{lock}(x)\{\Xi_p \star \Theta_p \star \Xi_r\}} \text{ (Seq)} \quad \frac{\frac{\frac{\Xi_p \text{ is } x\text{'s resource invariant}}{\{\text{emp}\}\text{lock}(x)\{\Xi_p\}} \text{ (Lock)}}{\{\Theta_p \star \Xi_r\}\text{lock}(x)\{\Xi_p \star \Theta_p \star \Xi_r\}} \text{ (Frame } \Theta_p \star \Xi_r)}{\{\Theta_p \star \Xi_r\}\text{lock}(x)\{\Xi_p \star \Theta_p \star \Xi_r\}} \text{ (Seq)}
 \end{array}$$

Guard:  $\Theta_f \Leftrightarrow \Xi_p \star \Xi_r$

↳ The guard means that command  $C'$  does not access  $x$ 's resource invariant:

- Better lock  $x$  after executing  $C'$ !

## Example (3)

```
requires tree(t); ensures emp;
disp_tree(t) {
  local i,j;
  if(t = nil){} else {
    i := t → l; j := t → r;
    disp_tree(i); disp_tree(j);
    dispose(t);
  }
}
```

→

```
requires tree(t); ensures emp;
disp_tree(t) {
  local i,j;
  if(t = nil){} else {
    i := t → l; j := t → r;
    dispose(t) ||
    (disp_tree(i) || disp_tree(j));
  }
}
```