Investigating the effects of cooperative vehicles on highway traffic flow homogenization: analytical and simulation studies

Julien Monteil

PhD Dissertation Defense

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Examining committee:

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Introduction



Cooperative vehicles = connected + autonomous vehicles?

- V2X communication channels (4G, WIFI...)
- In-vehicle sensors (embedded cameras, radars...)



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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Introduction



- V2X communication channels (4G, WIFI...)
- In-vehicle sensors (embedded cameras, radars...)



Future of traffic flow?



- Transition of a mixed traffic...
- Cooperative vehicles should relieve the driving task and adapt to safe drivers' behavior



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Context and motivations

Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Outline

Context and motivations

Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



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Context and motivations

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Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Automation and connection for vehicles

- Adaptive Driver assistance systems (ADAS) : Adaptive Cruise Control (ACC), collision avoidance systems, automated parking
- Autonomous vehicles : PROMETHEUS project, Google driverless car, Oxford car



- Platooning : PATH Automated Highway Systems, SARTRE project, NEDO driverless trucks
- Vehicular Ad hoc NETworks (VANET) for connected vehicles : toll collection, intersection warning, Cooperative ACC





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Context and motivations

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Stability analyses

State of the art

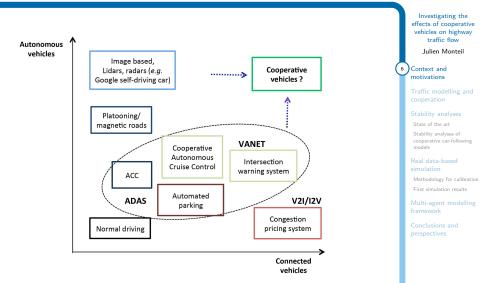
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibratior First simulation results

Multi-agent modelling framework

Towards cooperative vehicles



Sites for testing connected applications

- FOT, DRIVEC2X : methodology for implementation and evaluation on 7 European test sites
- Safety applications (traffic jam ahead, weather, obstacle warning), traffic efficiency applications (post crash warning) and selected infotainment (traffic information)



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Context and motivations

> Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework



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- Safety pilot, VTTI : large testbeds of connected vehicles in a real-life environment
- Focus on safety applications (crash warning, intersection management) and infrastructure assessment (pavement)

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Context and motivations

> Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework





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- Safety pilot, VTTI : large testbeds of connected vehicles in a real-life environment

Focus on safety applications (crash warning, intersection management) and infrastructure assessment (pavement)

Aim to evaluate the :

- efficiency of the applications, driver acceptance
- interoperability of dedicated wireless communications



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Context and motivations

> Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework







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8 Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusions and perspectives

Future situation : a mixed fleet made of cooperative vehicles and non-cooperative vehicles (normal drivers) on highways, with the goal to increase traffic flow safety.



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8 Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusions and perspectives

Future situation : a mixed fleet made of cooperative vehicles and non-cooperative vehicles (normal drivers) on highways, with the goal to increase traffic flow safety.

- 1. What physics to explain the formation of stop and go waves?
- 2. What information/data is relevant to exchange between cooperative vehicles?
- 3. How to use this information, how should cooperative vehicles behave?
- 4. How to deal with communication noises?
- 5. Is a mixed traffic made of cooperative and « normal »vehicles safer ?



Context and motivations

Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

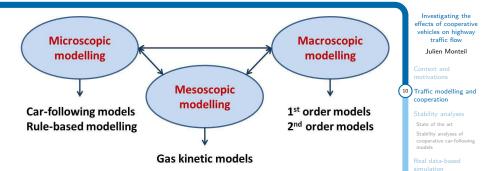
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

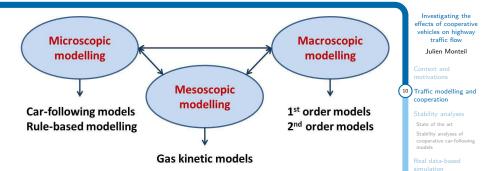
Modelling scales



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- Microscopic : particles with specificities $(x_n(t), LN_n(t))$
- Mesoscopic : probability density function f(x, V, t)
- Macroscopic : traffic density k(x, t), speed V(x, t), flow $\rho(x, t)$

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Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

11 Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Time discrete models



Vehicle n+1

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Stimulus-response models : Pipes GM-1 (1953), Greenberg GM-3 (1959), Van Aerde (1995), RPA (2009) models

GM-1:

$$\ddot{x}_n(t+\tau) = \alpha \cdot [\dot{x}_{n+1}(t) - \dot{x}_n(t)]$$

Other types : Gipps (1976), Newell (1961, 2002) Simplified Newell (2002) :

$$x_n(t+\tau) = x_{n+1}(t) - d$$



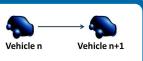
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Time continuous models

► General form :

$$\dot{x}_n = \frac{dx_n}{dt} \ddot{x}_n = f(\dot{x}_n, \Delta x_n, \Delta \dot{x}_n)$$





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Context and motivations

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Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Time continuous models

► General form :

$$\dot{x}_n = \frac{dx_n}{dt} \ddot{x}_n = f(\dot{x}_n, \Delta x_n, \Delta \dot{x}_n)$$

Examples : OVM (Bando et al., 1995), OVRV model (Jiang) et al., 2001), IDM (Treiber et al., 2000), IOVM (Treiber and Kesting, 2013)

OVRV:

$$f(\dot{x}_n, \Delta x_n, \Delta \dot{x}_n) = -\frac{1}{\tau} \dot{x}_n + \frac{1}{\tau} V(\Delta x_n) + \eta \Delta \dot{x}_n$$



Vehicle n+1



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Traffic modelling and cooperation

State of the art

Methodology for calibration



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Context and motivations

13) Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

ACC model : Kesting et al. (2010)

- ► IDM+CAH model for lane changing maneuvers
- Implemented on motorways



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Context and motivations

¹³Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

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Multi-anticipation framework : Ge *et al.* (2006), Hoogendoorn *et al.* (2006), Treiber *et al.* (2006)

- Physical behavior
- CACC framework





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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibratior First simulation results

Multi-agent modelling framework

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- Physical behavior
- CACC framework

Vehicle n Vehicle n+1 Vehicle n+2 Vehicle n+3

Flocking framework : Reynolds (1987), Olfati-Saber (2006)

- Behaviors of groups of particles in 3D
- Algorithms for speed homogenization and collision avoidance



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Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Modelling choice for future developments



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14 Traffic modelling and cooperation

State of the art

Methodology for calibration

Time continuous models







Modelling choice for future developments

Time continuous models





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Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusions and perspectives

$\ddot{x}_n = f(\dot{x}_n, \Delta x_n, \Delta \dot{x}_n)$

Why?

- Empirical models close to ground truth traffic
- Continuous formulation close to communication issues
- Favor stability analyses



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Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



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Context and motivations

Traffic modelling and cooperation

15 Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Stability criteria of traffic flow



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

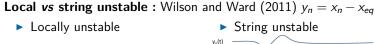
16

Stability analyses of cooperative car-following models

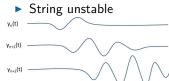
Real data-based

Methodology for calibration First simulation results

Multi-agent modelling framework







Stability criteria of traffic flow



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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

16

Stability analyses of cooperative car-following models

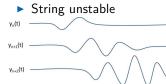
Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

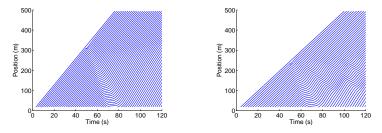
Conclusions and perspectives



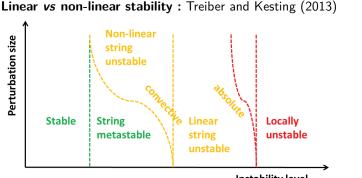


String convective *vs* **string absolute :** Treiber and Kesting (2012)

Local vs string unstable : Wilson and Ward (2011) $y_n = x_n - x_{eq}$



Stability criteria of traffic flow



Instability level

Usual approach : $\Delta y_n(t) = Y_0 e^{i(kn+zt)}$, $z = -i\omega$, $k \in [0,\pi]$

- Derivation of analytical conditions for linear string (small perturbations) and local stability
- In traffic, only convective instabilities are observed
- Forward multi-anticipation increases stability



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

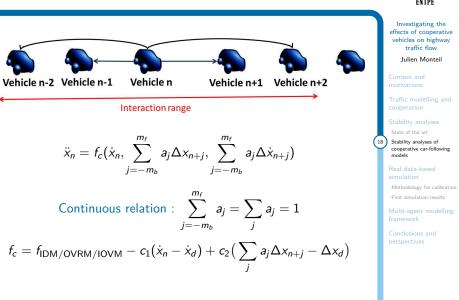
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Stability analyses Presentation of the cooperative car-following model



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Linear stability analyses $_{\text{Contributions }1/3}$

First order development : $\Delta \ddot{y}_n = f_1 \Delta \dot{y}_n + f_2 \sum_j a_j (\Delta y_{n+j+1} - \Delta y_{n+j}) + f_3 \sum_j a_j (\Delta \dot{y}_{n+j+1} - \Delta \dot{y}_{n+j}),$ with $f_1 = \partial f / \partial \dot{x} (\dot{x}_{eq}, \Delta x_{eq}, 0),...$

Dispersion relation : $z^{2} - z (f_{1} + f_{3} (e^{ik} - 1)) - f_{2} (e^{ik} - 1) = 0$



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

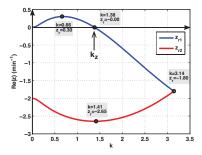
Methodology for calibration First simulation results

Multi-agent modelling framework

Linear stability analyses Contributions 1/3

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Dispersion relation : $z^{2} - z (f_{1} + f_{3} (e^{ik} - 1)) - f_{2} (e^{ik} - 1) = 0$



Let us remind $\Delta y_n(t) = Y_0 e^{i(kn+zt)}$. Growing perturbations are of the long wavelength type.

 $\begin{array}{l} \mbox{Result} : \mbox{without cooperation} \\ (a_0 = 1, \ a_{j \neq 0} = 0), \ k_z = \\ \mbox{arccos} \, \big(\frac{f_1^2 + 2f_3^2 - 3f_1f_3 - f_2}{f_2 + 2f_3^2 - f_3f_1} \big) \end{array}$



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

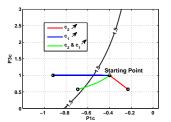
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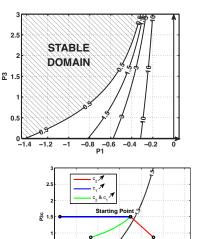
Linear stability analyses Contributions 2/3



Analytical results at long wavelengths

- 1. Bilateral traffic brings stability
- Linear control term c₁ brings stability





-0.6 P1c

-0.4 -0.2 0

0.

-1 -0.8

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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Linear stability analyses Contributions 3/3



Root locus : graphical tool to evaluate stability at all wavelengths.



Investigating the

effects of cooperative

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

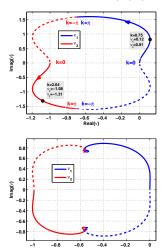
Real data-based simulation

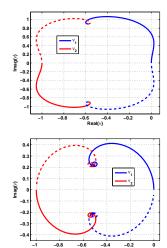
Methodology for calibration First simulation results

Multi-agent modelling framework

Linear stability analyses Contributions 3/3

Root locus : graphical tool to evaluate stability at all wavelengths.
▶ Influence of forward multi-anticipation (v = z/f₁) : cosine window, m = 1, 3, 4, 6







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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

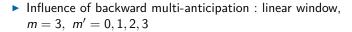
Stability analyses of cooperative car-following models

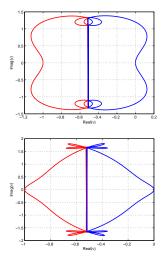
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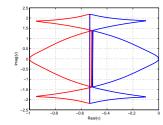
Methodology for calibration First simulation results

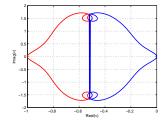
Multi-agent modelling framework

Linear stability analyses Contributions 3/3











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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

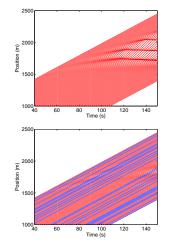
Real data-based simulation

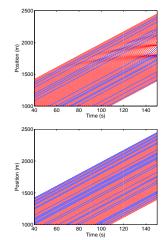
Methodology for calibration First simulation results

Multi-agent modelling framework

The needed percentage to remove instabilities depends on :

- the traffic state,
- the location of the perturbation.







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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Weakly non-linear stability analyses Contributions 1/2



Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

24

Stability analyses of cooperative car-following models

Real data-based

Methodology for calibration First simulation results

Multi-agent modelling framework

Time continuous CF (cooperative or not) have a Korteweg de Vries (Korteweg and de Vries, 1895; Nagatani, 2001) development for the perturbation growth.

Series of mathematical developments to get :

- ▶ the general expression of the KdV equation near the string stability surface for cooperative and non-cooperative traffic : $C_1 \partial_X^3 R + C_2 R \partial_X R + C_3 \partial_T R = 0$,
- a condition over the sign of the shock wave (same sign as C_2),
- the amplitude of the shock wave.

$$\Delta y_n(t) = \operatorname{sgn}(C_2) \mathbf{A} \operatorname{sech}^2 \left[\sqrt{\frac{|C_2| \mathbf{A}}{12C_1}} \left(n - \alpha_s t \right) \right]$$



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Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

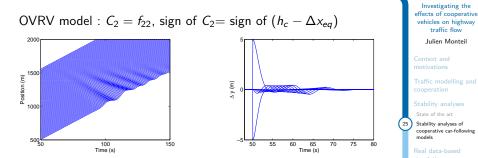
Methodology for calibration First simulation results

Multi-agent modelling framework

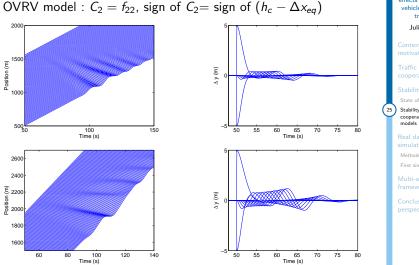
Weakly non-linear stability analyses Contributions 2/2



Methodology for calibration



Weakly non-linear stability analyses Contributions 2/2



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State of the art

Stability analyses of cooperative car-following

Stability analyses

Linear stability analyses

- Extension to bilateral multi-anticipation with linear control terms
- Use of the root locus graphical tool to design cooperative strategies

Weakly non-linear stability analyses

- KdV development
- Validation of : sign of the perturbation leading edge, amplitude value



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Stability analyses

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Needs of further investigation

- Insights from a deterministic approach
- Variability of drivers behavior?



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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework



Context and motivations

Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

27 Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Trajectory-based data calibration

Significant research in recent years

- Trajectory-based datasets (e.g. NDS, NGSIM, MOCoPo)
- Calibration methodology (MULTITUDE COST action)



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

28

Methodology for calibration

irst simulation results

Multi-agent modelling framework

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Selected dataset

- NGSIM dataset, US 101, Los Angeles
- Morning peak time, 3 left lanes



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

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Methodology from filtering to sampling

- Filtering trajectories
- Robust calibration for each leader-follower pair
- Statistical analyses of dependencies
- Discussion of sampling methods



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

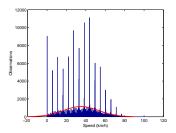
Methodology for calibration

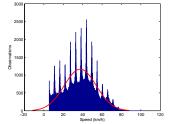
irst simulation results

Multi-agent modelling framework

Filtering trajectories

- Issues : spikes from post processing images
- Flat magnitude filter in its passband : Butterworth (order 4) (Punzo and Montanino, 2013).







Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

20

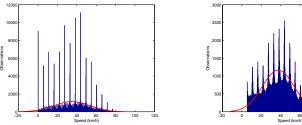
Methodology for calibration

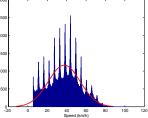
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State of the art

Methodology for calibration

Consequences on calibration

- Calibration objective : for each leader, match observed speed trajectory with the modelled trajectory
- Focus on speed trajectories as Measure of Performance (MoP)

Robust calibration Methodology 1/2

Statistical meaning of the Goodness of Fit (GoF) test (James, 2006)

$$\chi^2 = \sum_{i,j} (x_{i,\text{obs}} - y_i(a)) \Gamma_{ij}^{-1} (x_{j,\text{obs}} - y_j(a))$$

 Optimization procedure : genetics algorithms with penalty function (Kesting and Treiber, 2008)



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

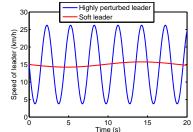
Robust calibration Methodology 1/2

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- Optimization procedure : genetics algorithms with penalty function (Kesting and Treiber, 2008)
- Selection of appropriate trajectories to be calibrated (filter the standard deviation of leaders speeds) to stimulate all parameters of the systems (except for V_{max})

An example on the importance of inputs





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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

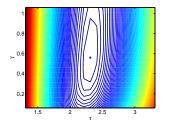
Methodology for calibration

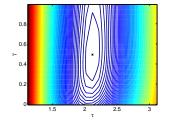
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Multi-agent modelling framework

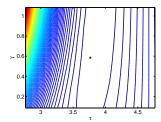
Robust calibration Methodology 2/2

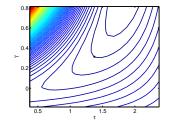
IOVM : calibration with/without added noise for perturbed input





Calibration with/without added noise for soft input







Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

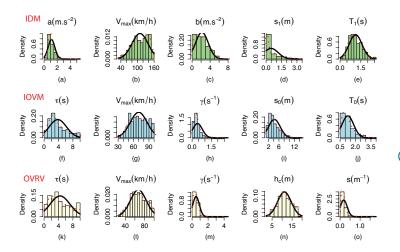
Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

Statistical dependencies Distributions



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

32

Methodology for calibration

irst simulation results

Multi-agent modelling framework

Statistical dependencies Analyses and correlation

Methods for correlation analyses

- The normality hypothesis does not stand for all parameters marginal distributions (based on the Shapiro-Wilk test)
- The Pearson test should be completed by the Kendall and Spearman methods, which account for the discordance and concordance values
- Principal Component analysis for linear correlation between parameters
- Observed correlations oppose reactive to passive driving styles



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

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Objectives to understand the correlation between parameters in order to

- Estimate joint distributions while preserving the correlation structure
- Sample a realistic traffic from the estimated joint distributions

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traffic flow Julien Monteil

Context and

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

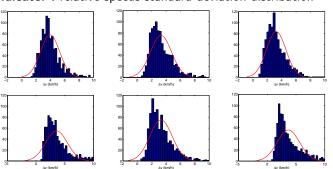
Real data-based simulation

(33

Methodology for calibration

Multi-agent modelling framework

Discussion of sampling methods



Indicator : relative speeds standard deviation distribution

Comparison of **5** sampling strategies of the OVRV parameters to the (a) ground truth : (b) random, (c) random with correlation, (d) from multivariate normal distribution, (e) from multi-variate normal distribution of only correlated parameters, (f) from Kernel density estimation.



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

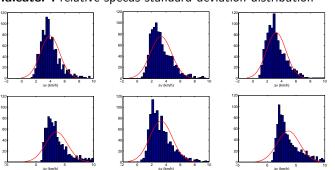
Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

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Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

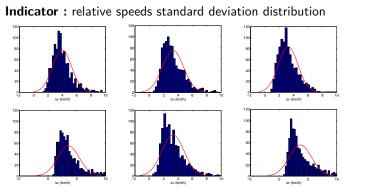
Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

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Investigating the effects of cooperative vehicles on highway traffic flow

FSTTAR

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

irst simulation results

Multi-agent modelling framework

Realistic traffic simulation $_{\mbox{\scriptsize Settings}}$



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

35 First simulation results

Multi-agent modelling framework

Realistic traffic simulation Settings

Simulation choices

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- IDM parameters sampled from random sampling with correlation (« mean »traffic linearly unstable)
- Lane-changing model : MOBIL model (Treiber and Kesting, 2009)
- Numerical scheme : mixed first order second order Euler scheme
- Cooperative law : cosine window, bilateral law with tuned linear control terms



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation Settings

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- ' Scenario
 - 6 minutes simulation, 200 vehicles per lane, 3 lanes, open boundaries
 - ▶ Perturbations from : initial conditions (global steady-state ≠ individual steady-state), regular « manual »perturbations, aggressive lane changes (set to 25%).
 - Graphical interface : GUIDE



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation Settings

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Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

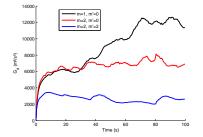
Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation Evolution of the group disagreement value





75% of equipped vehicles

- Positive impact of bilateral multi-anticipation
- Negative impact of a too high number of leaders/followers

Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

36

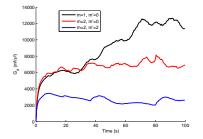
Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation Evolution of the group disagreement value



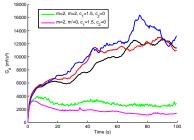


25% of equipped vehicles

- Positive impact of added linear control
- ▶ Bilateral multi-anticipation ≈ forward multi-anticipation

75% of equipped vehicles

- Positive impact of bilateral multi-anticipation
- Negative impact of a too high number of leaders/followers



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

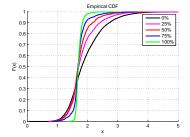
Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation





Evolution of the PET (s)

 Progressive homogenization with increasing % of cooperative vehicles Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

37

Methodology for calibration

First simulation results

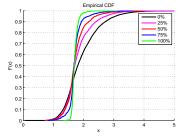
Multi-agent modelling framework

Realistic traffic simulation



Investigating the

effects of cooperative



Conclusions

For this traffic configuration, for a well tuned cooperative car-following model, assuming a prior knowledge of the drivers behavior variability, 20% of cooperative vehicles remove instabilities !

Evolution of the PET (s)

 Progressive homogenization with increasing % of cooperative vehicles vehicles on highway traffic flow Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

First simulation results

Multi-agent modelling framework

Realistic traffic simulation

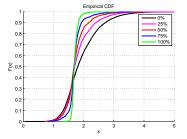


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effects of cooperative vehicles on highway

traffic flow

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Evolution of the PET (s)

 Progressive homogenization with increasing % of cooperative vehicles

Conclusions

- For this traffic configuration, for a well tuned cooperative car-following model, assuming a prior knowledge of the drivers behavior variability, 20% of cooperative vehicles remove instabilities !
- No more than 2 leaders/followers are required !
- How to deal with communication noises, to detect unreliable sensors?

Stability analyses State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

First simulation results

Multi-agent modelling framework



Context and motivations

Traffic modelling and cooperation

Stability analyses

Real data-based simulation

Multi-agent modelling framework

Conclusions and perspectives



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

38 Multi-agent modelling framework

Why multi-agent systems?

- Partial and noisy perception of the environment
- Flexibility of interactions
- Idea of self-organization



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

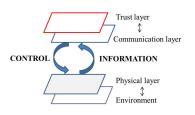
Methodology for calibration First simulation results

39 Multi-agent modelling framework

Why multi-agent systems?

- Partial and noisy perception of the environment
- Flexibility of interactions
- Idea of self-organization

Multi-agent structure with trust layer (Nguyen Vu et al., 2012)



- ► Physical layer → car-following rules
- ► Communication layer → proximity and reliability rules
- Trust layer \rightarrow sensors network



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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

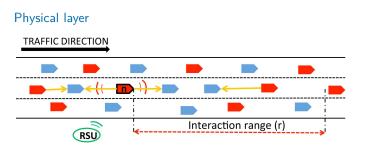
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

39 Multi-agent modelling framework

Multi-agent framework



- Cooperative IDM model
- Limited interaction range $(r = 4 \cdot \Delta x_{eq})$: avoid scaling effects for low coverage
- Limited number of information data points (m = 2 m' = 2) : avoid loss of reactivity to the leader trajectory



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

40 Multi-agent modelling framework

Multi-agent framework

Communication layer

 Cooperative coefficients as a multiplication (proximity×trust) rule

$$a_{ij} = \frac{\mathsf{p}_{ij} \cdot T_{ij}}{\sum_{l} \mathsf{p}_{il} T_{il}}$$

- 2. Required decreasing coefficients with distance
- Required minimum trust in the relative information to the leader
- 4. Multiplication of control gains by self-trust



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

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Trust layer

1. Relation between error measurements and direct trust

$$DT_{ij} = \max(1 - m_{ij}\sigma, 0)$$

- 2. Computation of an indirect trust
- 3. Update rule for the trust

$$T_{ij} = \frac{T_{ii}DT_{ij} + IT_{ij}}{T_{ii} + 1}$$

4. Update rule for the self-trust

Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Multi-agent framework Static trust layer

- Hypothesis : each vehicle has a prior knowledge of the quality of its sensors
- ► Scenario : → error measurement for 25% and 100% of cooperative vehicles



Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

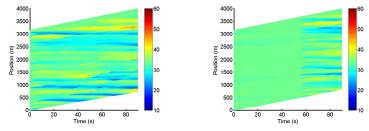
Real data-based simulation

Methodology for calibration First simulation results

42 Multi-agent modelling framework

Multi-agent framework Static trust layer

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- High robustness of the cooperative strategy to error measurements
- Threshold corresponding to the required minimum trust in the relative information to the leader



Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

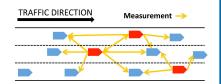
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

2) Multi-agent modelling framework

- Hypothesis : each vehicle senses its nearest neighbors
- Scenario : detection of unreliable sensors ?





Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

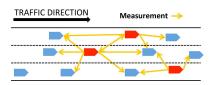
Real data-based simulation

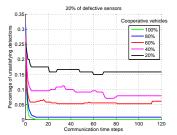
Methodology for calibration

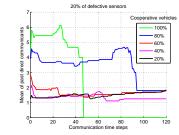
irst simulation results

43) Multi-agent modelling framework

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Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

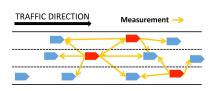
Real data-based simulation

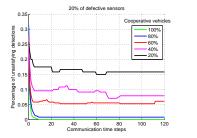
Methodology for calibration

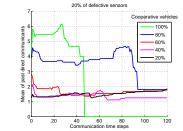
First simulation results

43 Multi-agent modelling framework

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Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration

First simulation results



Conclusions and perspectives

 \rightarrow Fundamental influence of direct information exchanges



- Context and motivations
- Traffic modelling and cooperation
- Stability analyses
- Real data-based simulation
- Multi-agent modelling framework
- Conclusions and perspectives



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusion

Performed stability analyses provided

- a complete framework for linear stability analyses of cooperative car-following models at all wavelengths
- new results in the weakly non-linear domain



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusion

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Parameters identification of car-following models

- was done through a robust calibration process
- lead to a dicussion on statistical dependencies and sampling of parameters



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Conclusion

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Simulations were conducted and a multi-agent modelling framework was designed, enabling

- to demonstrate the high potential of cooperation in traffic flow, even with low coverage of cooperative vehicles
- sensitivity analyses on control and communication strategies
- the real time detection of unreliable sensors



Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyse

State of the art

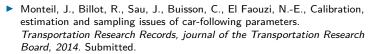
Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Publications



- Sau, J., Monteil, J., Billot, R., El Faouzi, N.-E., Design of cooperative car following models using root locus analysis. *Tranportmetrica B* : *Tranport Dynamics*. Submitted.
- Monteil, J., Billot, R., Sau, J., El Faouzi, N.-E., Linear and Weakly Non-linear Stability Analyses of Cooperative Car Following Models. *IEEE Transactions on Intelligent Transportation Systems*, 2013.
- Monteil, J., Nantes, A., Billot, R., El Faouzi, N.-E., Microscopic Cooperative Traffic Flow : calibration and simulation based on a NGSIM dataset. *IET Intelligent Transport Systems, 2013.*
- Monteil, J., Billot, R., Sau, J., Armetta, F., Hassas, S., El Faouzi, N.-E., Cooperative highway traffic : multi-agent modelling and robustness assessment to local perturbations. *Transportation Research Records, journal of the Transportation Research Board, 2013.*
- Monteil, J., Billot, R., El Faouzi, N.-E., Des véhicules coopératifs pour une gestion dynamique du trafic : approche théorique et simulation. *Revue Recherche Sécurité Transports, 2012.*

Investigating the effects of cooperative vehicles on highway traffic flow

Julien Monteil

Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Publications Conference publications

- Monteil, J., Billot, R., Gueriau, M., Armetta, F., Hassas, S., El Faouzi, N.-E., A three-layer multi-agent framework for sensor reliability issues : application to cooperative highway traffic. AAAI 2014.
- Monteil, J., Billot, R., Sau, J., Buisson, C., El Faouzi, N.-E., Calibration, estimation and sampling issues of car-following parameters. 93rd Annual Meeting of Transportation Research Board (TRB) 2014, Washington D.C., USA.
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Investigating the effects of cooperative vehicles on highway traffic flow

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Context and motivations

Traffic modelling and cooperation

Stability analyses

State of the art

Stability analyses of cooperative car-following models

Real data-based simulation

Methodology for calibration First simulation results

Multi-agent modelling framework

Perspectives of future work

Towards experimentation

- Online estimation of car-following parameters
- Incorporation of smoother acceleration patterns, *e.g.* in reaction to lane changes



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Developments of the presented work include

- Stability analyses of time discrete models
- Methodology for robust sampling of parameters
- Design of cooperative lane changing strategies, *e.g.* in the case of a necessary lane change
- Extension to optimal/robust control towards a desired stable traffic, e.g. in response to changing weather conditions



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Open questions

- Participation of in-vehicle sensors to the network knowledge?
- Importance of Road Side Units?



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Thank you



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49 Conclusions and perspectives

Thank you for your attention