



# SIMD-aware word length optimization for floating-point to fixed-point conversion targeting embedded processors

Ali Hassan El Moussawi

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présentée par

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# SIMD-aware Word Length Optimiza- tion for Floating- point to Fixed-point Conversion target- ing Embedded Pro- cessors

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**le 16/12/2016**

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*Certes, la science guide, dirige et sauve;  
l'ignorance égare, trompe et ruine.*



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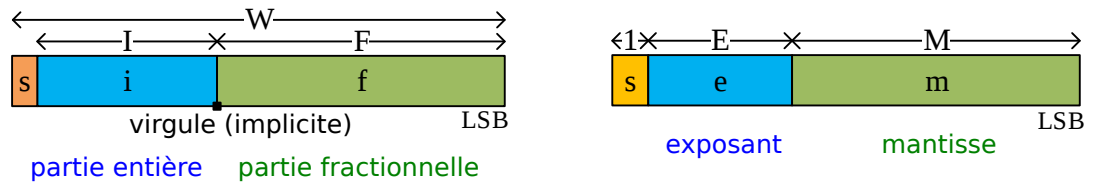


# Résumé en Français

Les processeurs embarqués sont soumis à des contraintes strictes de coût, consommation électrique et performance. Afin de limiter leur coût et/ou leur consommation électrique, certains processeurs ne disposent pas de support matériel pour l'arithmétique à virgule flottante.

D'autre part, les applications dans plusieurs domaines, tel que le traitement de signal et la télécommunication, sont généralement spécifiées en utilisant l'arithmétique à virgule flottante, pour des raisons de simplicité. Cette implémentation prototype est ensuite adaptée/optimisée en fonction de l'architecture cible.

Porter de telles applications sur des processeurs embarqués sans support matériel pour l'arithmétique à virgule flottante, nécessite une émulation logicielle, qui peut sévèrement dégrader les performances de l'application. Pour éviter cela, l'application est convertie pour utiliser l'arithmétique à virgule fixe, qui a l'avantage d'être plus efficace à implémenter sur des unités de calcul entier. Les deux représentations, à virgule flottante et à virgule fixe sont illustrées dans la fig. 1. La conversion de virgule flottante en virgule fixe est une procédure délicate qui implique



Nombre représenté:  $\text{sig} * 2^{-F}$   $(-1)^s * \text{mantisse} * 2^{\text{exposant}}$

Figure 1 – Comparaison des représentations à virgule flottante (droite) et à virgule fixe (gauche).

des compromis subtils entre performance et précision de calcul. Elle permet, entre autre, de réduire la taille des données au prix d'une dégradation de la précision de calcul. En effet, utiliser des opérations à virgule fixe, tout en gardant la précision complète des résultats, nécessite une augmentation considérable des tailles de mots des données. Par exemple, le résultat exact d'une multiplication entre deux nombres de taille  $w$ , nécessite une taille de  $2w$ . Cette augmentation de la taille de mots peut dépasser la taille maximale supportée par le processeur cible, nécessitant ainsi une émulation logicielle d'opérateurs de taille plus grande, qui peut aussi bien dégrader la performance de l'application. Afin d'éviter cela, les tailles des données (et des résultats des opérations) sont réduites en appliquant des quantifications, qui correspondent à éliminer les bits de poids faibles. Ces opérations de quantification introduisent des erreurs de calcul, appelées

*erreurs de quantifications*, qui se propagent dans le système et peut engendrer une erreur importante en sortie, dégradant ainsi la précision du résultat. En règle générale, plus la quantification est grande (i.e. plus la taille des données est réduite), plus la précision est faible mais meilleur est la performance. Il existe donc un compromis entre précision de calcul et performance.

Par ailleurs, la plupart des processeurs embarqués fournissent un support pour le calcul vectoriel de type *SIMD* ("Single Instruction Multiple Data") afin d'améliorer la performance. En effet, cela permet l'exécution d'une opération sur plusieurs données simultanément, réduisant ainsi le temps d'exécution. Cependant, il est généralement nécessaire de transformer l'application pour exploiter les unités de calcul vectoriel. Cette transformation de vectorisation est sensible à la taille des données; plus leurs tailles diminuent, plus le taux de vectorisation augmente. Il apparaît donc un autre compromis entre vectorisation et tailles de données.

En revanche, la vectorisation ne conduit toujours pas à une amélioration de performance, elle peut même la dégrader ! En fait, afin d'appliquer une opération vectorielle, il faut d'abord agréger ou *compacter* les données de chacun des opérandes pour former un vecteur, qui correspond en générale à un registre SIMD. De même, il faut décompacter les données afin de les utiliser séparément, comme le montre la fig. 2. Ces opérations de (dé)compactage peuvent engendrer

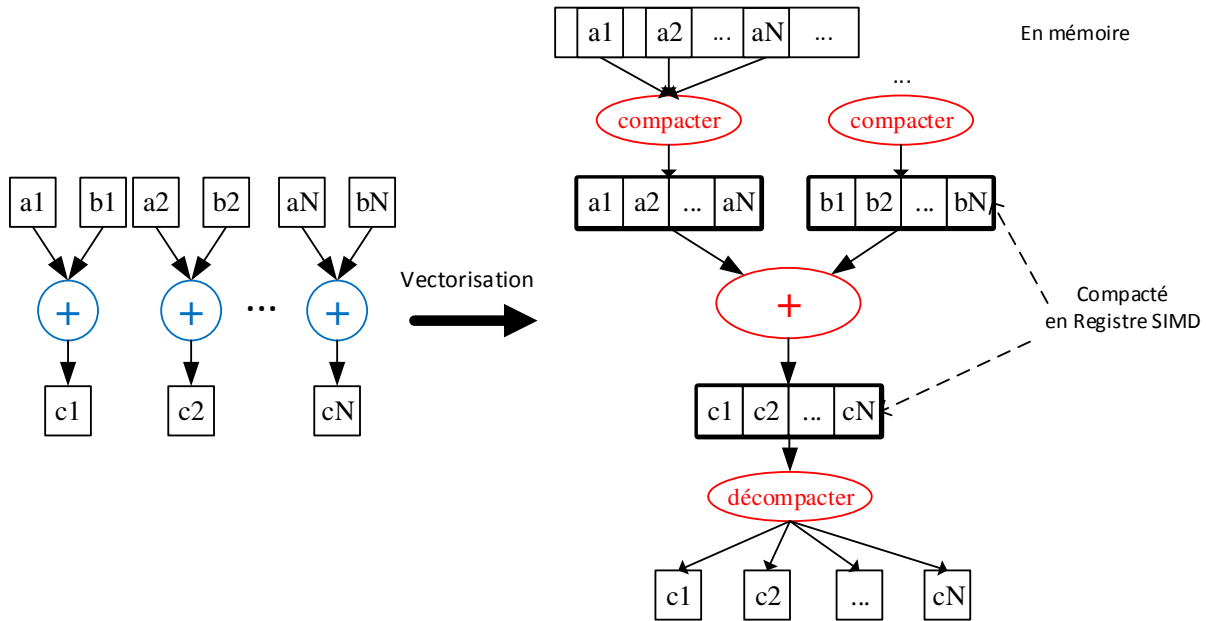


Figure 2 – Illustration de la transformation de vectorisation remplaçant  $N$  opérations scalaires par une seule opération SIMD plus les opérations de (dé)compactage.

un surcoût important dans le cas où les données sont mal organisées en mémoire. Du coup, afin d'améliorer efficacement la performance, la transformation de vectorisation doit prendre en considération ce surcoût.

La conversion de virgule flottante en virgule fixe et la vectorisation sont deux transformations délicates qui nécessitent un temps de développement très élevé. Pour remédier à ça et réduire les délais de mise sur le marché des applications, une multitude de travaux ont ciblé l'automatisation

(complète ou partielle) de ces transformations. Dans l'état de l'art, on trouve des méthodologies permettant la conversion de virgule flottante en virgule fixe, tel que [51, 26, 64, 85]. Ces méthodologies comportent en générale trois parties principales :

- La détermination des tailles des parties entières. En se basant soit sur des simulations, ou en utilisant des méthodes analytiques telle que l'arithmétique d'intervalles et l'arithmétique affine.
- La détermination des tailles des mots. Cela fait en générale l'objet d'une optimisation exploitant le compromis entre précision et performance, connue sous le nom "*Word Length Optimization*" ou WLO (optimisation de taille de mots). Pour ce faire, des méthodes permettant l'estimation de la précision de calcul et la performance, d'une implémentation à virgule fixe, sont nécessaires. Plusieurs méthodes ont été proposées.
- La génération de code à virgule fixe [50].

D'autre part, on trouve également des méthodologies permettant l'exploitation des unités de calcul SIMD, entre autre, les techniques d'extractions du parallélisme au niveau du bloque de base, connues sous le nom "*Superword Level Parallelism*" ou SLP (Parallélisme au niveau du super-mot) introduit en 2000 par LARSEN et AMARASINGHE [69]. Ces méthodes ont pour objectif de trouver des groupes d'opérations, dans un bloque de base, qui peuvent être replacer par des opérations SIMD. Un tel groupe, appelée groupe SIMD, doit contenir des opérations, indépendantes, du même type (addition, multiplication, ...) et traitant des données de même taille. Le but des algorithmes d'extraction du SLP [69, 125, 78] est de trouver la « meilleure » solution de groupage qui permet d'améliorer la performance en tenant en compte le surcoût lié aux opérations de (dé)compactage.

Cependant, dans l'état de l'art, ces deux transformations sont considérées indépendamment, pourtant elles sont fortement liées. En effet, WLO détermine la taille des données qui affectent directement l'espace de recherche du SLP, et par conséquence la performance de la solution trouvée. Si WLO n'est pas conscient des contraintes d'extraction du SLP et du surcoût associé, il sera incapable d'estimer correctement l'impacte de ces décisions sur la performance finale de l'application (après avoir appliquer la conversion en virgule fixe et l'extraction du SLP). Par conséquence, il sera incapable d'exploiter efficacement le compromis enter précision et performance. Afin de mieux exploiter ce compromis, WLO doit prendre en considération SLP, alors que ce dernier ne peut pas procéder sans avoir une connaissance sur les tailles des données. Ce problème d'ordonnancement de phase est illustré par la fig. 3.

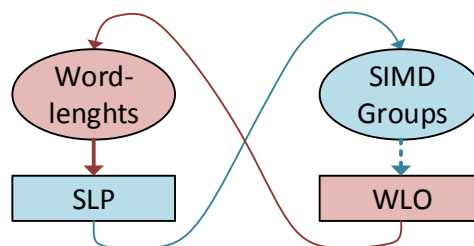


Figure 3 – Problème d'ordonnancement de phase entre WLO et SLP.

Dans ce contexte, on propose dans un premier temps un algorithme amélioré pour l'extraction du SLP. On se base sur un algorithme de l'état de l'art proposé en 2012 par LIU et al, on l'analyse soigneusement pour déterminer ses faiblesses puis on propose des améliorations pour y remédier. L'algorithme proposée est ensuite implémenté dans une plateforme de compilation source-à-source, [Generic Compiler Suite \(Gecos\)](#)[38], ainsi que l'algorithme de référence, afin de valider notre approche. Les résultats expérimentaux, extraits sur un ensemble de neuf applications de tests et ciblant plusieurs processeurs embarqués, montrent une amélioration claire apportée par notre algorithme.

Ensuite, on propose une nouvelle technique permettant l'application conjointe, de la conversion de virgule flottante en virgule fixe et de l'extraction du SLP. Au contraire des méthodologies de l'état de l'art, cette nouvelle technique permet de mieux exploiter le compromis entre la précision de calcul et la performance d'une application, ciblant des processeurs embarqués avec jeux d'instructions SIMD sans support matérielle pour l'arithmétique à virgule flottante. Cette approche consiste à combiner un algorithme d'extraction du SLP conscient de la précision de calcul, avec un algorithme de WLO conscient des opportunités de groupage SLP et du surcoût associé. Pour résoudre le problème d'ordonnancement de phases présenté précédemment, on a adapté l'algorithme d'extraction du SLP proposé, afin de relâcher les contraintes liées à la tailles des données. De cette façon, l'extraction du SLP peut désormais démarrer sans avoir à attendre le résultat du WLO. l'algorithme d'extraction du SLP est également conscient de la contrainte sur la précision de calcul, imposée par l'utilisateur. Cela permet d'éviter de sélectionner des groupes SIMD qui sont pas réalisable sans violer la contrainte de précision. Les groupes SIMD choisis, sont ensuite utilisés pour "guider" la sélection des tailles de mots par l'algorithme de WLO. La fig. 4 illustre cette approche. On implémente cette approche dans [Gecos](#) sous forme d'un flot

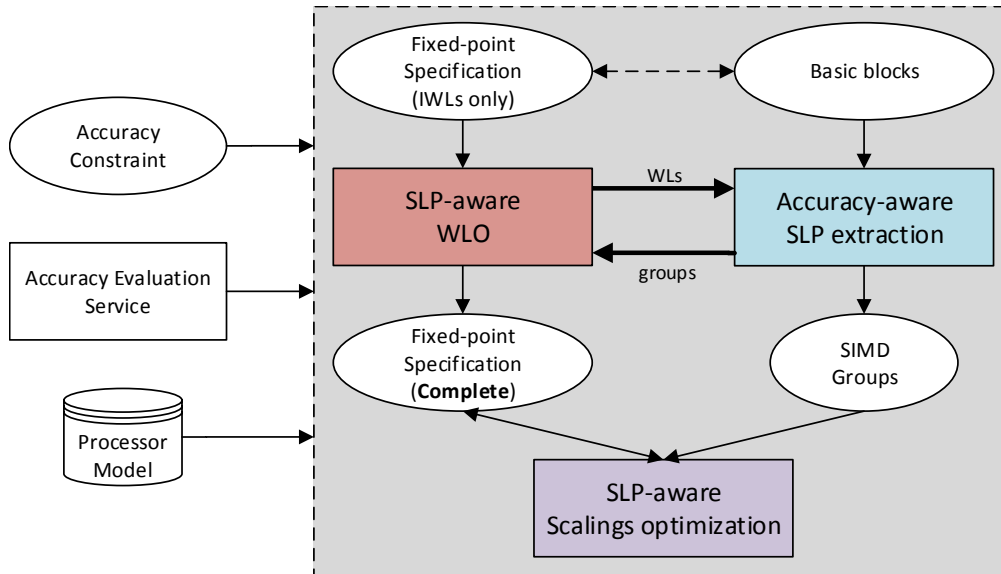


Figure 4 – Illustration de l'approche proposée.

de compilation source-à-source complètement automatisé. Afin de montrer la validité de notre

approche, on la compare contre une approche classique appliquant indépendamment, d'abord la conversion de virgule flottante en virgule fixe, ensuite l'extraction du SLP, qu'on implémente également dans [Gecos](#). On teste les deux flots sur plusieurs processeurs embarqués. Les résultats confirment l'efficacité de notre approche, dans l'exploitation du compromis entre performance et précision.





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# Glossary

**API** Application Programming Interface.

**DAG** Directed Acyclic Graph.

**DFG** Data Flow Graph.

**DLP** Data Level Parallelism.

**DSP** Digital Signal Processor.

**FWL** Fractional Word Length.

**GeCos** Generic Compiler Suite.

**HLS** High-Level Synthesis.

**HP** HAWLETT-PACKARD.

**IR** Intermediate Representation.

**ISA** Instruction Set Architecture.

**IWL** Integer Word Length.

**KIT** KARLSRUHE INSTITUTE OF TECHNOLOGY.

**LSB** Least Significant Bit.

**LTI** Linear Time-Invariant.

**MIS** Multimedia Instruction Set.

**MMX** Matrix Math eXtension.

**MSB** Most Significant Bit.

**PFCG** Pack Flow and Conflict Graph.

**SCoP** A loop nest in which all loop bounds, conditionals and array subscripts are affine functions of the surrounding loop iterators and parameters.

**SFG** Signal Flow Graph.



**SGG** Statement Grouping Graph.

**SIMD** Single Instruction Multiple Data.

**Simdization** The process of converting scalar instructions in a program into equivalent [SIMD](#) instructions.

**SLP** Superword Level Parallelism.

**SQNR** Signal-to-Quantization-Noise Ratio.

**SWP** Sub-word Level Parallelism.

**TI** TEXAS INSTRUMENTS.

**VLIW** Very Long Instruction Word.

**VP** Variable Pack.

**VPCG** Variable Pack Conflict Graph.

**WLO** Word Length Optimization.

# Chapter 1

## Introduction

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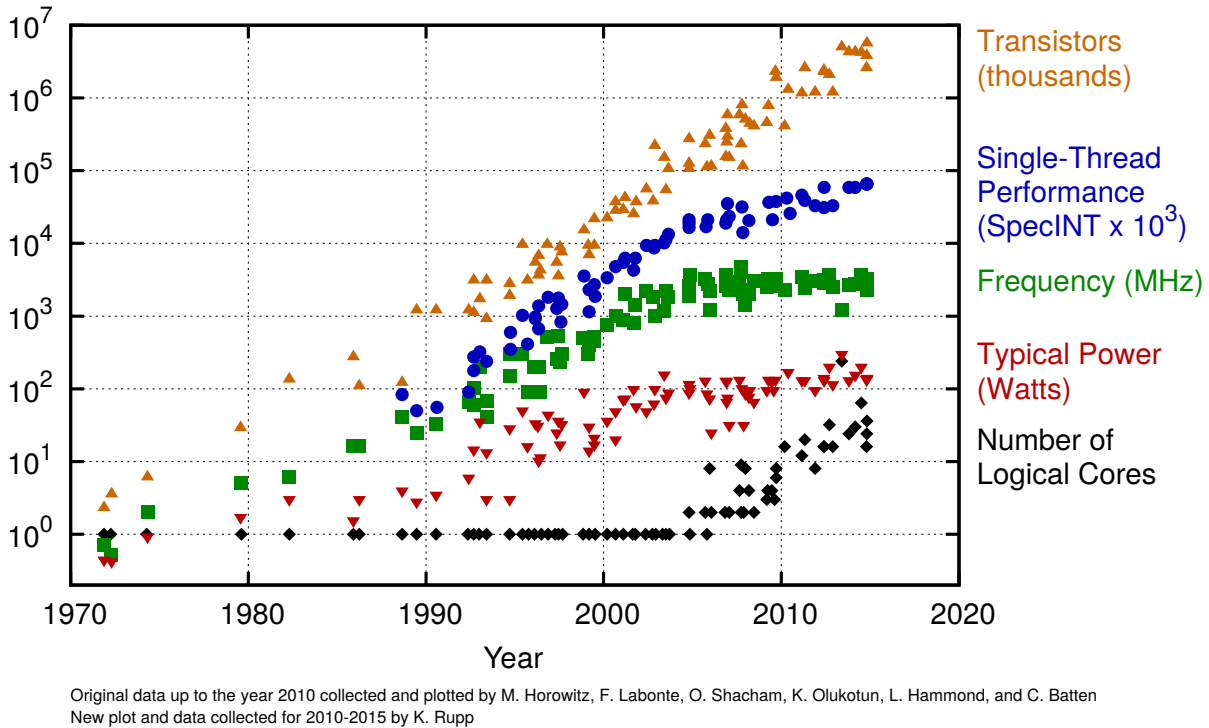


Figure 1.1 – CPU trend over the last 40 years. Published by K. Rupp at [www.karlrupp.net/2015/06/40-years-of-microprocessor-trend-data](http://www.karlrupp.net/2015/06/40-years-of-microprocessor-trend-data)

## 1.1 Context and Motivations

Ever since the first transistor computers appeared in the late '50s, manufacturing technologies kept continuously improving, allowing a steady exponential growth of the transistor count that can be integrated into a single die. This improvement rate was early observed by GORDON MOORE in the mid '60s, when he predicted that the transistor density in an integrated circuit would double every two years. This has later led to the famously known MOORE's law.

The transistor density growth, up to the early 2000s, was mostly invested in improving single core CPU performance, as shown in the graph of fig. 1.1. This was essentially achieved by increasing the core operational frequency, up to a point where the power density became too high for the generated heat to be practically dissipated. Limited by this *Power Wall*, frequency increase has stalled (mid 2000s) while the transistor density kept on increasing exponentially, causing a shift in focus toward multi-core parallelism. Though, other forms of (intra-core) parallelism have been exploited since the '60s, including pipelining, superscalar execution and [Single Instruction Multiple Data \(SIMD\)](#), which contribute to the continuous improvement of single-core performance.

Unlike general purpose (mainstream) processors, embedded ones are subject to stricter design constraints including performance, cost and power consumption. Indeed, they are destined to be

used in a wide variety of domain-specific applications with, for instance, a limited power source. In many application domains, such as signal processing and telecommunication, real numbers computation is employed. Since exact real numbers are not practically possible to represent in a processor, designers/developers resort to alternative, approximative representations of real numbers, which should be accurate enough while satisfying performance, power consumption and cost constraints of the targeted application. Among the most commonly used such representations are *floating-point* and *fixed-point*. Floating-point representation has the advantage to be very easy to use but it requires dedicated hardware support which increase the cost. On the other hand, fixed-point is cheaper since it is based on integer arithmetic but it is more complex to use, which increase the development time. So, the choice between these possibilities is mainly a tradeoff between cost (and power consumption) and ease of programmability.

Many embedded processors nowadays, such the ARM cortex-A family, provide hardware support for floating-point arithmetic, however a good number of ultra low power embedded processors, such as ARM cortex-M0/1/3, TI TMS320 C64x and Recore XENTIUM, do not. This comes at the cost of restraining programmability to the use of fixed-point arithmetic, while application prototyping generally employs floating-point the for sake of simplicity. This means that implementing the application on such processors requires either a software emulation of floating-point arithmetic or a conversion of floating-point into fixed-point. While feasible, software emulation of floating-point results in very poor performance. Alternatively, fixed-point implementation, if specified carefully, can achieve much (1 to 2 order of magnitude) better performance. However, this cannot always be done while keeping the same numerical accuracy, as it would require the use of increasingly large word-lengths, which unless supported by the target processor would also require software emulation, thus compromising performance. Instead, quantizations are applied to limit word-length growth at the cost of introducing *quantization errors* which alter the computation accuracy. This performance/accuracy tradeoff can be exploited during floating-point to fixed-point conversion in a process known as [Word Length Optimization \(WLO\)](#).

When targeting a processor that can only operate on data with a fixed word-length (the word-size, 32-bit in general), [WLO](#) does not make much sense. In fact, employing smaller data sizes does not necessarily benefit the application performance. On the one hand, it may require additional operations to perform data-type conversions, since all integer operations will eventually be performed on operands converted to the native word-size anyway. But on the other hand, it may reduce the memory footprint, which can improve performance. All in all, it is generally better to use the native word-size when targeting such processors.

The story changes when targeting processors with support for [SIMD](#) operations. In this case, smaller data word-lengths can be exploited to perform an operation on several (packed) data simultaneously, using [SIMD](#) instructions. In principle at least, this helps reducing the number of operations, thus ultimately improving performance. This can be exploited during [WLO](#) to explore the performance/accuracy tradeoff. Most embedded processors, such as XENTIUM and ARMv7, provide support for [SIMD](#) with various levels. However, taking advantage of [SIMD](#) capabilities to improve performance is a challenging task.

Automated methodologies for floating-point to fixed-point conversion and [Simdization](#)<sup>1</sup> are essential to reduce development cost and cut down time-to-market. None of the existing work tackles both transformations simultaneously, despite the strong relation between them. Typically, the floating-point to fixed-point conversion is performed first and then [Simdization](#) is (optionally) applied on the resulting fixed-point code.

In this thesis, we argue that considering both transformations independently yields less efficient solutions. We propose a new methodology to combine [WLO](#) with [Simdization](#).

## 1.2 ALMA Project

From a broader perspective, this thesis took place in the context of the European project ALMA [2]. As we mentioned previously, applications in many domains, such as signal processing, are prototyped or specified using floating-point arithmetic and without too much worry about the target architecture characteristics, such as parallelism, for the sake of simplicity. More often than not, the application prototyping is done using high-level numerical languages or frameworks such as MATLAB or SCILAB. Once the specification is ready, the implementation phase aims at providing an accurate and optimized implementation for the target architecture. In the case of embedded multi-core processors with no hardware support for floating-point arithmetic, this generally involves three main steps:

- MATLAB (or SCILAB) to C/C++ conversion.
- Floating-point to fixed-point conversion.
- Coarse and fine -grained Parallelization.

Each of these steps is time consuming and error prone, which greatly increases the development time.

To address this problem, MATHWORKS provides an automatic C code generator, from a subset of the MATLAB language. However, the generated C code uses library calls to MATLAB special functions, for which the source code is not provided. This makes the code difficult to optimize in a later stage. Besides, MATHWORKS tools are proprietary and open source alternatives, like SCILAB, do not provide a similar functionality. Hence, the main motivations behind the ALMA project is to provide an alternative solution to this problem.

The ALMA project [2] aims at addressing the aforementioned problems by providing a complete tool-chain targeting embedded multi-core systems. An overview of the proposed tool-chain flow is depicted in fig. 1.2.

Starting from a SCILAB code, the tool aims, in a first place, at automatically converting it into an annotated C code. The latter then undergoes a multitude of optimizations, mainly performing:

- Coarse-grain parallelization: to exploit the multi-core nature of the target processors.

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1. Simdization is the process of converting scalar instructions in a program into equivalent [SIMD](#) instructions.

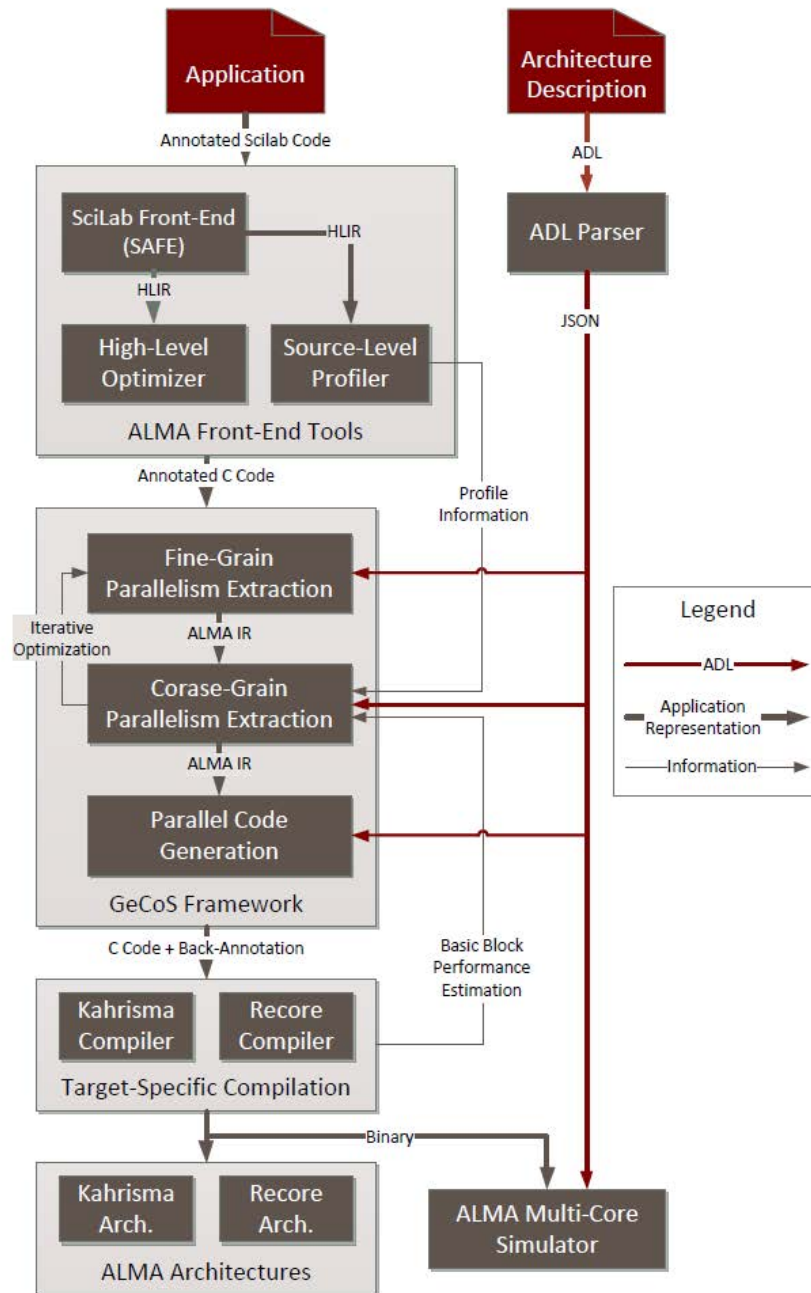


Figure 1.2 – ALMA tool-chain flow diagram.

- Floating-point to fixed-point conversion: to avoid performance degradation due to floating-point simulation.
- **Simdization**: to take advantage of the **SIMD** capabilities of the target processor cores.

The tool finally generates a parallel C code using a generic MPI (message passing interface), **SIMD** and fixed-point **Application Programming Interfaces (APIs)**.

ALMA targeted two multi-core architectures from RECORE SYSTEMS and [KARLSRUHE INSTITUTE OF TECHNOLOGY \(KIT\)](#), based on the XENTIUM [104] and KAHRISMA [58] cores respectively. None of which support floating-point arithmetic, but they provide subword [SIMD](#) capabilities.

### 1.3 Timeline

In this section, we present a brief timeline of the work done during this thesis, in order to help understanding the context, choices and contributions made during this work.

In the context of ALMA, we mainly had to:

- Implement a floating-point to fixed-point conversion, since both ALMA targets do not provide hardware support for floating-point arithmetic<sup>2</sup>.
- Implement an automatic [Simdization](#), since compilers of ALMA targets do not perform this transformation.
- Explore the performance/accuracy tradeoff using [WLO](#) and taking into account [SIMD](#) opportunities.

So, we explored the state-of-the-art for floating-point to fixed-point conversion targeting embedded processors (cf. chapter 2). We found that most approaches are similar in the way they address the problem:

1. First, the [Integer Word Lengths \(IWLs\)](#) are determined based on dynamic range values, which can be obtained using simulation or analytical methods.
2. Then, the word-lengths are specified, either by simply using a default word-length (generally the native word-size e.g. 32-bit), or by performing a [WLO](#) under an accuracy constraint.

The different approaches differ in the way dynamic ranges are obtained and/or the [WLO](#) algorithm and/or the accuracy estimation procedure.

Integrating such transformations into the target compilers is not a trivial task, but most importantly it should be done for each different target to be supported by the flow. Instead, we decided to implement this conversion at source code level using a source-to-source compiler flow. For this matter, we used the source-to-source compilation framework, [Generic Compiler Suite \(GecOs\)](#) [38], which already integrates a floating-point to fixed-point conversion tool, IDFIX [3], providing automatic dynamic range and analytical accuracy evaluation methods. Besides, this choice is also motivated by the fact that [GecOs](#)/IDFIX provides an extension mechanism allowing for "simple" integration of different methods for range evaluation and accuracy estimation without affecting our work. However, IDFIX was initially designed for targeting [High-Level Synthesis \(HLS\)](#) using C++ fixed-point libraries. Since not all embedded processor compilers support C++ and in order to avoid the performance overhead introduced by using such libraries, we implemented a fixed-point C code generator using native integer data-types and operations.

---

2. Besides, this is also the case for many embedded processors.

Similarly, we decided to implement [Simdization](#) at source code level so that it can be easier to extend in order to support other targets. We investigated the different ways of performing [Simdization](#). The existing techniques can be categorized into two groups:

- Loop-level vectorization.
- Basic-block level, also known as [Superword Level Parallelism \(SLP\)](#).

We decided to go with [SLP](#), since it can exploit more opportunities than loop vectorization without the need for "complex" dependency analysis and loop transformations. We investigated the state-of-the-art of [SLP](#) extraction algorithms and we decided to implement the algorithm proposed by LIU et al [78] in 2012. However, during the implementation we found many shortcomings, so we came up with an improved [SLP](#) extraction algorithm, that we present in chapter 4. We implemented it in addition to the aforementioned algorithm by LIU et al, so that we can compare them. We integrated the [SLP](#) extraction algorithms as well as a [SIMD](#) C code generator into the same source-to-source compilation framework, [GecOs](#).

At this point, we had at our disposal a complete source-to-source flow capable of automatically generating a fixed-point [SIMD](#) C code for different embedded processors. With all that out of the way, we started exploiting the interaction between [WLO](#) on the one side and [SLP](#) on the other. In the literature, few existing floating-point to fixed-point conversion approaches target embedded processors with [SIMD](#) capabilities. Existing work though, do not consider [Simdization](#) while performing [WLO](#); they simply assume that selecting narrower word-lengths would eventually increase the [SIMD](#) opportunities, and improve performance consequently. However, this assumption is very optimistic since the [WLO](#) is unaware of the [SIMD](#) opportunities and the associated cost overhead, which can result in a very high performance degradation<sup>3</sup>.

Using the source-to-source compilation flow we already implemented, we integrated a typical [WLO](#) strategy that aims essentially at reducing data word-lengths without considering [Simdization](#). In order to test how well such strategy can perform, we applied floating-point to fixed-point conversion (using the aforementioned [WLO](#) strategy), followed by [SLP](#) extraction, on some benchmarks for XENTIUM, KAHRIUMA and two other embedded processors. The results showed that such an approach is not very efficient for targeting [SIMD](#) processors; the observed speedup due to [Simdization](#) varies inconsistently, supporting our hypothesis about the fact that, simply minimizing word-lengths without taking into account the [Simdization](#) problem would yield inefficient solutions.

In order to solve this problem, we propose a new [SIMD](#)-aware floating-point to fixed-point conversion approach based on a joint [WLO](#) and [SLP](#) extraction algorithm. We also integrate the proposed joint [WLO](#) and [SLP](#) algorithm to the source-to-source compilation flow in order to test its validity compared to prior typical approach. Using our approach, we obtain more efficient overall solutions; it enables a better exploitation of the performance/accuracy tradeoff when targeting embedded processors.

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3. mainly due to data packing/unpacking operations



## 1.4 Contributions and Organization

More specifically the contributions of this work are the following ones:

- A new [Intermediate Representation \(IR\)](#) for [SLP](#) extraction (cf. chapter 4).
- A new [SLP](#) extraction algorithm (cf. chapter 4).
- A new approach for floating-point to fixed-point conversion considering, jointly, [WLO](#) and [SLP](#) extraction (cf. chapter 5).
- A fully automated source-to-source compilation flow<sup>4</sup> for [SLP](#) extraction and floating-point to fixed-point conversion, together with a fixed-point and [SIMD](#) C code generator with support for several embedded processors.

In the remainder of this manuscript, we first present some contextual background on floating-point and fixed-point representations and the conversion methodologies, in chapter 2. Then we present existing techniques for exploiting [SIMD](#) parallelism, in chapter 3.

In chapter 4, we present a thorough analysis of the state-of-the-art of [SLP](#) extraction algorithms and we propose a new enhanced algorithm. We implement the proposed algorithm as a source-to-source compilation flow and we compare it against a state-of-the-art [SLP](#) extraction algorithm.

In chapter 5, we investigate the interactions between floating-point to fixed-point conversion and [SLP](#) extraction and we propose a new [SLP](#)-aware [WLO](#) algorithm. We implement it as a source-to-source compilation flow and we compare it against a typical approach performing floating-point conversion first, then [SLP](#) extraction.

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4. using the compilation framework [Gecos](#) [38]

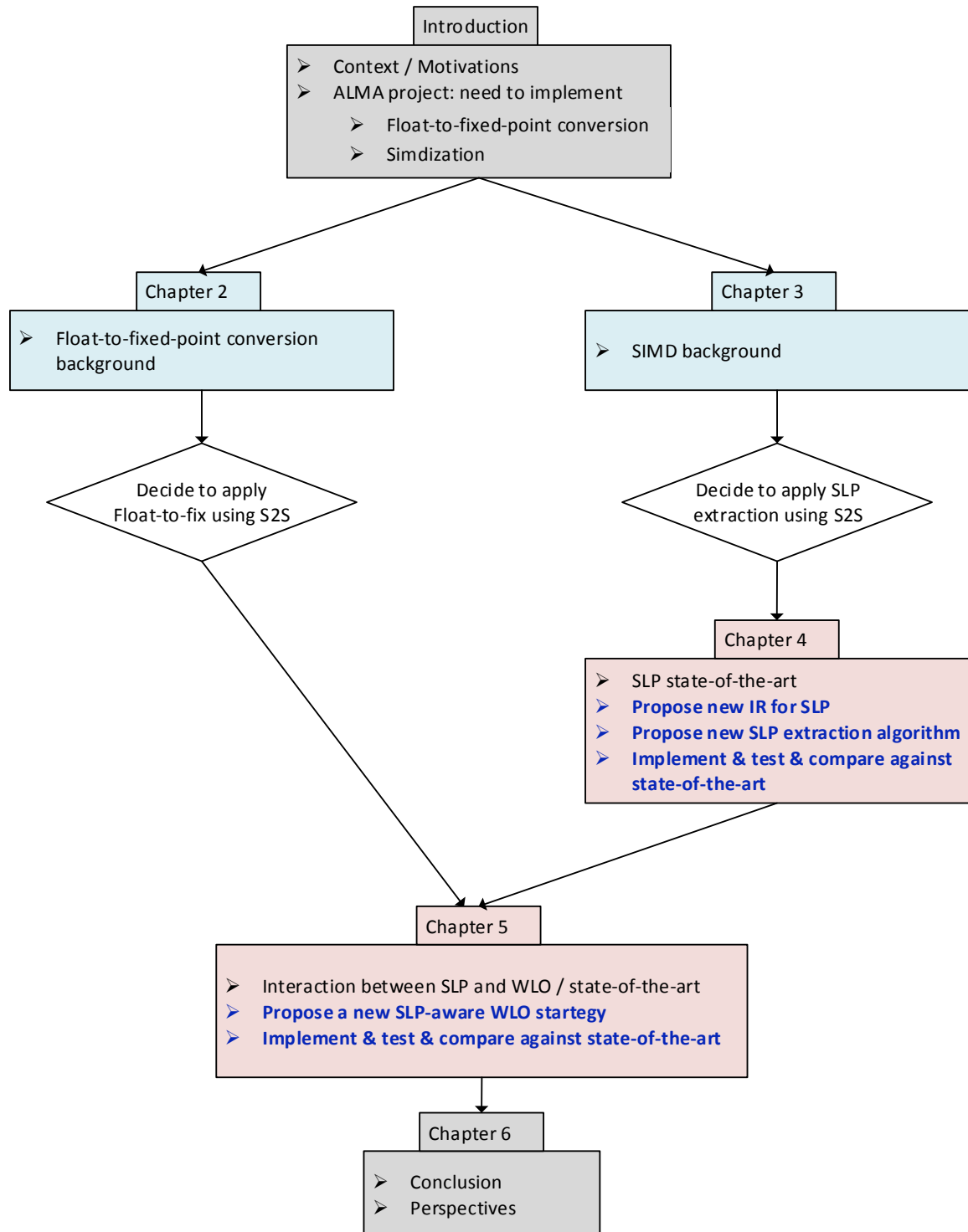


Figure 1.3 – Outline.



## Chapter 2

# Background: Floating-point to Fixed-point Conversion

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## 2.1 Introduction

Real number computations are employed in many application domains, such as digital signal processing. Exact representation for most real numbers, like  $\pi$  for instance, require unlimited precision, thus it is impossible to represent them explicitly. However, they can be represented with virtually unlimited precision using implicit representations instead, such as functions [17]. But such representations are generally not practical and require lots of computing labor. Besides, for most applications, limited precision real arithmetic approximations are good enough. In the following, we will consider two of the most commonly used real number approximations, namely floating-point and fixed-point representations.

The goal of this chapter is mainly to explore existing solutions for floating-point to fixed-point conversion. In sections 2.2 and 2.3 we introduce floating-point and fixed-point representations, then we compare them in section 2.4. Finally, we discuss existing methodologies for floating-point to fixed-point conversion in section 2.5 and we present some existing tools for automatic conversion in section 2.6.

## 2.2 Floating-point Representation

Floating-point representation is an approximation of real numbers using a limited precision mantissa (or significand), scaled by a **variable** factor specified by a limited precision exponent:

$$mantissa \times base^{exponent} \quad (2.1)$$

It is hence similar to scientific notation. The base is common to all numbers in a defined system, so it is implicit and not represented in the number. In addition to the base, the precision and format (interpretation) of the mantissa and the exponent define a floating-point representation.

Since multiple floating-point representations of a real number are possible, it is very hard to maintain portability between different architectures. To overcome this problem, IEEE has defined a standard representation for binary floating-point numbers. This standard, namely IEEE 754, defines the format of floating-point numbers in base two. The floating-point approximation  $FL(x)$  for a given real number  $x$  is represented as follows:

$$FL(x) = (-1)^s \times |mantissa| \times 2^{exponent} \quad (2.2)$$

The mantissa is represented in *sign-magnitude* representation where the sign bit is  $s$ , as depicted in fig. 2.1. The mantissa magnitude is normalized to the range  $[1, 2[$ . Only the fractional part is

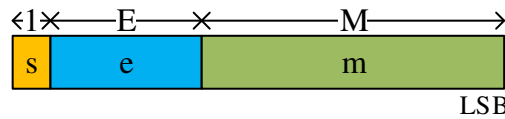


Figure 2.1 – Binary representation of floating-point numbers in IEEE 754 standard.

stored in the number as  $m$  on  $M$  bits, as depicted in fig. 2.1, and the leading integer bit, set to 1, is implicit.

$$mantissa = (-1)^s \times (1.m) \quad (2.3)$$

The exponent is a signed integer represented in *excess*  $(2^{E-1} - 1)$  representation. The biased exponent is stored in the number as  $e$  on  $E$  bits. The true exponent value is obtained from  $e$  by adding the bias  $2^{E-1} - 1$ :

$$exponent = e - (2^{E-1} - 1) \quad (2.4)$$

The exponent value ranges in  $[-(2^{E-1} - 1), 2^{E-1}]$ . The minimal value,  $-(2^{E-1} - 1)$ , indicates an *Underflow*. In this case, the mantissa is not normalized (denormalized mode), the implicit leading bit is 0 and the exponent value is set to  $-2^{E-1} - 2$ . The values  $\pm 0$  are represented in this mode with  $m = 0$ . Whereas, the exponent maximal value,  $2^{E-1}$ , represents two special cases:

- $\pm\infty$  for  $m = 0$ ,
- *NaN* (Not A Number) for  $m \neq 0$ .

When the exponent value exceeds  $2^{E-1}$  an *Overflow* occurs.

The IEEE 754 standard defines two main binary floating-point types, among others:

- 32-bit single precision for  $M = 23$  and  $E = 8$ ,
- 64-bit double precision for  $M = 52$  and  $E = 11$ .

It also defines the operations on floating-point numbers, the exceptions and the different rounding modes.

**Floating-point Addition/Subtraction** is performed through the following steps:

1. Align the operand exponents to the maximal one, which is set as the result exponent, by right shifting the mantissa of the smallest exponent number by the difference of exponents.
2. Add/Sub aligned operand mantissas to obtain the result mantissa.
3. Normalize the result. If the mantissa magnitude is out of range  $[1/2, 1 - 2^{-M-1}]$ , shift it into range and increment/decrease the result exponent accordingly.
4. Round the result mantissa and adjust the exponent if necessary.

**Floating-point Multiplication/Division** requires fewer steps:

1. Mul/Div operand mantissas to get the result mantissa and Add/Sub exponents to obtain the result exponent.
2. Normalize the result.
3. Round the result.

In addition, all operators should check for overflow and other exceptions such as division by zero.

The rounding step introduces a rounding error. Various rounding methods are possible such as round to nearest even (default), toward 0 or toward  $\infty$ . Besides, operands alignment, for

add/sub, may result in a precision loss due to the right shifting. Guard bits are generally added to reduce these errors.

## 2.3 Fixed-point Representation

Fixed-point representation is an approximation of real numbers using a limited precision integer, scaled by a **fixed**, implicit factor. For a given real number,  $x$ , a binary fixed-point approximation,  $FX(x)$ , is represented as follows:

$$FX(x) = sif \times 2^{-F} \quad (2.5)$$

Where  $sif$  is a limited precision integer. It is the only information stored in the number using two's complement representation for signed numbers, as depicted in fig. 2.2. The **Most Significant Bit (MSB)** of the integer,  $s$ , represents the sign in case of signed numbers. The integer (signed or not) is interpreted as though it is multiplied by a scaling factor,  $2^{-F}$ , specified by  $F$  which is referred to as the **Fractional Word Length (FWL)**.  $F$  determines the position of the virtual binary point in respect to the **Least Significant Bit (LSB)**. The remaining  $I$  MSBs are referred to as the **Integer Word Length (IWL)**. It can also be used to specify the position of the virtual binary point in respect to the MSB. All three parameters,  $W$ ,  $F$  and  $I$  are related by the following equation:

$$W = I + F \quad (2.6)$$

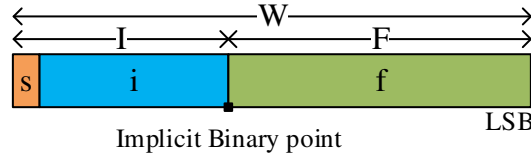


Figure 2.2 – Binary representation of a signed fixed-point number.

A fixed-point format is thus specified by at least two of the three parameters,  $I$ ,  $F$  and  $W$ , in addition to the signedness. We will use the notation  $\langle W, I, F \rangle$  to refer to a fixed-point format, though we may skip one of the three parameters for brevity. In this case, the skipped parameter will be replaced by a ' $\_$ ' and can be simply obtained using eq. (2.6). In the case of signed numbers, the sign bit is accounted for in  $I$ .

### Fixed-point Arithmetic

Fixed-point arithmetic is essentially integer arithmetic with proper handling of scaling factors. Let us consider two signed fixed-point numbers,  $f_1$  and  $f_2$ , represented by the integers  $x_1$  and  $x_2$  with respective formats,  $\langle W_1, I_1, F_1 \rangle$  and  $\langle W_2, I_2, F_2 \rangle$ .

For addition (and subtraction), the operands must first be aligned to the same scaling factor,

before applying the corresponding integer operation.

$$f_1 + f_2 = x_1 \times 2^{-F_1} + x_2 \times 2^{-F_2} = ((x_1 \times 2^{F-F_1}) + (x_2 \times 2^{F-F_2})) \times 2^{-F}, \quad F = \max(F_1, F_2) \quad (2.7)$$

To avoid precision loss, the operand with the smallest **FWL** is left shifted by  $|F_1 - F_2|$ , so that they both align to  $\max(F_1, F_2)$ . The operand word-length must also be increased by the same amount to avoid any potential overflow. Once the scaling factors are aligned, the underlying integers can be added/subtracted to obtain the result. This step may require sign extension. The format of the fixed-point result in this case is  $\langle \_, \max(I_1, I_2) + 1, \max(F_1, F_2) \rangle$

For multiplication, the underlying integer operand can be multiplied directly without aligning. The format of the fixed-point result is  $\langle W_1 + W_2, I_1 + I_2, F_1 + F_2 \rangle$ .

$$f_1 \times f_2 = (x_1 \times 2^{-F_1}) \times (x_2 \times 2^{-F_2}) = (x_1 \times x_2) \times 2^{-(F_1+F_2)} \quad (2.8)$$

Fixed-point operation	Integer operations	Exact result format
$f_1 + f_2$	Align to $\max(F_1, F_2)$ $x_1 + x_2$	$\langle \_, \max(I_1, I_2) + 1, \max(F_1, F_2) \rangle$
$f_1 - f_2$	Align to $\max(F_1, F_2)$ ; $x_1 - x_2$	$\langle \_, \max(I_1, I_2) + 1, \max(F_1, F_2) \rangle$
$f_1 \times f_2$	$x_1 \times x_2$	$\langle W_1 + W_2, I_1 + I_2, F_1 + F_2 \rangle$

Table 2.1 – Exact fixed-point operations.

As can be seen in table 2.1, exact computations over fixed-point numbers require an eventual growth of the underlying integer word-lengths, specially in case of multiplication where the exact result requires  $W_1 + W_2$  bits. Implementing such operations, when targeting a processor with predefined word-lengths, generally requires some sort of software emulation to support wider word-lengths, thus degrading performance. As a consequence, the fixed-point numbers are quantized to make them fit the target processor supported word-lengths.

### Quantization

To convert a fixed-point number from a format  $\langle W, \_, F \rangle$  to  $\langle W - k, \_, F - k \rangle$ , with  $k > 0$ , the  $k$  **LSBs** of the underlying integer should be eliminated by rounding the value of the number. This conversion is referred to as quantization.

Different rounding modes can be used, such as round toward zero (a.k.a. truncation) or round to the nearest value. Regardless of the rounding mode, the  $k$  **LSBs** are lost, resulting in potential precision loss. The error introduced due to quantization, known as *quantization error* (or noise), propagates in the computation system and may result in significant error at the system output.

### Overflow and Saturation

The range of representable numbers by a signed fixed-point format  $\langle W, \_, F \rangle$  is:

$$range = [-2^{W-1}, 2^{W-1} - 1] \times 2^{-F} = [-2^{W-1-F}, 2^{W-1-F} - 2^{-F}] \quad (2.9)$$



This corresponds to the range of the underlying integer format (on  $W$  bits) scaled by a factor determined by the value of  $F$ .

An overflow occurs when a value goes out of range. In this case, the underlying integer value cannot fit on  $W$  bits. Consequently, the value of the underlying integer is *wrapped around* and the **MSBs** are lost, thus introducing a very large error. This overflow behavior (or mode) is known as *wrap around*.

However, the introduced error can be reduced by clipping to the maximal (or minimal) representable value on overflow. This overflow mode is known as *saturation*.

## 2.4 Floating-point vs. Fixed-point

In this section, we compare floating-point and fixed-point representations based on different criteria, including range, precision, implementation cost and ease of use.

### Range and Precision

The precision of a fixed-point representation  $\langle W, \_, F \rangle$  is determined by the scaling factor or the unit-in-last-position (*ulp*). It is a constant given by:

$$ulp = 2^{-F} \quad (2.10)$$

In a IEEE floating-point representation, the mantissa magnitude can represent a set of  $2^M$  different floating-point numbers in the range  $[2^{exp}, 2^{exp+1} - 2^{exp-M}]$ , for a given exponent value  $exp \in [-(2^{E-1} - 2), 2^{E-1} - 1]$  (in normalized mode). The unit-in-last-position (or precision) is variable depending on the exponent value:

$$ulp = 2^{exp-M} \quad (2.11)$$

So all the numbers with same exponent have the same precision but numbers with higher exponent values are represented with lower precision as depicted in fig. 2.3. The range of representable floating-point positive numbers (normalized) is:

$$range = [2^{-(2^{E-1}-2)}, 2^{2^{E-1}-1-M}] \quad (2.12)$$

Therefore, floating-point representation has the advantage to cover a much wider dynamic range but with adaptive precision, whereas fixed-point representation has a constant precision but covers a much narrower dynamic range.

### Implementation

Hardware implementation of floating-point operators is expensive since it has to handle operands alignment, normalization, rounding and check for exceptions. This is mainly due to the fact that

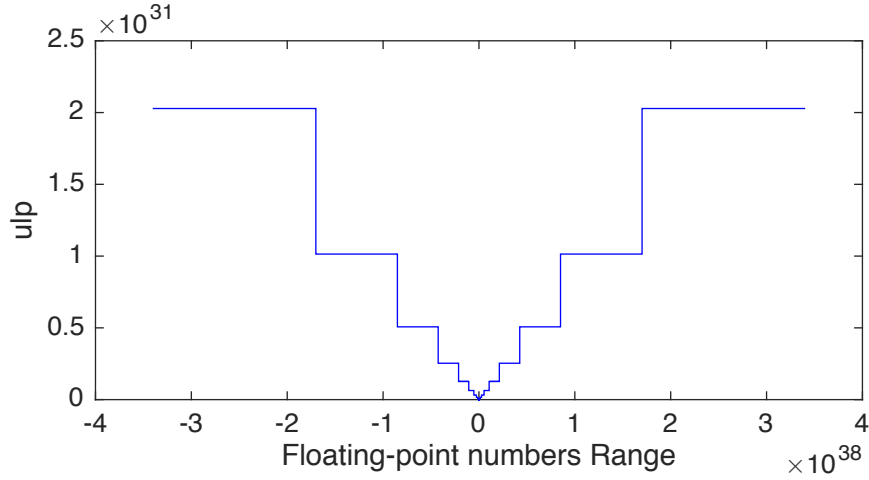


Figure 2.3 – IEEE single-precision floating-point numbers precision vs. range.

the alignment requires a right shifter and the normalization requires a left/right shifter for up to  $M$  positions. Implementing these shifters is a trade-off between execution speed and cost. For example shift registers are cheap to implement but require a variable number of cycles depending on the shifting amount. Barrel shifters on the other hand can perform any shift in constant time but are expensive. Generally multi-level barrel shifters are used.

On the other hand, since fixed-point essentially uses integer arithmetic, no special hardware implementation is required to support it.

For this reason, many embedded processors do not provide support for floating-point arithmetic, for the sake of reducing cost and/or power consumption; they only provide integer computation data-path. In order to perform real number computations on such processors, two options are possible: either emulating floating-point, or implementing fixed-point arithmetic using the integer data-path.

Floating-point arithmetic emulation has a great impact on performance since a single floating-point operation often requires tens of integer arithmetic, shift and branch operations to perform alignment, normalization and rounding as mentioned earlier. Also representing floating-point data requires either more memory, in case mantissas and exponents are stored separately, or extra computations to encode/decode them if they are stored on the same word. This overhead can be even greater depending on the accuracy of the emulation and its compatibility with IEEE 754; a full compliant simulation requires checking and handling of exceptions.

On the other hand, fixed-point arithmetic can be emulated much faster when limited to use the integer data types natively supported by the target. In this case most fixed-point operations can be computed directly using the corresponding integer operator with additional shift operations when scalings are needed (assuming truncation is used as quantization, and no saturation). However, since this method is limited to the precision of the native data-types, quantization should be applied to keep intermediate operation results fit. This procedure is tedious, error

prone and hard to debug since the programmer must keep track of the (implicit) fixed-point formats, for every variable and intermediate operation result, and perform necessary scalings accordingly.

Alternatively, using full-fledged fixed-point libraries, such as SystemC, can seamlessly emulate any fixed-point format with precisions higher than the native data types and can emulate operations with no precision loss. These libraries also support various quantization and saturation modes. But this is at the cost of much slower simulation speeds, by a factor of 20 to 400 as reported by KEDING et al [50].

Therefore the only viable option when seeking tight performance and power consumption goals is to use native data types to represent fixed-point numbers and perform quantizations to keep data fit. To enhance the performance and precision of this approach, some specialized processors provide fixed-point specific enhancements such as:

- Pre-scaling of the input operands and/or post-scaling of the result.
- Extended precision operators and registers.
- Hardware support for saturation and rounding.

### Programmability

Most programming languages, like C/C++, provide native seamless support for standard floating-point data-types and operations but not for fixed-point; this is one of the reasons why most applications are developed using floating-point.

Floating-point is simpler to use, since the hardware does all the hard work providing an intuitive and straightforward interface. However, it can be very tricky in some cases. Floating-point immediate numbers are generally expressed in base 10 for the sake of simplicity. More often than not, these numbers cannot be exactly represented by the floating-point system being used (generally base 2), causing unintuitive behavior. For instance, comparing the result of operation  $0.1 \times 10$  against 1 gives an unexpected result; both numbers are not equal as it might look like. Indeed, 0.1 is exactly representable in base 10 but not in base 2. In fact, C standard does not specify what base is used to represent floating-point data types, but in general it is base 2.

### Conclusion

The characteristics of floating-point and fixed-point representations are summarized in table 2.2. Due to the high implementation cost of floating-point, fixed-point representation is often preferred in the context of ultra low power embedded applications. However, the development time is higher. Thus, automated floating-point to fixed-point conversion methodologies are required to cut down the time-to-market.

Representation	Range	Precision	Cost	Programmability	Development Time
<b>Floating-point</b>	very wide	variable	high	easy	low
<b>Fixed-point</b>	limited	constant	low	difficult	high

Table 2.2 – Floating-point vs. Fixed-point.

## 2.5 Floating-point to Fixed-point Conversion Methodologies

As discussed earlier, floating-point is not suitable when targeting low power embedded processors, and fixed-point is preferably used instead. Therefore, when applications are designed using floating-point, a floating-point to fixed-point conversion is required.

This conversion aims at attributing a fixed-point format to each floating-point data, and at replacing floating-point operations with fixed-point operations along with proper handling of scalings. This conversion may introduce computation errors due the overflows and/or quantizations. The conversion process must be aware of these errors and be able to estimate their effects in order to make sure that the computation accuracy remains within an "acceptable" limit specified by the developer, according to the application tolerance.

Overflows generally induce large errors. However, they can be prevented by evaluating the dynamic value range of each variable and intermediate result and deducing, for each, the minimum **IWL** required to represent its value range. In this way overflows are mostly avoided. Alternatively, overflows can be allowed for cases with low occurrence probability to allow the use of smaller word-lengths. In this case saturation can be used to clip any overflow to the maximal (or minimal) value. In this case the induced errors should be analyzed since they may have a great impact on the computation accuracy.

In contrast, quantization errors are relatively small, but they can get amplified when propagated in the computation system and may result in a significant error at the system output. Therefore, it is very important to evaluate their effect on the computation accuracy and to make sure the latter stays within the specified limit.

Floating-point to fixed-point conversion generally involves three steps:

1. **IWL** determination of each variable and operation intermediate result in the system.
2. Word-length determination, to complement **IWL** determination in order to fully specify the fixed-point formats. This generally makes the subject of an optimization, called **Word Length Optimization (WLO)**.
3. Fixed-point code generation.

In the following, we discuss each of these steps.

### 2.5.1 Integer Word Length Determination

The **IWL** of a variable is determined based on its dynamic value range. The aim is to specify the binary point position in the fixed-point formats in such a way to avoid overflows. The dynamic

range can be obtained either using simulation-based methods [64] or analytical methods.

### Simulation-based Methods

The floating-point code is instrumented to collect statistics on floating-point variables and operation results using simulations with representative input samples. The collected statistics are used to determine the dynamic ranges of the corresponding floating-point variables, which is then used to determine their IWL.

Simulation-based methods have the advantage to find tight ranges and therefore do not allocate unnecessary bits for the integer part. However, they do not guarantee the absence of overflows since the measured range depends on the tested input samples. thus, a large and representative input samples must be used to obtain accurate enough estimations of the dynamic range. Regardless, overflows may still occur and in this case saturation can be used to limit overflow errors.

### Analytical Methods

Alternatively, analytical methods can be used to derive the dynamic range of each variable and intermediate result, in a given system. Range propagation can be achieved using interval arithmetic or affine arithmetic for instance. In this case the input ranges are propagated through operations by applying a correspondent propagation rule.

For example, using interval arithmetic we can deduce the range of variable  $y$ , at the output of the system depicted in fig. 2.4, given the range of inputs  $a$ ,  $b$  and  $c$ . Let  $a \in [a_m, a_M]$ ,  $b \in [b_m, b_M]$  and  $c \in [c_m, c_M]$ . The intermediate result of the multiplication is then  $t \in [t_m, t_M]$ , with:

$$t_m = \min(a_m \times b_m, a_M \times b_M, a_m \times b_M, a_M \times b_m) \quad (2.13)$$

$$t_M = \max(a_m \times b_m, a_M \times b_M, a_m \times b_M, a_M \times b_m) \quad (2.14)$$

Finally,  $y \in [t_m + c_m, t_M + c_M]$ .

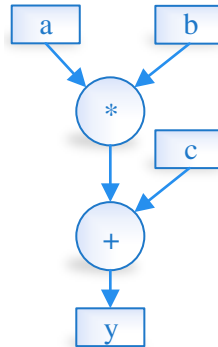


Figure 2.4 – Range propagation example.

Analytical methods have the advantage to be generally faster than simulation and results in

a certain range that ensures the absence of overflows. However, the obtained ranges may be over-estimated resulting in unnecessary bits being allocated for the integer parts.

### 2.5.2 Word Length Optimization

The aim of this step is to select the word-length of each variable and operation in the system. The **FWLs** are implicitly specified during this step following eq. (2.6), which directly affects the computation accuracy and performance. The word-length exploration space is generally specified depending on the target architecture. In the context of **High-Level Synthesis (HLS)** [65] targeting FPGA for instance, a wide range of custom word-lengths can be considered. However, when targeting an off-the-shelf processor, word-lengths are generally restricted to the ones natively supported (e.g. 8, 16 or 32 bits) by the processor. In order to explore this solution space for each variable/operation, a **WLO** algorithm [140, 85, 91] is generally used. It aims at selecting the best performance solution while maintaining accuracy within an "acceptable" limit. Therefore, this requires methodologies to evaluate the accuracy and the cost of a given fixed-point solution.

#### Cost Estimation

When targeting embedded processors, the goal is generally to optimize the execution time (although energy consumption could be also considered). Execution time can be estimated by running the application and collecting timing measurements. To do so, the fixed-point code implementing the solution to be tested should be generated, compiled and run on the target processor with representative input data samples. This has the advantage to give a precise estimation of the execution time. However, this method greatly increases the **WLO** time, since this needs to be done for each tested solution.

Alternatively, an estimation of the execution time can be obtained using static analysis or heuristic based on a cost model of the target architecture. Typically, a relative cost is associated to each operation type and size. In general, these methods do not lead to an accurate estimation of the execution time. However, it is often sufficient for comparing the cost between two different solutions.

#### Accuracy Evaluation

Accuracy evaluation aims at quantifying or measuring the accuracy of a given fixed-point solution. Many metrics can be used for this matter, such as Bit Error Rate (BER), generally used in communication applications, or **Signal-to-Quantization-Noise Ratio (SQNR)** often used in image/signal processing applications.

Simulation-based methods [128, 51, 65, 113] can be used for accuracy evaluation. They mainly consist of simulating the fixed-point system, with representative input samples, and comparing it against a baseline floating-point specification. The results are compared to find errors and compute the accuracy value. Such methods suffer from scalability issues, since the simulation time may be very high, specially in the context of design space exploration in which each tested

fixed-point solution should be simulated with enough input samples to evaluate its accuracy. This results in impractically long optimization times. On the other hand however, these methods have the advantage to be simple and applicable with no restrictions on the underlying computation system.

In order to cut-down the accuracy evaluation time, analytical methods [89, 87, 81, 83, 22, 109], aim at computing a closed-form generic expression, representing the fixed-point system accuracy, as a function of the number of bits assigned to different variables and operations in the system. Once this expression is generated, it can then be used to quickly evaluate the accuracy of any fixed-point solution for the system, by simply plugging-in the correspondent values of number of bits, making it more suitable for design space exploration. However, analytical methods are restricted to some particular systems, mainly [Linear Time-Invariant \(LTI\)](#) and non-recursive non-[LTI](#) systems.

For an [LTI](#) system, MENARD and SENTIEYS [89] proposed a method to automatically compute the quantization noise power expression based on a computation of the transfer function of the system, represented by its [Signal Flow Graph \(SFG\)](#). This is then used to determine the [SQNR](#).

MENARD et al [87] later extended this method to cover non-[LTI](#) non-recursive systems using only one floating-point simulation to determine statistical parameters of noise sources and signal. These techniques evaluate the first moments (mean and variance) of the quantization noise sources and propagate it in the system to the output. To do so, the system is represented by its [SFG](#), which can be constructed from the corresponding C code, but this requires flattening of all the control structures. For large systems, this make the computation of the analytical accuracy evaluation expression slow.

To solve this problem, DEEST et al proposed an alternative, more scalable, representation [30] of the system based on the polyhedral model.

SHI and BRODERSEN proposed an alternative method [121] using a model of the quantization noise based on perturbation theory. This method uses simulations to compute the value of some parameters needed to obtain the analytical expression of the output noise power.

Alternative methods [81, 137] use affine arithmetic to represent the quantization noise in order to compute an analytical expression of the accuracy.

### 2.5.3 Fixed-point Code Generation

As discussed earlier, fixed-point can be simulated using C++ libraries such as SystemC and Algorithmic C Datatypes [1]. This solution has the advantage to seamlessly represent arbitrary-precision fixed-point formats and supports different overflow and quantization modes. However, it introduces a significant performance overhead as shown by KEDING et al [50].

As mentioned earlier in section 2.4, the best performance option, when targeting embedded processor, is to limit fixed-point word-lengths to the natively supported ones. In this case, the fixed-point code can be generated using only native integer data-types to represent fixed-point

data. Fixed-point operations are directly performed using integer operations; however, scaling operations should be carefully added to reflect the fixed-point quantizations. This option is much more tedious and error prone to implement. Using automatic code generation to produce such code can alleviate this problem.

Scalings are implemented using shift operations. This can therefore severely impact the performance depending on the support provided by the target processor. For this reason, floating-point to fixed-point conversion methodologies should minimize the cost of scaling operations. KUM et al proposed a scaling optimization algorithm [64] that minimizes a scaling cost function using integer linear programming, taking into account whether or not the target processor has a barrel shifter. MENARD et al proposed a method [85] to reduce the impact of scaling operations on the execution time. This optimization, performed under accuracy constraint, aims at moving the scaling operations whenever possible: when a scaling operation is brought outside a loop structure, for instance, its impact on the execution time is greatly reduced.

## 2.6 Automatic Conversion Tools

In order to reduce time-to-market, automatic or semi-automatic tools are crucial in order to explore the fixed-point design space while obeying to strict time-to-market constraints.

Many simulation-based semi-automatic conversion tools are commercially available like MATLAB Fixed-point converter and SYNOPSIS System Studio. Such simulation-based tools suffer from high conversion latency, which limits the design space exploration, but it has a wide code coverage.

Alternatively, analytical-based conversion tools suffer from very restricted code coverage. For this reason they are generally limited to research tools like IDFIX [3]. Nevertheless, given a compatible system, they allow for faster conversion and hence more efficient design space exploration.

### 2.6.1 MATLAB Fixed-point Converter

MATLAB is widely used for many domain specific applications design like signal processing. In MATLAB, fixed-point programming is supported; fixed-point data types can be created via the MATLAB `fi` function.

Besides explicit fixed-point programming, MATLAB provides a semi-automatic simulation-based tool to assist the conversion of floating-point MATLAB programs to fixed-point. This tool is referred to by MATHWORKS as *Fixed-point Converter*. This tool mainly functions as follows:

- It takes as inputs a floating-point MATLAB function in addition to a testing MATLAB script that calls the function and provides simulation input samples.
- The first step consists in instrumenting the input floating-point code, which is then run via the testing script to collect statistics about floating-point variables and operations. These



statistics mainly include the dynamic maximal, minimal and mean values.

- The simulation dynamic range is then used to infer the [IWL](#) for each variable. The user can specify an additional safety margin to the simulation range in order to minimize overflow occurrences. Alternatively, he can specify a static range for each, or some, variables which are used instead of the simulation ranges.
- The user can then either specify a default word-length (or [FWL](#)) which will be used to infer the [FWLs](#) (or word-lengths). Alternatively, he can manually specify the fixed-point format for each or some variables.
- The operations intermediate result formats are inferred based on a user-defined default behavior for each operation type. It indicates whether the operation should keep full-precision or perform quantization. In the latter case it specifies what quantization mode is to be used.
- Finally, the fixed-point MATLAB code is generated to reflect the selected fixed-point specification, using `fi` function to create fixed-point types and specify default behaviors.
- The tool also provides a way to automatically instrument and simulate the resulting fixed-point code in order to compare it against the original floating-point version to verify its accuracy. This eases the fixed-point design space exploration.

Since MATLAB code is not suitable to run on embedded processors, the developer must port the generated MATLAB code to C/C++ in general. This process is time consuming and error prone. However, MATLAB also provides a tool to automate this task for a subset of MATLAB syntax. But this has several disadvantages:

- The generated C code uses library calls to MATLAB special functions, for which the source code is not provided. This make the code difficult to optimize in a later stage.
- These tools are proprietary, and alternative open source languages like SCILAB does not provide similar functionalities.

The ALMA [2] project, presented earlier in section 1.2, aimed at addressing these limitations by providing a complete tool-flow starting from SCILAB code down to C code with coarse- and fine- grained optimizations and parallelism extraction. In this context, a contribution of the work of this thesis was to provide floating-point to fixed-point conversion, along with [Simdization](#), to efficiently target embedded processors with no hardware floating-point support.

### 2.6.2 IDFix

IDFix is a research tool for automatic floating-point to fixed-point conversion using analytical methods, originally designed to target [HLS](#). It is developed by the Cairn/Irisa team and is integrated in the source-to-source compilation framework, [Generic Compiler Suite \(Gecos\)](#).

IDFix flow diagram is depicted in fig. 2.5. It takes as input an annotated floating-point C code, an accuracy constraint and a model of the target architecture. It comprises several stages that are described below.

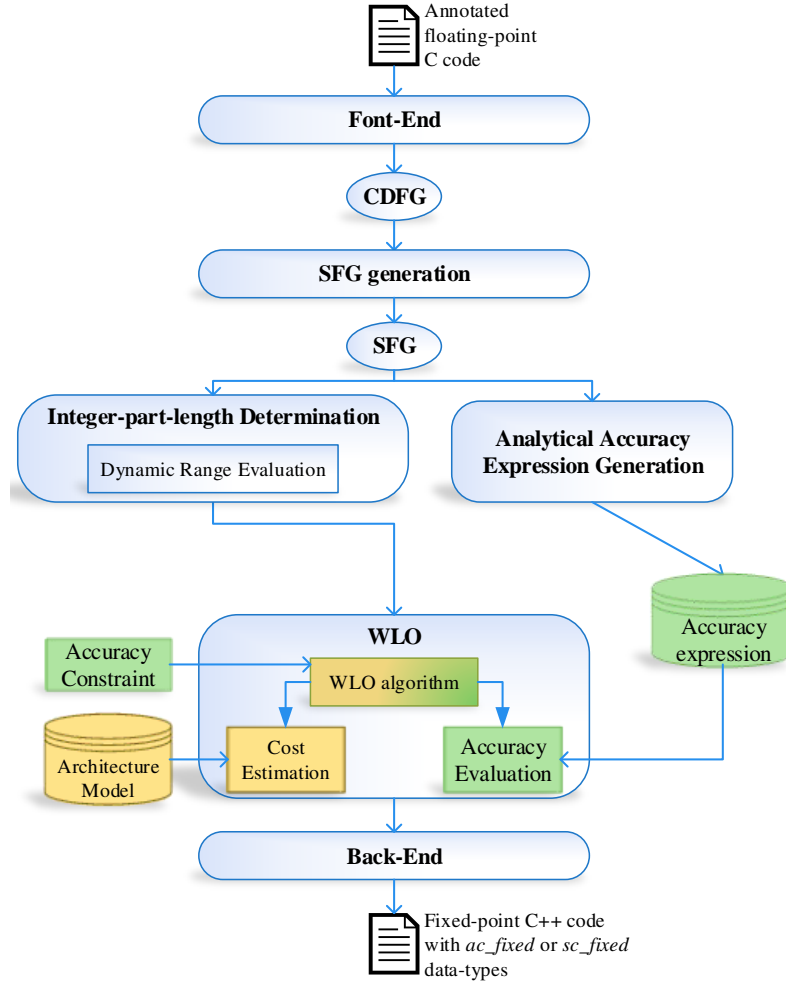


Figure 2.5 – IDFix flow diagram.

A **Font-End** parses the input floating-point C code and generate an **Intermediate Representation (IR)**, which is basically a control and data flow graph (CDFG).

The input C code must satisfy several constraints, mainly:

- All control structures, such as loop bounds, must be statically evaluable.
- The system input variables must be annotated with a *pragma* annotation specifying their dynamic values range (`#pragma DYNAMIC[min,max]`).
- The system outputs must be marked with a *pragma* annotation (`#pragma OUTPUT`).
- All variables used to represent a delay line<sup>1</sup> should be marked with a *pragma* annotation (`#pragma DELAY`).

1. a variable used to store previous values of a signal, often implemented using a circular buffer. For example, `X` represents a delay of the signal represented by `sample` in the following C code snippet: `int X[N]; X[0] = sample; ... for(int i=N-1; i>0; i--) X[i] = X[i-1];`

All control structures in the CDFG are then flattened, and loops are fully unrolled. The flattened CDFG is used to generate a **SFG** representing the computation system, which is later used to propagate dynamic range information and to compute the accuracy expression.

**Dynamic Range Evaluation** The user-specified input dynamic ranges are propagated in the **SFG**, using interval arithmetic, to infer the dynamic range of each variable and intermediate result (nodes). The dynamic range information is then used to determine, for each node, the minimum **IWL** such that no overflows can occur.

**Accuracy Expression Generation** The analytical accuracy expression of the system is generated as function of all node **FWLs** and their associated quantization modes. This is based on quantization error modeling and analytical **SQNR** evaluation presented in [89, 87], which only support **LTI** systems (and non-recursive non-**LTI** systems). The generated accuracy expression is later used to evaluate the accuracy for a given fixed-point solution during **WLO**.

**Word Length Optimization** **IDFIX** provides several **WLO** algorithms to explore the performance/accuracy tradeoff. It uses a modular and extensible design to allow for simple implementation of additional **WLO** algorithms.

The word-length solution space is constrained by the operators supported by the target architecture, described using a simple model, which specifies:

- For each supported operation type (add, mul, ...), the supported operators that can perform it. An operator is simply represented by the word-lengths of the operands on which it can operate. For example **ADD[32 32 32]**, represents an operator capable of adding two 32-bit operands to produce a 32-bit result.
- For each operator, a static cost representing either its execution time, its area, or its energy consumption.

A **WLO** aims at finding the best solution, according to a specified criteria, while maintaining the system accuracy within an "acceptable" limit, provided by the user. It uses the analytical accuracy expression, generated earlier, to evaluate the accuracy of a tested fixed-point solution.

**Cost Estimation** based on the specified cost criteria (execution time, area, or energy consumption), the cost of a given fixed-point solution is automatically estimated by adding the cost of the operators assigned to each operation in the system. The operator cost is retrieved from the architecture model.

**Back-End** generates a fixed-point C++ code, corresponding to the fixed-point specification resulting from the **WLO**, using either SystemC or Algorithmic C Datatypes C++ libraries targeting **HLS** tools like Catapult C. The fixed-point code is simply obtained by changing the data-types

of all floating-point variable to the corresponding fixed-point class. Operations, scalings, saturations and quantizations are seamlessly handled by the underlying C++ library using operators overloading.

## 2.7 Conclusion

In this chapter, we have presented and compared floating-point and fixed-point representations. We have also discussed existing methodologies for floating-point to fixed-point conversion.

In summary, we have observed that:

- Many embedded processors do not provide hardware support for floating-point arithmetic.
- Floating-point software-emulation greatly degrades performance.
- Fixed-point is more suitable in this case; it provides a better performance at the cost of degrading computation accuracy.
- C++ fixed-point libraries are seamless to use, but they can introduce an overhead. Best performance can be achieved using only native integer data-type word-lengths.
- Floating-point to fixed-point conversion can exploit this performance/accuracy tradeoff through [WLO](#).
- Automated conversion mainly requires a method for evaluating dynamic ranges and for evaluating the accuracy of a given fixed-point implementation.
- Simulation based methods are very slow, which make them not suitable for design space exploration.

Based on these conclusions, we decided to implement automatic floating-point to fixed-point conversion, in the context of the ALMA project, at source code level producing a fixed-point C code using only native integer data-types. We decided to use IDFIX, since it already provides a framework for analytical accuracy evaluation and dynamic range evaluation. In addition, it is already integrated into a source-to-source compilation framework, namely [GeCos](#).

Later on, in chapter 5, we will present the source-to-source compilation flow that we implemented for floating-point to fixed-point based on IDFIX. We will use this flow in conjunction with an automatic [Simdization](#) flow, which we will present in chapter 4, to explore the interaction between floating-point to fixed-point conversion and [Simdization](#) and their impact on performance/accuracy when targeting embedded processors. But first, in chapter 3, we will discuss another important performance-impacting factor when targeting embedded processors, namely [Single Instruction Multiple Data \(SIMD\)](#).



## Chapter 3

# Background: Single Instruction Multiple Data

### Contents

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### 3.1 Introduction

In the previous chapter we presented the floating-point and fixed-point representations of real numbers. We discussed their impact on performance and accuracy, in the context of embedded processors. We concluded that fixed-point is more suitable for many embedded processors, specially in the context of the ALMA project. So, we explored existing methodologies for converting floating-point applications into fixed-point. In this context (as explained in section 1.3), another important performance-impacting factor is [Single Instruction Multiple Data \(SIMD\)](#), which we will discuss throughout this chapter.

Ever since the first transistor computer, manufacturing technologies continue to push miniaturization to its limit allowing more and more transistors to fit into a single die [116]. A big share of this growth has been invested in providing parallelism at various levels. In 1966, FLYNN distinguished four classes of architectures according to the form and the grain of parallelism they provide. [SIMD](#) is one of them. It is the class of architectures capable of executing the same operation on several data simultaneously, thus providing a form of [Data Level Parallelism \(DLP\)](#). Figure 3.1 shows an illustration of a [SIMD](#) addition in contrast to its equivalent scalar operations. The [SIMD](#) operation performs the addition of all  $N$  data elements simultaneously, whereas  $N$  scalar additions are needed to perform the same operation.

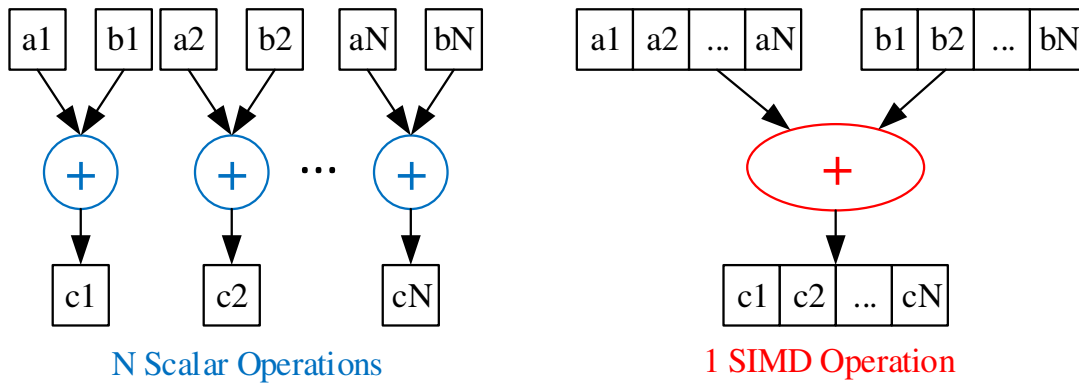


Figure 3.1 – Illustration of an [SIMD](#) addition operation in contrast to scalar addition operation.

Earliest form of [SIMD](#) architectures appeared in vector processors, used in supercomputers like the TI ASC and Cray-1 [115] in the 1970s. These supercomputers mainly targeted computation-intensive scientific applications. With the increasing interest in multimedia applications for general public, [SIMD](#) architectures found their way into mainstream desktop processors, in mid 1990s, as an economical yet effective way to boost performance for such data parallel applications [72, 15]. These newer [SIMD](#) architectures are commonly known as Multimedia extensions or [SIMD](#) extensions.

The lack of native support for [SIMD](#) operations in common programming languages, in addition to the irregularities between different [Multimedia Instruction Sets \(MISs\)](#), made it very challenging to take full advantage of parallelism provided by Multimedia extensions. Program-

mers had to explicit SIMD parallelism in the application code, which is tedious and error prone. The natural cure to this problem is to rely on compilers to automatically extract and generate SIMD code.

Alternative solutions, such as supporting SIMD parallelism in programming languages, has been also investigated in order to efficiently leverage Multimedia extensions. However, a huge base of legacy applications, coded with sequential (scalar) languages like C and Fortran (prior to Fortran90), has already been established. This fact makes such solutions less attractive.

In this chapter, we present the characteristics of some SIMD instruction sets, as well as the different techniques of exploiting them. In section 3.2, we present an overview of the evolution of SIMD instruction sets. We then discuss the different ways of exploiting them in section 3.3.

## 3.2 SIMD Instruction Sets

In this section we present an overview of the evolution of most common SIMD instruction sets. In section 3.2.1, we briefly describe conventional vector processor architectures. We then present the evolution of Multimedia extensions in section 3.2.2.

### 3.2.1 Conventional Vector Processors

Vector processors are among the first models of SIMD architectures. Development of such processors started in the 1960s. They were mainly used in supercomputers, like the TEXAS INSTRUMENTS (TI) Advanced Scientific Computer (ASC) and Cray-1 [115], targeting compute-intensive scientific applications. These processors support the execution of scalar and vector instructions. They have the ability to perform the same operation on several, say  $N$ , data elements, called vectors, by issuing a single vector instruction compared to  $N$  scalar instructions. Using vector instructions requires less instruction bandwidth, reduces loop control operations and reduces code size compared to scalar instructions.

Earlier vector processors, such as CDC's<sup>1</sup> STAR-100 and TI's ASC, used a memory-to-memory architecture. In such architectures, functional units operate on data directly from memory and write the results back to memory. The high latency associated with memory accesses is a limiting factor of such architectures.

Since Cray-1, this limitation is overcome by employing register-to-register architectures. The operands are first loaded to vector registers, on which vector instructions are applied. When needed, the results are stored back to memory. In order to do so, several vector registers are added, in addition to scalar registers. A vector memory access unit handles the transfer of data between the memory and vector registers, while functional units operates on registers.

In contrast to memory-to-memory architectures, the vector length is limited by the vector registers size (generally of several Kbits). Though, it can be changed dynamically through a

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1. Control Data Corporation



Vector Length Register. Furthermore, vector masking allows the conditional execution of a vector instruction on certain elements of the vector operands.

Such architectures generally use one or more pipelined functional units (FU). A vector instruction is fetched and decoded once and then executed on all vector elements sequentially, though in case of multiple FUs, multiple vector elements are processed in parallel. Also, thanks to vector chaining (also called bypassing) a vector instruction can start executing as soon as the first elements of its vector operand - resulting from a previous vector instruction - are ready instead of waiting for the previous instruction to finish processing the entire vector.

Besides, these architectures have no restrictions on vector memory accesses. Scatter/gather accesses are supported and the accessed data is not required to be aligned on the vector size.

All these features, allow vector processors to have a seamless, complete and efficient support for vector operations.

### 3.2.2 Multimedia extensions

Despite their advantages, vector processors were very expensive<sup>2</sup> and not as efficient executing scalar instructions compared to conventional microprocessors, which was a limiting factor (Amdahl's law).

For these reasons, vector processors lost interest in the 1990s. Few years later, due to the increasing popularity of multimedia applications, another form of SIMD instruction sets, known as Multimedia extensions or small-scale SIMD, found its way to mainstream (general-purpose) and embedded processors. The main goal of these extensions was to provide a performance boost when targeting multimedia applications, by supporting a MIS, with little cost overhead.

Contrary to conventional vector processors, Multimedia extensions are based on a partitioned data-path that simultaneously operates on all vector elements. The vector representation in Multimedia extensions is different than in vector processors:

- Vector size is fixed and generally small (between 32 and 256 bits).
- Multiple vector element sizes are supported (generally 8, 16 and 32-bit).
- Vector elements must be packed into a register. Some Multimedia extensions use dedicated SIMD registers while others make use of the same scalar registers.

This means that for smaller element sizes, more elements can be processed simultaneously. Though, the number of cycles required to execute a SIMD instruction on a Multimedia extension is the same regardless of the number of elements and their size (generally the same as its scalar counterpart). This is generally not the case for conventional vector processors, where the maximum number of vector elements does not change with element size (the elements are not packed) and the number of cycles required to execute a vector instruction vary according to the number of elements. Consequently, when targeting Multimedia extensions the program must handles data packing and unpacking.

---

2. A Cray-1 supercomputer was sold for few million dollars.

Besides, the main difference between vector processors and Multimedia extensions is in the memory unit. Unlike vector processors, most Multimedia extensions do not support scatter/-gather memory accesses and require data to be contiguous and aligned to the vector size, in order to be directly loaded into a vector register. Otherwise, multiple memory accesses have to be performed and data have to be rearranged in vector registers. Multimedia extensions provide data permutation operations to allow the reordering of vector elements in registers. This, furthermore complicates the programming of Multimedia extensions.

**MISs** are designed to suit multimedia application needs. Since multimedia application domains are numerous and sometimes have different requirements, various **MISs** have been introduced by processor manufacturers with differences in vector size, supported element data-types and supported **SIMD** operations. Choosing among these criteria is generally a tradeoff between the coverage of the targeted application domain(s), the desired performance enhancement and the associated cost overhead.

Multimedia extensions have been constantly evolving ever since they were introduced. The vector size tends to increase with time, from 32-bit to 512-bit nowadays, and is expected to continue growing. Supported data-types are generally common powers of 2, starting from 8-bit for integers, in addition to single, double and, recently, half precision floating-point. The **SIMD** instructions set, also become richer with time by including more specialized instructions, composite instructions and/or horizontal **SIMD** instructions. All this led to many irregularities and variations between different **MISs**, which make them even harder to program.

All in all, Multimedia extensions generally suffer from various shortcomings that the programmer should handle:

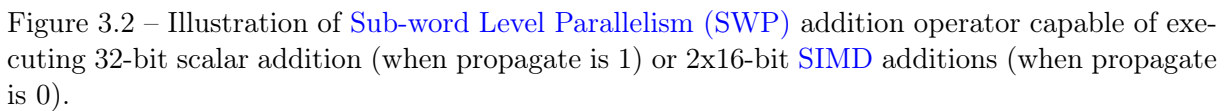
- Vector elements packing and unpacking.
- Data permutations to handle unsupported memory operations (scatter/gather and alignment).
- Variations between different **MISs**.

In the remainder of this section we present an overview of the evolution of Multimedia extensions. We distinguish two main categories, *Subword* Multimedia extensions and *Superword* Multimedia extensions.

### 3.2.2.1 Subword Multimedia extensions

First Multimedia extensions were achieved by partitioning the existing scalar data-path, usually of 32-bit or 64-bit wide, into several smaller parts. This gives the processor the ability to operate on registers as a whole (in case of scalar instructions) or as aggregates of several, usually 8, 16 or 32-bit wide, independent subwords. In such architectures, the registers used by both scalar and **SIMD** instructions are thus the same.

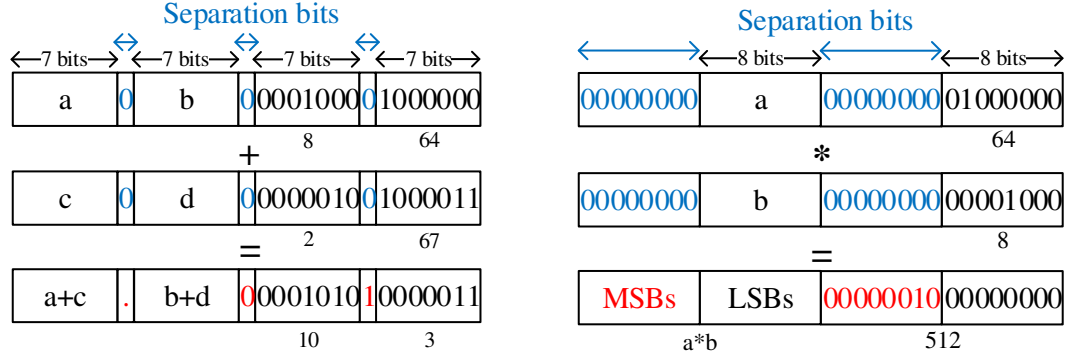
The data-path is partitioned by introducing logic to handle propagation across subword boundaries. The same functional unit can be configured, by the instruction, to execute an operation



The **Instruction Set Architecture (ISA)** is extended by adding a **MIS**. It generally provides **SIMD** instructions for basic arithmetic operations (add, mul, ...) supporting different subword data-types. In addition, it also provides **SIMD** instructions for data packing, unpacking and permutation.

**Soft SIMD** To a certain extent, [SWP](#) can be exploited by software with no special hardware support, using but scalar instructions, this is known as Soft [SIMD](#) [37, 61].

Figure 3.3a shows an example of a soft SIMD operation performing four 7-bit integer additions.



(a) Soft SIMD operation performing four 7-bit additions using scalar integer 32-bit adder. Operands are packed into 32-bit registers, each separated by one separation bit.

(b) Soft SIMD operation performing two 8-bit multiplications using scalar integer 32-bit multiplier. Operands are packed into 32-bit registers, each separated by eight separation bits.

Figure 3.3 – Illustration of some soft SIMD operations.

The operands of these additions are packed into 32-bit scalar registers with one separation bit between each two subwords. The potential overflow of one addition is caught by the separation bit on its **Most Significant Bit (MSB)** side, this way the result of one addition cannot pollute the result of the other. Since the addition of two 7-bit operands requires at most 8-bit to hold the result, only one separation bit is enough to avoid interferences. In case of multiplication, however, more separation bits are needed, as illustrated in the example of fig. 3.3b.

Soft SIMD requires careful management of separation bits in order to avoid subword operation interferences. This greatly limits the efficiency of such approach, especially in the case of chained operations, where the number of required separation bits rapidly grow. The more separation bits are needed the less subwords can be packed together. Nevertheless, soft SIMD can still be useful in some cases, especially when handling very small data sizes or irregular data-types (e.g. 10-bit) that are generally not supported by the hardware.

### 3.2.2.2 Superword Multimedia extensions

Later Multimedia extensions are based on special hardware extensions dedicated to support SIMD instructions. Similar to subword extensions, they are based on partitioned data-path. However this data-path is dedicated to SIMD and is generally separated from the scalar data-path. These extension units use special SIMD registers that are wider than the machine's native word size (hence the name superword). In contrast to subword, superword Multimedia extensions are more costly but offer higher vectorization factors. Also, since registers are not shared with the regular scalar data-path, register transfer instructions are generally added to move data between regular and SIMD registers.

One of the first such Multimedia extensions is Intel **Matrix Math eXtension (MMX)** [98] that equipped Pentium processors in 1997 providing support for 64-bit integer SIMD instructions

capable of operating on eight 8-bit, four 16-bit or two 32-bit packed data.

Ever since, most processor manufacturers continuously enhance and extend these [MISs](#). SSE and later SSE2, 3 and 4 were successively proposed by Intel to support wider [SIMD](#) vector size, more subword data-types and/or more [SIMD](#) operations. As of today, Intel AVX-512 provides 512-bit [SIMD](#) support for all powers of 2 integer data-types starting from 8-bit, as well as single and double precision floating-point data-types.

Nowadays, superword Multimedia extensions are found in most general-purpose processors. They tend to have the same features as conventional vector processors by supporting wider vector sizes and less restricted memory accesses.

In low power embedded processors, it is more frequent to find support for [SWP](#) due to their near-zero cost and power consumption overhead. This is the case of many low power [Very Long Instruction Word \(VLIW\)](#) architectures such as RECORE SYSTEMS Xentium[104], [TI TMS320 C64x](#) and [STMicroelectronics ST240](#), as well as [ARMv7](#) processors except those equipped with the [NEON SIMD](#) extension providing 128-bit [SIMD](#) support. In the context of this thesis, we mainly target this kind of architectures.

### 3.3 Exploiting Multimedia extensions

As mentioned in the previous section, the potential of [SIMD](#) architectures was recognized very early. Hardware support for [SIMD](#) has been provided through different architectures. Nowadays almost all processors, both general-purpose and embedded, provide a certain form of [SIMD](#) support through Multimedia extensions. In this section we discuss the different ways of exploiting the potential of these extensions to improve performance.

Since the hardware does not automatically make use of Multimedia extensions, the software must explicitly invoke [SIMD](#) instructions. However, most applications are generally coded in a scalar fashion<sup>3</sup>. Therefore, in order to make use of Multimedia extensions, a scalar code must be transformed to explicitly use [SIMD](#) instructions. We refer to this transformation as [Simdization](#).

[Simdization](#) mainly requires two steps:

- First, exposing and uncovering [SIMD](#) parallelism in the scalar code. This generally requires code analysis and transformations, such as dependences analysis and loop transformations, to help exposing and enhancing [SIMD](#) parallelism.
- Converting groups of independent scalar instructions into equivalent [SIMD](#) instructions. This requires proper handling of data packing and unpacking taking into account memory access constraints.

In the following, we present the different ways of applying [Simdization](#). We first discuss manual [Simdization](#) techniques, then we present various automatic [Simdization](#) methodologies.

---

3. using scalar instructions only. We will refer to this as scalar or sequential code.

### 3.3.1 Manual Simdization

When seeking maximal performance, hand-written optimized code is still the best bet. This is a difficult task, however. The programmer must have good knowledge of the target [ISA](#), but also should have some skills in program transformations in order to efficiently expose and leverage parallelism provided by Multimedia extensions. This task is known to be tedious and error prone. Manual [SIMD](#) programming can be performed at various abstraction levels:

#### Inline Assembly

Inline assembly code can be used from within C/C++ code to explicitly invoke [SIMD](#) instructions. This is however very tedious and error prone. Furthermore, it is not portable since it is architecture-dependent. However, it allows fine-tuning to achieve best performance.

#### Intrinsics

Most [SIMD](#) processors provide a set of compiler-known intrinsics to invoke [SIMD](#) instructions. This allows a very similar expressibility as inline assembly programming, but has the advantage to be simpler, since it provides a function-like [Application Programming Interface \(API\)](#). However, it still mostly architecture-dependent and lacks portability.

#### [SIMD](#) Libraries

Another alternative consists of using pre-optimized libraries that implement certain functionalities using highly optimized [SIMD](#) code. This solution is very easy to use and more portable, but it is limited to few functionalities. It generally allows to achieve good performance, however, since the compiler is not aware of the optimized functions code, it cannot perform certain (inter-procedural) analysis and optimizations.

#### [SIMD](#) Programming Languages

Many high-level programming languages, with native support for vector operations, have been proposed as a mean to ease the use of [SIMD](#) hardware. Fortran 8x, later known as Fortran 90, C\* [111] are early examples of such languages, which were introduced in the 80s to simplify programming vector processors. More recent languages, like Cilk Plus and [SIMD](#) directives of OpenMP, are more suitable for targeting Multimedia extensions.

Although [SIMD](#) programming languages provide a clean, efficient and portable way to target Multimedia extensions, they still require additional effort to figure out parallelism and express it correctly when designing the application, but most importantly they are of no use for already existing software. One solution to overcome this limitation consists in using source-to-source compilers to convert legacy (scalar) code to a [SIMD](#) language. An example of this approach is the Fortran-to-Fortran8x compiler [10].

### 3.3.2 Automatic Simdization Methodologies

As mentioned previously, manual [Simdization](#) is generally tedious, hard to maintain and lacks portability. [SIMD](#) programming languages can simplify these problems, but they are helpless for legacy software. The ultimate solution consists in relying on compilers to automatically detect and expose [SIMD](#) opportunities and efficiently generate [SIMD](#) code.

We can distinguish two main methodologies of automatic [Simdization](#) which emerged in harmony with the evolution of [SIMD](#) hardware architectures. The first, rather known as *Loop Vectorization*, was first introduced to target vector processors. It has later been adapted to target Multimedia extensions (mid 90s). And the second, basic-block level [Simdization](#), appeared in 2000s as an alternative efficient way to target Multimedia extensions.

#### 3.3.2.1 Loop Vectorization

Loop vectorization is a [Simdization](#) code transformation targeting loop nests. It aims at exploiting vector parallelism, a subset of loop-level parallelism. It basically consists of converting a "vectorizable" scalar loop into equivalent loop with vector instructions. A vectorizable loop is a loop that does not carry dependencies between its iterations (i.e. its body instruction instances can be executed in parallel) and that has a number of iterations equal to the vector size. Such loops are rarely present in a code, thus loop transformations allowing to exhibit them constitute a key part of loop vectorization techniques.

An auto-vectorizing compiler relies on instance-wise dependency analysis and loop transformations, such as loop interchange, fission, fusion, shifting, skewing and strip-mining to name a few, in order to detect and expose vectorizable loops.

Figure 3.4 illustrates a simple example of loop vectorization. The loop in the original code (fig. 3.4a) is dependence-free, but it has  $N$  iterations which may be different from the vector size  $V$ . Applying loop peeling and strip-mining in this case allows to expose a vectorizable loop (fig. 3.4b), which can be then replaced by equivalent vector code (fig. 3.4c).

First attempts of auto-vectorizing compilers were targeting vector processors, like Cray-1's Fortran compiler (CFT). The quality of such compilers is greatly limited by their ability to perform precise dependence analysis and advanced loop transformations. PADUA and WOLFE highlight the importance of data dependence analysis in automatic loop parallelization compilers [96]. NOBAYASHI and EOYANG published a study [92] comparing auto-vectorizing compilers targeting conventional vector processors in 1989 and outlined the importance of loop transformations to expose vectorizable loops.

In this context, the polyhedral model is well fitted to provide such services. Indeed, the polyhedral model offers an instance-wise abstract representation of some compatible loop nests, known as [Static Control Parts \(SCoPs\)](#) or [ACL \(Affine Control Loop\)](#)<sup>4</sup>. This mathematical

---

4. Basically a loop nest in which all loop bounds, conditionals and array subscripts are affine functions of the surrounding loop iterators and parameters.



```

//V: the vector size
for (ii = 0; ii < [N/V]*V; ii += V)
    for(i = ii; i < ii+V; i++) //vectorizable
        Y[i] = X[i] + C[i];
for (; ii < N; ++ii)
    Y[i] = X[i] + C[i];

```

(a) Original code

(b) After applying peeling and strip-mining

```

for (ii = 0; ii < [N/V]*V; ii += V)
    //this is later replaced by SIMD instructions
    Y[ii:ii+V-1] = X[ii:ii+V-1] + C[ii:ii+V-1];
for (; ii < N; ++ii)
    Y[i] = X[i] + C[i];

```

(c) After applying vectorization.  $[min : max]$  represents a vector access to contiguous array elements starting at offset  $min$  till offset  $max$  included.

Figure 3.4 – Example of Vectorization.

representation is used to derive a precise instance-wise and array element-wise dependence analysis [32], based on which the space of valid loop transformations (also known as schedules) can be explored. A loop transformation corresponds to a mathematical relation that reschedules the loop instances. It is valid if it does not violate any dependency [33, 34]. With the advance of polyhedral model techniques and tools, such as PLUTO[19] and ISL [139], auto-vectorizing transformations become more robust, and easier to implement [60].

Most compilers nowadays, such as GNU GCC and LLVM, provide support for polyhedral transformations and automatic loop vectorization.

### Adapting Loop Vectorization to Multimedia extensions

When Multimedia extensions emerged, due to their resemblance to vector processors, the trend was to adapt loop vectorization techniques in order to automatically generate SIMD code targeting Multimedia extensions. Indeed, the same loop analysis and transformations can be employed to expose vectorizable loops, which are then transformed into equivalent SIMD instructions from the target MIS.

However, unlike vector processors, MISs are irregular and vary significantly between different extensions. But most importantly, they do not provide a complete support for vector operations, especially memory accesses. This makes the conversion of vectorizable loops into SIMD code more complex as compared to vector processors, for which this conversion is straightforward. FISHER and DIETZ discussed this problem and proposed to complement hardware SIMD instructions with software emulated ones [37] (soft SIMD) in order to have better support for vector operations.

On the other hand, vectors are represented differently in Multimedia extensions. Unlike vector processors, vector elements must be *packed* in SIMD registers in order to be processed by SIMD instructions. Thus, the compiler must be able to handle data packing and unpacking, in order



to load vector elements from memory and pack them into **SIMD** registers, and unpack elements to store them back into memory. This step is particularly sensitive especially in case of complex memory accesses (scatter/gather or unaligned accesses). Since most Multimedia extensions only support aligned<sup>5</sup> unit-stride<sup>6</sup> vector memory accesses, an important overhead is associated with the packing/unpacking operations, which are required in the case of complex memory accesses. Figure 3.5 illustrates an example of vector memory load for such Multimedia extensions. In case of unaligned (left) or non unit-stride memory access (right), additional operations are needed in order to pack vector elements into a register. This further complicates the task of auto

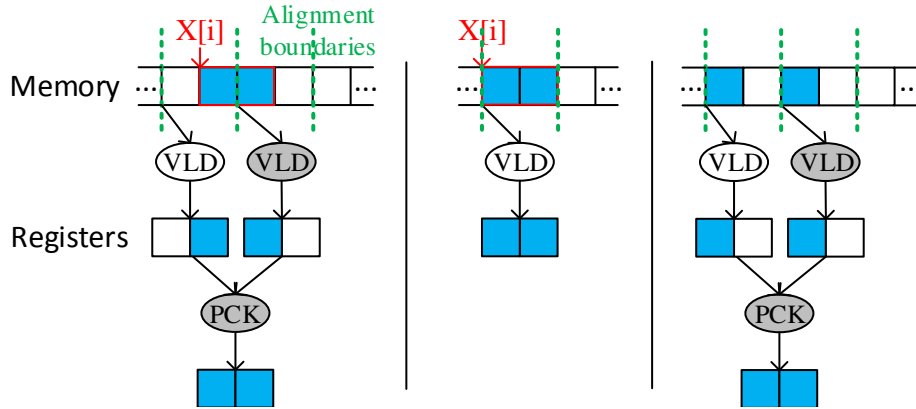


Figure 3.5 – Illustration of vector memory load from an aligned stride-1 reference (middle) versus unaligned stride-1 (left) and aligned stride-2 (right), in case of a Multimedia extension with no support for unaligned accesses and with vector size of 2.

vectorization. Additional code analysis and transformations are required in order to produce efficient **SIMD** code, such as memory reference alignment and pointer analysis [114, 101], handling of unaligned memory accesses [31, 141], data layout transformations [48, 44] and more advanced loop transformations [35, 60].

### 3.3.2.2 Basic-Block Level Simdization

Due to the complexity of loop vectorization techniques when targeting Multimedia extensions as discussed above, a new concept of **Simdization** emerged in the 2000s. It consists in exploiting **SIMD** parallelism at the basic-block level rather than loop-level.

In 2000, LEUPERS proposed a basic-block level **Simdization** technique [74]. It is performed at instruction selection stage in two main steps. First, the **Data Flow Graph (DFG)** representing a basic block is partitioned into Data Flow Trees (DFT), each of which is covered using tree pattern matching. Multiple alternative covers are permitted including sub-**SIMD** covers which represent a sub-operation (or element) in a **SIMD** instruction. The second step then uses integer linear programming to determine the best cover for the **DFG** while aiming at minimizing the

5. Access to memory at address aligned to the SIMD registers size.

6. Access to contiguous elements in memory (stride = 1).

implementation cost. Tree covers can be merged to form **SIMD** covers. This technique mainly lacks scalability with respect to the basic block size and **SIMD** data-path size. Also, this method does not consider data transfer, which often prevent the exploitation of SIMD instructions.

TANAKA et al proposed an extension [131] to the aforementioned work, taking data transfer operations into account.

LARSEN and AMARASINGHE proposed a new method for exploiting **SIMD** at the basic-block level, they referred to it as **Superword Level Parallelism (SLP)** [69]. They define **SLP** as a new type of parallelism, distinguishing it from conventional vector parallelism. **SLP** aims at finding in a basic block, similar independent statements that can be packed together and replaced by **SIMD** instructions. Thus, in contrast to loop vectorization, **SLP** does not have to deal with loop carried dependencies or employ sophisticated loop transformations to uncover parallelism. Hence, it is simpler to apply. Although they are not necessary, loop transformations can still be used to convert loop-level parallelism into **SLP** (using unroll-and-jam or register level tiling [49, 108] for example).

In fact, **SLP** is a superset of vector parallelism. The latter can only pack instances of the same statement in a vectorizable loop (inter-loop instances parallelism), whereas **SLP** can pack different statements in a basic block, which can be part of a loop body (intra-loop parallelism). **SLP** is, hence, able to exploit a finer level of parallelism, since loop-level parallelism is easily amenable to intra-loop parallelism by mean of loop transformations such as loop unrolling. This allows **SLP** to find more and/or better opportunities when targeting Multimedia extensions.

Note that **SLP** extraction techniques are applicable to Subword Multimedia extensions as well, since subword parallelism is actually a special case of **SLP**.

To illustrate **SLP** let us consider the example in fig. 3.6, targeting a 64-bit wide Multimedia extension supporting 32-bit integer data type as vector elements. The loop in the original code (fig. 3.6a) does not carry any dependency, thus all its iterations can be executed in parallel. The loop is partially unrolled by a factor of 2 (fig. 3.6b).

Using **SLP**, we can either:

- Pack statements *S0* and *S1* in the loop body as illustrated in fig. 3.6c.
- Or pack consecutive instances of each statement separately, after applying loop unrolling by a factor 2, as illustrated in fig. 3.6d.

The first solution is likely to give better performance than the second one since it requires less packing/unpacking operations (assuming vector memory accesses are aligned).

Using loop vectorization, only the second solution is possible.

As mentioned earlier, when targeting Multimedia extensions, the compiler must deal with data packing/unpacking and memory access alignment, which can represent a significant overhead hindering the **Simdization** benefits. This is not different in case of **SLP**. In fact, this is the main challenge for **SLP** extraction algorithms, which attempt to address it by adopting heuristics promoting the packing of statements that lead to less packing/unpacking overhead. The state-

<pre> for (i = 0; i &lt; N ; i++) { S0:  Y[2i] = X[2i] + A[i]; S1:  Y[2i+1] = X[2i+1] + B[i]; } </pre>	<pre> for (i = 0; i &lt; N ; i+=2) { //i S0:  Y[2i] = X[2i] + A[i]; S1:  Y[2i+1] = X[2i+1] + B[i]; //i+1 S0:  Y[2i+2] = X[2i+2] + A[i+1]; S1:  Y[2i+3] = X[2i+3] + B[i+1]; } </pre>
--	---

(a) Original code.

(b) 2x unroll.

```

for (i = 0; i < N ; i+=2) {
S0S1: Y[2i:2i+1] = X[2i:2i+1] + <A[i],B[i]>; //i
S0S1: Y[2i+2:2i+3] = X[2i+2:2i+3] + <A[i+1],B[i+1]>; //i+1
}

```

(c) Packing  $S0_i$  and  $S1_i$  together. Note that the unrolling is not necessary in this case

```

for (i = 0; i < N ; i+=2) {
S0:  <Y[2i],Y[2i+2]> = <X[2i],X[2i+2]> + A[i:i+1]; // <i,i+1>
S1:  <Y[2i+1],Y[2i+3]> = <X[2i+1],X[2i+3]> + B[i:i+1]; // <i,i+1>
}

```

(d) Packing two consecutive instances of  $S0$  ( $S0_i$  and  $S0_{i+1}$ ) and  $S1$ .

Figure 3.6 – Example illustrating the difference between loop vectorization and **SLP**.  $[min : max]$  represents a vector memory access to consecutive array elements starting at offset  $min$  till offset  $max$  included.  $<a, b>$  represents a packing/unpacking operation.

of-the-art of **SLP** is discussed later in chapter 4.

### 3.4 Conclusion

In this chapter we have presented the characteristics of some **SIMD** instruction sets and we have discussed the existing techniques for exploiting them.

In summary, we can observe that:

- Most embedded processors provide **SIMD** capabilities, mainly as subword Multimedia extensions.
- **Simdization** can be performed either at loop-level using loop vectorization techniques, or at the basic-block level using **SLP** extraction techniques.
- **SLP** can exploit more parallelism than loop vectorization. The latter can be amenable to **SLP** using simple loop transformations.
- **SLP** extraction is simpler since it does not require advanced loop dependencies analysis and transformations to uncover parallelism.

Based, on these conclusions, we decided to implement [SLP](#) extraction to perform [Simdization](#) in the context of the ALMA project.

In the next chapter, we discuss the state-of-the-art of [SLP](#) and we propose an enhanced [SLP](#) extraction algorithm, which we then implement as a source-to-source transformation along with a [SIMD](#) C code generator, and compare it against a state-of-the-art algorithm.



## Chapter 4

# Superword Level Parallelism

### Contents

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## 4.1 Introduction

In the context of the ALMA project, as presented in sections 1.2 and 1.3, we needed to implement an automatic **Simdization** in order to exploit the **Single Instruction Multiple Data (SIMD)** capabilities of the targeted embedded processors, namely XENTIUM [104] provided by RECORE SYSTEMS and KAHRISMA [58] provided by **KARLSRUHE INSTITUTE OF TECHNOLOGY (KIT)**. In fact, both embedded processors provide support for integer subword **SIMD** operations. They support 2x16-bit operations, in addition KAHRISMA supports 4x8-bit operations. However, none of the back-end compilers provided for each target implements a automatic **Simdization** optimization. Instead, they provide a set of intrinsics to access **SIMD** instructions. This is also the case of many other embedded processors, such as ST240 [4].

As we discussed in the previous chapter, performing **Simdization** manually using intrinsics is a tedious, error prone and time consuming task. Therefore, one of the goals of the ALMA project is to automate this transformation. This can be achieved by integrating an automatic **Simdization** transformation into the back-end compiler of each one of the target processors. However, this is not a practical solution since it should be done for each new target processor to be supported. In order to avoid this, we decided to implement **Simdization** at source code level using a source-to-source compilation flow capable of generating a C code with **SIMD** intrinsics. In the previous chapter, we discussed different methodologies for performing **Simdization**, mainly loop vectorization and **Superword Level Parallelism (SLP)**. We decided to use **SLP** since it does not require advanced loop dependencies analysis and transformations, in addition it can exploit more parallelism.

**SLP** concept was first defined and presented by LARSEN and AMARASINGHE in 2000 [69]. In the same work they also presented an algorithm allowing to extract **SLP** in a given basic-block. In the remainder of this chapter we will refer to this algorithm as **original SLP**. The statements grouping strategy used in **original SLP** aims at reducing data packing/unpacking cost. However, it is based on a local heuristic ignoring some packing possibilities. A more detailed analysis of **original SLP** is presented later on in section 4.2.1. Several work [124, 125, 36, 46] aimed at enhancing **original SLP**, we present some of them in section 4.2.2.

Recently a new **SLP** extraction algorithm was introduced by LIU et al in 2012 [78] to address the shortcoming of **original SLP**. Unlike **original SLP**, the statements grouping strategy they propose is based on a *global* estimation of the data packing/unpacking cost, taking into account all (size-two) packing possibilities in the basic-block. We will refer to this method as **holistic SLP** and we will discuss it thoroughly later on in section 4.3.

Based on the advantage of **holistic SLP** over **original SLP**<sup>1</sup>, we decided to go with **holistic SLP** for implementing **Simdization** in the ALMA flow. However, after a thorough analysis of the **holistic SLP** algorithm we discovered several shortcomings. In section 4.3.2, we present an elaborate explanation of these shortcomings. In short, we noticed that **holistic SLP** yields

---

1. experimental results presented in [78], shows a performance improvement as high as 15% over **original SLP**

poor performance without applying data layout transformation, mainly due to the grouping candidate benefit estimation method they use. In fact, data layout transformations are not always applicable (the method they propose is only applicable in the context of the polyhedral model), and they increase the memory footprint (due to arrays replication). This is not suitable when targeting embedded platforms with limited memory resources, such is the case in the context of ALMA. Furthermore, the [Intermediate Representation \(IR\)](#) they propose in order to represent [SLP](#) grouping solutions, is bulky and does not provide necessary information for rapid estimation of the amount of reuse between different statement grouping candidates.

In section 4.4, we propose several improvements to solve these problems. More specifically, we propose:

- A new [IR](#) for [SLP](#) extraction capturing grouping opportunities with conflicts and superword reuse information. It is more expressive and compact compared to `holistic SLP`.
- A new grouping candidate benefit estimation together with a new group selection method, allowing to achieve up to 40% performance improvement compared to `holistic SLP` without the need for data layout transformations.

Finally, in section 4.5 we present the implementation and some experimental results comparing our proposed [SLP](#) extraction algorithm against `holistic SLP` on a set of nine benchmarks targeting four different embedded processors.

## 4.2 Related work

In this section we discuss the state-of-the-art of [SLP](#) algorithms. We start by presenting `original SLP`, we highlight its shortcomings and then we present an overview of the work improving them.

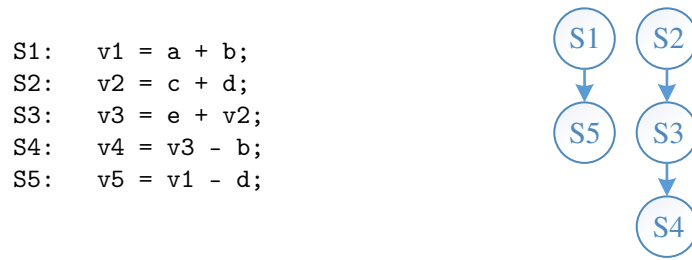


Figure 4.1 – Example C code snippet (left) and its statements dependence graph (right).

**Définition 4.1 (Statement)** *A statement is a root instruction in a basic block. It contains one or more operations. Two statements are isomorphic if they both contain the same operations in the same order.*

**Example 1** *S1, S2, ..., S5 in the C code example of fig. 4.1 are all statements. S1, S2 and S3 are isomorphic statements, and so are S4 and S5. Statement S3 depends on S2.*



**Définition 4.2 (Superword Statement)** *A superword statement is a list of isomorphic independent statements that can be implemented using one or more SIMD instructions. Superword statement's operands are superwords (or vectors).*

#### 4.2.1 Original SLP

**Original** SLP algorithm aims at extracting SIMD parallelism at basic block level. Given a list of a basic block's statements, it aims to combine several isomorphic, independent statements into superword statements. This is known as statements packing or grouping. The superword statements are then implemented using SIMD instructions.

Statements packing is a combinatorial optimization problem. Using exhaustive search is often not realistically feasible. Therefore, **original** SLP, and all other SLP extraction algorithms for this matter, use a heuristic to find a satisfying solution within a reasonable time.

The heuristic employed by **original** SLP exploits two observations:

- Accesses to aligned contiguous memory references is efficiently implemented in Multimedia extensions.  $N$  individual memory access operations can be performed using one SIMD access which transfers packed data directly to/from a SIMD register with no need for additional packing/unpacking or shuffling operations. This roughly saves  $N - 1$  memory accesses along with their address calculation operations.
- No packing/unpacking or shuffling operation is needed when a SIMD instruction's operand has been produced by another SIMD instruction since it is already packed in a SIMD register (assuming enough registers are available).

This heuristic consists of starting by packing statements that contain contiguous memory accesses. And then find additional statement packs by following the def-use and use-def chains of the already formed ones. At first, only groups of two statements are packed together (to reduce the search space) and then multiple groups are merged to obtain larger superword statements to better utilize the SIMD data-path.

This imposes that each superword statement contains either a vector access to contiguous region in memory or/and reuses superwords resulting from other superword statements directly, which minimizes the need for overhead packing/unpacking and permutation operations. But still, some packed statements might have an important overhead that can degrade performance. To avoid such cases, a cost model is used during statements packing process. It estimates the speedup of each potential packed statements and discards those with negative effects. This estimation takes into account the necessary packing/unpacking operations as well as reuses of already existing superwords. It is also used to select between conflicting statements packing possibilities.

This heuristic aims at minimizing the overhead of packing/unpacking operations by maximizing superwords reuse, starting from and/or leading to, in-memory packed and aligned superwords. Statement packs are selected based on their superword reuse with previously decided statement packs, leading to a local optimization that is strongly affected by the previously made packing decisions. Furthermore, it completely ignores statement packing possibilities which are not in a

superword reuse chain coming from, or leading to, an in-memory packed superword.

This main shortcoming has been identified and addressed by LIU et al who recently proposed an alternative [SLP](#) statements packing heuristic [78] based on a global, or holistic, superword reuse estimation. This work is thoroughly discussed later in section 4.3.

#### 4.2.2 Original SLP Extensions and Enhancements

SHIN et al introduced superword-level locality [124, 122], a technique allowing the use of [SIMD](#) register file as a compiler-controlled local memory. They propose superword replacement transformation, which substitutes vector memory accesses to arrays by accesses to superword temporaries allocated in [SIMD](#) registers. In addition, they employ unroll-and-jam loop transformation to enhance locality and shorten superword reuse distance, along with index set splitting to increase the amount of aligned memory accesses.

Besides, they also proposed an extension of [original SLP](#) allowing it to be applied beyond simple basic block, in the presence of control flow structures [125, 122]. To do so, they perform if-conversion prior to extracting [SLP](#) in order to convert control structures into predicated instructions. After superword packing, they restore control structures to be able to target Multimedia extensions with no support for predication.

KUDRIAVTSEV and KOGGE [63] proposed an alternative packing strategy to extract [SLP](#). Unlike [original SLP](#), it allows the exploration of superword reordering to efficiently generate and optimize permutation operations. It borrows from the work of LEUPERS [74] the fact of leveraging tree pattern matching to find covers for data flow trees – obtained by partitioning the basic block’s [Data Flow Graph \(DFG\)](#) – and then find a cover for the entire [DFG](#) using [SIMD](#) instructions.

They start by grouping contiguous memory accesses to form [SIMD](#) groups<sup>2</sup>, then they find further [SIMD](#) groups by traversing the [DFG](#) starting from memory operations appearing in [SIMD](#) groups. Then, in the [DFG](#), they replace the nodes of each [SIMD](#) group by a node representing the group. Finally they try to find an order, for the elements of each [SIMD](#) group, that minimizes the cost. For doing so, they use order propagation starting from memory access [SIMD](#) groups, which have a fixed order, to obtain the set of possible permutations per [SIMD](#) group, then they use Integer Linear Programming to find the best ordering assignment per group.

REN et al proposed a standalone algorithm to optimize data permutations [107] in a given basic block that can be used in complement to other [Simdization](#) transformations. First it converts all permutations in a source code into a generic representation. Then it tries to optimize the permutations inside each basic block before regenerating the corresponding target-dependent permutation instructions.

---

2. A [SIMD](#) group is a set of operations that can be implemented with a [SIMD](#) instruction.

### 4.3 Holistic SLP

The statements packing heuristic employed by **original SLP** aims at maximizing superword reuse by following def/use and use/def chains starting from, or leading to, in-memory packed superwords. However, it does not consider statement packing options unless they are in a superword reuse chain seeded by one or more unit-stride (and aligned) memory accesses pack. Also, it does not consider superword permutations (or shuffling). In fact, it only qualifies as superword reuse, superwords containing the same elements in the *same* order. This ignores the possibility of employing shuffling operations to reuse a superword containing the same elements but in a different order. Shuffling operations are generally much less costly than packing/unpacking operations.

This results in a local optimization since statement packs are selected based on their superword reuse with already formed statement packs only, and not across the whole basic block.

To address this shortcoming, LIU et al proposed an alternative statement packing heuristic [78] based on a global, or holistic, estimation of superword reuse across the entire basic block. We refer to it as **holistic SLP**.

In section 4.3.1 we present the **holistic SLP** extraction algorithm, we then analyze it and discuss several shortcomings in section 4.3.2, that we try to address in section 4.4. But, first we start by giving several related definitions:

**Définition 4.3 (SIMD Group Candidate)** A *SIMD* group candidate is an unordered pair (pair set) of isomorphic and independent statements, yielding superwords compatible with the *SIMD* data-path size. All elements in a superword must have the same size, that need to be supported by the target *SIMD Instruction Set Architecture (ISA)*, and the total size should not exceed the *SIMD* vector size.

**Définition 4.4 (Variable Pack)** A *Variable Pack (VP)* is an unordered pair (pair set) of operands from same position of both statements in a *SIMD* group candidate. Two *VPs* are equivalent if they contain the same elements (regardless of their order). We use the symbol  $\equiv$  to mark equivalence.

**Définition 4.5 (Candidate Conflict)** Two candidates are considered in conflict if, they either share a common statement or there exist a cyclic dependency between them. We refer to the first case as common statement conflict and to the second as cyclic dependency conflict.

We distinguish two types of cyclic dependency conflict:

- *Direct*: occurs between two candidates only.
- *Indirect*: occurs between more than two candidates.

**Example 2** Consider the example of fig. 4.1 with 32-bit data-types and targeting a 64-bit wide *SIMD* data-path.

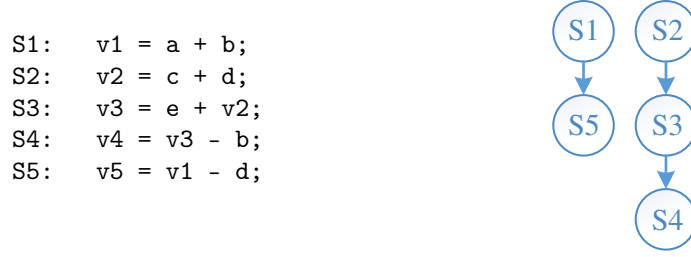


Figure 4.2 – Recall example of fig. 4.1.

- $\{S1, S2\}$  is a **SIMD** group candidate, and so are  $\{S1, S3\}$  and  $\{S4, S5\}$ .  $\{S2, S3\}$  is not a candidate, though  $S2$  and  $S3$  are isomorphic.
- The **VPs** of the candidate  $\{S1, S3\}$  are  $\{v1, v3\}$ ,  $\{a, e\}$  and  $\{b, v2\}$ . **VPs**  $\{v1, v3\}$  from candidate  $\{S1, S3\}$ , denoted  $\{v1, v3\}_{\{S1, S3\}}$ , and  $\{v3, v1\}$  from  $\{S4, S5\}$  are equivalent i.e.  $\{v1, v3\}_{\{S1, S3\}} \equiv \{v3, v1\}_{\{S4, S5\}}$ .
- Candidates  $\{S1, S2\}$  and  $\{S1, S3\}$  have a common statement conflict.  
Figure 4.7 shows an indirect cyclic dependency conflict case.

#### 4.3.1 Overview

Holistic SLP extraction algorithm overview is depicted in fig. 4.3. It consists of several steps that we illustrate in this subsection based on its presentation by LIU et al in [78].

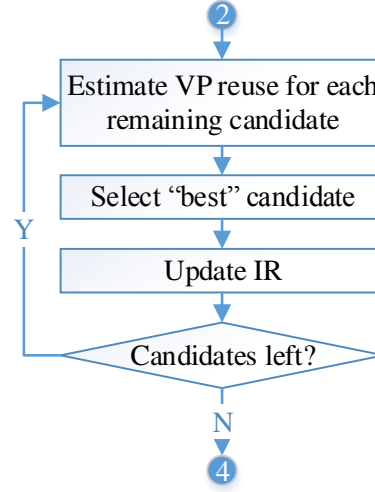
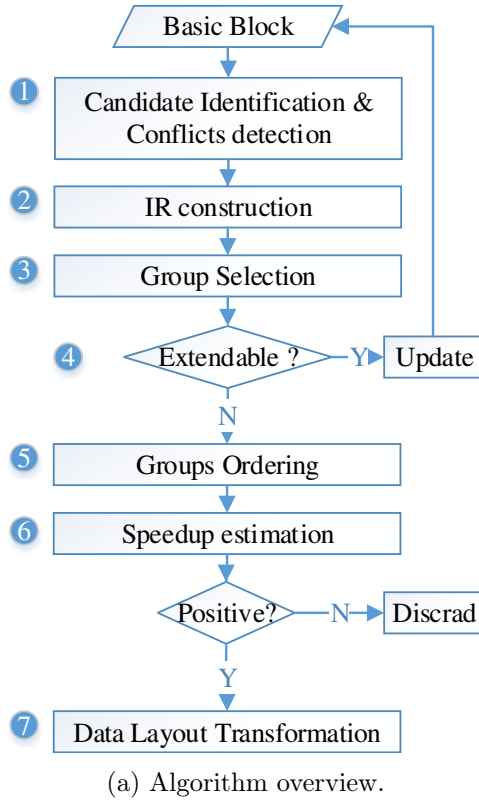
In a nutshell, **holistic SLP** aims at finding as much statement packs (or groups) as possible while maximizing superword reuse throughout the entire basic block. Exploiting the fact that, increasing superword reuse reduces the need for data packing/unpacking operations, which generally introduce an important overhead that might eclipse the potential benefit of **SLP** and degrade performance. To do so, it considers all statement grouping candidates available in the basic block (step 2), among them, it then selects the ones that are more likely to bring the most superword reuse and discard those conflicting with them (step 3).

Since considering all possible statement packing combinations, with different sizes and different statements order, yields a very high number of possibilities, **holistic SLP**, in fact, only considers statement groups of size two and ignores the order of statements inside a group. Such statements group is referred to as **SIMD** group candidate (definition 4.3) and represents two statement packs possibilities.

In order to extend the statement groups size beyond two and fully utilize the target **SIMD** datapath, the selected **SIMD** groups at step 3 are integrated in the basic block before starting a new iteration, as shown in step 4.

The order of statements inside each selected group is then specified, at step 5, with the objective of maximizing the direct superword reuse and hence minimizing the need for permutation operations.

At last, **holistic SLP** optionally applies a data layout transformation (step 7) to optimize superwords placement in memory, when possible, in order to minimize the overhead associated



(b) Group Selection procedure overview.

Figure 4.3 – Holistic SLP algorithm flow diagram.

with accessing them.

### Step 1: SIMD Group Candidates and Conflicts Identification

This step aims at constructing the set of all possible **SIMD** group candidates as well as the set of all conflicts between them. **SIMD** group candidate and conflict definitions are given by definition 4.3 and definition 4.5 respectively.

### Step 2: Intermediate Representation (IR) Construction

To capture all the information required by the algorithm, an intermediate representation is build. This representation consists of two undirected graphs:

- **Statement Grouping Graph (SGG)**: It is a weighted undirected graph. Its nodes are the set of all statements present in at least one candidate. An edge represents a possible **SIMD** group candidate; so that two nodes are connected by an undirected weighted edge if they belong to the same candidate. The weight of each edge represents the benefit, described later on, associated with the selection of the corresponding candidate. All edge weights are computed in the next step.

- **Variable Pack Conflict Graph (VPCG)**: This graph captures **VP** reuses and conflicts across all candidates. It is used to ease the computation of **VP** reuse benefit of each candidate as we will explain in the next step.

**VPCG** is an unweighted undirected graph. Its nodes are the variable packs (**VPs**), as defined by definition 4.4, from each **SIMD** group candidate. In order to distinguish equivalent **VPs** belonging to two different candidates, each **VP** node is tagged by the candidate to which it belongs. Two **VP** nodes are connected by an undirected edge in **VPCG** if their corresponding candidates conflict with each other.

**Example 3** In the ongoing example of fig. 4.1:

The set of **SIMD** group candidates is:

$$C = \{c1 = \{S1, S2\}, c2 = \{S1, S3\}, c3 = \{S4, S5\}\} \quad (4.1)$$

There is only one conflict, a common statement conflict in fact, between the candidates. The conflicts set is:

$$\{\{c1, c2\}\}$$

The corresponding **VPCG** and **SGG** are shown in fig. 4.4b and fig. 4.4c respectively.

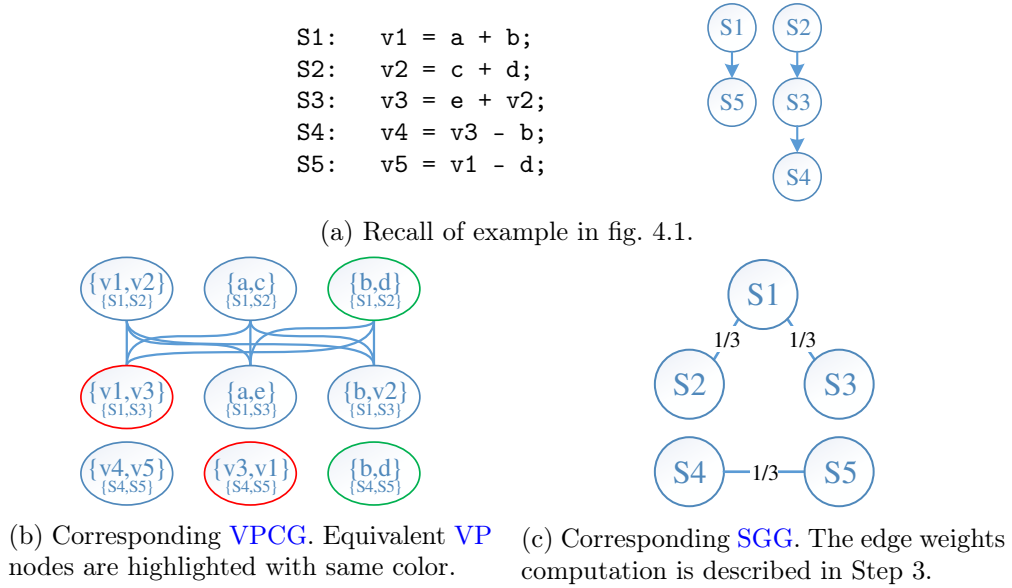


Figure 4.4 – **VPCG** and **SGG** of the example in fig. 4.1.

### Step 3: SIMD Group Candidate

The **SGG** constructed in step 2 represents all the possible **SIMD** group candidates, not all of which can coexist together since some conflict with others. The aim of this step is to select the most profitable (in term of **VP** reuse) conflict-free subset of candidates.

The selection procedure employed by **holistic** SLP, illustrated in fig. 4.3b, is based on a global (holistic) estimation of the amount of **VP** reuse each **SIMD** group candidate can bring to the entire basic block. It operates as follow:

- First, for each of the remaining group candidates (edges in **SGG**), **VP** reuse across the entire basic block is estimated assuming the candidate at hand get selected. This **VP** reuse estimation is attributed as weight to the corresponding edge in **SGG**. The method used for estimating **VP** reuse is presented later on.
- Then, the candidate whose selection brings the maximum **VP** reuse, that is the edge in **SGG** with highest weight, is selected to be part of the solution. In case multiple candidates yield the same highest **VP** reuse, only one of them is selected randomly.
- Finally, both **SGG** and **VPCG** are updated before starting the next selection iteration until no more candidates remain (**SGG** has no edges anymore). **SGG** is updated by removing both nodes belonging to the selected group candidate as well as all nodes/edges connected to any of them<sup>3</sup>. Similarly, **VPCG** is updated by removing all nodes belonging to the selected group candidate as well as all nodes/edges connected to any of them.

### Variable Pack Reuse Estimation

The **SIMD** group selection process is iterative. In order to decide which candidate should be selected at a given iteration, all remaining candidates are evaluated. For each of them, the average **VP** reuse among the entire basic block is estimated. The aim is to find the candidate that, if selected, is more likely to bring the highest **VP** reuse across the whole basic block.

Since the actual **VP** reuse across the basic block cannot be computed before the selection process is completed and the final grouping solution is obtained, the authors of **holistic** SLP propose a heuristic to estimate this reuse. The intuition is to consider the context in which the tested candidate,  $c$ , get selected. In this context, the actual **VP** reuse among already selected groups can be computed, but this does not include the potential contribution of the remaining candidates (from which, some would be selected in the next selection iterations to become part of the final solution). In order to estimate the potential contribution of these candidates, a greedy heuristic is employed. It aims at finding a conflict free subset of the remaining candidates which have reuses with  $c$ . This is achieved by considering all **VPs**, from the remaining candidates, that are equivalent<sup>4</sup> to any of  $c$ 's **VPs**. These **VPs** may be conflicting with each other, which means they cannot coexist in any possible grouping solution. Therefore, these conflicts are solved by, iteratively, eliminating the **VP** which has the most conflicts, until no conflicts remain. The number of remaining **VPs** represent an estimation of the amount of reuse of  $c$ 's **VPs** by future selected candidate in case  $c$  get selected.

All in all, **VP** reuse among already established part of the grouping solution as well as remaining group candidates are considered, making this approach more *holistic* than **original** SLP.

To formally define the benefit evaluation of an **SIMD** group candidate, let:

---

3. **SGG** nodes connected to any of both nodes of the selected candidate are part of conflicting candidates.

4. Two **VPs** are equivalent if they contain the same elements (see definition 4.4). Equivalent **VPs** indicate a reuse.

- $G$  be the set of already selected groups.
- $C$  be the set of remaining candidates.

To estimate the benefit associated with  $c \in C$ , denoted  $VPR(c)$ ,  $c$  is assumed to be selected. So:

- $G' = G \cup \{c\}$  is the set of selected groups.
- $C' = C \setminus (\{c\} \cup \text{conf}(c))$  is the set of remaining group candidates, if  $c$  get selected. Where  $\text{conf}(c)$  is the set of candidates in  $C$  conflicting with  $c$ .

$VPR(c)$ , as described in **holistic SLP** [78], is computed as follows:

$$VPR(c) = \frac{|V(G')| - |P(G')| + |R(c)|}{|P(G')|} \quad (4.2)$$

The definition of  $V$ ,  $P$  and  $R$  is provided below, intuitively:

- $|P(G')|$  represents the number of packing/unpacking operations required by all groups in  $G'$ .
- $|V(G')| - |P(G')|$  represents the actual number of **VP** reuses between the selected groups in  $G'$ .
- $|R(c)|$  is the estimation of reuses of  $c$ 's **VPs** by the remaining candidates (in  $C'$ ).

Where:

- $V$  is a function that, given a set,  $S$ , of **SIMD** group candidates, returns the set of all their **VPs**, each candidate's **VPs** are distinguished from others by tagging them with the candidate to which they belong so that, equivalent<sup>5</sup> **VPs** from distinct candidates are distinguishable.

$$V(S) = \bigcup_{c \in S} \{v_c, v \in c\} \quad (4.3)$$

Where  $v_c$  is the variable pack  $v$  of the candidate  $c$ , tagged by  $c$ . So that,  $v_{c1} \equiv v_{c2} \equiv v$  but  $v_{c1} \neq v_{c2}$  i.e.  $\{v_{c1}\} \cup \{v_{c2}\} = \{v_{c1}, v_{c2}\}$  (assuming  $c1 \neq c2$ ).

- $P$  is a function that, given a set,  $S$ , of **SIMD** group candidates, returns the set of **VPs** of all group candidates in  $S$ . Note that in contrast to  $V$ , the returned **VPs** are not tagged so that, equivalent **VPs** from different candidates are not distinguishable i.e.  $\{v \text{ from } c1\} \cup \{v \text{ from } c2\} = \{v\}$

$$P(S) = \bigcup_{c \in S} \{v \in c\} \quad (4.4)$$

- $R(c)$  is a conflict-free subset of, the set of **VPs** of candidates in  $C'$  which are equivalent to (i.e. reuses) any of  $c$ 's **VPs**. In **holistic SLP**,  $R(c)$  is obtained by:
  1. First, constructing an *auxiliary graph* (as they refer to it in **holistic SLP**), associated with  $c$ , denoted  $AG(c)$ . It is a subgraph of **VPCG**, built by extracting all nodes (and all edges connected to them) equivalent to, but not connected to those of  $c$ .  $AG(c)$  nodes are therefore, all the tagged **VPs** from  $C'$  that are equivalent to any **VP** from  $c$ .

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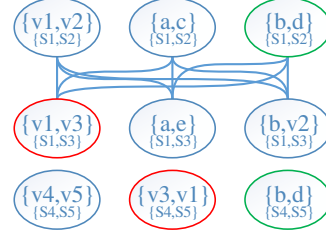
5. Two **VPs** are equivalent (denoted by  $\equiv$ ) if they contain the same elements (definition 4.4).



2. And then eliminating all conflicts (edges) in  $AG(c)$ , by iteratively discarding a node with highest degree, that is a **VP** node which has the highest number of conflicts, until all conflicts are eliminated yielding  $R(c)$ .

**Example 4** To illustrate this step, let's consider the ongoing example of fig. 4.1.

S1:  $v1 = a + b$ ;  
 S2:  $v2 = c + d$ ;  
 S3:  $v3 = e + v2$ ;  
 S4:  $v4 = v3 - b$ ;  
 S5:  $v5 = v1 - d$ ;



(a) Recall of example of fig. 4.1.

(b) Recall **VPCG** at first iteration.

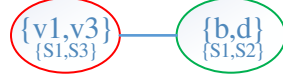


Figure 4.5 –  $AG(\{S4, S5\})$  at the first selection iteration of the example of fig. 4.1.

At the first selection iteration:

- $G = \emptyset$  and  $C = \{c1 = \{S1, S2\}, c2 = \{S1, S3\}, c3 = \{S4, S5\}\}$
- **VPCG** is shown in fig. 4.4b.
- In order to compute  $VPR(c3)$ :
  - Extract  $AG(c3)$  from **VPCG**.  $AG(c3)$  is depicted in fig. 4.5.
  - Eliminate conflicts(edges) from  $AG(c3)$ : iteratively remove one node with highest degree. Both nodes in  $AG(c3)$  have degree of one, so removing any of them will do. Therefore, the number of remaining nodes  $ES = |AG(c3).V| = 1$ .
  - $V(G') = V(\{c3\}) = \{\{v4, v5\}_{c3}, \{v3, v1\}_{c3}, \{b, d\}_{c3}\}$ . Thus,  $|V(G')| = 3$ .
  - $P(G') = P(\{c3\}) = \{\{v4, v5\}, \{v3, v1\}, \{b, d\}\}$ . Thus,  $|P(G')| = 3$ .
  - Hence,  $VPR(c3) = \frac{1 + 3 - 3}{3} = 1/3$ .
- Similarly,  $VPR(c1) = 1/3$  and  $VPR(c2) = 1/3$ . The edges of **SGG** are weighted by the corresponding  $VPR$  as shown in fig. 4.4c.
- Since all candidates have same weight, one of them is selected randomly. Let's assume it's  $c3$  that got selected.
- The updated **VPCG** and **SGG** are represented in fig. 4.6.

At the second selection iteration:

- $G = \{c3\}$  and  $C = \{c1, c2\}$
- In order to compute  $VPR(c1)$ :
  - $AG(c1)$  is empty  $\Rightarrow ES = 0$ .
  - $V(G') = V(\{c3, c1\}) = \{\{v4, v5\}_{c3}, \{v3, v1\}_{c3}, \{b, d\}_{c3}, \{v1, v2\}_{c1}, \{a, c\}_{c1}, \{b, d\}_{c1}\} \Rightarrow |V(G')| = 6$ .

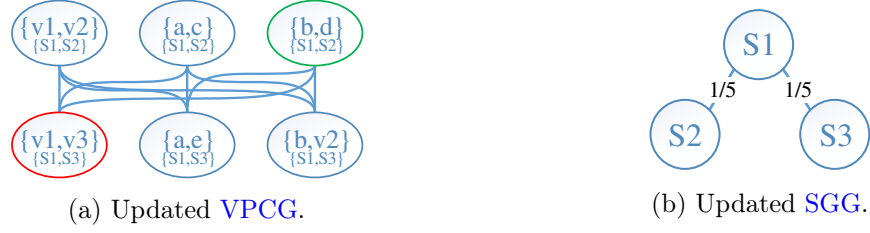


Figure 4.6 – Updated **VPCG** (left) and **SGG** (right) after the selection of  $\{S4, S5\}$  of the example of fig. 4.1.

- $P(G') = P(\{c3, c1\}) = \{\{v4, v5\}, \{v3, v1\}, \{b, d\}, \{v1, v2\}, \{a, c\}\} \Rightarrow |P(G')| = 5.$
- Therefore  $VPR(c1) = \frac{0 + 6 - 5}{5} = 1/5.$
- Similarly,  $VPR(c2) = 1/5.$
- Again, both candidates have same weight, so one of them is selected randomly. Let's assume it's  $c2$ .
- **SGG** is then updated by removing  $c2$ 's nodes,  $S1$  and  $S3$ , but also all nodes connected to them i.e  $S2$ .
- No more candidates are left, thus the selection procedure is done.

Thus, the final set of selected groups is  $\{c3, c1\}$ .

#### Step 4: Groups Extension

This step aims at overcoming the size limitation, of only two statements per group, imposed by the first step. This allows the algorithm to efficiently target **SIMD** with wider data-path size.

Once **SIMD** group selection is done, if there is any group that can be extended, the basic block is updated by replacing each selected group's statements by a single new statement with new variables to represent its **VPs** (superwords), then the algorithm starts over at step 1 until no further grouping extension is possible.

#### Step 5: **SIMD** Groups Ordering

At this level, each selected **SIMD** group is a set of two or more, isomorphic independent, statements from the original basic block. The order of statements inside a group is not defined yet. So far, it has been assumed that, if two groups have an equivalent **VP**, it counts as a superword reuse regardless of the order of statements inside each group. In fact, this is not always true and a superword permutation/shuffling may be required in order for this reuse to happen. The cost overhead of these permutation operations may hinder the benefit of **Simdization**.

Hence, the aim of this step is to order statements inside each group in such a way that the number of necessary permutations is minimized. The ordered groups are then implemented as superword statements in the basic block.

### Step 6: Speedup Estimation

At this level, the necessary [SIMD](#) instructions to implement the superword statements obtained from previous step, specially packing/unpacking and permutations, can now be accurately determined. A speedup estimation of the transformed basic block is performed and compared to that of the original scalar basic block. In case this indicates a performance degradation, the superword transformation is discarded and the basic block is left unchanged. The aim of this step is to make sure the generated superword solution will most likely perform better than the scalar one. However, this tightly depends on the cost model used for the target architecture.

### Step 7: Data Layout Transformation

It is important to note that **holistic SLP** does not impose any constraints on packing array references. Consequently, the group selection step is likely to produce superwords with accesses to non-contiguous memory locations. Such superwords require costly packing operations which hinder the [Simdization](#) benefits, as illustrated in fig. 3.5.

To overcome this problem, **holistic SLP** optionally applies a data layout transformation to optimize superwords placement in memory, when possible, so that to minimize the overhead associated with accessing them.

The aim of this transformation is to minimize the cost of required packing/unpacking operations by trying to place the superword elements in contiguous (and aligned) memory locations, so they can be accessed using vector memory access operations without additional shuffling/insert/extract operations, as was shown in fig. 3.5.

This optimization targets two kind of superwords:

- Scalar superwords whose elements are all scalar variables.
- Array reference superwords whose elements are all array elements.

Scalar superwords are relatively simple to optimize. All is needed is to assign the superword elements consecutive memory locations. However, when two scalar superwords have elements in common and requires conflicting memory layouts, only one of them can be optimized.

The method employed in **holistic SLP** consists of optimizing the most reused scalar superword first and skipping all other conflicting superwords.

Optimizing array reference superwords, on the other hand, is more complex. In general, an element of such superword is a reference to a variable location in an array, usually determined by the surrounding loop iterators.

**Holistic SLP** leverages the polyhedral model and array replication to map elements of an array reference superword to contiguous memory locations in the transformed data layout. This transformation is only applicable to [Static Control Parts \(SCoPs\)](#) for superwords whose elements refer to the same, read-only, array.

### 4.3.2 Shortcomings

The **holistic** SLP algorithm, presented earlier in section 4.3.1 has several shortcomings. In this section we present and illustrate some of them. Later on, we propose some improvements to address them and further enhance the **holistic** SLP algorithm's efficiency.

#### 4.3.2.1 Cyclic Dependencies

The group selection algorithm employed by **holistic** SLP as described in [78] does not consider cyclic dependency conflicts between **SIMD** group candidates. Thus, the obtained grouping solution is not guaranteed to be cyclic dependency free and might thus be illegal.

In fact, only common statement conflicts are considered when building the **VPCG** and **SGG**. That means none of them is carrying any information about cyclic dependency conflicts.

Actually, the described **SGG** model (see section 4.3.1) only carries information about common statement conflicts. A **SGG** node with degree higher than one represents a common statement between multiple ( = degree of node) group candidates. Cyclic dependency conflicts, however, are not represented in this **SGG** model.

On the other hand, when **SGG** and **VPCG** are updated after the selection of a new **SIMD** group, only nodes representing the selected group and those connected to them are removed (see section 4.3.1). This only includes nodes representing candidates in common-statement-conflict with the selected candidate. In other words, nodes representing candidates in cyclic dependency conflict with the selected one remains in **SGG** and **VPCG** and may be selected in later iterations, thus, potentially introducing a cyclic dependency between the selected groups. Since the algorithm does not check for such cycles, the resulting grouping solution is not guaranteed to be legal and a valid schedule may not exist unless some selected groups are discarded!

Regardless, if we assume the lack of management of cyclic dependency conflicts in the algorithm they give is just for simplification (even though this was not stated). Then, given that no check for cycles is performed during group selection, the only way the final grouping solution will be guaranteed to be legal is by:

- Detecting all possible cyclic dependency conflicts before starting the selection process.
- And, represent all these conflicts in **VPCG** and **SGG**.

This solution is over conservative and prevent the selection of some candidates otherwise possible. For instance, in the aforementioned example of fig. 4.7a, if all cyclic dependency conflicts are considered, then the conflicts set is  $\{\{c1, c2\}, \{c1, c3\}, \{c2, c3\}\}$ . In this case only one candidate can be selected. However, if any two candidates are selected the solution would still be valid.

**Example 5** *The example in fig. 4.7a illustrates this problem.*

*At the first selection iteration:*

- *The set of **SIMD** group candidates is  $\{c1 = \{S1, S4\}, c2 = \{S2, S5\}, c3 = \{S3, S6\}\}$ .*
- *The set of common statement conflicts is empty.*

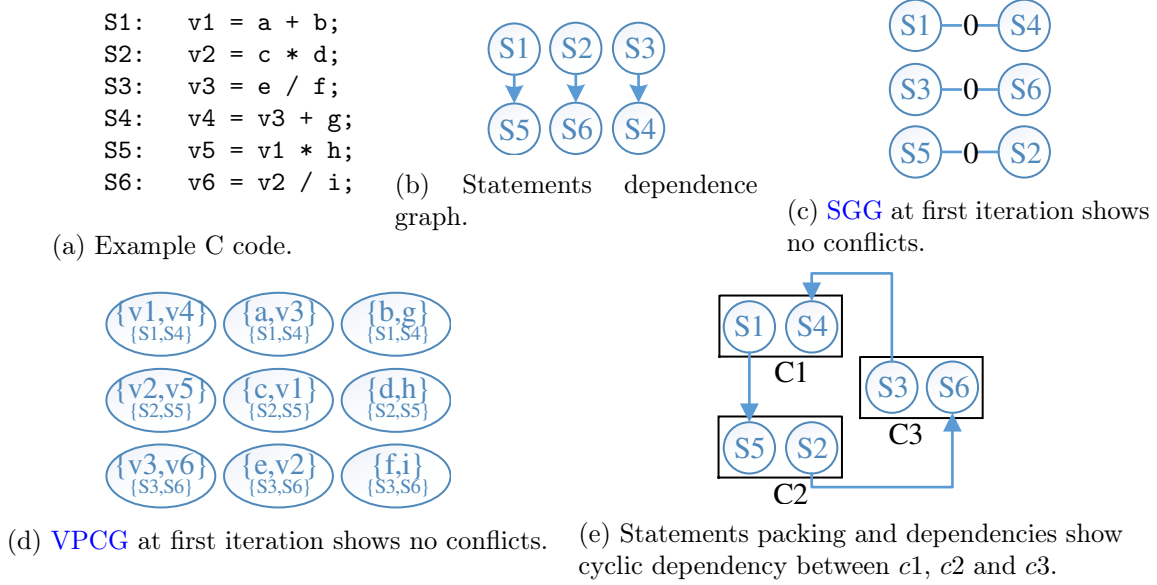


Figure 4.7 – Example illustrating **holistic** SLP algorithm. It shows that **VPCG** and **SGG** do not represent cyclic dependency conflicts. The grouping solution is  $\{c1, c2, c3\}$  which is not legal due to cyclic dependency between  $c1$ ,  $c2$  and  $c3$ .

- The corresponding **VPCG** and **SGG** are depicted in fig. 4.7d and fig. 4.7c, respectively. They show no conflicts between candidates.
- All candidates have same weight, so either of them can be selected (randomly). Let's assume it's  $c1$  that get selected.
- **SGG** is updated accordingly: nodes  $S1$  and  $S4$  (and the edge connecting them) are removed.
- **VPCG** is updated by removing all nodes belonging to  $c1$ , namely:  $\{v1, v4\}_{c1}$ ,  $\{a, v3\}_{c1}$  and  $\{b, g\}_{c1}$ .

At the second selection iteration:

- The set of remaining **SIMD** group candidates is  $\{c2, c3\}$ .
- Still no conflicts represented!
- Either  $c2$  or  $c3$  get selected ( $VPR(c2) = VPR(c3) = 0$ ).
- **VPCG** and **SGG** are updated accordingly.

At the third selection iteration:

- Only one candidate is left and it get selected.

The final grouping solution is, therefore,  $\{c1, c2, c3\}$ . This solution is not legal due to the cyclic dependency between  $c1$ ,  $c2$  and  $c3$  as can be seen in the data dependence graph in fig. 4.7e.

#### 4.3.2.2 Group Selection Process

**Holistic** SLP employs **VP** reuse estimation, detailed in section 4.3.1, to evaluate the benefit associated with the selection of a **SIMD** group candidate. This estimation is a key element since

it is the driver of the grouping decisions leading to the statements packing solution.

When this estimation is not accurate or precise enough, it can misleads the group selection process to make the “wrong” choice resulting in a less efficient solution.

The method used by **holistic SLP** suffers from two main shortcomings. It accounts for invalid **VP** reuse and it considers the same cost for all **VP** types.

### Invalid VP Reuse

The **holistic SLP** algorithm considers a reuse between two **VPs** when they are equivalent<sup>6</sup> regardless of the type of dependency between them. In other words, if there exists an anti-dependency<sup>7</sup> or an output dependency<sup>8</sup> between two **VPs**, a reuse is accounted for. However, in such a case there is no actual reuse between them. This may result in a misleading estimation that prevents the algorithm from selecting the "best" group.

This problem can be easily fixed by eliminating anti- and output dependencies in the basic block prior to applying **SLP** extraction.

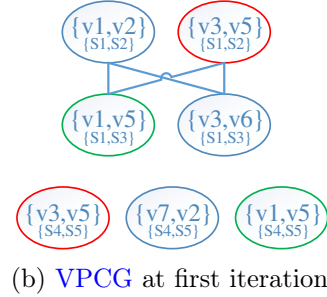
**Example 6** An example of such a case is illustrated in fig. 4.8. In this example the set of candidates is

$$C = \{c1 = \{S1, S2\}, c2 = \{S1, S3\}, c3 = \{S4, S5\}\} \quad (4.5)$$

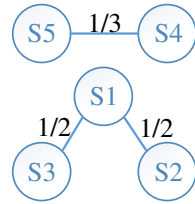
$c1$  conflicts with  $c2$ . The corresponding initial **VPCG** and **SGG** are represented in fig. 4.8b and

S1:  $v1 = v3$ ;  
 S2:  $v2 = v5$ ;  
 S3:  $v5 = v6$ ;  
 S4:  $v3 = v7 + v1$ ;  
 S5:  $v5 = v2 + v5$ ;

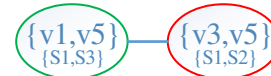
(a) example C code.



(b) **VPCG** at first iteration.



(c) **SGG** at first iteration.



(d) Auxiliary graph for candidate  $\{S4, S5\}$  before conflicts elimination.

Figure 4.8 – Example showing how fake dependencies affect **holistic SLP** VP reuse estimation.

fig. 4.8c respectively. Following the VP reuse estimation method described by **holistic SLP**, a reuse is accounted for between  $c1$  and  $c3$  on the **VP**  $\{v3, v5\}$  even though it is an anti-dependency. Consequently:

- 
- 6. contain the same elements (see definition 4.4)
  - 7. Write-after-Read dependency.
  - 8. Write-after-Write dependency

- $VPR(c1) = VPR(c2) = 1/2$
- $VPR(c3) = 1/3$ ;  $VP \{v3, v5\}$  is reused once by  $c1$  and  $\{v1, v5\}$  is also reused once by  $c2$ , but they both conflict with each other as shown in  $AG(c3)$  depicted in fig. 4.8d, thus only one reuse is considered.

Since  $c1$  and  $c2$  both have the maximum  $VPR$  value, one of them is selected randomly. If  $c1$  is selected, the final grouping solution would be  $\{c1, c3\}$ . In this solution there is no actual  $VP$  reuse since  $\{v3, v5\}$  used by  $c1$  is not reused by  $c3$  but written to. In other words, a packing is needed to form  $\{v3, v5\}$  in order to be used by  $c1$  and also an unpacking is needed to write the result of  $c3$  to  $\{v3, v5\}$  (unless  $\{v3, v5\}$  is contiguous (and aligned) in memory).

However, if the anti-dependency on  $\{v3, v5\}$  was not considered as a reuse,  $VPR(c1)$  would be 0 and the final solution would become  $\{c2, c3\}$  in which there is an actual reuse of  $\{v1, v5\}$  between  $c2$  and  $c3$  (the packed value written to  $\{v1, v5\}$  by  $c2$  can be directly reused by  $c3$ ).

### Same Cost for all **VP** Types

In **holistic** SLP, when forming **SIMD** group candidates, **VPs** are consequently obtained as the set of variables from the same position of the statements inside a group candidate. **Holistic** SLP does not impose any additional constraint on forming **VPs**, which can thus contain any variable whether it is a scalar or an array reference. In particular, **VPs** can contain references to different arrays and/or references to non-contiguous elements of the same array. Such **VPs** induce a high packing/unpacking cost.

During group selection, **holistic** SLP ignores the cost difference between different **VP** types when computing the **VP** reuse estimation associated with a candidate. In fact, only the number of **VPs** is used, thus assuming a unique cost regardless of the **VP** type. This may lead the group selection to select **SIMD** groups with many array reference superwords referring to different arrays or to non-contiguous array elements, completely ignoring the high packing/unpacking cost associated with implementing them.

To counter this problem, **holistic** SLP relies on data layout transformation to hopefully optimize the memory layout of such superwords and avoid the need for packing/unpacking operations. However, the data layout transformation, employed by **holistic** SLP, for array reference superwords suffers from many shortcomings:

- It is very restrictive; it can only be applied in the context of **SCoPs** for array reference superwords referring to the *same* array, that should be *read-only*.
- It may introduce significant additional memory requirements. Up to an array replication per array reference superword, in fact. When targeting embedded platforms, memory resources are generally very limited. In particular, the data cache or local scratchpad memory.
- It may also introduce execution time overhead to initialize the array replications with the transformed data layout from the original layout, which is generally performed at runtime. But also due to the increasing cache (or local memory) pressure.

All in all, completely ignoring packing/unpacking cost associated with array reference superwords

during group selection, and relying solely on data layout transformation to hopefully optimize superwords placement in memory and eliminate the packing/unpacking cost overhead is not a good strategy given the limitations and drawbacks of data layout transformations.

This problem can be solved by using a more accurate candidate benefit estimation method, taking into account the cost difference of various **VP** types. Alternatively, we propose to consider array access operations to contiguous elements of the same array as **SIMD** group candidates, rather than **VPs**, to make them part of the **SLP** solution space. We will discuss this solution later in section 4.4.2.

**Example 7** To illustrate this case, let's consider the example of fig. 4.9 assuming a maximum vector size of two.

At the first iteration, only two candidates are available:  $c1 = \{S1, S2\}$  and  $c2 = \{S1, S3\}$ . Since they have no **VP** reuse,  $VPR(c1) = VPR(c2) = 0$ . Therefore, either  $c1$  or  $c2$  is selected randomly.

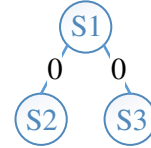
If  $c1$  is selected then the  $\{a, b\}$  and  $\{A[i], B[i]\}$  should be packed into **SIMD** vectors and the result should be unpacked to store it in  $\{x, y\}$ .  $\{a, b\}$  and  $\{x, y\}$  are scalar superwords and can be optimized by data layout transformation. However,  $\{A[i], B[i]\}$  cannot since it contains accesses to different arrays. Therefore a packing operation is required in this case.

However, if  $c2$  is selected no packing operations are required to pack  $\{A[i], A[i + 1]\}$  (assuming alignment).

In this case,  $c2$  is more likely to be better than  $c1$  however **holistic SLP** cannot distinguish them and considers them as equally beneficial.

```
S1:  x = a + A[i];
S2:  y = b + B[i];
S3:  z = y + A[i+1];
```

(a) C code snippet.



(b) **SGG** at first iteration.

Figure 4.9 – Example illustrating **holistic SLP** candidate benefit estimation.

### Only consider the **VPs** of the candidate at hand

The candidate benefit estimation method used by **holistic SLP** only considers the amount of reuses of the **VPs** of the candidate at hand, say  $c$ , by the remaining candidates (in addition to already selected groups) – as shown in eq. (4.2). In other words, it does not consider the potential benefit of the remaining candidates, which have no reuse of  $c$ 's **VPs**.

This has a great impact specially during the first group selection iteration, since no groups have been yet selected. In this case:

$$G' = \{c\} \tag{4.6}$$



and consequently, eq. (4.2) becomes:

$$VPR(c) = \frac{|V(\{c\})| - |P(\{c\})| + |R(c)|}{|P(\{c\})|} = \frac{|R(c)|}{|P(\{c\})|} \quad (4.7)$$

This means that the only contribution to the benefit evaluation of  $c$  in this case, is the estimation of the number of reuses of **VPs** of  $c$  (only) by the remaining candidates. This generally leads to situations where many candidates are estimated to have the same (maximum) benefit. In such cases the group selection process is unable to decide which candidate is better and will randomly select one of them, like in the examples 5 and 6 for instance.

In section 4.4.2, we show through experimental results, that this problem greatly impacts the performance of the **SLP** solution and we then propose a solution.

## 4.4 Proposed Holistic SLP Algorithm Enhancements

To recall the context of this work, the aim is to provide an efficient source-to-source **Simdization** transformation to target embedded processors in the context of the ALMA project, mainly XENTIUM and KAHRISMA. However, in order to better illustrate the advantage of our approach, we also considered two other embedded processors, namely, ST240 [4] and VEX [5]. All four target compilers cannot perform **Simdization**, therefore we implement a source-to-source transformation to convert a sequential C code into one with **SIMD** intrinsics of the target processor.

In order to do that, we first present several enhancements to the **holistic SLP** algorithm proposed by LIU et al, **holistic SLP** [78], thoroughly discussed in section 4.3. In this section, we address the issues of cyclic dependency conflicts and invalid **VP** reuse, described in sections 4.3.2.1 and 4.3.2.2. But more importantly, we:

- Define a more efficient and compact **IR**. We refer to it as **Pack Flow and Conflict Graph (PFCG)**.
- Propose an alternative candidate benefit estimation and group selection method.
- Implement the proposed **SLP** extraction method and compare it against **holistic SLP** for a set of benchmarks on three different embedded processors.

The overview of the modified **holistic SLP** extraction algorithm is depicted in fig. 4.10. It is similar to the one used by **holistic SLP**, the main difference lies in the candidates identification and **IR** construction as well as the group selection process.

First we obtain the **DFG** of the input basic block, then we identify isomorphic operations as well as contiguous accesses to same arrays. Next we build the **PFCG**, that captures both, the candidate conflicts and the **VP** flow information. We present the **PFCG** in section 4.4.1. Like **holistic SLP**, we only consider **SIMD** group candidates of size two and we iteratively extends the selected ones when possible. However, the group selection process is based on a new candidate estimation method, that we later present in section 4.4.2. After selecting a new group,

we update the [PFCG](#) by eliminating all conflicting candidates and we eliminate any possible cyclic dependencies. Finally, the selected groups order is specified in such a way to minimize permutations. We can then, optionally, estimate the speedup of the obtained solution and prune it accordingly to make sure it performs better than the original scalar code, but in this work we only focus on the group selection process.

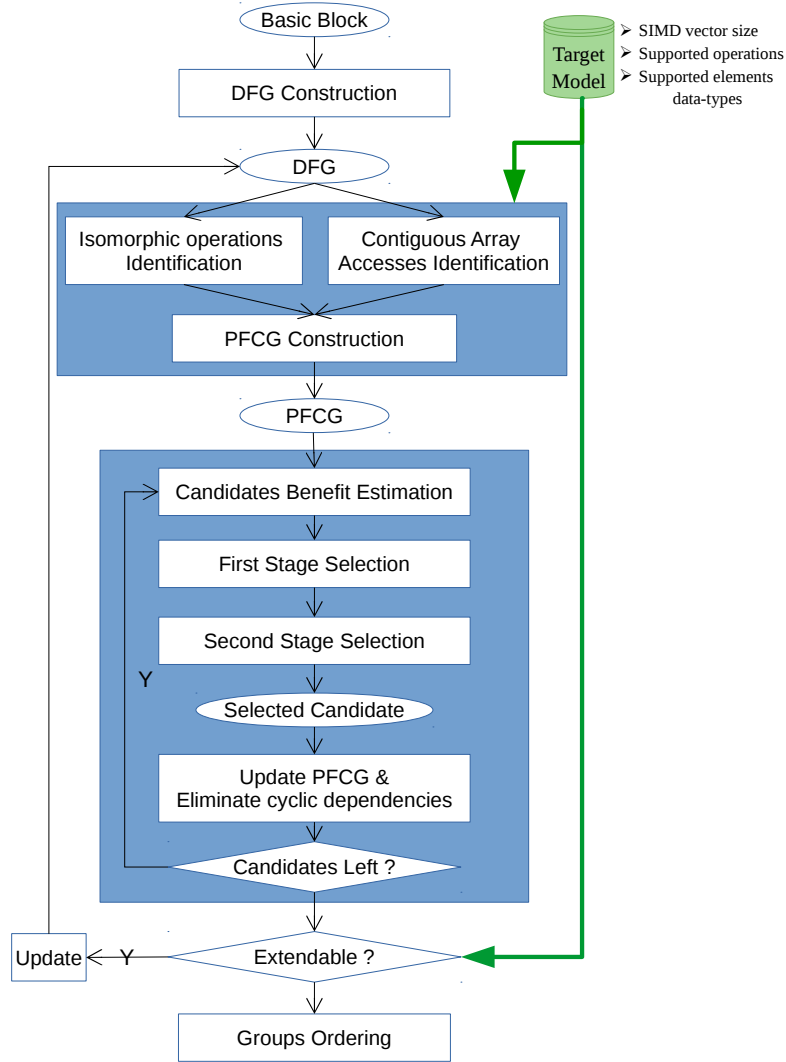


Figure 4.10 – [SLP](#) extraction framework overview.

#### 4.4.1 Pack Flow and Conflict Graph (PFCG)

The [IR](#) used by holistic SLP, namely [SGG](#) and [VPCG](#), holds necessary information for the [SLP](#) extraction process. [SGG](#) provides statement compatibility (group-ability) i.e. group candidates, as well as candidate common statement conflicts information. Whereas [VPCG](#) provides, [VPs](#) per candidate information, in addition to [VP](#) conflicts.

This information is partly redundant with **SGG**, since **VPs** of a candidate is an atomic property of the candidate, so that all **VPs** of a candidate  $c$  conflict with all **VPs** of another candidate in conflict with  $c$ . This redundancy is unnecessary. Note that **VPCG** does not explicitly hold information about **VP** reuse. Comparing **VPCG** nodes is necessary in order to identify equivalent **VPs** and account for reuse.

All in all, **holistic SLP IR** has several disadvantages:

- **SGG** cannot represent cyclic dependency conflicts (see section 4.3.2.1).
- Conflicts information is, unnecessarily, redundant between **SGG** and **VPCG**.
- **VP** reuse information is not captured explicitly in **VPCG**.

To address these disadvantages, we define a new **IR**, that we refer to as **PFCG**. It is a combination of a **VP** Flow Graph, similar to a **DFG**, and a Candidate Conflict Graph.

**Définition 4.6 (PFCG)** *PFCG is a mixed graph  $(P \cup C, X, F)$  where:*

- $P \cup C$  is the set of nodes.  $C$  is the set of **SIMD** group candidate nodes.  $P$  is the set of input variable pack nodes, which are not in  $C$ . Note that in this representation, a **SIMD** group candidate node also represents a **VP**; its output **VP**.
- $X$  is a set of undirected edges representing conflicts between **SIMD** group candidate nodes. It includes all common statement conflicts as well as direct cyclic dependency conflicts<sup>9</sup>. Note that we only consider direct cyclic dependency conflicts when building the **PFCG**, indirect ones are dealt with during group selection step (see section 4.4.2).
- $F$  is a set of directed edges representing **VP** flow between nodes.

The **PFCG** is constructed from the basic-block's **DFG** as depicted by the procedure **BUILD PFCG** in algorithm 2 (in section 4.4.4). We use **DFG** form of the basic block, to increase the potential of finding **SLP** at a finer level. We also eliminate anti- and output dependencies that might otherwise affect **VP** reuse estimation as illustrated in section 4.3.2.2.

The advantages of using the **PFCG** are its ability to represent **VP** flow information, which eases the detection of **VP** reuse – for a given candidate, we only need to check its neighbors on flow edges to detect its **VP** reuses – and its ability to represent cyclic dependency conflicts while being more compact than **VPCG** and **SGG**.

**Example 8** Figure 4.11 shows the **PFCG** of the example of fig. 4.1 (recalled). Note the difference with **VPCG** and **SGG**, of the same example, depicted in figs. 4.4b and 4.4c, respectively. Using the **PFCG** we can easily detect, for instance, that the **VP**  $\{b, d\}$  is used by both candidates  $\{S1, S2\}$  and  $\{S4, S5\}$ . Also it is more compact than the **VPCG** and **SGG**.

#### 4.4.2 Group Selection Procedure

We propose an alternative group selection heuristic to the one employed by **holistic SLP** in order to address the shortcomings illustrated in section 4.3.2.2.

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9. Direct cyclic dependency occurs between two candidates only. Indirect cycle occurs between more than two candidates.

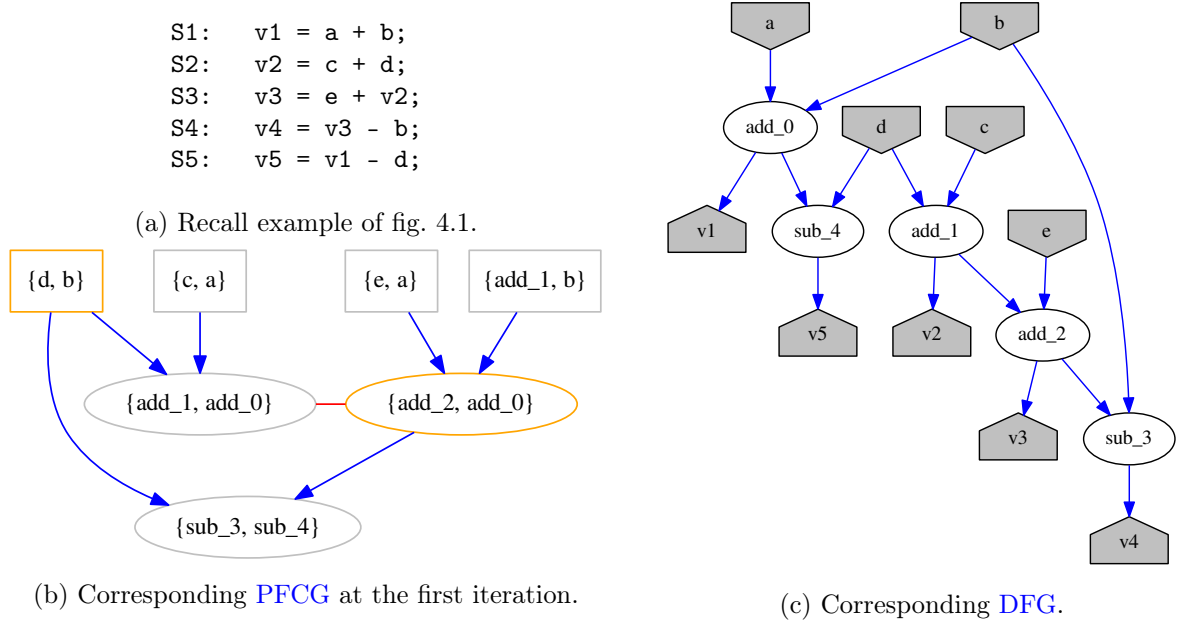


Figure 4.11 – **DFG** and **PFCG** of the example in fig. 4.1. Rectangular nodes in the **PFCG** represent pack nodes, whereas elliptic shaped ones represent candidate nodes. Undirected edges represent conflicts between candidates and directed edges represent **VP** Flow. Highlighted nodes (with orange) indicate a reuse.

Unlike **holistic SLP**, we consider array access operations to contiguous elements of the same array as **SIMD** group candidates, rather than **VPs**, when building the **PFCG**. This will distinguish such **VPs** and make them part of the **SLP** solution space. This way the group selection procedure can decide to select such candidate based on its benefit estimation instead of being implicitly selected due to the selection of a candidate that uses/defines it.

Furthermore, we use a two-stages selection procedure based on a new candidate benefit estimation method that we present in section 4.4.2.1. In the first stage, we select the set of all candidates with the highest **VP** reuse-to-cost ratio. Among them, we select one with highest reuse-to-conflict ratio in the second stage.

The pseudo code of the group selection procedure is listed in algorithm 1. Each remaining candidate in the **PFCG** is evaluated using the candidate benefit estimation method. The one estimated as the most beneficial is selected, the **PFCG** is updated accordingly and the potential cyclic dependency conflicts are eliminated before starting a new iteration until all conflicts in the **PFCG** are resolved.

#### 4.4.2.1 Candidate Benefit Estimation

The candidate benefit estimation method used by **holistic SLP** only considers the first neighbors of the candidate being evaluated, say  $c$ , in the **PFCG**. In fact, **holistic SLP** only considers

the reuses of  $c$ 's VPs by the remaining candidates in addition to reuses of already selected groups, as shown in eq. (4.2). In other words, the potential benefit of the remaining candidates which have no reuse of  $c$ 's VPs (i.e. which are not direct neighbors of  $c$  in the PFCG) is not considered.

This problem generally leads to situations where many candidates have the same maximum benefit. In such case the **holistic SLP** algorithm is not able to decide which candidate is better and will randomly select one of them. For instance, example 6 illustrates this case. This is specially frequent during the first iteration where no groups have been selected yet. In this case the only contribution to the benefit evaluation is the estimation of the number of reuses of VPs of  $c$  by the remaining candidates, as shown in eq. (4.7).

To illustrate the impact of this problem, we applied **holistic SLP** repeatedly (ten times) on each benchmark<sup>10</sup>. Every time multiple candidates can be selected (i.e. have the same maximum benefit), only one of them is selected randomly, as specified by **holistic SLP**.

For each benchmark, after applying **Simdization** using **holistic SLP**, we report the execution time improvement of the generated **SIMD** code over the original (sequential) code. We repeat this ten times, on three embedded processors, namely XENTIUM, KAHRISMA and ST240<sup>11</sup>. The graphics of fig. 4.12 plot the execution time improvement obtained for each time the test is run. This results show a significant variation of the execution time improvement for most benchmarks, when using **holistic SLP**, across different runs. For instance, the generated **SIMD** code, obtained by applying **holistic SLP** on the infinite impulse response filter benchmark (**iir**), for ST240, can perform up to 23% better or as low as 2% worst than the original (sequential) code version, all depending on the **SIMD** group candidates being randomly selected each time multiple ones are judged equally beneficial by the candidate benefit estimation method of **holistic SLP**. This indicates that the **holistic SLP** candidate benefit estimation method is not precise enough and often lead to situations where the group selection process cannot decide which candidate is better and thus select randomly. This random selection often lead to a poor **SLP** solution as shown by the results in fig. 4.12.

In order to address this issue, we propose to consider more than the first neighbors of the candidate being evaluated, say  $c$ , in the PFCG. This allows to get a more global picture of the effect of selecting  $c$ . In addition, we also use a two-stage selection procedure to further reduce the cases where multiple candidates have same benefit estimation. First, we select the set of all candidates with the highest VP *reuse-to-cost* ratio, among which we then select one with highest *reuse-to-conflict* ratio in the second stage.

The pseudo code of the proposed candidate benefit estimation is listed in algorithm 5. Given a candidate  $c$ , we first extract a subgraph,  $sub(c, N)$ , from the PFCG containing  $c$  and its neighbors up to  $N$  levels. We then eliminate all conflicts in  $sub(c, N)$  by iteratively removing a candidate with highest *conflict-degree-to-flow-degree*<sup>12</sup> ratio. The resulting subgraph not only represents

---

10. the benchmarks are described in section 4.5.3)

11. the target processors are described in section 4.5.2

12. Conflict degree of a candidate is the number of conflicting edges connected to it in  $sub(c, N)$ . Its Flow degree is the number of flow edges connected to it (it is an indication of the amount of VP reuse of the candidate).

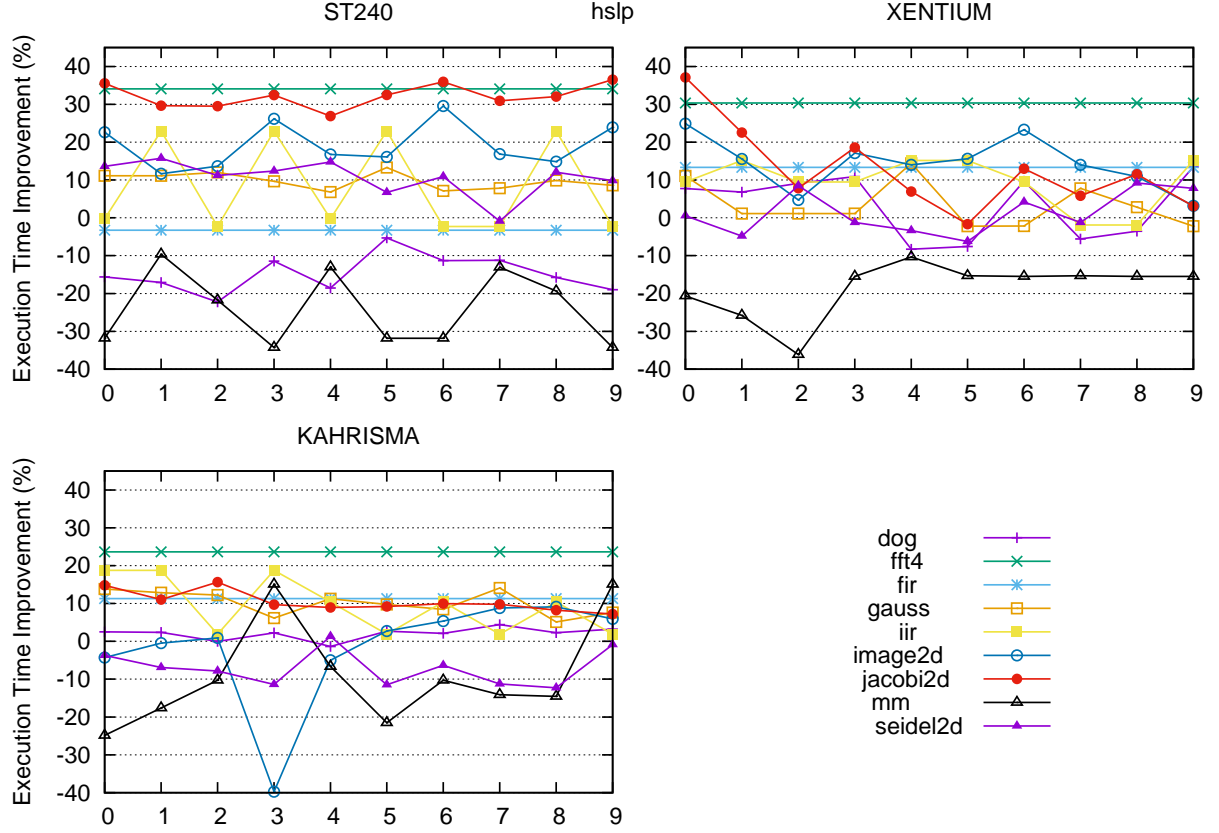


Figure 4.12 – Execution time improvement, over the sequential version, of various benchmarks obtained by applying `holistic SLP` for ten times.

the reuses of  $c$ 's  $VP$ s but also those of some other non-conflicting candidates. Once the subgraph extracted, we compute the ratio of, the number of  $VP$  reuses of all candidates in the subgraph, to the estimated packing/unpacking cost.

To evaluate the proposed method, we run the same test as before but using our proposed method for  $SLP$  extraction (for  $N = 3$ ) instead of `holistic SLP`. The results, reported in fig. 4.13, show much less variation in the execution time improvement for all benchmarks, suggesting that our method achieves a more precise candidate benefit estimation and is less prone to the random selection factor.

**Example 9** Back to example 7 (recalled in fig. 4.14).

Using our proposed  $SLP$  extraction method, the set of candidates is:

$$\{c1 = \{add\_1, add\_2\}, c2 = \{add\_1, add\_3\}, c3 = \{A[i], A[i + 1]\}\} \quad (4.8)$$

Note that  $\{A[i], A[i + 1]\}$  is considered as a candidate, unlike `holistic SLP`. The corresponding  $PFCG$  is depicted in fig. 4.15. The benefit estimation of the candidates is computed following the method listed in algorithm 3. For  $c1$ , the neighborhood graph only contains  $c1$ , therefore:

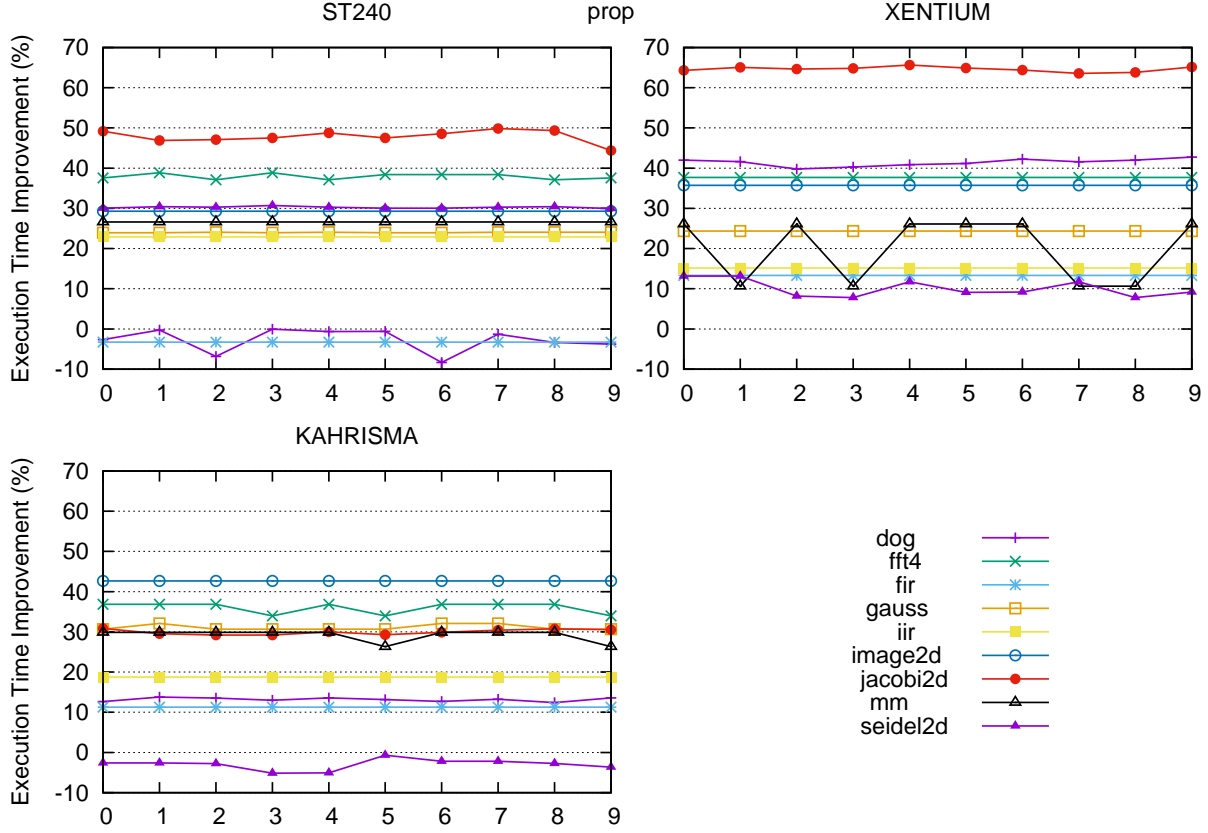


Figure 4.13 – Execution time improvement, over the sequential version, of various benchmarks after applying the proposed SLP extraction for ten times.

- $N_R = 1$ . There is no reuse.
- $N_{pack} = 2$ . Estimated number of required packs is 2;  $\{b, a\}$ ,  $\{B[i], A[i]\}$  and  $\{add\_2, add\_1\}$ .
- $N_{unpack} = 1$ . Estimated number of required unpacks is 1 since  $c1$  has no successors.
- Thus the benefit of  $c1$  is  $\frac{1 + N_R}{1 + N_{pack} + N_{unpack}} = 2/4$

For  $c2$  and  $c3$  the neighborhood graph contains both  $c2$  and  $c3$ . Thus, the benefit estimation for  $c2$  is  $(1 + 2)/(1 + 1 + 1) = 3/3$  and is the same for  $c3$ . In this case either  $c2$  or  $c3$  is selected at the first iteration, then the other will be selected in the next iteration. Hence, the final grouping solution is  $\{c2, c3\}$ .

In contrast, when using *holistic SLP*  $c3$  is not considered as candidate and  $c1$  and  $c2$  are estimated to have the same benefit as illustrated in example 7. Therefore, the final grouping solution could be  $\{c1\}$  or  $\{c2\}$  (randomly).  $\{c2\}$  – equivalent to the solution  $\{c2, c3\}$  obtained by using our proposed method – would more likely perform better than  $\{c1\}$ .

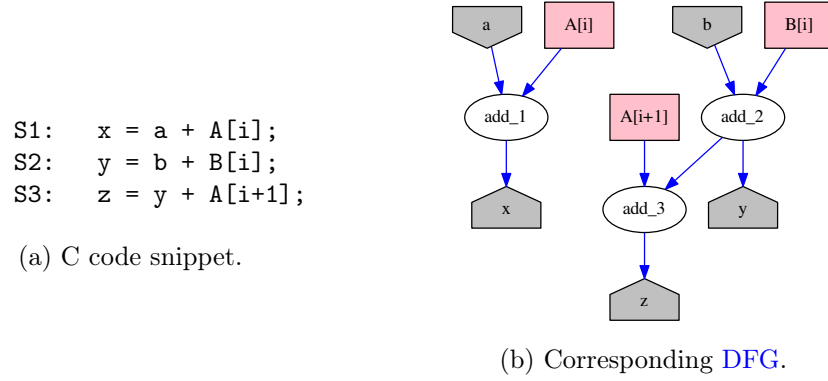


Figure 4.14 – Recall the example of fig. 4.9.

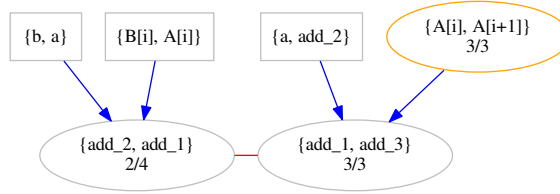


Figure 4.15 – PFCG of the example in fig. 4.14 at the first iteration using prop-2.

#### 4.4.2.2 Update PFCG

After selecting of a new SIMD group,  $g$ , we update the PFCG following the procedure UPDATEPFCG listed in algorithm 7. First, we move the node representing  $g$  in the PFCG from the candidates set to the selected groups set. Then, we eliminate all candidates in the PFCG that conflicts with  $g$ , that is all nodes connect to  $g$  by a conflict edge. When eliminating a candidate,  $c$ , we make sure to keep the PFCG consistent. So:

- If  $c$  has flow successors, we convert it into a VP node, i.e. it is not a group candidate anymore, and we remove all its incoming flow edges. If the source of the removed incoming flow edge is a VP node that is only connected to  $c$  then we remove it as well.
- Otherwise, we first handle the incoming flow edges of  $c$  similarly, before removing it.

#### 4.4.2.3 Cyclic Dependency Conflicts Elimination

Since we do not consider all cyclic dependency conflicts, namely indirect ones, when building the PFCG, we eliminate such conflicts after updating the PFCG due to the selection of a new SIMD group. For each of the remaining candidates we check whether it may introduce a cyclic dependency, with previously selected SIMD groups, if it get selected. If so, we eliminate it from the PFCG in order to guarantee the final grouping solution to be cyclic dependency free. The pseudo-code of the cyclic dependency conflicts elimination procedure is listed in algorithm 8.



### 4.4.3 Algorithm complexity

#### Problem size

The **IR** construction time, whether for the **VPCG** used by **holistic SLP**, or the **PFCG** in our proposed algorithm, is roughly quadratic with respect to the number of group candidates. However, the **IR** is constructed only once before starting the group selection procedure.

Our proposed **IR** (**PFCG**) is more compact than the one used by **holistic SLP** (**VPCG** + **SGG**). If  $C$  is the set of **SIMD** group candidates then:

- The number of nodes in the **PFCG** is equal to the number of candidates ( $|C|$ ) plus the number of input **VPs** which are not in  $C$  (cf. definition 4.6), i.e.:

$$N_{PFCG} = |C| + \sum_{c \in C} |\{v \in V_{in}(c) : v \notin C\}| \quad (4.9)$$

- The number of nodes in the **VPCG** equals the sum of **VPs** in each candidate:

$$N_{VPCG} = \sum_{c \in C} |V(\{c\})| = \sum_{c \in C} (1 + |V_{in}(c)|) = |C| + \sum_{c \in C} |V_{in}(c)| \quad (4.10)$$

Where  $V_{in}(c)$  is a function that returns the set of *input VPs* for the candidate  $c$ . A candidate has only one output **VP**, therefore, the number of **VPs** for  $c$  is  $|V(\{c\})| = 1 + |V_{in}(c)|$ <sup>13</sup>.

$$\{v \in V_{in}(c) : v \notin C\} \subset V_{in}(c) \implies N_{VPCG} \geq N_{PFCG} \quad (4.11)$$

#### Candidate benefit estimation

In order to estimate the benefit of a candidate  $c$ , **holistic SLP** requires to build an *auxiliary graph* for  $c$ ,  $AG(c)$  (see section 4.3.1). The time for building  $AG(c)$  from the **VPCG** (the method used by **holistic SLP**) is linear with respect to the number of nodes in the **VPCG**.

On the other hand, our candidate benefit estimation method requires to build a sub-**PFCG** ( $sub(c)$ ) obtained by extracting the distance- $N$  neighborhood of  $c$  on the Pack flow edges in the **PFCG**. The building time of  $sub(c)$  is roughly constant with respect to the **PFCG** size, specially since very small values of  $N$  ( $\leq 3$ ) are sufficient, as shown in the results of fig. 4.16. The test setup, benchmarks and target processors are presented later on in section 4.5.

#### Group selection

The group selection procedure (assuming no group size extension is performed) is roughly the same for our approach and that of **holistic SLP**. However, due to the difference in the complexity of candidate benefit estimation, the group selection of **holistic SLP** is:

$$O(|C| \times |V(C)|) \approx O(|C|^2) \quad (4.12)$$

---

13. the function  $V$  is defined in eq. (4.3)

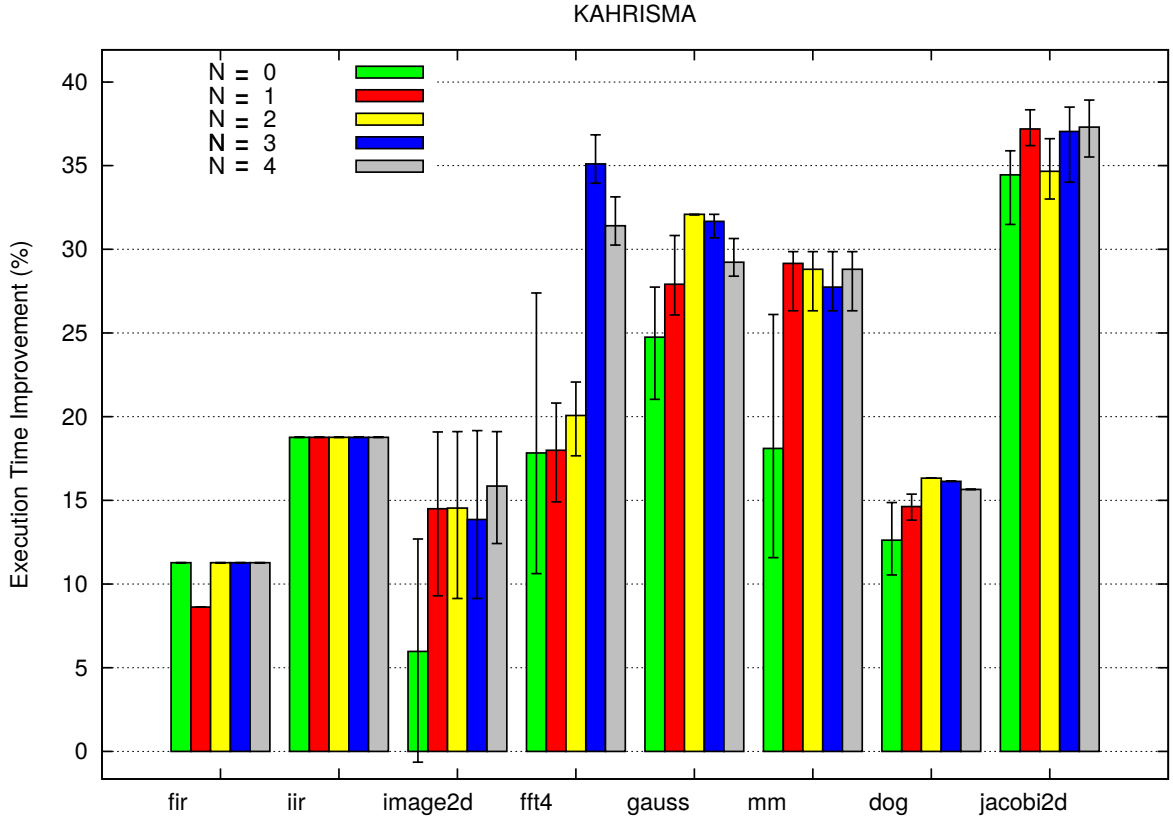


Figure 4.16 – Execution time improvement of the **SIMD** code obtained by applying our proposed **SLP** extraction method, compared to the original (sequential) code, for different values of  $N$  considered for constructing the distance- $N$  neighborhood of a candidate (sub-**PFCG**) in the **PFCG**. The targeted processor is KAHRISMA.

Where  $C$  is the set of **SIMD** group candidates and  $|V(C)|$  is the number of nodes in the **VPCG**. On the other hand, the complexity of our approach is roughly  $O(|C|)$ .

The group selection time of our approach varies, roughly, linearly with respect to the number of candidates, whereas that of **holistic SLP** varies quadratically. The experimental results presented in section 4.5.5.2 (figs. 4.21 and 4.22a) shows the same behavior.

#### 4.4.3.1 Controlling **PFCG** Size

When building the **PFCG**, we consider each pair of isomorphic operations in the **DFG** for finding **SIMD** group candidates, as shown in algorithm 2. With larger basic blocks, the size of the **PFCG** (number of candidates) grows quadratically. In fact, for a set of  $K$  isomorphic operations, we can obtain up to

$$f(K) = (K - 1) \times K / 2 \quad (4.13)$$

candidates.

In order to reduce the **PFCG** size, and consequently cut down the groups selection time, we decompose each set of isomorphic operations into *batches* of limited size, and we only search for candidates inside each batch separately. In this case, for a set of  $K$  isomorphic operations and a batch size  $S$ , we can obtain up to:

$$(K/S) \times f(S) + f(K \% S) \approx \frac{K \times S}{2} \quad (4.14)$$

candidates. Hence, the number of candidates roughly increases linearly with the increase of the batch size.

The *batch size* allows to control the **PFCG** size and consequently the group selection time, at the cost of degrading the grouping solution performance. This is illustrated in the experimental results in section 4.5.5.2.

This concept is similar to basic-block splitting. But, in order to increase the potential of finding relevant candidates inside each batch, we first sort the set of isomorphic operations in topological order. This way independent operations are more likely to end up in the same batch.

#### 4.4.4 Pseudo-code

In this section, we simply list the pseudo-code of **PFCG** construction and group selection procedures that we discussed earlier, for the sake of keeping them closer to each other.

---

**Algorithm 1** Group Selection Procedure

---

```

1: // Input: Pack Flow and Conflict Graph pfcg
2: // Output: Set of selected groups.
3: procedure GROUPSELECTION(pfcg)
4:   while pfcg.C  $\neq \emptyset$  do
5:     for each candidate  $c \in \text{pfcg.C}$  do
6:       BENEFITESTIMATION( $c, \text{pfcg}$ )
7:     end for
8:      $best \leftarrow \text{SELECT}(\text{pfcg})$ .
9:     UPDATEPFCG( $best, \text{pfcg}$ ) // mark best as selected and Update pfcg
10:    ELIMINATECYCLES(pfcg)
11:  end while
12:  return pfcg.S
13: end procedure

```

---

**Algorithm 2** Building PFCG

---

```

1: // Input: Data Flow Graph  $dfg$ . It is a Directed Acyclic Graph (DAG)
2: // Output: Pack Flow and Conflict Graph  $pfcg$ 
3: procedure BUILDPFCG( $dfg$ )
4:    $pfcg.C \leftarrow \emptyset$  // Set of SIMD group candidate nodes
5:    $pfcg.P \leftarrow \emptyset$  // Set of input Pack nodes
6:    $pfcg.F \leftarrow \emptyset$  // Set of pack flow edges
7:    $pfcg.X \leftarrow \emptyset$  // Set of candidate conflict edges
8:    $pfcg.S \leftarrow \emptyset$  // Set of Selected candidates
9:   for each pair  $(o_1, o_2)$  of isomorphic operations or contiguous array accesses in  $dfg$  do
10:    // Operations batching is omitted
11:    if  $o_1$  and  $o_2$  are independent and have compatible data-types then
12:       $c \leftarrow \{o_1, o_2\}$ 
13:       $pfcg.C \leftarrow pfcg.C \cup \{c\}$ 
14:      // connect  $c$ 's flow successors
15:      if  $\exists p \in pfcg.P : p \equiv c$  then
16:         $pfcg.P \leftarrow pfcg.P \setminus \{p\}$ 
17:        substitute  $(p, x)$  by  $(c, x)$ ,  $\forall (p, x) \in pfcg.F$ 
18:      end if
19:      // connect  $c$ 's flow predecessors
20:      //  $dfg.preds(n)$  is the set of predecessors of node  $n$  in the  $dfg$ 
21:      for each  $v1_i, v2_i : v1_i \in dfg.preds(o_1)$  and  $v2_i \in dfg.preds(o_2)$  do
22:        if  $\exists v \in pfcg.C : v \equiv \{v1_i, v2_i\}$  then
23:           $pfcg.F \leftarrow pfcg.F \cup \{(v, c)\}$ 
24:        else if  $\exists v \in pfcg.P : v \equiv \{v1_i, v2_i\}$  then
25:           $pfcg.F \leftarrow pfcg.F \cup \{(v, c)\}$ 
26:        else
27:           $pfcg.P \leftarrow pfcg.P \cup \{\{v1_i, v2_i\}\}$ 
28:           $pfcg.F \leftarrow pfcg.F \cup \{(\{v1_i, v2_i\}, c)\}$ 
29:        end if
30:      end for
31:      // connect  $c$ 's conflicts
32:       $pfcg.X \leftarrow pfcg.X \cup \{\{c, c'\} : c' \in pfcg.C \text{ and } (c' \cap c \neq \emptyset \text{ or } c', c \text{ introduce a cyclic dependency})\}$ 
33:    end if
34:  end for
35:  return  $pfcg$ 
36: end procedure

```

---

**Algorithm 3** Estimate the benefit associated with selection of a candidate

---

```

1: // Inputs: A candidate  $c$  and the pack flow and conflict graph  $pfcg$ 
2: // Output: Set the benefit of candidate  $c$ 
3: procedure BENEFITESTIMATION( $c, pfcg$ )
4:    $sub \leftarrow \text{EXTRACTSUBPFCG}(c, pfcg)$ 
5:    $\text{ELIMINATESUBCONFLICTS}(c, sub)$  //  $sub$  is now conflict-free
6:    $\text{COMPUTEbenefit}(c, sub, pfcg)$ 
7: end procedure

1: //  $N$  is a positive integer parameter
2: // Output: distance- $N$  pack flow neighborhood of  $c$  in  $pfcg$ 
3: procedure EXTRACTSUBPFCG( $c, pfcg$ )
4:    $sub.V \leftarrow \{x \in pfcg.C \cup pfcg.S : \text{distance}(x, c) \leq N, \{x, c\} \notin pfcg.X\}$ , where:
5:    $\text{distance}(x, c)$  is the distance between nodes  $c$  and  $x$  in respect to Pack Flow edges.
6:    $sub.X \leftarrow \{\{x, y\} \in pfcg.X : x, y \in sub.V\}$  // Set of conflict edges
7:    $sub.F \leftarrow \{(x, y) \in pfcg.F : x, y \in sub.V\}$  // Set of pack flow edges
8:   return  $sub$ 
9: end procedure

```

---

**Algorithm 4** Eliminate Conflicts in  $sub$ 


---

```

1: procedure ELIMINATESUBCONFLICTS( $c, sub$ )
2:   // Iteratively eliminate the candidate with highest conflict-to-reuse ratio
3:   while  $sub.X \neq \emptyset$  do
4:      $x \leftarrow \text{node} \in sub.V \setminus \{c\}$  with highest  $\frac{\text{conflict degree}}{1 + \text{flow degree}}$ 
5:      $sub.V \leftarrow sub.V \setminus \{x\}$ 
6:      $sub.X \leftarrow sub.X \setminus \{\{x, y\} \in sub.X\}$ 
7:      $sub.F \leftarrow sub.F \setminus \{(x, y), (z, x) \in sub.F\}$ 
8:   end while
9: end procedure

```

---

**Algorithm 5** Compute Candidate Benefit.

---

```

1: procedure COMPUTEBENEFIT( $c, sub, pfcg$ )
2:    $N_R \leftarrow |sub.V|$  // Estimated number of VP reuse in  $sub$ 
3:   // Estimated number of additionally required packings.
4:    $N_{pack} \leftarrow |\{x \in pfcg.C \setminus sub.V : \exists (x, y) \in pfcg.F, y \in sub.V \setminus pfcg.S\}|$ 
5:   // Estimated number of additionally required unpackings.
6:    $N_{unpack} \leftarrow |\{x \in sub.V \setminus pfcg.S, x \text{ is not a Store candidate} : \nexists y \in sub.V \cup pfcg.S : (x, y) \in sub.pfcg\}|$ 
7:    $c.reuse \leftarrow N_R$ 
8:    $c.benefit \leftarrow \frac{1 + N_R}{1 + N_{pack} + N_{unpack}}$ 
9:    $c.conflict \leftarrow |\{\{x, y\} \in pfcg.X : (x \in sub.V) \oplus (y \in sub.V)\}|$ 
10: end procedure

```

---

**Algorithm 6** Select the ‘best’ candidate in the PFCG

---

```

1: procedure SELECT( $pfcg$ )
2:   // First Stage: Set of candidates with maximum benefit estimation
3:    $bestSet \leftarrow \{c \in pfcg.C : c.benefit = max\}$ 
4:   // Second Stage:
5:    $best \leftarrow c \in bestSet$  with maximum  $\frac{c.reuse}{c.conflict}$ 
6:   return  $best$ 
7: end procedure

```

---

**Algorithm 7** Updating PFCG after selecting a new group

---

```

1: procedure UPDATEPFCG( $c, pfcg$ )
2:   // Mark  $c$  as selected
3:    $pfcg.S \leftarrow pfcg.S \cup \{c\}$ 
4:    $pfcg.C \leftarrow pfcg.C \setminus \{c\}$ 
5:   // Eliminate candidates conflicting with  $c$ 
6:   for each  $\{x, c\} \in pfcg.X$  do //  $x$  conflicts with  $c$ 
7:     ELIMINATECANDIDATE( $pfcg, x$ )
8:   end for
9: end procedure

1: procedure ELIMINATECANDIDATE( $pfcg, x$ )
2:   for each  $(p, x) \in pfcg.F$  do //  $p$  is a predecessor of  $x$ 
3:      $pfcg.F \leftarrow pfcg.F \setminus \{(p, x)\}$  // disconnect  $p$  from  $x$ 
4:     if  $p \in pfcg.P$  and  $\nexists (p, s) \in pfcg.F$  then
5:        $pfcg.P \leftarrow pfcg.P \setminus \{p\}$  //  $p$  is a pack node with no other successors
6:     end if
7:   end for
8:   if  $\exists (x, y) \in pfcg.F$  then // if  $x$  has successors
9:      $pfcg.P \leftarrow pfcg.P \cup \{x\}$  // convert  $x$  into a pack node
10:  end if
11:   $pfcg.C \leftarrow pfcg.C \setminus \{x\}$ 
12:   $pfcg.X \leftarrow pfcg.X \setminus \{\{x, y\} \in pfcg.X\}$ 
13: end procedure

```

---

**Algorithm 8** Eliminate cyclic dependency conflicts

---

```

1: procedure CYCLEELIMINATION( $pfcg$ )
2:   for each  $c \in pfcg.C$  do
3:     if  $pfcg.S \cup \{c\}$  have a dependency cycle then
4:       ELIMINATECANDIDATE( $pfcg, c$ )
5:     end if
6:   end for
7: end procedure

```

---

## 4.5 Experimental Setup and Results

In this section, we present the implementation of the proposed **SLP** extraction framework in section 4.5.1. We then present the test setup, benchmarks and target architectures in section 4.5.4, section 4.5.3 and section 4.5.2 respectively. Finally we present the experimental results in section 4.5.5.

### 4.5.1 Implementation

We implemented the proposed **PFCG** model along with the enhanced **holistic SLP** extraction framework, presented in section 4.4, as a source-to-source transformations in the **Generic Compiler Suite (Gecos)**. The corresponding pseudo-code is listed in section 4.4.4.

We also implemented the original **holistic SLP** extraction framework as described in section 4.3.1 and based on its presentation [78] by LIU et al.

**Gecos** [47] is an open source, model-driven, eclipse-based compiler framework developed in the CAIRN/INRIA research team. It is mainly targeted towards, but not limited to, source-to-source transformations for embedded platforms and hardware generation using **High-Level Synthesis (HLS)**.

The proposed **holistic SLP** flow implementation is illustrated in fig. 4.17.

The **Gecos** C front-end, based on the C/C++ CDT front-end, parses the input C code and generates the equivalent **Gecos IR** (CDFG).

Multiple pre-optimizations can be performed at this level, such as constant propagation, array scalarization, loop unrolling as well as polyhedral loop analysis and transformations, such as register level tiling.

The basic blocks annotated for **SLP** extraction, either manually using *pragma* annotations or based on previous transformation, are then converted to **DFG** representation, on which we apply **SLP** extraction. Note that in this implementation, we only support basic arithmetic **SIMD** operations such as additions, multiplications and shifts in addition to vector memory accesses. **SLP** extraction determine the set of decided **SIMD** groups, which are then used to vectorize the **DFG** to **SIMD** form reflecting the **SLP** grouping.

The vectorized **DFG** is then converted back to CDFG introducing **SIMD** instructions and data-types. At this level, the **SIMD** instructions and data-types are generic and target-independent. However, the main characteristics of the target architecture were considered during **SLP** extraction, such as the **SIMD** vector size, the supported **SIMD** operations and the vector elements data-types.

Post-optimizations can be performed at this level, such as superword promotion ([124]).

Finally, the **SIMD** C code generation converts the **Gecos IR** into a C code with **SIMD** macros implementing the **SIMD** data-types and operations. The implementation of these generic macros is target-dependent and is generated as a *.h* file by **Gecos**. It defines the corresponding **SIMD** types and operations using the target's compiler **SIMD** intrinsics when available. This makes the

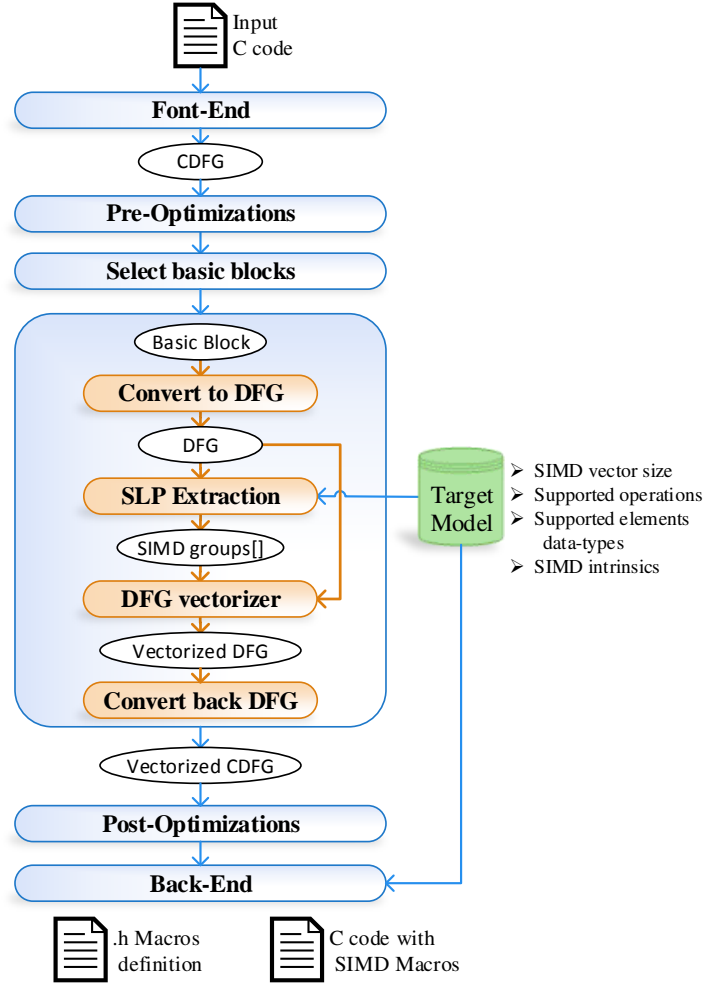


Figure 4.17 – SLP Extraction Framework implementation in GeCos.

framework easily expendable to support additional targets.

## 4.5.2 Target processors

We target three different embedded architectures, XENTIUM, ST240 and KAHRISMA.

### 4.5.2.1 XENTIUM

XENTIUM is a low energy consumption 32-bit (with 40-bit extension support) 12-issues wide Very Long Instruction Word (VLIW) Digital Signal Processor (DSP) core from RECORE SYSTEMS [104]. It has ten functional units, six of which can perform integer arithmetic and logic operations, two can perform multiply operations and two can perform load/store operations. XENTIUM also supports 2x16-bit SIMD operations. In this work, we only consider add, sub, mul, shifts and data manipulation SIMD instructions. It has four 8 32-bit and one 16 32-bit



register files, each of which has two read and two write ports.

An LLVM based compiler and a cycle-accurate simulator for the XENTIUM core are provided by RECORE SYSTEMS.

#### 4.5.2.2 KAHRISMA

KAHRISMA (KArlsruhe's Hypermorphic Reconfigurable-Instruction-Set Multi-grained-Array) is a heterogeneous dynamically reconfigurable multi-core research architecture [58], developed by KIT.

In this work we use its 2-issue width single VLIW core configuration.

KAHRISMA core provides support for 4x8-bit and 2x16-bit SIMD integer arithmetic operations including addition, subtraction, multiplication and shifts as well as data manipulation operations.

An LLVM based compiler and a cycle-approximate simulator [127] for this core configuration are provided by KIT.

#### 4.5.2.3 ST240

ST240 [4] is a 4-issues wide VLIW media processor from the ST200 family of STMicroelectronics. It has four integer units, 2 multiplication units, 1 branch unit and 1 load/store unit. It has a general purpose register file of 64 32-bit registers with 8 read and 4 write ports. ST240 also supports 2x16-bit SIMD operations. In this work, we only consider add, sub, mul, shifts and data manipulation SIMD instructions.

A compiler based on GNU GCC and Open64 as well as a cycle-accurate simulator for the ST240 core are provided STMicroelectronics.

#### 4.5.2.4 VEX

VLIW EXample (VEX) is a configurable compilation-simulation system targeting a wide class of VLIW architectures [5]. It is developed by HAWLETT-PACKARD (HP). The interesting point about the VEX toolchain is that it is highly configurable. The configuration parameters includes: the number of clusters, the number of ways, functional units and registers per cluster as well as the latency associated with various operations in addition to the memory hierarchy parameters. But also the possibility to extend its instruction set to include new instructions.

We use this possibility to extend the default instruction set by implementing a 4x8-bit and 2x16-bit integer arithmetic SIMD instruction set. In this model, the SIMD registers are common with the scalar registers. In this work, we use the default configuration, with one cluster and 4 issues. We refer to it as VEX-4.

### 4.5.3 Benchmarks

We use several signal and image processing benchmarks for testing the proposed [SLP](#) extraction framework. They are listed in table 4.1 and the breakdown of the operations in the considered basic blocks is reported in table 4.2.

Each benchmark function is pre-optimized to expose [SLP](#) by applying either loop unrolling or register level tiling. And the kernel basic blocks are *pragma* annotated to be considered for [SLP](#) extraction.

The main function of each benchmark allocates and initializes the required data, it then resets the statistics counters before launching the benchmark function. Finally, it stops the statistics counters before generated the output.

Benchmark	Info	Pre-optimizations
<b>fir</b>	128-tap FIR Filter	partial 4x unrolled
<b>iir</b>	64 IIR Filer	partial 4x unrolled
<b>fft4</b>	size 4 Fast Fourier Transform	fully unrolled
<b>image2d</b>	2D 3x3 linear image filter	2x2 register level tiling
<b>gauss</b>	vertical followed by horizontal filter	2x2 register level tiling
<b>mm</b>	2D Matrix Multiplication	2x2x2 register level tiling
<b>dog</b>	Difference of Gaussian (2D stencil)	2x2x2 register tiling
<b>jacobi2d</b>	2D stencil from polybench-c-4.1	2x2x2 register tiling
<b>seidel2d</b>	2D stencil from polybench-c-4.1	2x2x2 register tiling

Table 4.1 – Test Benchmarks.

Benchmark	add	sub	mul	Total	Load	Store	CAA
<b>fir</b>	4	0	4	8	8	0	6
<b>iir</b>	0	4	8	12	16	0	12
<b>image2d</b>	0	9	0	9	18	0	12
<b>mm</b>	8	0	8	16	12	4	8
<b>gauss</b>	16	0	24	40	14	8	12
<b>fft4</b>	12	12	16	40	48	16	128
<b>dog</b>	32	0	48	80	37	16	44
<b>jacobi2d</b>	64	0	0	64	51	16	69
<b>seidel2d</b>	64	0	0	64	47	8	80

Table 4.2 – Number of operations and memory accesses in benchmarks. CAA represents the number of contiguous array access candidates.

### 4.5.4 Tests Setup

In order to compare the proposed [SLP](#) extraction method against **holistic** [SLP](#), we employ the test setup illustrated in fig. 4.18.

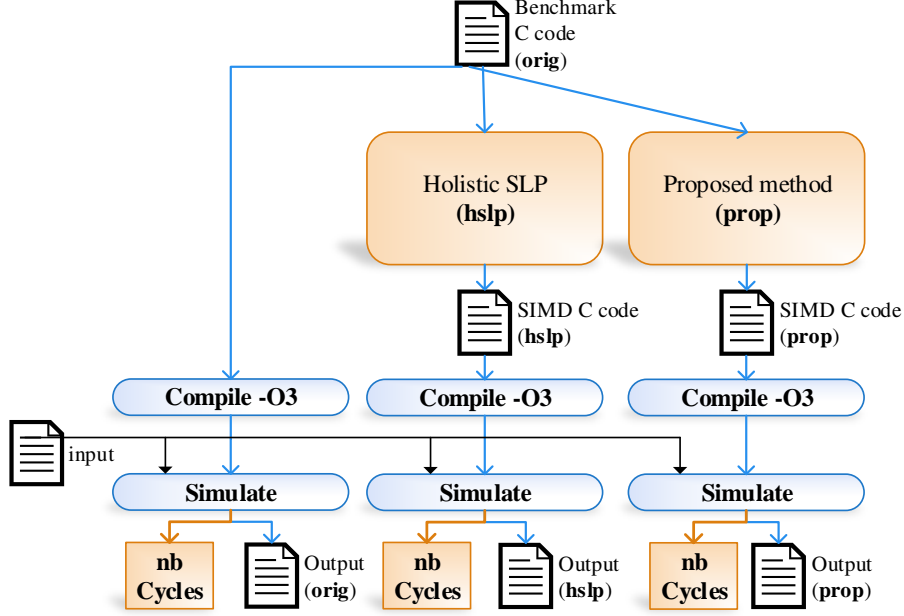


Figure 4.18 – Test procedure diagram.

For each benchmark, we generate three **SIMD** versions:

- **hslp**: obtained by applying **holistic SLP** extraction.
- **prop**: obtained by applying our proposed **SLP** extraction method.

We then compile all the **SIMD** versions, as well as the original (scalar) version – to which we refer by **orig** – using the target processor’s with the optimization flag (-O3). We consider multiple embedded architectures presented in section 4.5.2.

Finally, we simulate each version on the target processor’s simulator, using the same input data samples, and we extract the number of cycles required for executing the benchmark function.

## 4.5.5 Results

### 4.5.5.1 Proposed **SLP** extraction vs. Holistic SLP

In order to compare the proposed **SLP** extraction method (**prop**) against **holistic SLP** (**hslp**), we apply both **SLP** extraction flows ten times each (to capture the impact of the random selection factor in the group selection procedure discussed in section 4.4.2.1). And that is for all the benchmarks with 16-bit integer data-types. We report the average execution time improvement for **hslp**, and **prop** over **orig** (across the ten runs), in the histograms of figs. 4.19a, 4.19b, 4.20a and 4.20b for the targets XENTIUM, KAHRISMA, St240 and VEX-4 respectively. The minimum and maximum execution time improvement values over the ten runs are also reported

in the histograms.

The execution time improvement of each **SIMD** version,  $v$ , over the original version (**orig**) is computed as follows:

$$Improvement(v) = 100 * \frac{cycles(orig) - cycles(v)}{cycles(orig)} \quad (4.15)$$

Note that for **prop**, we did not apply batching for **PFCG** construction (cf. section 4.4.3.1), and we used distance-3 neighborhood for candidate benefit estimation (cf. section 4.4.2.1).

Results on all targets show a consistent trend of **prop** performing better than **hslp** for all benchmarks.

For **fir**, both versions perform the same on all targets and are not affected by the random selection factor, simply because this benchmark is very simple and both methods always find the best possible grouping solution. Though on ST240 the scalar performs better than the both **SIMD** versions.

For **iir**, **image2d**, **gauss** and **jacobi2d**, **prop** consistently performs better on all targets with near zero variation across different runs. Whereas **hslp** performance varies significantly between runs, but on average it still performs better than the scalar version. This is because **hslp** candidate benefit estimation is unable to distinguish between candidates leading to a random group selection.

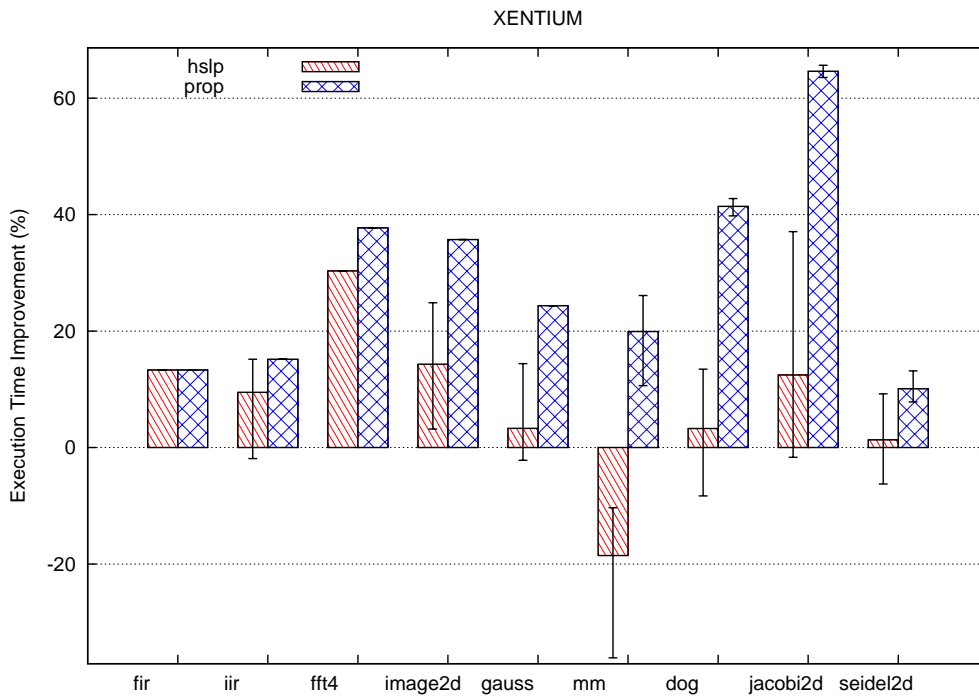
For **fft4**, both **SIMD** version performs good compared to the scalar version on all targets and across all runs. Though, **prop** still performs better. Note that **hslp** performance does not vary across runs. This is because of the operations scheme of **fft4**, which despite of **hslp** being sometimes unable of distinguishing between candidates, it still end up with the same grouping solution, mainly due to the high number of contiguous array accesses as shown in table 4.2.

For **mm**, **hslp** performs very poorly, it degrades performance compared to the scalar version on all targets (up to 20% worst) and varies very significantly between runs. On the other hand, **prop** consistently performs significantly better than the original version on all targets (up to 30% better).

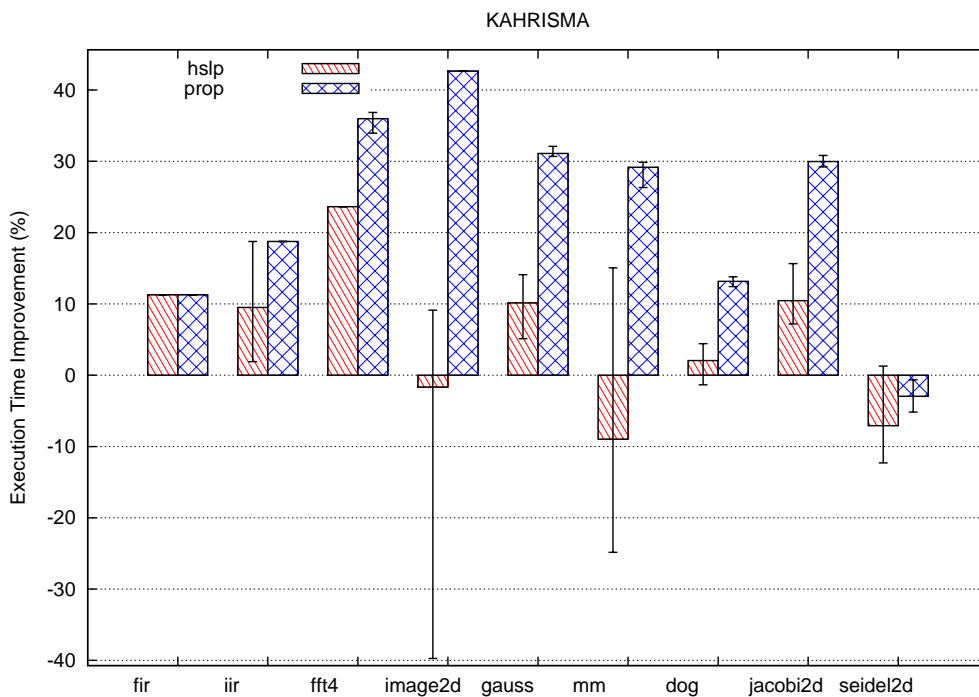
For **dog** and **seidel2d**, the results vary across targets. **prop** results in significant performance improvement on XENTIUM for **dog** (40%), slight improvement on KAHRIUMA (10%) and slight degradation on ST240 (3%). Whereas **hslp** often results in performance degradation.

All in all, these results point towards two main conclusions:

- **prop** performs better on all benchmarks and almost always lead to performance improvement over the scalar version on all three targets. Also it has very slight variations across different runs. This indicates that the candidate estimation and group selection method is precise and accurate enough.
- On the other hand, **hslp** performance varies significantly across runs, on all targets, and often lead to performance degradation compared to the scalar version. This indicates that the **hslp** candidate benefit estimation and group selection method is not accurate/precise enough.

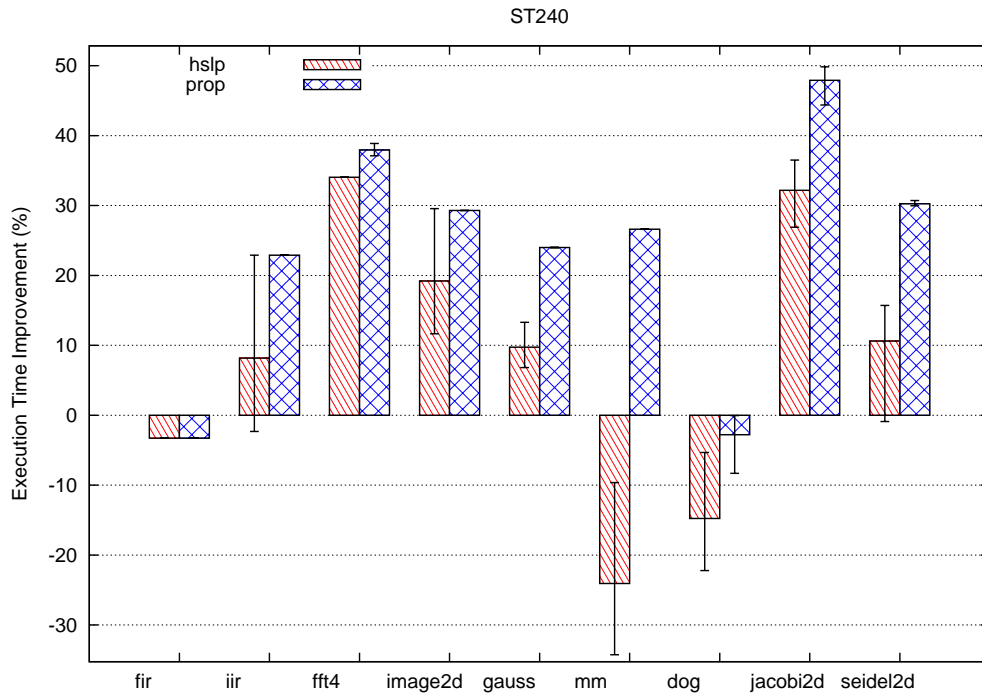


(a) Running on XENTIUM.

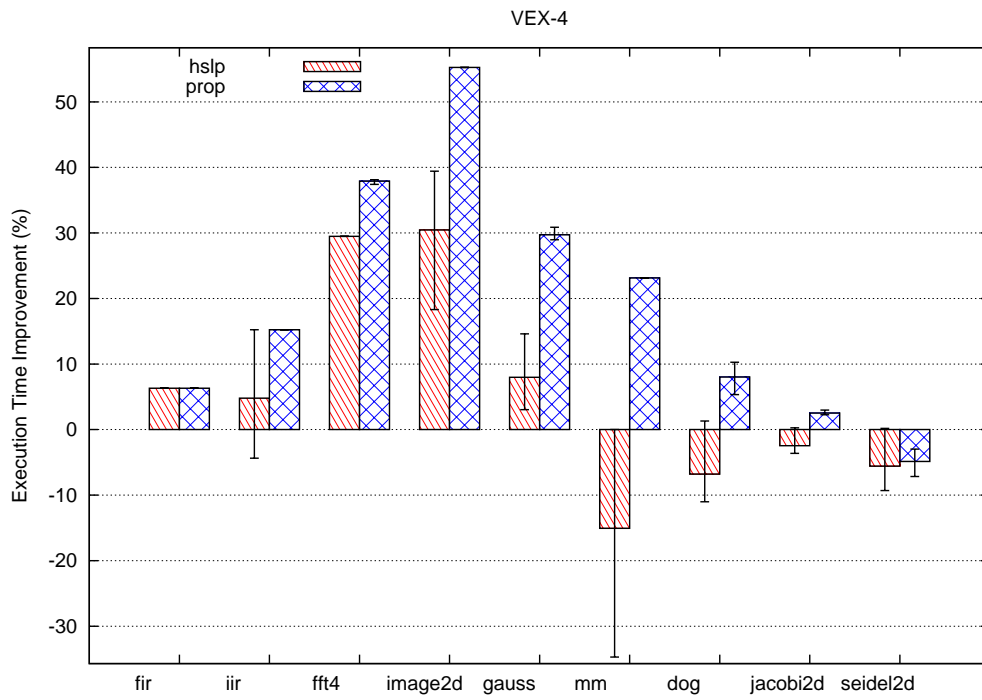


(b) Running on KAHRISMA.

Figure 4.19 – Execution time improvement of the **SIMD** code obtained by **prop** vs. **hslp**, over **orig**. The test is repeated 10 times for each benchmark. A bar represent the mean value and a line segment represents the minimum and maximum values of the execution time improvement.



(a) Running on ST240.



(b) Running on VEX-4.

Figure 4.20 – Execution time improvement of the **SIMD** code obtained by **prop** vs. **hslp**, over **orig**. The test is repeated 10 times for each benchmark. A bar represent the mean value and a line segment represents the minimum and maximum values of the execution time improvement.

#### 4.5.5.2 Simdization Time vs. Performance

In order to evaluate the **PFCG** size control strategy presented earlier in section 4.4.3.1, we apply both **prop** and **hslp** on the **jacobi2d** benchmark for different batch size values and we measure the time it takes for group selection to finish. We refer to this as **Simdization** time. It includes **PFCG** construction and groups selection. We then generate, compile and simulate the generated **SIMD** code for each approach and report the execution time improvement (i.e. performance improvement) compared to the original (sequential) version, **orig**.

The **Simdization** time and performance improvement variations in respect to the batch size, for the benchmark **jacobi2d** running on KAHRISMA, are reported in figs. 4.21 and 4.22a for **prop** and **hslp**, respectively.

The **Simdization** time increases, roughly, linearly for **prop** and quadratically for **hslp**, with the increase of the batch size value and consequently with the number of candidates<sup>14</sup>. This results are in sync with the complexity analysis of **prop** and **hslp**, discussed earlier in section 4.4.3.

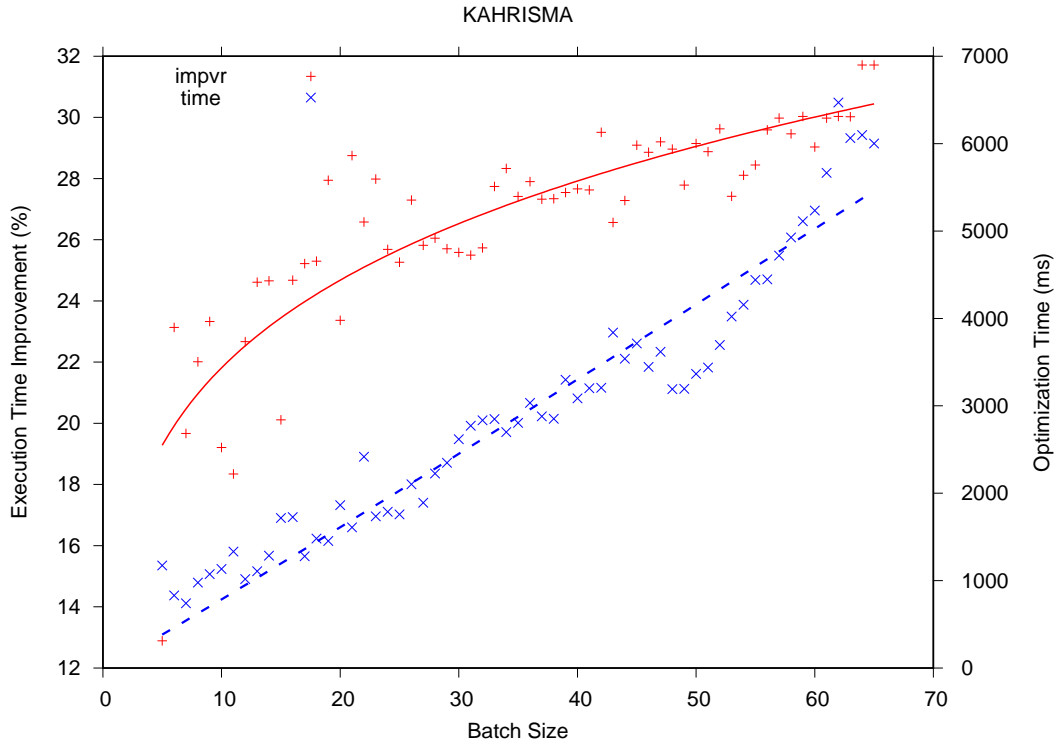
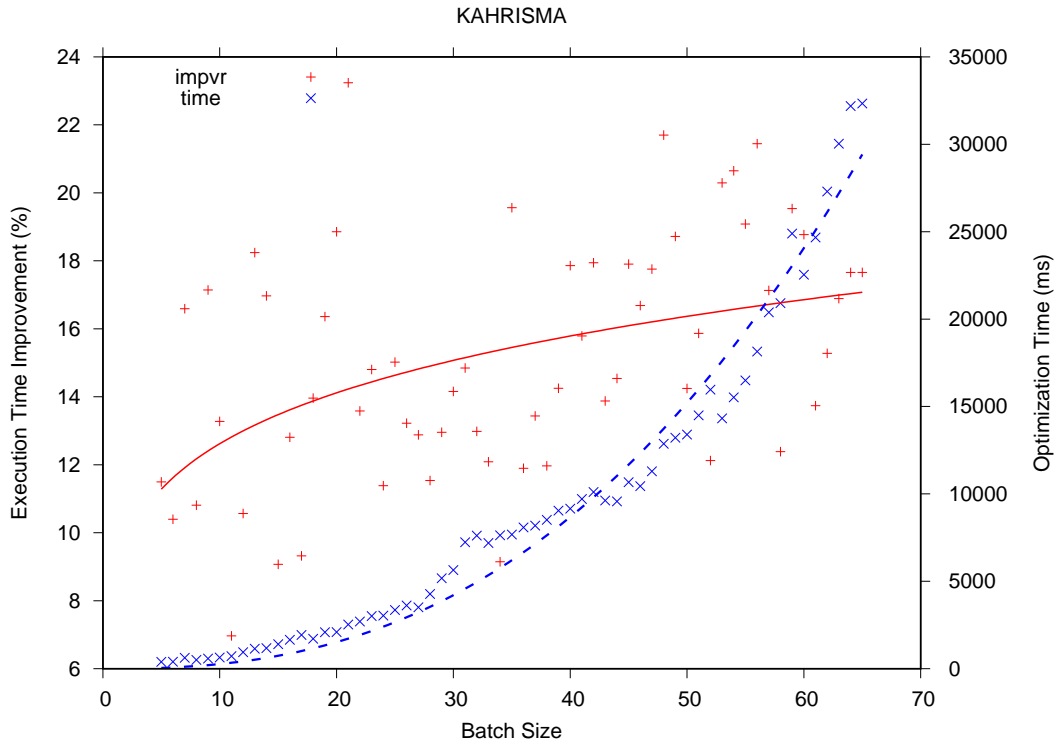
Besides, for **prop** the performance improvement increases logarithmically with the batch size, while **Simdization** time increases linearly. This means that selecting smaller batch sizes, down to a certain threshold (about 20 for **jacobi2d**), yields more **Simdization** time savings than performance penalties.

All in all, this results show that smaller operation batch sizes can effectively be used to shorten the **Simdization** time, which varies linearly. This does of course affect the performance but with a lesser degree, as can be clearly seen for **jacobi2d**. As a rule of thumb, the batch size value should be higher than half the size of the largest isomorphic operations set.

Note that the source-to-source compilation flow was implemented with no regard for the performance (**Simdization** time). It is implemented in Java and integrated to **GecOs** which is an eclipse application that heavily relies on the Eclipse Modeling Framework (EMF). Therefore, the absolute values of the **Simdization** time are not very representative and can be reduced by using an optimized implementation, but the main point here is the trending of these values with respect to the batch size.

---

14. The number of candidates roughly increases linearly with the increase of the batch size, as shown in section 4.4.3.1.

Figure 4.21 – Using `prop`.(a) Using `hs1p`Figure 4.22 – Execution time improvement and `Simdization` time variation with respect to the batch size, for the **jacobi2d** benchmark running on KAHRISMA.



## 4.6 Conclusion

In this chapter, we presented the state-of-the-art of **SLP**, we thoroughly discussed **holistic SLP**, a **SLP** extraction algorithm proposed by LIU et al in 2012 [78], and shed light on some of its shortcomings. We then proposed several modifications to overcome them and improve its efficiency. More specifically:

- We proposed a new more compact and more efficient **IR** for **SLP** extraction, the **PFCG**.
- We proposed an alternative **SIMD** group selection and candidate benefit estimation method based on **PFCG**.
- We implemented and compared the propose solution against **holistic SLP** on several embedded processors using a set of signal and image processing benchmarks.

Experimental results showed a significant performance improvement of the obtained **SLP** solution, by using our proposed method compared to **holistic SLP**, without the need for data layout transformations. The proposed **PFCG** helps to speedup the candidate benefit estimation and consequently reduces the complexity of the group selection algorithm. In addition, the proposed operation batching method can effectively be used to reduce the size of the **PFCG**; the latter varies linearly with the value of the batch size. This helps reducing the group selection time, while still achieving good **SLP** solutions.

By this point, we have at our disposal a complete source-to-source flow capable of automatically generating a **SIMD** C code for different embedded processors. In the next chapter, we discuss the interaction between floating-point to fixed-point conversion and **SLP** extraction. We show that, existing approaches considering both transformations independently, yields less efficient solutions. We argue that considering **SLP** extraction in conjunction with **Word Length Optimization (WLO)** helps achieving better results. So, we propose a new **SLP-aware WLO** algorithm, which we integrate into the source-to-source compilation flow that we implemented.

## Limitations

In this work we ignore the alignment constraint during group selection, we assume that all contiguous array reference superwords are aligned. When such superword is not actually aligned it induces a cost penalty, especially if the target does not support unaligned memory accesses. However, this cost penalty is generally not as high as in the case where the data are not contiguous, as previously illustrated in fig. 3.5. Indeed, a contiguous but unaligned data can be packed into a **SIMD** register by the mean of two vector loads followed by a permutation operation (assuming the target does not support unaligned accesses), whereas packing non-contiguous data may require as many loads as the number of elements in addition to several packing/permutation operations in order to pack all elements into one **SIMD** register (assuming the target does not support scatter/gather memory accesses).

The alignment problem can also be dealt with using post-optimization of the memory layout (such as array padding) and/or using loop transformation (and register shuffling like in [31]). In

anyway, this is worth considering in a future work.

In addition, in this work we only consider "simple" integer arithmetic [SIMD](#) operations (add, mul,...). We also use a very basic instruction selection procedure for [SIMD](#) code generation. However, many embedded processors ([DSPs](#)), such as XENTIUM and ST240, provide multiple "complex" [SIMD](#) operations, such as *muladd* and *addsubb*. Considering such [SIMD](#) operations during the [Simdization](#) would provide more alternatives to improve performance. This could be considered in the [SLP](#) extraction phase, during [SIMD](#) group candidates identification. Alternatively, a more complex [SIMD](#) instruction selection can be also used. This is also worth considering.

Besides, the performance of [SLP](#) solutions can be improved by considering inter basic-block (and inter-procedural) analysis to reduce packing/unpacking overhead by reusing superwords across basic blocks.

Finally, in this work we only targeted embedded processors with *subword* [SIMD](#) support. It would be interesting to see how the proposed [SLP](#) extraction method performs when targeting processors with wider [SIMD](#) data-path, such as the NEON extension for ARM processors.



## Chapter 5

# SLP-aware Word Length Optimization

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## 5.1 Introduction

Unlike general purpose processors, embedded processors must satisfy increasing need for computation power while complying to strict design constraints such as cost, performance and power consumption. Even though, many embedded processors, such as ARM cortex-A, provide hardware support for floating-point arithmetic, a good number of ultra low power embedded processors, such as ARM cortex-M0/1/3, TI TMS320C64x and Recore XENTIUM [104] do not, in order to reduce die area (cost) and/or minimize power consumption. This comes for the cost of restraining programmability to the use of fixed-point arithmetic, while application prototyping in many domains, such as signal processing and telecommunication applications, employs floating-point representation.

Although floating-point can be soft-emulated on such processors, it drastically degrades performance (up to 45x as reported in section 5.5.6). Instead, fixed-point implementations are preferably used. Hence, floating-point to fixed-point conversion is a crucial step for an efficient implementation when targeting such processors.

On the other hand, most embedded processors nowadays provide support for (subword) [Single Instruction Multiple Data \(SIMD\)](#) as a mean to improve performance for little cost overhead. In order to make efficient use of such processors, the software should also exploit [SIMD](#) opportunities.

As discussed previously, floating-point to fixed-point conversion (see chapter 2) and [Simdization](#) (see chapter 3) are tedious, error prone and time consuming transformations. Therefore, automated methodologies and tools are necessary in order to cut down applications time-to-market and consequently development cost.

Floating-point conversion consists of attributing a fixed-point format for each floating-point data and operation's intermediate result. The fixed-point format should specify the word-length in addition to the binary-point position.

Keeping full operations precision, in a fixed-point implementation, requires large word-lengths which, unless supported by the target processor, would also require costly software emulation, yielding a poor performance. Rather, quantizations are applied to limit word-lengths growth and consequently improving performance, for the cost of degrading the application's quality by introducing errors. Overflow errors, while significant, can be easily avoided by employing a conservative approach for [Integer Word Length \(IWL\)](#) determination. Quantization errors, however, propagate throughout the system, get amplified and can lead to significant error on the output. To avoid that, the conversion process must account for these errors and carefully select fixed-point formats that keep the computation's accuracy within an "acceptable" limit while maximizing performance.

This performance/accuracy trade-off has been identified and exploited when targeting customizable architectures, in the context of HLS [65] for instance, where the designer has more flexibility in customizing word-lengths supported by the architecture.

This is not the case when targeting processors with fixed data-path size. Employing smaller data

sizes – in the absence of [SIMD](#) – does not really benefit the application’s performance. On one hand, it may require additional operations to perform data-type conversions, since all integer operations are performed on operands with the native word-size anyway (type promotion). But on the other hand, it may reduce the memory footprint which can improve performance. For example, in the C code snippet of fig. 5.1, the addition’s operands are generally promoted, by the compiler, to `int` before performing the operation and the result is then converted back to `char`.

So all in all, it does not make much sense to use smaller word-lengths in this context.

```
char a,b,c;
...
c = a + b;
```

Figure 5.1 – C code snippet.

However, since most embedded processors nowadays provide support for [SIMD](#), using smaller data word-lengths can be exploited by [SIMD](#) instructions to perform an operation on several packed data simultaneously, thus ultimately improving performance.

Intuitively, in this context using narrower word-lengths should normally translate to better performance on one side, due to the increased vectorization factor, but lower quality on the other side due to the reduced data precision. Previous work [85] followed this intuition when applying floating-to-fixed-point conversion. They aim at minimizing word-lengths without taking into account [Superword Level Parallelism \(SLP\)](#), which can be applied, independently, later on.

However, this intuition is unrealistically optimistic since, selecting narrower word-lengths during [Word Length Optimization \(WLO\)](#) does not necessarily result in performance improvement after applying [SLP](#) extraction, mainly because [WLO](#) is unaware of [SLP](#) grouping possibilities and the associated overhead.

In this chapter, we address these problems by jointly considering [SLP](#) extraction and [WLO](#). More specifically:

- We propose a new [SLP](#)-aware [WLO](#) algorithm. To the best of our knowledge this is the first work to jointly consider both, [WLO](#) and [SLP](#) extraction.
- We implement it as a fully automated source-to-source compilation flow with a customizable and extensible fixed-point/[SIMD](#) back-end supporting multiple target architectures.
- We test our approach on several embedded processors against some signal processing applications.

The chapter is organized as follows:

First, we illustrate the aforementioned problems and discuss the related work in section 5.2. Then we present our proposed joint [WLO](#) and [SLP](#) extraction approach in section 5.3. In section 5.4, we present the fully-automated, floating-to-fixed-point conversion and [SLP](#) extraction source-to-source compilation flow. Finally, we present the experimental setup and results in section 5.5.

## 5.2 Motivations and Related Work

In many application domains, such as signal processing, floating-point arithmetic is used for rapid prototyping. When targeting embedded [SIMD](#) processors with no floating-point support, a floating-point to fixed-point conversion step is crucial to achieve good performance, by:

- Eliminating the need for software floating-point emulation which drastically impact performance.
- Reducing data sizes and consequently reducing the memory footprint, which may also improve performance.
- Enabling the exploitation of SIMD capabilities which can further improve performance.

The down side is mainly the complexity of fixed-point implementation.

In this context, floating-point conversion can be either applied manually or using automated tools as discussed in chapter 2.

Manual conversion is very tedious, error prone and time consuming, which limits the ability to explore the fixed-point design space, and generally pushes toward using uniform word-length fixed-point representations using the target’s native word size. This often leaves no room for [Simdization](#) when targeting subword Multimedia extensions and limits [SIMD](#) opportunities when targeting superword Multimedia extensions (see section 3.2.2).

On the other hand, automatic floating-point to fixed-point conversion allows for better and faster exploration of the fixed-point design space, but existing methodologies and tools, at best, only exploit the fact that [SIMD](#) processors can operate on different data word-lengths and assumes that selecting smaller word-lengths yields better performance without considering the effective consequences of such choices on [Simdization](#) and ultimately on performance.

Cilio and Corporaal [26] presented an approach for automatic conversion of floating-point C code into fixed-point C code targeting embedded processors. The [IWLs](#) of some variables are specified by the user via `pragma` annotations. This information is propagated to determine the [IWLs](#) of the remaining variables. The proper scaling operations are then automatically inserted. Kum et al.[64] proposed a similar method except they used simulation to determine [IWLs](#). Also, they proposed a scaling optimization algorithm that minimizes a scaling cost function, taking into account whether or not the target processor has a barrel shifter, using integer linear programming or simulated annealing.

Both of these approaches, only use the target’s native word-length and no [WLO](#) is performed. Therefore, they are unable to take advantage of the [SIMD](#) capabilities of a processor.

In fact, during [WLO](#) the goal is to minimize a certain cost function – generally representing the performance (execution time) – as much as possible while keeping the accuracy within an acceptable limit. The quality of the cost evaluation or its ability to properly distinguish between two fixed-point solutions is crucial, since it is the main driver of the [WLO](#) decisions (along with the accuracy constraint).

A straightforward way to evaluate the cost associated with a fixed-point solution, while considering [Simdization](#), could be obtained using simulation. The tested fixed-point solution needs

to be implemented, compiled (with applying [Simdization](#)) and run on the target processor, or simulated, with representative data samples in order to obtain a performance estimation. While accurate, this method is extremely slow, rendering it unpractical for design space exploration. Alternatively, the tested fixed-point solution could be only compiled and then the execution time can be estimated using a cost model. Again, this method is very slow and unpractical, specially if optimizations such as [Simdization](#) are to be applied during compilation for each tested fixed-point solution.

Following the same logic, Menard et al proposed a simpler and less aggressive method [85]. It consists of considering all supported instructions, including [SIMD](#), that can implement a given operation in the system. The goal of their proposed [WLO](#) is to select, for each operation, the instruction (associated to a word-length) which minimizes the overall execution time, subject to an accuracy constraint. The execution time is estimated using a simple model. The execution time associated with an instruction is provided by the processor's model. In case a [SIMD](#) instruction is selected to implement an operation, its execution time is simply divided by the maximum number, say  $N$ , of operations that can be executed in parallel by this instruction. For example, when targeting a 32-bit processor with all instructions having an execution time of 1. If a 32-bit (scalar) instruction is selected to implement an operation, then the operation's execution time is 1. However, in case a 16-bit [SIMD](#) instruction is selected then its execution time is  $1/2$ .

This implies two main assumptions:

- First, it assumes that when an [SIMD](#) instruction is selected to implement a (scalar) operation,  $N$  similar operations will ultimately be executed in parallel –if [Simdization](#) is later applied– by the same instruction, without actually knowing whether or not this is possible. Hence, the operation's execution time is estimated as  $1/N$  th of the instruction's execution time provided by the model.
- Second, it assumes that no overhead is associated with a [SIMD](#) instruction. In another word, it completely ignores the overhead associated with the required data packing/unpacking operations.

These assumptions are very optimistic and unrealistic.

**Example 10** *To illustrate this, let's consider the dummy example of fig. 5.2. For the sake of illustration, let's assume that [WLO](#) decides to attribute the following word-lengths:*

- 16-bit for  $A[]$ ,  $x$ , operations 1 and 3
- 32-bit for  $y$  and operation 2

*Assuming a 32-bit target processor with 2x16-bit [SIMD](#) support.*

*If we consider applying loop vectorization after floating-point to fixed-point conversion. The for loop cannot be vectorized since it carries a dependency on  $A$ .*

*Also, if we consider applying [SLP](#) extraction on the loop's body, whose [Data Flow Graph \(DFG\)](#) is depicted in fig. 5.2. No [SIMD](#) group candidates are available because 1 and 2 have different word-lengths, and 1 and 3 have a dependency.*

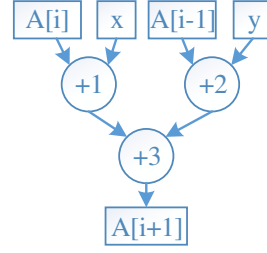


```

float A[N], x, y;
...
for(int i=1; i<N-1; i++)
    A[i+1] = (A[i] + x) + (A[i-1] + y);

```

(a) C code snippet.



(b) Loop's body DFG.

Figure 5.2 – Motivating example.

So, in both cases the assumptions made by *WLO* are wrong since *Simdization* of any of the operations is not possible.

However, if *WLO* would have selected operations 1 and 2 to be 16-bit, *SLP* extraction would be able to pack them together into a *SIMD* group. But again, the overhead associated with packing/unpacking operation could be very high.

The bottom line is that, unless *WLO* is aware of the *Simdization* opportunities and the associated cost, it has no way of predicting the impact of the decisions it takes on *SIMD* exploitation, and consequently on performance.

In this work, we propose to jointly consider *Simdization* and *WLO* as a solution to this problem. We focus on *SLP* extraction as *Simdization* method and we present a *SLP*-aware *WLO* algorithm.

### 5.3 Joint WLO and SLP extraction

Applying *WLO* without taking into account *SLP* extraction constraints will most likely yield inefficient solutions. This is because *WLO* decisions directly dictate the search space of *SLP* extraction. It may prevent, otherwise possible, *SIMD* grouping candidates by selecting, for instance, different word-lengths for operations that can be, otherwise, grouped together<sup>1</sup>.

Besides, it is very important to note that *WLO* is performed under accuracy constraint. In other words, only a limited accuracy-degradation *budget* can be used to try to improve performance as much as possible. In this context, one of the main factors impacting performance is how well *SIMD* capabilities are being exploited. It is not wise for the *WLO* to spend the accuracy-degradation budget on optimizing operations that cannot be efficiently exploited by *SLP* to improve performance. If *WLO* is unaware of *SIMD* grouping possibilities and their associated overhead, it will blindly optimize word-lengths of operations that may not end-up in a *SIMD* group, either due to dependencies or conflicts with other groups. Even worse, it may optimize operations which lead to a *SLP* solution with a high packing/unpacking overhead.

Moreover, the order in which the operations are to be optimized is crucial. For instance, in the example 10, we know that only operations 1 and 2 can be grouped together. If we optimize first

1. Recall that all operations in a *SIMD* group must have the same word-length.

the word-length of 1 to make it "fit" in a **SIMD** instruction and then optimize 3, the accuracy-degradation budget may run out before getting the chance to optimize 2, so that it can be grouped with 1 in the same **SIMD** instruction. To avoid this, 2 should be preferably optimized before 3. This is not possible unless **SLP** opportunities (and their associated cost) are known to the **WLO** process.

Besides, the scaling operations, required to correctly implement a fixed-point specification using integer arithmetic operators, have a major impact on performance. Therefore scalings are also taken into account.

In order to address these problems, we propose an approach to jointly perform floating-point to fixed-point conversion and **SLP** extraction. We couple an accuracy-aware **SLP** extraction with a **SLP**-aware **WLO** algorithm. We also propose an **SLP**-aware scalings optimization algorithm. In the remainder of this section we present these algorithms.

### 5.3.1 Overview and Intuition

Since any decision of **WLO** can directly affect **SLP**, as shown previously, we use **SLP** extraction to guide it through. The aim is to let **WLO** focus on optimizing operations that belong to **SIMD** groups which are selected by the **SLP** extraction algorithm as the "best" **SLP** solution, taking into account the data packing/unpacking overhead.

The problem is that **SLP** extraction requires to know the operations data-types and word-lengths to construct the set of group candidates. Recall that all operations in a **SIMD** group candidate must have the same word-length, which have to be supported by the target **SIMD Instruction Set Architecture (ISA)**, and that the overall size should not exceed the **SIMD** vector size. However, before **WLO** is performed the word-lengths of operations are not known yet! Thus, **SLP** extraction depends on **WLO** which requires **SLP** solution to guide it in order to find an efficient solution.

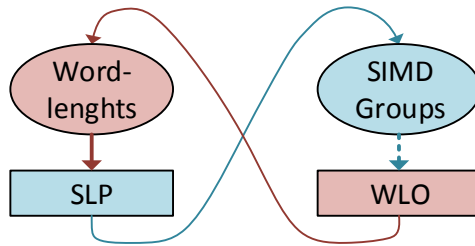


Figure 5.3 – WLO/SLP phase ordering problem.

To solve this phase ordering problem, we break the cycle by loosening the aforementioned word-length constraints on **SIMD** group candidates. This means we no longer impose that two operations must have the same word-length to form a group candidate. This way **SLP** extraction will have the "freedom" to select which candidate is most beneficial to become a **SIMD** group. Once **SLP** extraction makes its decision, the selected group is provided to **WLO** which sets the word-

length of all its operations in such a way that the group becomes valid and implementable on the target processor (i.e. that the previously loosen constraints become enforced). The diagram of fig. 5.4 depicts the functional overview of the proposed approach.

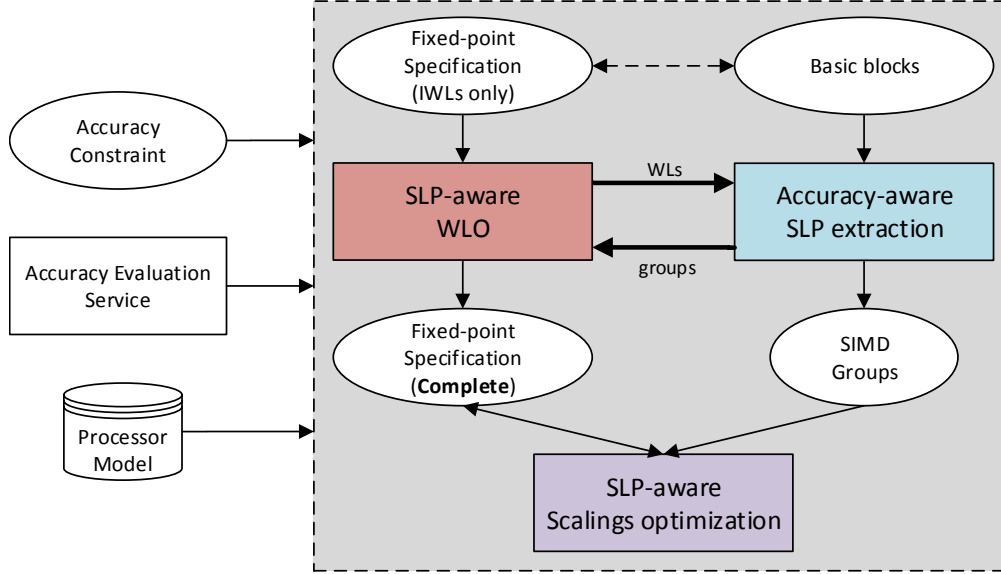


Figure 5.4 – Overview of the joint **WLO** and **SLP** extraction approach

Both, **SLP** extraction and **WLO**, require some knowledge about the target processor. In fact, **SLP** extraction is limited to the **SIMD** operations supported by the target and to the size of its **SIMD** data-path. For instance, if the target does not support **SIMD** division, then division operations will not be considered during group candidates extraction. Also, the size of a group cannot exceed the maximum size supported by the target, and its elements data-type/size must be supported by the target as well. For instance, only groups of two 16-bit elements are allowed when targeting a processor supporting only 2x16-bit **SIMD**. Similarly, we limit **WLO** to the word-lengths natively supported by the target processor, for two reasons. First, to avoid "expensive" software emulations and second, to limit the fixed-point solution space. The drawback is that it may not be always possible to find a valid solution which respects very tight accuracy constraints.

Therefore, both transformations are provided with a model of the target processor containing all necessary information. This model is presented in section 5.3.2.

### 5.3.2 Processor Model

A processor's model provides necessary information about the characteristics of the operations it can perform, which are needed for both **SLP** extraction and **WLO**. In this work, we model a processor by the following:

- $O$ : the set of supported operators.
- $V$ : the **SIMD** registers size.

**Définition 5.1 (Operator)** *An operator is specified by:*

- *T*: the type of operation it can perform (add, sub, mul, shr, ...).
- *WS*: the word-lengths of all its input operands ( $in_0, in_1, \dots$ ) and output ( $out$ ). For a binary operator:

$$WS = (in_0.W, in_1.W, out.W) \quad (5.1)$$

- *N*: the number of operations it can perform simultaneously ( $\geq 1$ ).
- *PM*: the precision mode which determines whether the operator keeps full precision, *Least Significant Bits (LSBs)* only (case of typical integer operators) or *Most Significant Bits (MSBs)* only (case of fixed-point operators).
- *QM*: the quantification mode (truncation, rounding).
- *OM*: the overflow mode (wrap-around, saturation). This is not important in this work since we do not allow overflows.
- *S*: the amount of pre/post-scaling for each input/output operand (0 if none,  $> 0$  if right shift,  $< 0$  if left shift).
- *SIMD* intrinsics for code generation.

This model allows the representation of a wide variety of operators. It can represent scalar ( $N = 1$ ) and *SIMD* ( $N \geq 1$ ) operators. It can also represent generic integer as well as fixed-point specific operators thanks to *PM*, *QM*, *OM* and *S* parameters.

The models of the processors targeted in this work are presented in appendix A.

### Multiplication Operators

For multiplication operators, the precision mode *PM* complements the information specified by the operand word-lengths to determine what operation is performed by the operator.

For a full-precision operator (*op*), the output's word-length ( $out.W$ ) must be at least as wide as the sum of both input word-lengths:

$$op.out.W \geq op.in_0.W + op.in_1.W \quad (5.2)$$

In this case no quantization is applied by the operator and the full precision is preserved. In embedded processors, this usually corresponds to operators of size  $(w, w, 2w)$ , where the output is generally stored in a pair of registers; one containing the *MSBs* and the other containing the *LSBs* of the result. In the case of a *SIMD* operator, the results of the  $N$  operations performed in parallel might be organized in different ways in the output *SIMD* registers. For instance, the 2x16-bit multiplication instruction of XENTIUM returns the full-precision 32-bit result of each operation in a separate register. In case the output is used by another *SIMD* instruction, the *LSBs* (or *MSBs*) of both result registers must first be packed together into one register. An additional packing instruction is required in this case.

To avoid the word-length growth, integer multiplication operators generally only keep the *LSBs* of the result. It's up to the developer to deal with potential overflows. Assuming no

overflows, the **LSBs** of the result correspond to the exact result of the multiplication and the **MSBs** can be simply discarded. This is not the case when using such operator to implement a fixed-point multiplication. In fact, the result of the multiplication of two signed fixed-point numbers,  $a$  and  $b$ , with respective formats,  $\langle W_1, I_1, F_1 \rangle$  and  $\langle W_2, I_2, F_2 \rangle$ ,  $c = a * b$  is of format  $\langle W_1 + W_2, I_1 + I_2, F_1 + F_2 \rangle$  (see section 2.3). Using a keep-**LSBs** ( $w, w, w$ ) operator to implement such operation means that the **MSBs** which generally represent the integer part are discarded. The result in this case would be meaningless as illustrated in fig. 5.5. To avoid this,



Figure 5.5 – Fixed-point multiplication example.

the operand formats must satisfy the following constraints:

- $I_3$  must be wide enough to contain the values range of the multiplication's result (i.e. no overflow).
- $F_1 + F_2 \leq F_3$

The first condition is enforced during **IWL** determination (see section 5.4.2). The second condition can be enforced during **WLO**, by reducing the **Fractional Word Lengths (FWLs)** on the inputs so that their sum  $(F_1 + F_2)$  "fits" in the available bits for the output's **FWL**, which can be determined based of the operators output word-length value ( $W_3$ ) and the **IWL** ( $I_3$ ), as such  $F_3 = W_3 - I_3$ .

In fact, when a keep-**LSBs** ( $w, w, w$ ) operator is selected to implement this multiplication, the maximum number of bits available for the **FWL** of:

- $a$  is  $AF_1 = w - I_1$
- $b$  is  $AF_2 = w - I_2$
- $c$  is  $AF_3 = w - I_3$

In order to be able to correctly use this operator, the **FWL** of the output must not exceed  $AF_3$  (i.e.  $F_3 \leq AF_3$ ). To get the maximum available precision we set  $F_3 = AF_3$ . This constraint must be satisfied, otherwise the result would be meaningless as shown above in the example of fig. 5.5. In this example actually,  $w = 8, I_3 = 7$  so  $AF_3 = 8 - 7 = 1$ , however,  $F_3 = F_1 + F_2 = 9$  thus  $F_3 > AF_3$  !

To enforce this constraint, the **FWLs** of the inputs ( $F_1$  and  $F_2$ ) must be reduced so that their sum become at least equal to  $F_3$  (i.e. reduced by a total of  $e = (AF_1 + AF_2) - AF_3$  bits. The

"extra"  $e$  bits can be entirely reduced from  $F_1$  or  $F_2$  or some from each. Thus, multiple solutions are possible here (they can be considered during WLO).

Reducing the FWL can be achieved by increasing the IWL by the same amount, since the FWL is implicitly determined from the values of the word-length and the IWL. For the example of fig. 5.5,  $F_3 = AF_3 = 1$  and  $e = (5 + 4) - 1 = 8$ . A possible solution is to remove 4 bits from the  $F_1$  and 4 bits from  $F_2$ , as illustrated in fig. 5.6. In this case the result of the keep-LSB operator is correct.

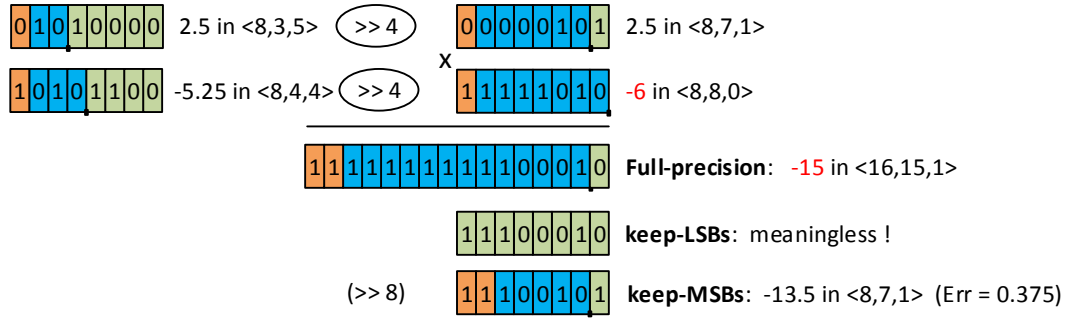


Figure 5.6 – Fixed-point multiplication example.

Alternatively, we can restrict the word-length of the input operands of a keep-LSBs ( $w, w, w$ ) multiplication operator to  $w/2$ , thus emulating a full-precision ( $w/2, w/2, w$ ) operator. This solution is less flexible as it does not allow to assign more precision for the operands that needs it the most (e.g.  $(w/3, 2w/3, w)$ ). However, it simplifies the exploration of the solution space because, unlike the first solution, it does not require to modify the IWLs during WLO. Therefore, IWLs, and consequently the scaling operations, can be determined before and remain fix during WLO.

### Add/Sub Operators

As discussed previously in section 2.3, performing full-precision fixed-point add/sub operations requires the operands to be aligned to their maximum FWL. This may require increasing the operands word-length, and consequently the size of the operator, specified by  $WS$ . To avoid this, we limit the fixed-point formats of the operands in such a way to ensure that the underlying integer operation can be performed on the selected operator. We do so by aligning the operands to the *minimum* (instead of maximum) FWL; the operand with the highest FWL is right shifted by  $|F1 - F2|$ . In this case, up to  $|F1 - F2|$  precision bits can be lost, but no overflow can be introduced, hence no word-lengths increase is required.

### 5.3.3 SLP-aware WLO algorithm

In this section we present the proposed SLP-aware WLO algorithm. We start by defining the solution space in section 5.3.3.1, and we present the algorithm in section 5.3.3.2. The latter relies

on an accuracy-aware [SLP](#) extraction algorithm, which we will present later on in section 5.3.4

### 5.3.3.1 Solution space definition

A fixed-point computation system is represented by a *fixed-point specification*. This specification is defined below:

**Définition 5.2 (Fixed-point Specification)** *The fixed-point specification of a system is a directed graph where a node represents either a data (definition 5.4) or an operation (definition 5.5). A fixed-point format is associated to each data node and operation's operand. A scaling amount (definition 5.6) is associated to each edge, representing a dependency between two nodes.*

*For instance, fig. 5.7 illustrates the representation of a fixed-point specification containing one operation node and three data nodes.*

**Définition 5.3 (Fixed-point Format)** *A fixed-point format (see section 2.3) is specified by at least two of the following three parameters:*

- Integer word-length:  $I$  (including sign bit for signed numbers)
- Fractional word-length:  $F$
- Total word-length:  $W = I + F$

**Définition 5.4 (Data Node)** *A data node represents either a program variable, constant or an implicit operation's intermediate result. It may have multiple inputs and/or multiple outputs. All elements of an array variable are represented with the same data node. Only one fixed-point format is associated to a data node.*

**Définition 5.5 (Operation Node)** *An operation node represents an operation in the [DFG](#). It has one data node as output and may have several data nodes as inputs. The output, and each input, have each an associated fixed-point format, which may be different from the format of the predecessor/successor data node as depicted in fig. 5.7.*

**Définition 5.6 (Scaling)** *To each edge is associated a scaling amount, computed based its predecessor (*pred*) and successor (*succ*) fixed-point formats:*

$$\text{amount} = \text{pred}.F - \text{succ}.F \quad (5.3)$$

*If the scaling amount is zero, no scaling operation is required, otherwise, a right or left shift is necessary if the amount is respectively positive or negative.*

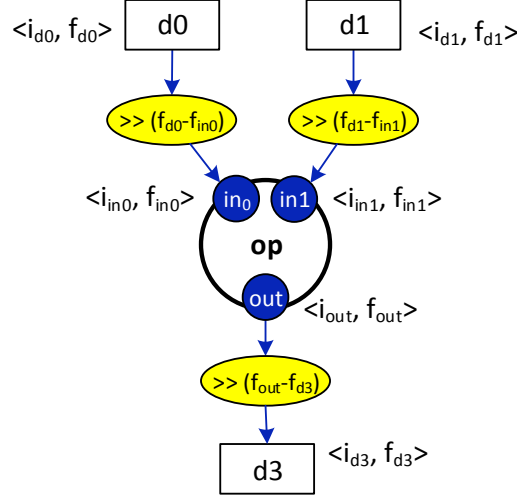


Figure 5.7 – Representation of an operation node ( $op$ ) and its predecessors/successor data nodes ( $d_x$ ) in a fixed-point specification.  $\langle i_x, f_x \rangle$  represents a fixed-point format with  $i_x$  representing the **IWL** and  $f_x$  the **FWL**. Elliptical nodes represent scaling operations; a negative amount corresponds to a left shift by the absolute value.

Each fixed-point format (definition 5.3) is specified by the values of its word-length ( $W$ ) and **IWL** ( $I$ ). We assume that the **IWLs** are pre-specified before starting **WLO**. The **IWLs** determination is presented later on in section 5.4.2.

The set of all possible word-length values, that each fixed-point format can take, is constrained by the target processor. In fact, an operation node in the fixed-point specification can be implemented using any operator, among the set of all supported operators of the target that can implement the correspondent operation type (add, mul, ...). Operators of the same type ( $T$ ) generally corresponds to different word-lengths on which the operation can be performed on. For instance, when targeting ST240, providing 32-bit (scalar) and 2x16-bit **SIMD** add operators (see table A.2), an add operation node in the fixed-point specification, can be implemented using either operators. Therefore, the set of possible word-length values for the operation's operands is limited to  $\{16, 32\}$ , in this case. Even though this limitation can be lifted, by soft-emulating different precision operators for instance, we restrict word-lengths to those natively supported by the target processor. Not only to limit the solution space's size, but also to avoid the overhead associated with software emulations of the unsupported operators. In other words, we ensure that the required operators, needed to implement the fixed-point solution produced by **WLO**, are natively supported by the target processor.

The solution space of **WLO**, constructed based on the target processor's model, associates a set of possible operators for each operation in the fixed-point specification. Consequently, it associates a set of possible word-length values for each fixed-point format, in the fixed-point specification.



**Algorithm 9** SLP-aware WLO algorithm pseudo-code

---

```

1: // Input: sorted list (by priority) of basic blocks for SLP extraction, BBs
2: // Input: fixed-point specification with IWLs pre-determined, SPEC
3: // Input: accuracy constraint, A
4: // Output: set of selected SIMD groups, G. determine word-lengths in SPEC
5: procedure SLP-WLO(BBs, SPEC, A)
6:   for each fixed-point format f in SPEC do
7:     f.W  $\leftarrow$  maximum possible word-length (in the solution space)
8:   end for
9:   for b in BBs do // visit in priority order (see section 5.4.4)
10:    G  $\leftarrow \emptyset$ 
11:    while not done do
12:      pfcg  $\leftarrow$  BUILDPFCG(b, SPEC, A) // see algorithm 11
13:      Selected  $\leftarrow$  GROUPSELECTION(pfcg, spec, A) // see algorithm 12
14:      if Selected =  $\emptyset$  then
15:        done
16:      end if
17:      Update b and prepare it for next iteration
18:      G  $\leftarrow G \setminus \{e_1, e_2 : \{e_1, e_2\} \in pfcg.S\}$ 
19:      G  $\leftarrow G \cup pfcg.S$ 
20:    end while
21:    SCALOPTIM(G, SPEC, A)
22:  end for
23:  return G, SPEC
24: end procedure

```

---

**5.3.3.2 Algorithm**

The fixed-point specification representing the solution space along with the accuracy constraint are taken as inputs. The IWLs of all nodes in the fixed-point specification are assumed to be pre-determined. This step is detailed later on in section 5.4.2. The accuracy constraint, specified by the user, represents the maximum allowed noise power of the quantization error at the system's output.

The pseudo-code of the SLP-aware WLO algorithm is listed in algorithm 9.

**Step 1:** We start by selecting the highest precision solution available in the solution space. We do so by setting the word-length of each fixed-point format to the maximum value, in the associated set of possible word-lengths present in the solution space (lines 6-8). This solution generally corresponds to the case where minimum SLP is available, but on the other hand, it represents the highest precision fixed-point specification, that can be obtained using natively supported operators (word-lengths).

**Step 2:** Next, we process each basic block to be considered for **SLP** extraction, starting by the higher priority ones. Priority here depends on the contribution of the basic block to the overall execution time; a higher priority is attributed to the one that occupies more of the execution time. This is to ensure that the accuracy-degradation budget is wisely spent on optimizing most performance-impacting basic blocks first. The selection and sorting of basic blocks to be considered for **SLP** extraction is performed beforehand. We discuss this step in section 5.4.4.

For each basic block we iteratively apply the accuracy-aware **SLP** extraction (lines 11-20). At each iteration, we build the **Pack Flow and Conflict Graph (PFCG)** (line 12), representing the **SLP** solution space, and then we use the **SLP** extraction procedure to obtain the set of selected **SIMD** groups (line 13).

For **SLP** extraction we adapt the algorithm that we proposed earlier in chapter 4 to the accuracy constrained context of this work. This accuracy-aware **SLP** extraction algorithm is detailed in section 5.3.4. In a nutshell, when building the **PFCG** we drop the data-size constraints and we make sure that each **SIMD** group candidate can be selected without violating the accuracy constraint. Whenever a new **SIMD** group is selected, all the operation nodes (in the fixed-point specification) it contains are assigned the same operator (from the target model), which is capable of implementing the overall **SIMD** operation with the highest possible precision. Let:

- $spec = (nodes, edges)$  be a fixed-point specification.
- $g = \{e_1, e_2, \dots, e_n\}$  be a selected **SIMD** group,  $e_i$  is an element in  $g$ , it represents an (scalar) operation node:  $e_i \in spec.nodes$ . All elements in  $g$  have the same operation type,  $t$ , by definition (see definition 5.7).
- $O = (o_1, o_2, \dots, o_k)$  the list of all operators, of type  $t$ , available in the target processor model. The list is ordered by increasing precision, as such  $precision(o_i) \leq precision(o_{i+1})$ .

Initially (in step 1), all operation nodes in  $spec$  are assigned the highest precision operator of the corresponding type. For  $e_i$  nodes, this correspond to the operator  $o_k$ . Now when  $g$  is selected, the operator  $o_j \in O$  is assigned for all nodes  $e_i$  ( $i \in [1, n]$ ), such that:

$$\begin{cases} j \in [1, k] \\ o_j.N \geq n \\ j \geq x, \forall x \in [1, k] : o_x.N \geq n \end{cases} \quad (5.4)$$

In other words,  $o_j$  is the highest precision operator that can implement  $g$ . This corresponds to the procedure SETMAXWL, whose pseudo-code is listed in 10. In the remainder of this chapter, we will assume that this action is performed whenever we say a group is *selected*.

**Example 11** To illustrate this, let's consider the **KAHRISMA** processor's model (see table A.3) which supports 1x32-bit ( $o_3$ ), 2x16-bit ( $o_2$ ) and 4x8-bit ( $o_1$ ) add operators. In this case, if a **SIMD** group of two add operations,  $\{e_1, e_2\}$  is selected, then the operator  $o_2$  is assigned for both  $e_1$  and  $e_2$ .

The elements of each selected group are then replaced by a new operation (representing the

---

**Algorithm 10** Set the word-length of a **SIMD** group to the maximum possible

---

```

1: // Input: fixed-point specification, SPEC
2: // Input: a SIMD group, c
3: procedure SETMAXWL(c, SPEC)
4:   o ← highest precision operator that can implement c // as defined in eq. (5.4)
5:   for operation node e ∈ c (e ∈ SPEC.nodes) do
6:     assign Operator o to e in SPEC // this sets the word-lengths of the fixed-point
       formats of e's operands according to o.WS.
7:   end for
8: end procedure

```

---

group) in the basic block (line 17) in order to prepare for the next **SLP** extraction iteration, which allows the extension of the groups size when possible, otherwise the processing of the basic block is completed and we move to the next one (lines 14-16).

**Step 3:** The global set of selected groups (*G*) is updated after each iteration (lines 18-19). It is used to optimize scaling operations (line 21). The scaling optimization algorithm is presented in section 5.3.5.

As an output we obtain a complete fixed-point specification for the system, along with the set of selected **SIMD** groups. These information are finally used to generate fixed-point and **SIMD** C code, as presented in section 5.4.5.

### 5.3.4 Accuracy-aware SLP extraction algorithm

For **SLP** extraction we adapt the algorithm that we proposed earlier in chapter 4 to the accuracy constrained context of this work.

#### Building **PFCG**

First, we adapt the **PFCG**<sup>2</sup> construction procedure. The corresponding pseudo-code is listed in algorithm 11.

When constructing the **PFCG** of a given basic block, we identify the set of **SIMD** group candidates (*C*) as well as the conflicts (*X*) between them. Recall that, a group candidate (definition 4.3) is a pair of isomorphic and independent operations with same size yielding superwords that does not exceed the **SIMD** data-path size. And, that two groups are in conflict (definition 4.5) if they contain the same operation or if they cause a cyclic dependency.

However, in the context of this work, the word-lengths are not known at this level. Therefore, we loose all size constraints (line 6) when identifying group candidates. A candidate is thus defined as specified by Definition 5.7 .

---

2. **PFCG** is the **Intermediate Representation (IR)** we proposed in order to represent the **SLP** extraction solution space. See section 4.4.1.

**Définition 5.7 (SIMD group candidate)** *In this accuracy-constrained context, a SIMD group candidate is a pair of independent operations of the same type (add, sub, mul, ...). No constraints are imposed on the word-lengths.*

---

**Algorithm 11** Adapt Building PFCG (algorithm 2)

---

```

1: // Input: Data Flow Graph  $dfg$ . It is a Directed Acyclic Graph (DAG)
2: // Output: Pack Flow and Conflict Graph  $pfcg$ 
3: // EVALACC(SPEC): evaluates the accuracy of the current fixed-point specification
4: procedure BUILDPFCG( $dfg, SPEC, A$ )
5:   for each pair  $(o_1, o_2)$  of isomorphic operations or contiguous accesses to same array in
      $dfg$  do
6:     if  $o_1$  and  $o_2$  are independent then
7:        $c \leftarrow \{o_1, o_2\}$ 
8:       // make sure  $c$  is valid
9:       SETMAXWL( $c, SPEC$ )
10:      if EVALACC( $SPEC$ ) violates  $A$  then
11:        skip  $c$ 
12:      end if
13:      revert WL of  $c$ 
14:       $pfcg.C \leftarrow pfcg.C \cup \{c\}$ 
15:      // ... connecting  $c$ 's flow edges is omitted; same as algorithm 2
16:      // connect  $c$ 's conflicts
17:       $pfcg.X \leftarrow pfcg.X \cup \{\{c, c'\} : c' \in pfcg.C \text{ and } (c' \cap c \neq \emptyset \text{ or } c', c \text{ introduce a cyclic}$ 
        dependency)  $\}$ 
18:      SETMAXWL( $c, SPEC$ ); SETMAXWL( $c', SPEC$ );
19:      if EVALACC( $SPEC$ ) violates  $A$  then
20:         $pfcg.X \leftarrow pfcg.X \cup \{\{c, c'\}\}$ 
21:      end if
22:      revert WL of  $c, c'$ 
23:    end if
24:  end for
25:  return  $pfcg$ 
26: end procedure

```

---

Furthermore, in this accuracy constrained context, some candidates in  $C$  may not be valid. This is the case of a candidate  $c$ , that if *selected*<sup>3</sup> while all other candidates are not *selected*, the accuracy constraint is violated. In this case,  $c$  can never be implemented, using an available SIMD operator, without violating the accuracy constraint. Hence, we eliminate all invalid candidates in  $C$  (lines 8-13).

Besides,  $X$  does not represent all the conflicts in this context. In fact, two candidates are in conflict if: when both are *selected* while all other candidates are not *selected*, the accuracy

---

3. Recall that when a group is selected, the word-length of all the operation nodes it contains is set as specified earlier by eq. (5.4).

constraint is violated. In this case both candidates cannot coexist without violating the accuracy constraint, hence they are considered in conflict (lines 34-38). We refer to this type of conflicts as *accuracy conflict*.

### SIMD Group Selection

After the PFCG is properly built, the group selection estimates the benefit associated with each remaining candidate and then iteratively selects the most beneficial one,  $g$ . This procedure is the same as presented earlier in section 4.4.2. the pseudo code is recalled in algorithm 12.

---

**Algorithm 12** Recall Group Selection Procedure from algorithm 1

---

```

1: // Input:  $pfcg$ , is the PFCG.
2: // Input:  $SPEC$ , is the fixed-point specification.
3: // Output: Set of selected groups.
4: procedure GROUPSELECTION( $pfcg, SPEC$ )
5:   while  $pfcg.C \neq \emptyset$  do
6:     for each candidate  $c \in pfcg.C$  do
7:       BENEFITESTIMATION( $c, pfcg, SPEC$ )
8:     end for
9:      $best \leftarrow \text{SELECT}(pfcg)$ .
10:    UPDATEPFCG( $best, pfcg$ ) // mark  $best$  as selected and Update  $pfcg$ 
11:    ELIMINATECYCLES( $pfcg$ )
12:  end while
13:  return  $pfcg.S$ 
14: end procedure
15:
16: // Output: Set the benefit of candidate  $c$ 
17: procedure BENEFITESTIMATION( $c, pfcg, SPEC$ )
18:    $sub \leftarrow \text{EXTRACTSUBPFCG}(c, pfcg)$  // see algorithm 3
19:   ELIMINATESUBCONFLICTS( $c, sub, SPEC$ ) // see algorithm 13
20:   COMPUTEBENEFIT( $c, sub, pfcg$ )
21: end procedure

```

---

However, the candidate benefit estimation method is modified to adapt to the accuracy-constraint context of this work.

First, after extracting the sub PFCG graph of a give candidate  $c$ ,  $sub(c, N)$  (representing the distance- $N$  pack flow neighborhood of  $c$ ), we make sure the remaining candidates in  $sub(c, N)$  can all coexist without violating the Accuracy constraint. The pseudo-code of this procedure is listed in algorithm 13.

Then, we also modify the computation of the benefit associated with the selection of  $c$  in order to take into account its impact of the accuracy. The pseudo-code of the modified candidate benefit estimation is listed in algorithm 14. We measure the deferential of accuracy,  $\delta Acc$ , before and after (temporarily) *selecting* all remaining candidates in  $sub(c, N)$  (lines 10-17).

Finally, we modify the "best" candidate selection procedure. The corresponding pseudo-code

**Algorithm 13** Eliminate Conflicts in *sub*


---

```

1: // Input: c, a SIMD group candidate.
2: // Input: sub, a subgraph of the PFCG; it is the distance-N pack flow neighborhood of c.
3: // Input: SPEC, the fixed-point specification.
4: procedure ELIMINATESUBCONFLICTS(c, sub, SPEC, A)
5:   apply conflict elimination as in algorithm 4
6:   // Make sure the remaining candidates can all coexist without violating the Accuracy
   constraint.
7:   for n ∈ sub.V do
8:     SPEC.save(n)
9:     SETMAXWL(n, SPEC)
10:  end for
11:  while EVALACC(SPEC) violates A do
12:    x ← node ∈ sub.V \ {c} with highest  $\frac{\text{deltaACC}}{1 + \text{flow degree}}$ 
13:    sub.V ← sub.V \ {x} // set of nodes
14:    sub.X ← sub.X \ {{x, y} ∈ sub.X, ∀y} // set of conflict edges
15:    sub.F ← sub.F \ {(x, y), (z, x) ∈ sub.F, ∀y, z} // set of pack flow edges
16:  end while
17: end procedure

```

---

is listed in algorithm 15. In the first stage (line 3), we select the set of all candidates which have the maximum value of benefit (Pack reuse-to-cost ration), among them we select (line 5) the candidate inducing the minimum accuracy degradation (*deltaAcc*).

When a candidate is selected, the PFCG is updated normally, by eliminating all conflicting candidates (see section 4.4.2.2). Additionally, the word-length of all its elements is specified as explained earlier in eq. (5.4).

### 5.3.5 SLP-aware Scalings Optimization

Another major impact on the performance of a fixed-point implementation is the cost of scaling operations. Their impact depends on how well the target processor supports shifting operations. For example, a barrel shifter can generally perform a shift operation of any amount in constant time. Whereas shift registers require a variable time depending on the shifting amount.

In the context of SLP an additional critical factor is the fact that scaling operations may break some superword (vector) reuse chains and hence require the introduction of packing/unpacking operations. Thus, severely impacting the performance, not only due to the scalings cost but also to the additionally introduced packing/unpacking overhead. This is, in fact, because most embedded processors only support SIMD shifting instructions by the same amount of all the vector elements. Therefore in case two elements of the same vector have to be shifted by different amounts, they need to be unpacked first, shifted independently and then repacked, before being

**Algorithm 14** Compute Candidate Benefit.

---

```

1: procedure COMPUTEBENEFIT( $c, sub, pfcg$ )
2:    $N_R \leftarrow |sub.V|$ 
3:   // Estimated number of additional required packings.
4:    $N_{pack} \leftarrow |\{x \in pfcg.C \setminus sub.V : \exists (x, y) \in pfcg.F, y \in sub.V \setminus pfcg.S\}|$ 
5:   // Estimated number of additional required unpackings.
6:    $N_{unpack} \leftarrow |\{x \in sub.V \setminus pfcg.S, x \text{ is not a Store candidate} : \nexists y \in sub.V \cup pfcg.S : (x, y) \in sub.pfcg\}|$ 
7:    $c.reuse \leftarrow N_R$ 
8:    $c.conflict \leftarrow |\{\{x, y\} \in pfcg.X : x \in sub.V\}|$ 
9:    $c.benefit \leftarrow \frac{1 + N_R}{1 + N_{pack} + N_{unpack}}$ 
10:  SPEC.save
11:   $acc_o \leftarrow EvalAcc(SPEC)$ 
12:  for  $x \in sub.V$  do
13:    SETMAXWL(x, SPEC)
14:  end for
15:   $acc_1 \leftarrow EvalAcc(SPEC)$ 
16:  SPEC.revert
17:   $c.deltaAcc \leftarrow acc_1 - acc_o$ 
18: end procedure

```

---

**Algorithm 15** Select the ‘best’ candidate in the PFCCG

---

```

1: procedure SELECT( $pfcg$ )
2:   // First Stage: Set of candidates with maximum benefit estimation
3:    $bestSet \leftarrow \{c \in pfcg.C : c.benefit = max\}$ 
4:   // Second Stage:
5:    $best \leftarrow c \in bestSet$  with minimum  $c.deltaAcc$  value
6:   return  $best$ 
7: end procedure

```

---

able to be used by an SIMD instruction<sup>4</sup>.

**Example 12** For instance, in the example of figure 5.8, operations 1 and 2 are in a group. The scaling amounts associated to the output superword, used by group  $\{3, 4\}$ , are  $f1 - f3$  and  $f2 - f4$ , where  $fx$  is the FWL of operation  $x$ .

---

4. In case masking operations are supported, packing/unpacking are not required but multiple SIMD instructions would still be needed to perform such operations. Though masking operations are rarely supported.

**Algorithm 16** SLP-aware Scaling optimization pseudo-code

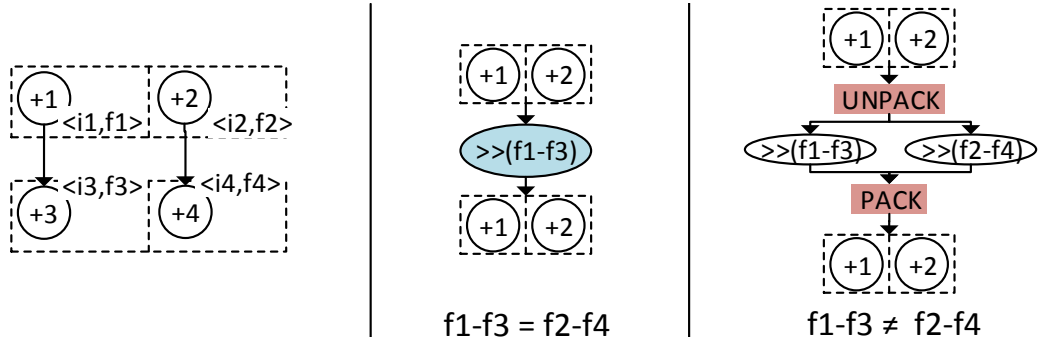
---

```

1: // Input:  $G$ , the set of selected SIMD groups.
2: // Input:  $SPEC$ , fixed-point specification.
3: // Input:  $A$ , the accuracy constraint.
4: procedure SCALOPTIM( $G, SPEC, A$ )
5:   for each superword reuse  $(g_1, g_2): g_1, g_2 \in G$  do
6:      $S \leftarrow g_1.elements.FWL - g_2.elements.FWL$  // list of required scaling amounts
7:     if all amounts in  $S$  are equal then
8:       skip
9:     else if all amounts are positive (i.e. right shifts are required) then
10:       $m \leftarrow \max(S)$ 
11:       $SPEC.save\ g_1$ 
12:      for  $e \in g_1$  do
13:        reduce FWL of  $e$  by  $(m - S[e])$ 
14:      end for
15:      if EVALACC( $SPEC$ ) violates  $A$  then
16:         $SPEC.revert\ g_1$ 
17:      end if
18:    end if
19:  end for
20: end procedure

```

---

Figure 5.8 – Scaling example.  $f_x$  represents the FWL.

When the amount is zero it indicates that no scaling is required. If it is positive a right shift is required. In case  $f1 - f3 \neq f2 - f4$ , the scaling amounts are different, thus the shifting operations cannot be grouped and therefore packing/unpacking operations are required.

In this work, we address this problem by proposing an SLP-aware, accuracy-aware scaling optimization algorithm, which is listed in algorithm 16. The goal is to try to make all elements of an SIMD group scalable by the same amount, so that the scaling operations can be grouped together and implemented using an SIMD instruction without the need for packing/unpacking.

To avoid this case, we reduce the FWLs while keeping word-lengths intact (by increasing the corresponding IWLs) so that the scaling amounts of all elements in a group become equal. By



reducing the [FWLs](#), the accuracy of the fixed-point specification may degrade, therefore this optimization is performed as long as the accuracy constraint is not violated.

Additionally, if the accuracy constraint allows it, we can try to eliminate scaling operations altogether, by reducing [FWLs](#) of all elements in a group so that their corresponding scaling amounts become zero.

## 5.4 Source-to-source Compilation Flow

We implemented the proposed, joint floating-point to fixed-point conversion and [SLP](#) extraction approach, as a fully automated source-to-source transformation in the compiler framework, GeCoS[47]. In section 5.4.1, we present an overview of this source-to-source flow. We then present the [IWL](#) determination, accuracy evaluation and basic-blocks selection procedures in sections 5.4.2 to 5.4.4. Finally we present the fixed-point and [SIMD](#) C code generator in section 5.4.5.

### 5.4.1 Flow Overview

The source-to-source flow diagram is depicted in figure 5.9. Starting from an annotated floating-point C code, we first construct the correspondent [IR](#), which is then analyzed to determine the set of basic blocks to be considered for [SLP](#) extraction (see section 5.4.4), as well as to construct the fixed-point specification (see definition 5.2).

Then, the dynamic range of each node in the fixed-point specification is determined using IDFIX [3], a floating-to-fixed-point conversion framework integrated to [Generic Compiler Suite \(GeCos\)](#). This information is later used to specify the [IWLs](#) (see section 5.4.2) of all formats in the fixed-point specification.

Besides, we also use IDFIX in order to evaluate the accuracy of a given fixed-point specification solution. To do so, the analytical expression of the system's output noise power is generated as a function of the fixed-point specification (see section 5.4.3). This is used during [WLO](#) as a metric to evaluate the fixed-point specification's accuracy and compare it against the user specified constraint.

The half-specified ([IWLs](#) only) fixed-point specification along with the model describing the target processor (see section 5.3.2) are used to determine the search space for [WLO](#), as explained earlier in section 5.3.3.1. The proposed joint [WLO](#) and [SLP](#) extraction algorithm is used to obtain a fully specified fixed-point specification and the set of [SIMD](#) groups that yields the "best" performance while satisfying the accuracy constraint.

These information are finally used by the back-end to convert the original floating-point C code into fixed-point using native integer C data-types with explicit scaling operations in order to match the fixed-point specification. Furthermore, it implements the [SIMD](#) groups using an abstract C macros [Application Programming Interface \(API\)](#) and generates the corresponding

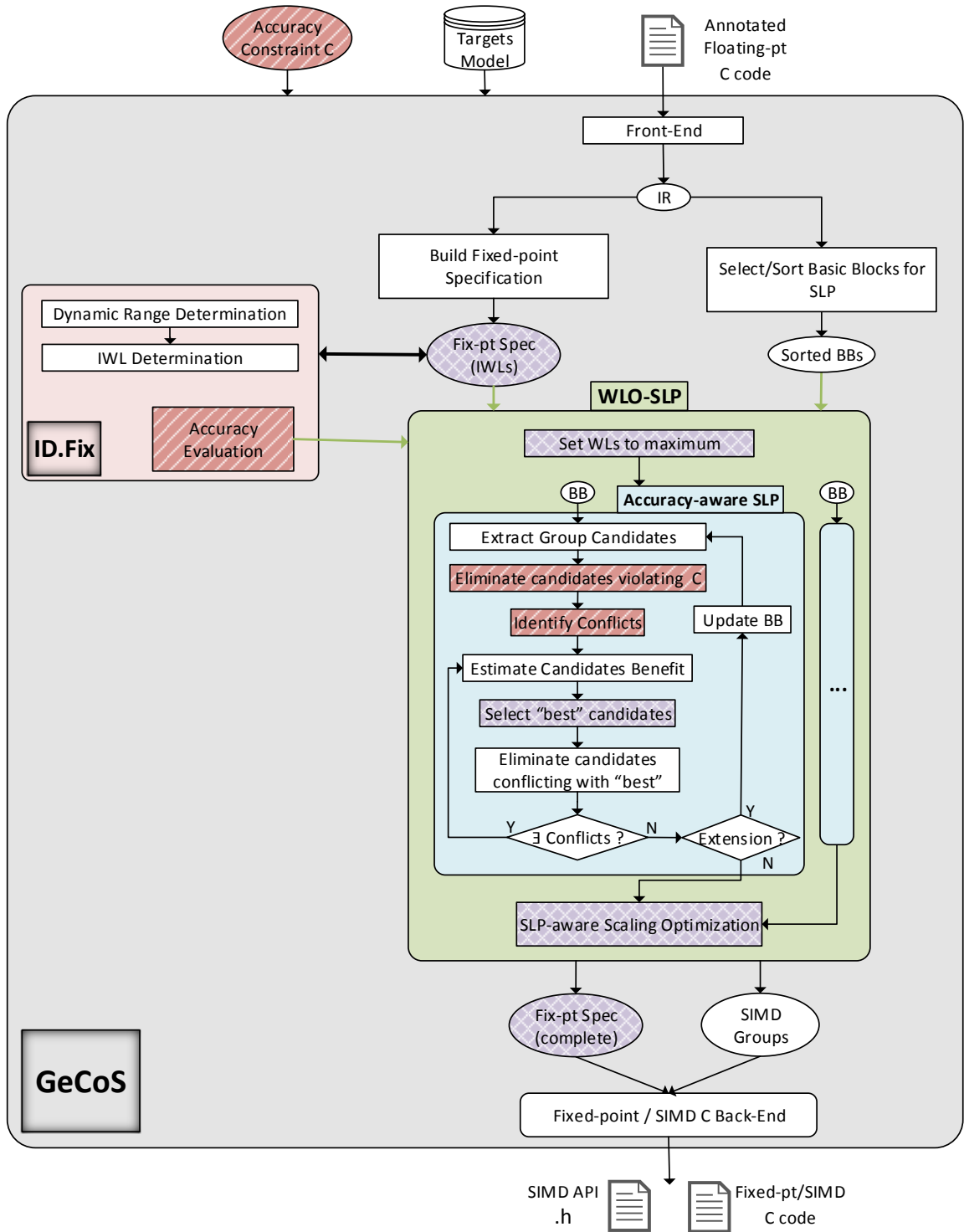


Figure 5.9 – SLP-aware WLO source-to-source compilation flow diagram.

[API](#)'s implementation for the specified target processor, using its corresponding [SIMD](#) intrinsics. The implementation of the back-end is presented later in section 5.4.5.

### 5.4.2 Integer Word Length determination

The integer word-lengths of each data node  $d$  in the fixed-point specification is first determined based on its dynamic range, in such a way to avoid overflows:

$$d.DIWL = \max(nbBits(MIN), nbBits(MAX)) + Sign \quad (5.5)$$

Where:

—  $[MIN, MAX]$  is the values range interval of data  $d$ .

$$nbBits(n) = \begin{cases} \lfloor \log_2(n) \rfloor + 1, & (n > 0) \\ \lceil \log_2(|n|) \rceil, & (n < 0) \\ 0, & (n = 0) \end{cases}$$

$$Sign = \begin{cases} 1, & (MIN < 0) \\ 0, & (MIN \geq 0) \end{cases}$$

So, we set the [IWL](#) of each data to its DIWL and from now on, when modifying the IWL, we make sure that it never goes below DIWL:

$$d.I \geq d.DIWL \quad (5.6)$$

In other words,  $d.DIWL$  is the minimum possible value for  $d.I$ .

The dynamic range intervals are obtained using interval arithmetic (see section 2.5.1) to propagate the user-specified ranges for all the inputs of the system. This method is already implemented in IDFIX (see section 2.6.2). For doing so, each variable, in the input C code, representing an input of the system must be annotated by a `pragma` specifying the  $MIN$  and  $MAX$  values.

Then, we specify the [IWLs](#) of the inputs ( $in_0$  and  $in_1$ ) and output ( $out$ ) fixed-point formats of each operation, based on its predecessors ( $d_0$  and  $d_1$ ) and successor ( $d_3$ ) data nodes, as illustrated in fig. 5.7. For an add (or sub) operation:

$$\begin{aligned} &— m = \max(d_0.I, d_2.I, d_3.I) \\ &— in_0.I = in_1.I = out.I = m \end{aligned}$$

For a mul operation:

$$\begin{aligned} &— in_0.I = p_0.I \\ &— in_1.I = p_1.I \\ &— in_2.I = in_0.I + in_1.I \end{aligned}$$

### 5.4.3 Accuracy evaluation

In order to evaluate the accuracy of a given fixed-point specification solution during **WLO**, we use the analytical accuracy evaluation method that is already implemented in **IDFIX** (see section 2.6.2). Currently, this method only supports **Linear Time-Invariant (LTI)** and non-recursive non-**LTI** systems. Besides, the C code must satisfy various constraints, as mentioned in section 2.6.2, mainly. The code is later flattened by **IDFIX** in order to construct the **Signal Flow Graph (SFG)**. Thus, this method is currently not suitable for large applications.

Even though, accuracy evaluation is an essential part of this flow, it is however completely independent and orthogonal to the proposed **SLP**-aware **WLO** algorithm. Therefore, any alternative method can be seamlessly used instead. The same applies for dynamic range evaluation.

### 5.4.4 Select and sort Basic-blocks for SLP

In this accuracy constrained context, the order in which basic blocks are optimized is important. It is better to use the accuracy-degradation budget on fully optimizing a more performance-impacting basic block before moving to another one. This way we ensure that all potential superword reuses, in a basic block, are being exploited as much as the accuracy constraint allows it. Therefore, we assign a priority to each basic-block to be considered for **SLP** extraction. Priority here depends on the contribution of the basic block to the overall execution time; a higher priority is attributed to the one that occupies more of the execution time. This can be determined automatically based on profiling or static analysis, for instance. However, in this work we use **pragma** annotations to specify the set of basic blocks to be considered for **SLP** extraction and to determine their associated priority.

Since this step is completely separated from the proposed joint **WLO** and **SLP** extraction algorithm, an automated approach can easily replace the one currently used.

### 5.4.5 Fixed-point/SIMD Code Generation

First, we adapted the C++ code generator that was already implemented in **IDFIX** (see section 2.6.2). It can generate Algorithmic C Datatypes or SystemC C++ code. This in fact already existed in **IDFIX**, however it was only converting the data-type of floating-point variables into the corresponding fixed-point format specified by the fixed-point specification. The existing generator did not modify operations and relied on the C++ fixed-point library to perform scalings when needed. This can actually be a problem, since the implementation of the fixed-point operations in such libraries usually keep full precision by automatically increasing the word-lengths when needed (for example in Algorithmic C Datatypes, the operands of and add/sub are aligned to the maximum **FWLs**, and their word-length are extended), unless the result is explicitly casted or assigned to a variable. This means, that all operations whose results are not directly assigned to a variable, are implemented using full precision. Thus the generated code may not correspond exactly to the fixed-point specification. This is very important when

targeting a processor, since it may require simulation of full-precision operators, thus degrading the performance. Therefore we added support for proper operation scaling (casting) to reflect the exact specification.

On the other hand, we also implemented a configurable fixed-point C code generator. We did that for two reasons, first to avoid the unnecessary overhead inducing by using such libraries. Second, in order to target processors which do not have C++ compilers, such as VEX. The code generator can generate fixed-point C code using only native integer data-types and operations with proper scaling using shift and cast operations. Alternatively, it can generate code using a generic macros [API](#), to represent fixed-point data-types and operations. This [API](#) can then be implemented for the target architecture. This helps make the code more readable. It currently only support truncation as rounding mode and does not support saturation.

For [SIMD](#) C code generation, we use the same code generator presented earlier in section 4.5.1.

## 5.5 Experimental evaluation and Results

In this section, we present the experimental evaluation process we used to test the validity of our proposed approach, performing joint [SLP](#) extraction and float-to-fixed-point conversion, compared to a classical approach, applying both transformations independently.

### 5.5.1 Experimental Setup

To represent our approach, we use the source-to-source compilation flow, presented earlier in section 5.4. We will refer to it as **WLO+SLP**.

The goal is to test how efficient **WLO+SLP** is in exploiting the accuracy/performance tradeoff, compared to a classical approach performing, first, float-to-fixed-point conversion, and then [SLP](#) extraction independently. To represent the latter approach, we implement a similar source-to-source compilation flow. This flow is presented below in section 5.5.2, we refer to it by **WLO-then-SLP**.

The experimental setup is illustrated in figure 5.10. Starting from the original floating-point (single-precision) version, called **float**, of a benchmark's C code, we apply both **WLO+SLP** and **WLO-then-SLP**, for a given accuracy constraint value. **WLO+SLP** generates one fixed-point [SIMD](#) C code. Whereas, **WLO-then-SLP** first generates a fixed-point C code (without [SIMD](#)), and then it generates the fixed-point [SIMD](#) C code (after applying [SLP](#) extraction). All four C code versions, are then compiled (with -O3) and simulated on the target processor's simulator, using the same floating-point input data. The floating-point input data is pre-converted to the corresponding fixed-point formats, for all versions except **float**. The number of cycles spent executing the benchmark function is finally reported for each version. The data allocation, initialization and conversion are not included.

We run this procedure for each benchmark, on different target processors and for different

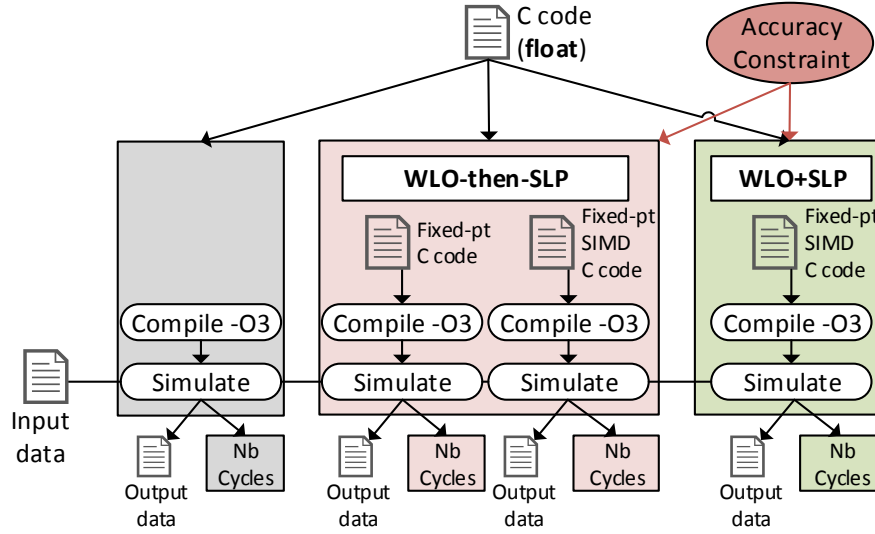


Figure 5.10 – Test setup

values of the accuracy constraint. The benchmarks we use are presented in section 5.5.3, and the targeted processors are presented in section 5.5.4.

### 5.5.2 WLO-then-SLP source-to-source flow

The source-to-source compilation flow implemented to represent **WLO-then-SLP** approach, is depicted in fig. 5.11. Unlike our approach, it first performs float-to-fixed-point conversion, and then **SLP** extraction independently.

We implement it in **Gecos** and we also use the framework, **IDFix**, to perform float-to-fixed-point conversion. For **WLO** we used the Tabu search algorithm presented by NGUYEN et al [91]. To estimate the cost of a given fixed-point specification, a relative execution time is associated to each operation depending on its attributed operator's precision (word-length). This is very similar to the approach proposed by MENARD et al [85]. For instance, when targeting ST240, which provides the possibility to implement an operation using either 32-bit or 2x16-bit operators, then the corresponding cost for the 32-bit operator is set as the double of that of 16-bit.

Once the word-lengths have been determined, the fixed-point specification is used to convert the **IR** from floating-point to fixed-point. This is used to perform **SLP** extraction using the algorithm we presented earlier in section 4.4.

Finally, we use the same back-end to generate both fixed-point and **SIMD** C code versions for the target processor.

Contrary to our approach, **WLO-then-SLP** performs **WLO** independently from **SLP** extraction i.e. without considering the impact of word-length selection on **SLP** opportunities and the associated overhead due to data packing/unpacking. Instead, it simply assumes that selecting narrower word-lengths is always better for **SLP**.

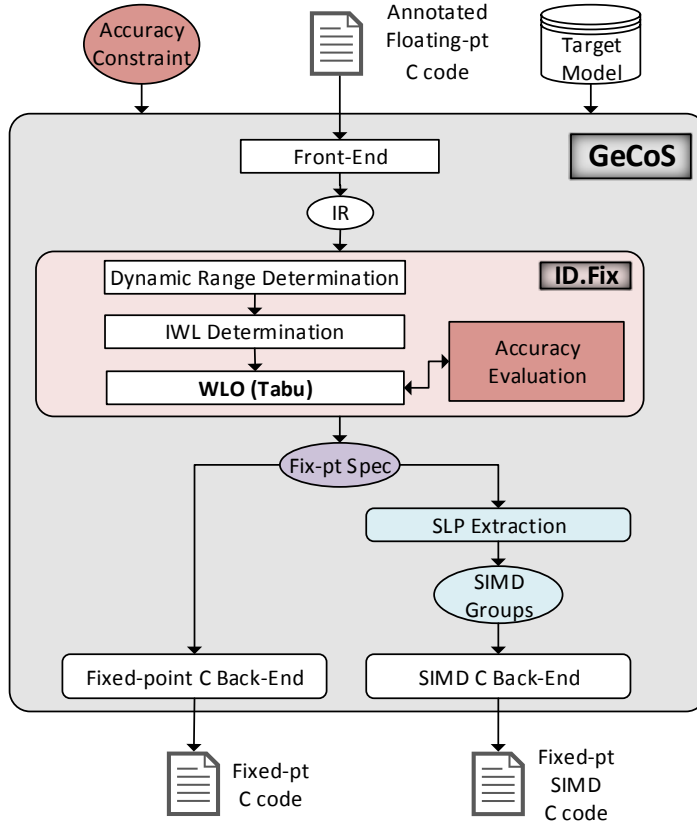


Figure 5.11 – WLO-then-SLP source-to-source compilation flow diagram.

### 5.5.3 Benchmarks

A 64-tap FIR, a 10th order IIR filters and a 3x3 image convolution (CONV) are used as benchmarks. The single-precision floating-point C code of each benchmark respects all the constraints of IDFIX, discussed in section 2.6.2. It is annotated with `pragmas`, mainly in order to specify the dynamic range interval of the inputs and to determine the basic block to be considered for SLP extraction.

The benchmarks description is summarized in table 5.1. The innermost loop in FIR and IIR

App	Description
FIR	64-tap FIR filter, samples size 1x1024
IIR	10th order IIR filter, samples size 1x1024
CONV	3x3 image convolution, sample image size 32x32

Table 5.1 – Benchmarks

is partially unrolled by a factor of four to expose SLP, whereas the convolution kernel (3x3), CONV, is fully unrolled. The input samples, of size 1024 for FIR and IIR and 32x32 for CONV, are normalized to [0, 1].

The main application used to invoke a benchmark function, allocates and initializes the necessary variable. Then it starts the execution cycles counter, depending on the target processor, just before invoking the benchmark function. It stops the counter right after the function returns and then it writes the output into a file.

#### 5.5.4 Target Processors

In the context of the ALMA project, we target two embedded processors, XENTIUM and KAHHRISMA. In addition, we also consider two other processors, ST240 and VEX, in order to test the validity of our approach. None of these target compilers provide automatic [Simdization](#) support.

XENTIUM [104] is a low energy consumption 32-bit 12-issue wide Very Long Instruction Word (VLIW) DSP core from RECORE SYSTEMS. It has ten functional units, six of which can perform integer arithmetic and logic operations, two can perform multiply operations and two can perform load/store operations. XENTIUM supports 2x16-bit SIMD operations. It has four 8 32-bit and one 16 32-bit register files, each of which has two read and two write ports. The model we use to represent XENTIUM is provided in table A.1.

KAHRISMA [58] is a heterogeneous, dynamically reconfigurable, multi-core research architecture developed by the [KARLSRUHE INSTITUTE OF TECHNOLOGY \(KIT\)](#). In this work we use its 2-issue width single [Very Long Instruction Word \(VLIW\)](#) core configuration. It provides support for 4x8-bit and 2x16-bit SIMD integer arithmetic operations. The model we use to represent XENTIUM is provided in table A.3.

ST240 [4] is a 4-issue wide [VLIW](#) media processor from the ST200 family of STMicroelectronics. It has four integer units, 2 multiplication units, 1 branch unit and 1 load/store unit along with a general purpose register file of 64 32-bit registers with 8 read and 4 write ports. ST240 also supports 2x16-bit SIMD operations. The model we use to represent ST240 is provided in table A.2. Besides, ST240 provides hardware support for single-precision floating-point operations but without [SIMD](#) support.

VEX [5] is a parameterizable and extensible [VLIW](#) architecture model. We use it in two configurations; VEX-1 and VEX-4 with an issue width of 1 and 4 respectively. Since VEX does not provide support for [SIMD](#), we implemented a 16-bit and 8-bit [SIMD](#) instruction set extension for supporting integer arithmetic, shift and data manipulation operations, using the provided extension mechanism. The model we use to represent VEX is provided in table A.4.

The main characteristics of these processors are summarized in table 5.2.

#### 5.5.5 Results

In this section we report the experimental results. First, we compare the execution time of fixed-point [SIMD](#) C code obtained by our source-to-source flow, against the original floating-point version. Then, we compare the performance of the solution obtained by our approach



Processor	single-float	1x32-bit int	2x16-bit int	4x8-bit int
XENTIUM	×	✓	✓	×
ST240	✓	✓	✓	×
VEX	×	✓	✓	✓
KAHRISMA	×	✓	✓	✓

Table 5.2 – Target processors supported operations.

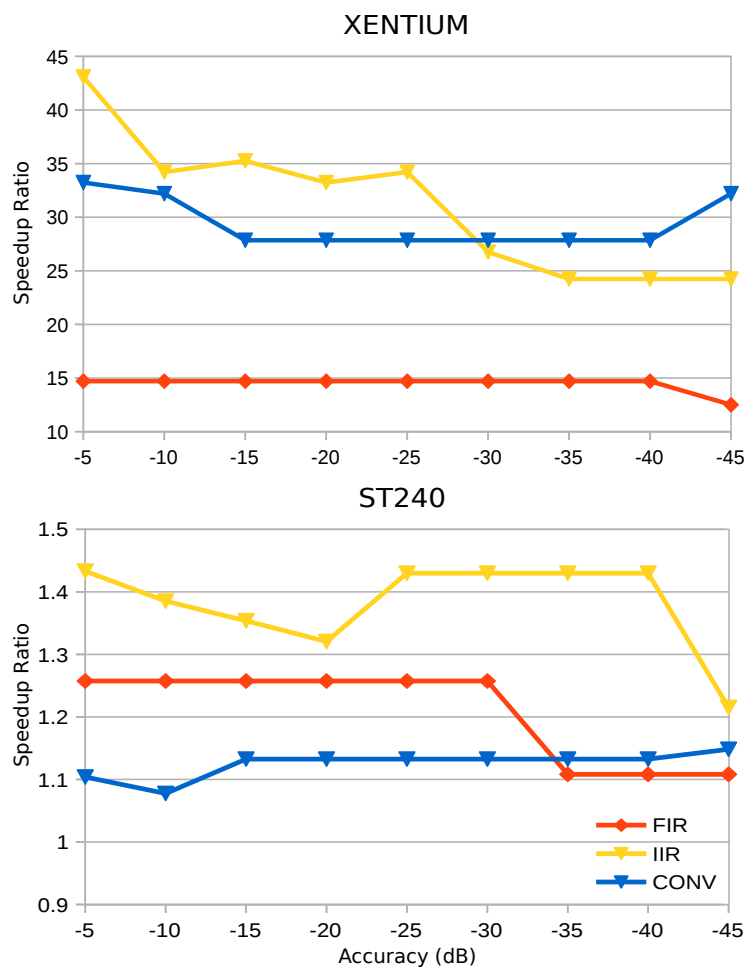


Figure 5.12 – Speedup of **SIMD** code version obtained by **WLO+SLP** flow, over the original **float** version, for different accuracy constraints expressed in dB (higher values (to the left) are less accurate)

(**WLO+SLP**) against a typical approach (**WLO-then-SLP**).

### 5.5.6 Floating-point vs. Fixed-point

In order to compare the performance of the fixed-point implementation (with **SIMD**) against floating-point, we run the fixed-point **SIMD** code obtained by **WLO+SLP** as well as the original single-precision floating-point code (**float**) on both XENTIUM and ST240, for different accuracy constraints. The execution time speedup of the fixed-point **SIMD** (**simd**) over **float** is computed as:

$$\text{speedup} = \text{nb Cycles(float)} / \text{nb Cycles(simd)}$$

The graphics of figure 5.12 plot the obtained speedup on both XENTIUM and ST240, for different accuracy constraints. The latter represents the maximum tolerable quantization noise power at the system output, specified in dB; smaller values represent tighter accuracy constraints (i.e. more accurate).

On XENTIUM, a speedup by a factor of 15 to 45 is achieved. This results are as expected, since this processor does not have a hardware support for floating-point arithmetic. Thus, floating-point support is provided by software emulation.

On ST240, even though it has hardware support for floating-point, a speedup up to 1.4x is obtained. It is mainly due to the exploitation of **SIMD** capabilities.

### 5.5.7 WLO+SLP vs. WLO-then-SLP

In order to compare the performance of our approach (**WLO+SLP**), performing **SLP** extraction and float-to-fixed-point jointly, against a typical approach (**WLO-then-SLP**), we run the test setup presented earlier, for all benchmarks, on each target processor and for different values of the accuracy constraint. For each test we compare the execution time speedup of the fixed-point **SIMD** version obtained by **WLO+SLP** against the one obtained by **WLO-then-SLP**. The speedup is computed against the fixed-point version (without **SIMD**) obtained by **WLO-then-SLP**, called **fixed**, as follows:

$$\text{speedup} = \text{nb Cycles(fixed)} / \text{nb Cycles(simd)}$$

The results are reported in the graphics of figure 5.13.

The overall results clearly show the advantage of our approach across all benchmarks on all processors.

For FIR, we can see our approach trading accuracy for performance improvement. It manages to efficiently exploit **SIMD** to achieve performance improvement (up to 1.6x on KAHRISMA and 1.3x on XENTIUM), whereas **WLO-then-SLP** mostly result in performance degradation after applying **SLP** extraction, illustrating the fact that **WLO** in this case is blindly optimizing without considering the impact of **SLP** on performance.

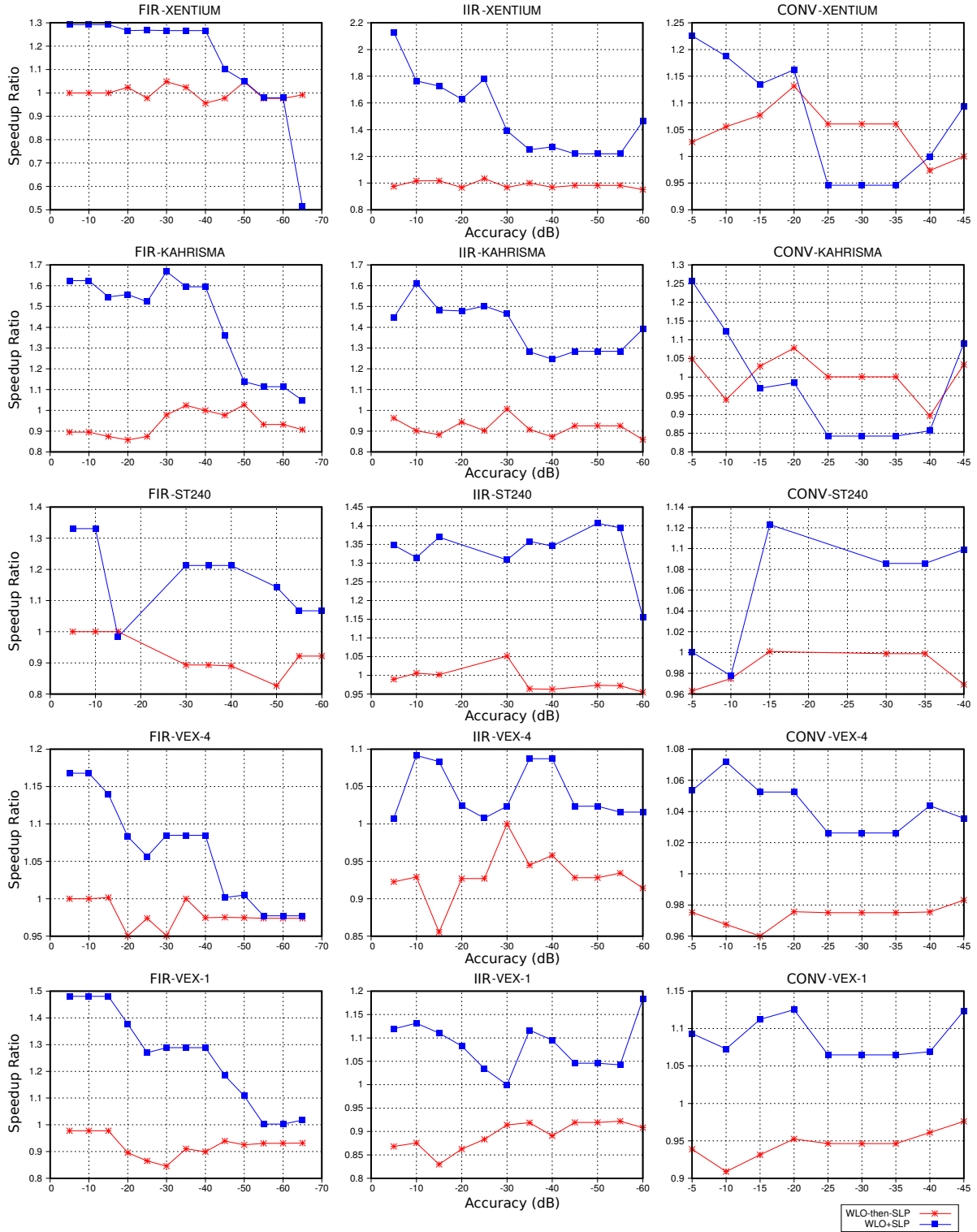


Figure 5.13 – Speedup (higher is better) comparison between SIMD versions of WLO-then-SLP and WLO+SLP vs. accuracy constraint expressed in dB (higher values(to the left) are less accurate). The baseline is the execution time of the (non SIMD fixed-point version of WLO-then-SLP).

The few points where our approach yields performance degradation, for FIR on XENTIUM at -65 db for instance, are due to a reduction in the execution time of the baseline fixed-point version, where the Tabu [WLO](#) algorithm manages to find a better fixed-point solution, since at this high accuracy constraint not many [SLP](#) opportunities are available.

Similarly for IIR, our approach yields consistently better performance improvement on all target processors, up to 2x on XENTIUM, 1.6x on KAHRISMA and 1.4x on ST240. [WLO-then-SLP](#) still mostly result in performance degradation after applying SLP extraction.

For CONV, on XENTIUM and KAHRISMA, a slight slowdown is observed between -25 dB and -40 dB. In this case, the selected [SLP](#) solution has a high packing/unpacking cost compared to the performance gain it achieves, thus inducing a performance degradation. However, a performance estimation of the [SLP](#) grouping solution can be used to discard such solutions, when a performance degradation is detected.

Besides, by comparing the results on VEX-1 and VEX-4<sup>5</sup> we can notice the impact of instruction level parallelism (ILP). On VEX-4, with higher ILP capabilities, the speedup due to [SIMD](#) is less important than on VEX-1.

## 5.6 Conclusion

In this work we discussed the interaction between floating-point to fixed-point conversion and [SLP](#) extraction. We argued that considering both transformations jointly can yield more efficient [SIMD](#) solutions compared to a approach where the floating-point to fixed-point conversion is applied first, followed by [SLP](#) extraction. So, we propose a new [SLP](#)-aware [WLO](#) algorithm capable of efficiently exploit the performance/accuracy tradeoff when targeting embedded processors.

We implemented the proposed, joint floating-point to fixed-point conversion and [SLP](#) extraction approach, as a source-to-source compilation flow in [GecOS](#). We also implement a typical approach in order to test the validity of our approach. For this, we tested both approaches on several embedded processors. The experimental results show the advantage of our approach in exploiting the performance/accuracy tradeoff compared to a typical approach. A speedup by a factor higher than 1.5 is achieved on XENTIUM and KAHRISMA for an IIR benchmark.

In summary, we concluded that:

- Fixed-point is more suitable when targeting embedded processors with no hard-float support: a speedup by a factor of up to 45 is observed on XENTIUM.
- Even on processors with floating-point support, using fixed-point in combination with [SIMD](#) can achieve better performance: a speedup by a factor of up to 1.4 is observed on ST240.
- Using [SIMD](#) does not always improve performance, especially if the [WLO](#) is not aware of the [SIMD](#) opportunities and their associated cost overhead.

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5. VEX-1 and VEX-4 only differ in the issue-width; the former has only 1 and the latter has 4.

- Jointly performing [WLO](#) and [SLP](#) extraction helps achieving more efficient solutions, compared to the typical approach.

## Limitations

The source-to-source compilation flow, we implemented in this work, is currently limited by the analytical accuracy evaluation procedure, which imposes many constraints on the input C code (as explained earlier in section 2.6.2). These constraints limit the coverage of the flow to "simple" applications. However, This limitation can be alleviated by using less constrained accuracy evaluation techniques such as simulation-based or simulation-analytical mixed approaches, for instance.

On the other hand, the proposed source-to-source compilation flow does not integrate common optimizations, such as constant propagation. In fact, the [WLO](#) and [SLP](#) extraction are performed on the original code without such pre-optimizations. Therefore, the generated C code, which uses [SIMD](#) intrinsics, seems to be preventing the target compiler from being as efficient in optimizing this code compared to the original C code with no [SIMD](#) intrinsics. This makes it very hard to fairly compare the performance between the generated [SIMD](#) code and the original one. This can be addressed either by integrating such optimization to the source-to-source flow and applying them prior to the [WLO](#) and [SLP](#) extraction.

## Chapter 6

# Conclusion

In this manuscript, we discussed the impact of two important code transformations when targeting low power embedded processors, namely, floating-point to fixed-point conversion and [Superword Level Parallelism \(SLP\)](#) extraction. This work was inducted in the context of the ALMA project, which aimed at providing a complete toolflow to target embedded multi-core architectures, starting from SCILAB or MATLAB down to parallel C code. Among other optimizations, floating-point to fixed-point conversion and [Simdization](#) are performed to improve performance of an application when targeting embedded processors. Especially, since ALMA target processors do not provide support for floating-point arithmetic.

Despite the fact that many embedded processors provide hardware support for floating-point arithmetic, a good number of ultra low power embedded processors, such as ARM cortex-M0/1/3, [TEXAS INSTRUMENTS \(TI\)](#) TMS320 C64x and RECORE SYSTEMS's XENTIUM, do not. This makes floating-point to fixed-point conversion a crucial optimization when targeting such processors. Specially when most application prototyping employs floating-point arithmetic. The results shown in chapter 5, reinforces this fact, since they show a speedup of up to 45x when converting floating-point to fixed-point in the case the target processor does not have hardware support for floating-point arithmetic. On the other hand, most of such embedded processors provide support for vector operations through subword [Single Instruction Multiple Data \(SIMD\)](#) instructions. These [SIMD](#) capabilities can be efficiently exploited using [SLP](#) extraction methodologies.

In chapter 4, we discussed the state-of-the-art of [SLP](#) extraction algorithms. We then proposed a new [Intermediate Representation \(IR\)](#), called [Pack Flow and Conflict Graph \(PFCG\)](#), for [SLP](#) extraction together with an improved [SIMD](#) group selection method, which we implemented as a source-to-source compilation flow. Experimental results showed a significant performance improvement (up to 50%) of the obtained [SLP](#) solution, by using our proposed method compared to a state-of-the-art [SLP](#) extraction algorithm (which we also implemented as a source-to-source compilation flow), without the need for data layout transformations. The proposed [IR](#) helps to speedup the [SIMD](#) group candidate benefit estimation and consequently reduces the complexity of the [SIMD](#) group selection algorithm. In addition, we proposed a way to control the size of

the [PFCG](#) by splitting the operations into batches. Experimental results showed that this can be used to reduce the group selection time, while still achieving good [SLP](#) solutions.

By this point, we have at our disposal a complete source-to-source flow capable of automatically generating a [SIMD](#) C code for different embedded processors. In the next chapter, we discuss the interaction between floating-point to fixed-point conversion and [SLP](#) extraction. We show that, existing approaches considering both transformations independently, yields less efficient solutions. We argue that considering [SLP](#) extraction in conjunction with [Word Length Optimization \(WLO\)](#) helps achieving better results. So, we propose a new [SLP](#)-aware [WLO](#) algorithm, which we integrate into the source-to-source compilation flow that we implemented.

However, exploiting [SLP](#) in a floating-point application, when targeting embedded processors with no support for floating-point, is not possible. In this case no [SLP](#) is available since the target does not provide a floating-point [SIMD](#) instruction set. In this case, in addition to its aforementioned positive impact on performance, floating-point to fixed-point conversion can additionally "unlock" [SLP](#) opportunities. In fact, during the [WLO](#) step in floating-point to fixed-point conversion, smaller data word-lengths can be selected for the cost of degrading the computation accuracy. But, selecting smaller word-lengths can increase the amount of potential [SLP](#) opportunities.

In chapter 5, we showed that existing methods use this observation to improve performance using [SIMD](#). However, they do not consider [Simdization](#) during [WLO](#). In other words, they perform floating-point to fixed-point conversion first, and later they can independently perform [Simdization](#). In chapter 5, we show that such methodologies are not efficient in exploiting [SLP](#) opportunities. We argued that [WLO](#) and [SLP](#) extraction are inter-dependent, thus they should be applied jointly to achieve better results. So, we proposed a new methodology for joint [WLO](#) and [SLP](#) extraction and we implemented it in our source-to-source compilation flow. To demonstrate the validity of our approach we also implemented a compilation flow performing a typical approach, that converts floating-point to fixed-point first, and then apply [SLP](#) extraction independently. Experimental results comparing both approaches on a variety of embedded processors, showed that our methodology can achieve more efficient [SIMD](#) solutions.

## Perspectives

In the work presented in chapter 4, we ignore the memory alignment constraints during [SIMD](#) group selection; we assume that all contiguous array reference superwords are aligned. When such superword is not actually aligned, it induces a cost penalty, especially if the target does not support unaligned memory accesses. This problem can be addressed by integrating a memory access alignment analysis to the compilation flow, based on which we can then modify the [SIMD](#) candidate benefit estimation to take the alignment cost overhead into account. Besides, optimization of the memory layout, such as array padding combined with some loop transformations, such as loop peeling, register level tiling with index set splitting, can also be used to reduce the amount of unaligned memory accesses. This is worth considering in a future work

to improve the performance of the proposed source-to-source flow. Also, the performance of SLP solutions can be improved by considering inter basic-block and inter-procedural analysis to reduce packing/unpacking overhead by capturing superwords reuse across basic blocks.

In addition, in this work we use a very basic SIMD instruction selection method and we only consider "simple" SIMD operations (add, sub, mul,...). However, many embedded processors (Digital Signal Processors (DSPs)), such as XENTIUM and ST240, provide multiple "complex" SIMD operations, such as *muladd*. Considering such SIMD operations can help achieving better performance. This could be considered during SLP extraction phase, by allowing the construction of "complex" SIMD group candidates to represent the aforementioned operations. Alternatively, this can be performed after SLP extraction by using a more complex SIMD instruction selection capable of detecting such operations patterns.

In this work, we mainly targeted embedded processors with *subword* SIMD support. We believe that such limited SIMD support would continue to be used in ultra low power embedded processors, since it comes for almost no extra cost, by simply partitioning the existing data-path. However, with the advances of computer architectures and manufacturing technologies, *superword* SIMD extensions, would be supported by more embedded processors. These extensions support wider SIMD vector sizes, which is expected to keep increasing. For instance, some ARM processors support 128-bit SIMD operations via the NEON extension. Therefore, it would be interesting to see how the proposed SLP extraction method performs when targeting such processors with wider SIMD data-path.

Besides, ARM processors, for instance, also support half-precision floating-point SIMD. In this context, a performance/accuracy exploration for different floating-point precisions can be achieved using a similar approach as the one we proposed in chapter 5. In fact, our approach can be easily adapted to perform joint SLP extraction and floating-point precision selection, under accuracy constraint. This would require a floating-point implementation accuracy evaluation; simulation-based methods can be used as a straightforward solution to provide this service.





## Appendix A

# Target Processor Models

In this appendix we present the models we use in this thesis work to represent the target processors. The model is defined in section 5.3.2.

### A.1 XENTIUM

The model we use to represent the XENTIUM processor is summarized in table A.1.

<b>T</b>	<b>WS</b>	<b>N</b>	<b>PM</b>	<b>QM</b>	<b>OM</b>	<b>S</b>	
add	(32, 32, 32)	1	LSB	Trunc	Wrap	(0, 0, 0)	
add	(32, 32, 32)	1	LSB	Trunc	SAT	(0, 0, 0)	
add	(16, 16, 16)	2	LSB	Trunc	Wrap	(0, 0, 0)	
add	(16, 16, 16)	2	MSB	Trunc	Wrap	(0, 0, 1)	
add	(16, 16, 16)	2	MSB	Round	Wrap	(0, 0, 1)	
sub	(32, 32, 32)	1	LSB	Trunc	Wrap	(0, 0, 0)	
sub	(32, 32, 32)	1	LSB	Trunc	SAT	(0, 0, 0)	
sub	(16, 16, 16)	2	LSB	Trunc	Wrap	(0, 0, 0)	
sub	(16, 16, 16)	2	MSB	Trunc	Wrap	(0, 0, 1)	
mul	(32, 32, 64)	1	FULL	-	-	(0, 0, 0)	
mul	(16, 16, 32)	2	FULL	-	-	(0, 0, 0)	

Table A.1 – XENTIUM Model.

### A.2 ST240

The model we use to represent the ST240 processor is summarized in table A.2.

<b>T</b>	<b>WS</b>	<b>N</b>	<b>PM</b>	<b>QM</b>	<b>OM</b>	<b>S</b>	
add	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
add	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
sub	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
sub	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
mul	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
mul	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	

Table A.2 – ST240 Model.

### A.3 KAHRISMA

The model we use to represent the KAHRISMA processor is summarized in table A.3.

<b>T</b>	<b>WS</b>	<b>N</b>	<b>PM</b>	<b>QM</b>	<b>OM</b>	<b>S</b>	
add	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
add	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
add	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	
sub	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
sub	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
sub	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	
mul	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
mul	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
mul	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	

Table A.3 – KAHRISMA Model.

### A.4 VEX

The model we use to represent the VEX processor is summarized in table A.4. We implement the [SIMD](#) instruction set as an extension to the [Instruction Set Architecture \(ISA\)](#).

<b>T</b>	<b>WS</b>	<b>N</b>	<b>PM</b>	<b>QM</b>	<b>OM</b>	<b>S</b>	
add	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
add	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
add	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	
sub	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
sub	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
sub	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	
mul	(32,32,32)	1	LSB	Trunc	Wrap	(0,0,0)	
mul	(16,16,16)	2	LSB	Trunc	Wrap	(0,0,0)	
mul	(8,8,8)	4	LSB	Trunc	Wrap	(0,0,0)	

Table A.4 – VEX Model.



# Publications

- [EMD17] A. H. EL MOUSSAWI et S. DERRIEN, “Superword level parallelism aware word length optimization”, in *2017 Design, Automation Test in Europe Conference Exhibition (DATE)*, 2017.
- [EDEM16] N. ESTIBALS, G. DEEST, A. H. EL MOUSSAWI et S. DERRIEN, “System level synthesis for virtual memory enabled hardware threads”, in *2016 Design, Automation Test in Europe Conference Exhibition (DATE)*, p. 738–743, March 2016.
- [EMD16] A. H. EL MOUSSAWI et S. DERRIEN, “Demo: Slp-aware word length optimization”. DASIP, 2016.
- [FYEM<sup>+</sup>13] A. FLOC’H, T. YUKI, A. H. EL MOUSSAWI, A. MORVAN, K. MARTIN, M. NAULLET, M. ALLE, L. L’HOURS, N. SIMON, S. DERRIEN *et coll.*, “Gecos: A framework for prototyping custom hardware design flows”, in *Source Code Analysis and Manipulation (SCAM), 2013 IEEE 13th International Working Conference on*, p. 100–105, Sept 2013.
- [GVA<sup>+</sup>13] G. GOULAS, C. VALOUXIS, P. ALEFRAGIS, N. S. VOROS, C. GOGOS, O. OEY, T. STRIPF, T. BRUCKSCHLOEGL, J. BECKER, A. H. EL MOUSSAWI, M. NAULLET et T. YUKI, “Coarse-grain optimization and code generation for embedded multicore systems”, in *Digital System Design (DSD), 2013 Euromicro Conference on*, p. 379–386, Sept 2013.



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## Résumé

Afin de limiter leur coût et/ou leur consommation électrique, certains processeurs embarqués sacrifient le support matériel de l'arithmétique à virgule flottante. Pourtant, pour des raisons de simplicité, les applications sont généralement spécifiées en utilisant l'arithmétique à virgule flottante.

Porter ces applications sur des processeurs embarqués de ce genre nécessite une émulation logicielle de l'arithmétique à virgule flottante, qui peut sévèrement dégrader la performance. Pour éviter cela, l'application est convertie pour utiliser l'arithmétique à virgule fixe, qui a l'avantage d'être plus efficace à implémenter sur des unités de calcul entier. La conversion de virgule flottante en virgule fixe est une procédure délicate qui implique des compromis subtils entre performance et précision de calcul. Elle permet, entre autre, de réduire la taille des données pour le coût de dégrader la précision de calcul.

Par ailleurs, la plupart de ces processeurs fournissent un support pour le calcul vectoriel de type SIMD (*Single Instruction Multiple Data*) afin d'améliorer la performance. En effet, cela permet l'exécution d'une opération sur plusieurs données en parallèle, réduisant ainsi le temps d'exécution. Cependant, il est généralement nécessaire de transformer l'application pour exploiter les unités de calcul vectoriel. Cette transformation de vectorisation est sensible à la taille des données ; plus leurs tailles diminuent, plus le taux de vectorisation augmente. Il apparaît donc un compromis entre vectorisation et précision de calcul.

Plusieurs travaux ont proposé des méthodologies permettant, d'une part la conversion automatique de virgule flottante en virgule fixe, et d'autre part la vectorisation automatique. Dans l'état de l'art, ces deux transformations sont considérées indépendamment, pourtant elles sont fortement liées.

Dans ce contexte, nous étudions la relation entre ces deux transformations, dans le but d'exploiter efficacement le compromis entre performance et précision de calcul. Ainsi, nous proposons d'abord un algorithme amélioré pour l'extraction de parallélisme SLP (*Superword Level Parallelism* ; une technique de vectorisation). Puis, nous proposons une nouvelle méthodologie permettant l'application conjointe de la conversion de virgule flottante en virgule fixe et de l'exploitation du SLP. Enfin, nous implémentons cette approche sous forme d'un flot de compilation source-à-source complètement automatisé, afin de valider ces travaux. Les résultats montrent l'efficacité de cette approche, dans l'exploitation du compromis entre performance et précision, vis-à-vis d'une approche classique considérant ces deux transformations indépendamment.

## Abstract

In order to cut-down their cost and/or their power consumption, many embedded processors do not provide hardware support for floating-point arithmetic. However, applications in many domains, such as signal processing, are generally specified using floating-point arithmetic for the sake of simplicity.

Porting these applications on such embedded processors requires a software emulation of floating-point arithmetic, which can greatly degrade performance. To avoid this, the application is converted to use fixed-point arithmetic instead. Floating-point to fixed-point conversion involves a subtle tradeoff between performance and precision ; it enables the use of narrower data word lengths at the cost of degrading the computation accuracy.

Besides, most embedded processors provide support for SIMD (Single Instruction Multiple Data) as a mean to improve performance. In fact, this allows the execution of one operation on multiple data in parallel, thus ultimately reducing the execution time. However, the application should usually be transformed in order to take advantage of the SIMD instruction set. This transformation, known as Simdization, is affected by the data word lengths ; narrower word-lengths enable a higher SIMD parallelism rate. Hence the tradeoff between precision and Simdization.

Many existing work aimed at providing/improving methodologies for automatic floating-point to fixed-point conversion on the one side, and Simdization on the other. In the state-of-the-art, both transformations are considered separately even though they are strongly related.

In this context, we study the interactions between these transformations in order to better exploit the performance/accuracy tradeoff. First, we propose an improved SLP (Superword Level Parallelism) extraction (an Simdization technique) algorithm. Then, we propose a new methodology to jointly perform floating-point to fixed-point conversion and SLP extraction. Finally, we implement this work as a fully automated source-to-source compiler flow. Experimental results, targeting four different embedded processors, show the validity of our approach in efficiently exploiting the performance/accuracy tradeoff compared to a typical approach, which considers both transformations independently.

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