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# Quantitative material decomposition methods for X-ray spectral CT

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**Quantitative material decomposition  
methods for X-ray spectral CT**

**Méthodes de décomposition quantitative des  
matériaux pour la tomographie spectrale aux  
rayons X**

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Finally, I would like to dedicate this thesis to my dear mother in heaven. You were a big part of my life and made me who I am today. I will miss you and love you as always.



## Abstract

X-ray computed tomography (X-ray CT) plays an important part in non-invasive imaging since its introduction. During the past few years, numerous technological advances in X-ray CT have been observed, including spectral CT, which uses photon counting detectors (PCDs) to discriminate transmitted photons corresponding to selected energy bins in order to obtain spectral information with one single acquisition.

Spectral CT enables us to overcome many limitations of the conventional CT techniques and opens up many new application possibilities, among which quantitative material decomposition is the hottest topic. A number of material decomposition methods have been reported and different experimental systems are under development for spectral CT. According to the type of data on which the decomposition step operates, we have projection domain method (decomposition before reconstruction) and image domain method (decomposition after reconstruction).

The commonly used decomposition is based on least square criterion, named proj-LS and ima-LS method. However, the inverse problem of material decomposition is usually ill-posed and the X-ray spectral CT measurements suffer from Poisson photon counting noise. The standard LS criterion can lead to overfitting to the noisy measurement data. In the present work, we have proposed a least log-squares criterion for projection domain method to minimize the errors on linear attenuation coefficient: proj-LLS method. Furthermore, to reduce the effect of noise and enforce smoothness, we have proposed to add a patchwise regularization term to penalize the sum of the square variations within each patch for both projection domain and image domain decomposition, named proj-PR-LLS and ima-PR-LS method.

The performances of the different methods were evaluated by spectral CT simulation studies with specific phantoms for different applications: (1) Medical application: iodine and calcium identification. The decomposition results of the proposed methods show that calcium and iodine can be well separated and quantified from soft tissues. (2) Industrial application: ABS-flame retardants (FR) plastic sorting. Results show that 3 kinds of ABS materials with different flame retardants can be separated when the sample thickness is favorable.

Meanwhile, we simulated spectral CT imaging with a PMMA phantom filled with Fe, Ca and K solutions. Different acquisition parameters, i.e. exposure factor and number of energy bins were simulated to investigate their influence on the performance of the proposed methods for iron determination.

**Keywords:** Computed tomography, X-ray, Spectral CT, Photon counting detector, material decomposition, simulation



## Résumé

La tomographie (CT) aux rayons X joue un rôle important dans l'imagerie non invasive depuis son introduction. Au cours des dernières années, de nombreuses avancées technologiques en tomographie par rayons X ont été observées, notamment la CT spectrale, qui utilise un détecteur à comptage de photons (PCD) pour discriminer les photons transmis correspondant à des bandes d'énergie sélectionnées afin d'obtenir une information spectrale.

La CT spectrale permet de surmonter de nombreuses limitations des techniques précédentes et ouvre de nombreuses applications nouvelles, parmi lesquelles la décomposition quantitative des matériaux est le sujet le plus étudié. Un certain nombre de méthodes de décomposition des matériaux ont été rapportées et différents systèmes expérimentaux sont en cours de développement pour la CT spectrale. Selon le type de données sur lequel l'étape de décomposition fonctionne, nous avons les méthodes du domaine des projections (décomposition avant reconstruction) et les méthodes du domaine de l'image reconstruite (décomposition après reconstruction).

La décomposition couramment utilisée est basée sur le critère des moindres carrés, nommée proj-LS et méthode ima-LS. Cependant, le problème inverse de la décomposition du matériau est généralement mal posé et les mesures du CT spectral aux rayons X souffrent de bruits de comptage de photons de Poisson. Le critère des moindres carrés peut conduire à un surajustement des données de mesure bruitées. Dans le présent travail, nous avons proposé un critère de moindre log-carré pour la méthode du domaine de projection afin de minimiser les erreurs sur le coefficient d'atténuation linéaire : méthode proj-LLS. De plus, pour réduire l'effet du bruit et lisser les images, nous avons proposé d'ajouter un terme de régularisation par patch pour pénaliser la somme des variations au carré dans chaque zone pour les décompositions des deux domaines, nommées proj-PR-LLS et ima-PR-LS méthode.

Les performances des différentes méthodes ont été évaluées par des études de simulation avec des fantômes spécifiques pour différentes applications : (1) Application médicale : identification de l'iode et du calcium. Les résultats de la décomposition des méthodes proposées montrent que le calcium et l'iode peuvent être bien séparés et quantifiés par rapport aux tissus mous. (2) Application industrielle : tri des plastiques avec ou sans retardateur de flamme. Les résultats montrent que 3 types de matériaux ABS avec différents retardateurs de flamme peuvent être séparés lorsque l'épaisseur de l'échantillon est favorable.

Enfin, nous avons simulé l'imagerie par CT spectrale avec un fantôme de PMMA rempli de solutions de Fe, Ca et K. Différents paramètres d'acquisition, c'est-à-dire le facteur d'exposition et le nombre de bandes d'énergie, ont été simulés pour étudier leur influence sur la performance de décomposition pour la détermination du fer.

**Keywords :** Tomographie, Rayons X, CT spectrale, Détecteur à comptage de photons, Décomposition de matériaux, Simulation

# Résumé étendu

## 1 Introduction

La tomographie (CT - computed tomography) aux rayons X est introduite pour la première fois dans les années 1970 par Cormack et Hounsfield, pour laquelle ils ont reçu le prix Nobel de physiologie ou de médecine en 1979. Cette invention a montré la possibilité de donner des images en coupe de haute qualité avec des mesures multi-angles et des calculs mathématiques complexes. La Figure 1 montre la mécanique de l'imagerie CT, dont les composants de base sont la source de rayons X, l'objet et le détecteur. Par la suite, l'avancement de la CT aux rayons X a grandement bénéficié des algorithmes de reconstruction développés, de la technologie informatique avancée et des améliorations technologiques des sources et détecteurs. Il y a maintenant de nombreuses applications dans les domaines médical, industriel, caractérisation des matériaux, aérospatial et géologique.

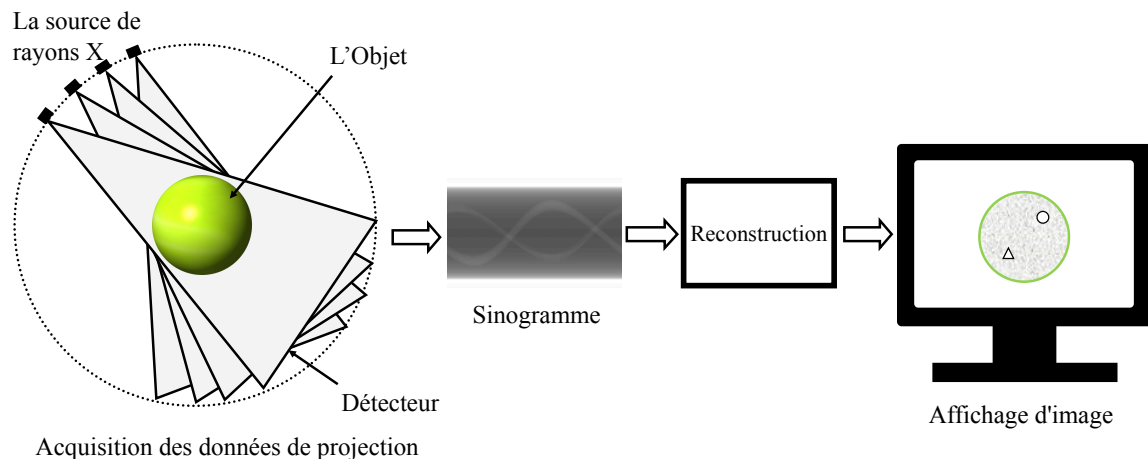


Figure 1: Schéma de l'imagerie CT: l'image en coupe transversale est reconstruite à partir de données de projection mesurées à partir d'angles multiples..

Les sources de rayons X utilisées actuellement sont constituées d'un spectre d'énergies.

Cependant, les détecteurs conventionnels en mode intégration d'énergie donnent un signal proportionnel à l'énergie totale absorbée. Ainsi, le signal regroupe toutes les informations d'énergie en donnant proportionnellement moins de poids aux photons de plus faible énergie que les photons d'énergie plus élevée (Figure 2 (a)).

Le concept de CT résolue en énergie a été discuté depuis l'invention de la CT. Dans la publication référence [Hounsfield, 1973] de Hounsfield, il a déjà été proposé de prendre des mesures de la même tranche d'un matériau à deux tensions différentes afin de déterminer le numéro atomique des matériaux. En 1976, Alvarez et Macovski ont proposé d'extraire l'information dépendant de l'énergie en représentant l'atténuation totale avec des fonctions correspondant à l'effet photoélectrique et Compton, et les parties indépendantes de l'énergie des deux effets ont ensuite été reconstruites respectivement [Alvarez and Macovski, 1976]. En 1977, Riederer et al. ont présenté leur travail d'imagerie sélective de l'iode par CT en utilisant trois faisceaux de rayons X fortement filtrés [Riederer and Mistretta, 1977]. L'imagerie sélective des matériaux utilisant la CT à bi-énergie (DECT dual energy computed tomography) s'étend également à l'imagerie radiographique aux rayons X [Brody et al., 1981, Lehmann et al., 1981] désormais couramment utilisée dans les systèmes de contrôle de bagages dans les aéroports.

Suivant le concept ci-dessus, une variété de systèmes DECT a été construite pour l'imagerie à résolution d'énergie. Il existe actuellement trois techniques principales pour réaliser la DECT. Le premier est appelé technique de commutation rapide des kilovolts, où la tension du tube à rayons X est rapidement commutée pour produire deux faisceaux de rayons X avec des énergies différentes pour balayer toutes les autres projections pendant toute la durée du balayage. Son principe est représenté sur la Figure 2 (b). Le second est une technique CT à double source dans laquelle deux tubes à rayons X et deux détecteurs correspondants sont équipés dans le système pour acquérir simultanément deux ensembles de données pour la même tranche de l'objet. Ces deux techniques utilisent toutes deux des spectres de rayons X différents et leurs principes sont représentés sur la Figure 2 (b). La troisième est une technique de détection à double couche (détecteur sandwich), qui utilise encore un détecteur intégrant l'énergie, mais deux ensembles de réseaux de scintillateurs et de photodiodes empilés les uns sur les autres, de sorte que les photons de basse énergie sont absorbés par le réseau scintillateur supérieur, tandis que les photons de plus haute énergie traversent la couche supérieure et sont absorbés par le réseau de scintillateurs du dessous [Nasirudin, 2015], voir la Figure 2 (c).

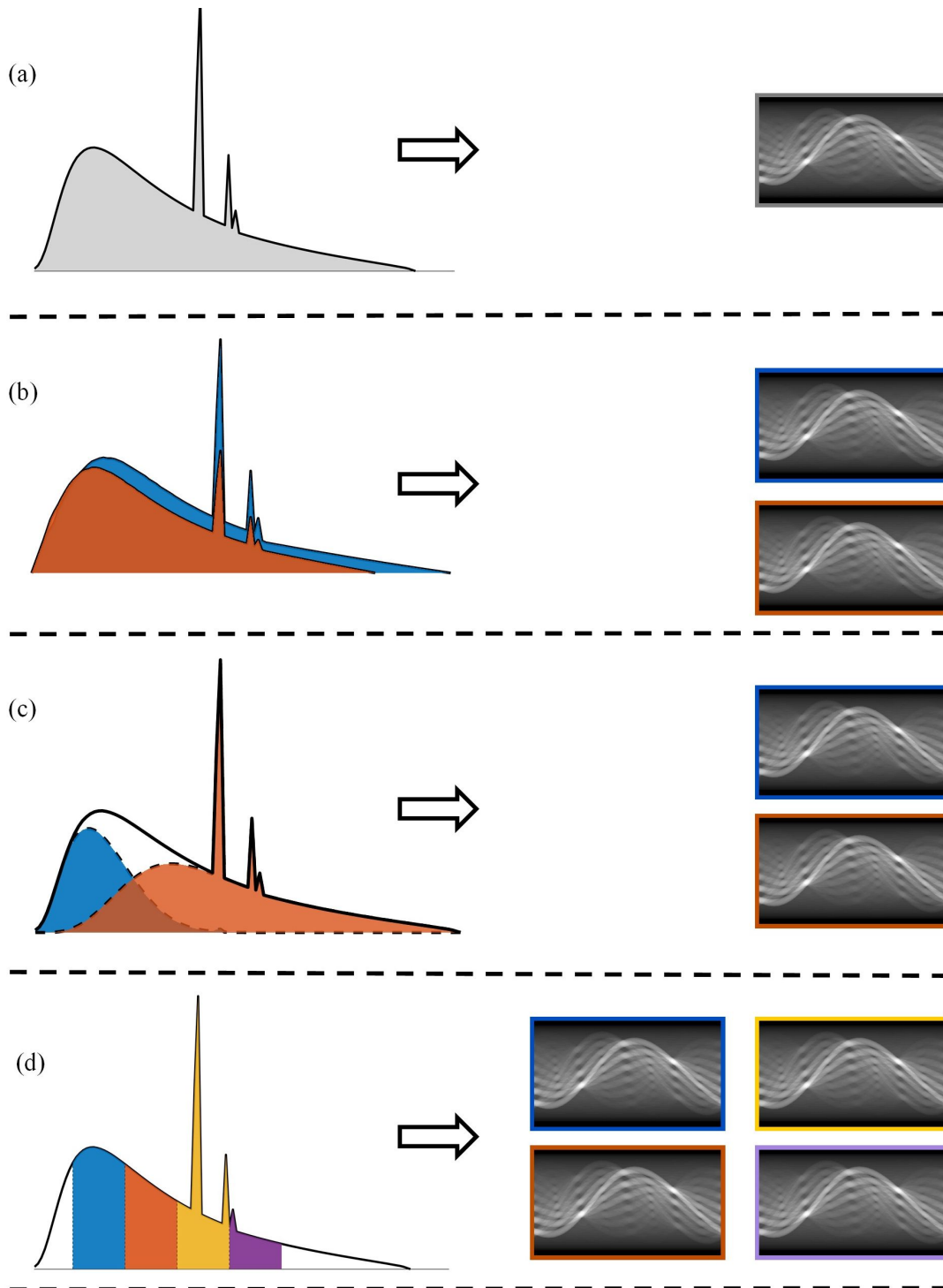


Figure 2: Illustration de l'acquisition de données à partir de différents systèmes CT: système CT classique où les détecteurs intégrateurs acquièrent un seul sinogramme (a); DECT utilisant une technique de commutation rapide des kilovolts ou une technique à double source (b), ou une technique de détection à double couche (c) pour obtenir deux ensembles de données de projection; Le système de CT spectrale (d) avec un détecteur de comptage de photons qui acquiert plusieurs ensembles de données de bandes d'énergie sélectionnées.

A la différence de la DECT, la CT spectrale emploie un détecteur à comptage de photons (PCD photon counting detector) qui est capable d'obtenir des informations spectrales de plusieurs bandes d'énergie avec une seule acquisition, Figure 2 (d). La CT spectrale permet de surmonter de nombreuses limitations des techniques précédentes et ouvre de nombreuses nouvelles applications. La décomposition quantitative des matériaux est le sujet le plus étudié, y compris l'imagerie K-edge pour des matériaux de contraste et l'imagerie sélective d'autres matériaux auparavant indiscernables. D'autres applications incluent la pondération énergétique et l'imagerie monochromatique virtuelle pour améliorer la qualité de l'image.

Dans le présent travail, nous nous concentrons sur l'application de la décomposition quantitative des matériaux par CT spectrale. Un certain nombre de méthodes de décomposition des matériaux ont été rapportées et différents systèmes expérimentaux sont en cours de développement pour la CT spectrale. Cependant, la plupart des recherches se concentrent sur l'imagerie des agents de contraste avec des numéros atomiques élevés ( $Z$ ), tels que l'iode, le gadolinium et l'or, qui ont des raies K uniques dans la gamme d'énergie de détection. Il est très difficile de distinguer les éléments qui ont de faibles numéros atomiques, surtout quand leurs nombres  $Z$  sont proches. Dans cette phase primaire des systèmes expérimentaux, il est difficile d'obtenir les données brutes pour le traitement de la recherche. La simulation est un moyen efficace, rentable et réalisable de résoudre ce problème. Par conséquent, la thèse se concentre autour de trois aspects: (1) l'étude des méthodes de décomposition en matériaux pour la CT spectrale; (2) la validation et l'évaluation des méthodes proposées par simulation d'applications médicale et industrielle; (3) l'étude de l'influence de différents paramètres d'acquisition, c'est-à-dire le facteur d'exposition et le nombre de bandes d'énergie, sur les performances de décomposition.

La thèse s'organise comme suit:

Dans le Chapitre 2, intitulé "General principles of spectral CT", les principes des interactions des rayons X avec la matière sont introduits, y compris l'absorption photoélectrique, la diffusion Compton et la production de paires; Les principes de la CT par rayons X sont présentés, en ce qui concerne la CT conventionnelle, la CT à double énergie et la CT spectrale.

Dans le Chapitre 3, intitulé "Material decomposition methods", une revue des méthodes de décomposition en matériaux existantes pour la CT spectrale est présentée. Sur la base des méthodes existantes, nous avons proposé des méthodes de décomposition régularisées en zones (patch) dans le domaine des projections et dans le domaine de l'image reconstruite.

Dans le Chapitre 4, intitulé "Material decomposition results for different applications: phantoms study", la procédure de simulation d'imagerie spectrale aux rayons X est détaillée et les résultats de la décomposition par les méthodes proposées est démontrée par une étude

d'un fantôme pour une application médicale et un 'autre pour une application industrielle.

Dans le Chapitre 5, intitulé "Exploring the influence of different acquisition parameters", plusieurs séries d'acquisitions de CT spectrale ont été simulées avec différents paramètres et l'influence de ces paramètres sur la performance de décomposition des méthodes proposées est étudiée.

Dans le Chapitre 6, intitulé "Conclusion and perspectives", un bref résumé des principaux résultats et perspectives d'avenir est présenté.

## 2 Méthodes de décomposition en matériaux

Selon la formulation de la décomposition en matériaux, les méthodes de décomposition existantes peuvent être divisées en deux catégories. La première est la décomposition basée sur l'effet physique, également appelée imagerie K-edge, où l'atténuation est considérée comme une combinaison linéaire de l'effet photoélectrique, de l'effet Compton et des composants K-edge s'il y a des matériaux dont le saut d'absorption K est compris dans la gamme d'énergie du détecteur de CT. La deuxième est la méthode basée sur les matériaux, notre travail était autour de celle-ci, où le coefficient d'atténuation linéique est décrit comme les contributions d'une base de matériaux. Ensuite, selon le type de données sur lequel l'étape de décomposition fonctionne, les méthodes peuvent également être divisées en méthodes fonctionnant dans le domaine des projections (sinogramme ou projection radiographique) ou bien dans le domaine de l'image reconstruite (coupe 2D ou volume 3D). Le premier type, également appelé méthode de pré-reconstruction, décompose les données de projection en plusieurs composants désirés (i.e. base des matériaux), puis applique une reconstruction indépendante à chaque composant pour obtenir leur distribution respective dans l'espace. Le deuxième type, également connu sous le nom de méthode de post-reconstruction, fonctionne sur des images CT reconstruites de manière conventionnelle correspondant aux différentes bandes d'énergie acquises pour obtenir la concentration de matériaux cibles en utilisant une inversion de matrice linéaire, voir la Figure 3. Les deux méthodes ont leurs avantages et leurs inconvénients, en fonction de différentes situations. Dans la suite, ces deux méthodes seront dénommées "projection" ou "image" et repérées par le préfixe "proj" ou "ima".

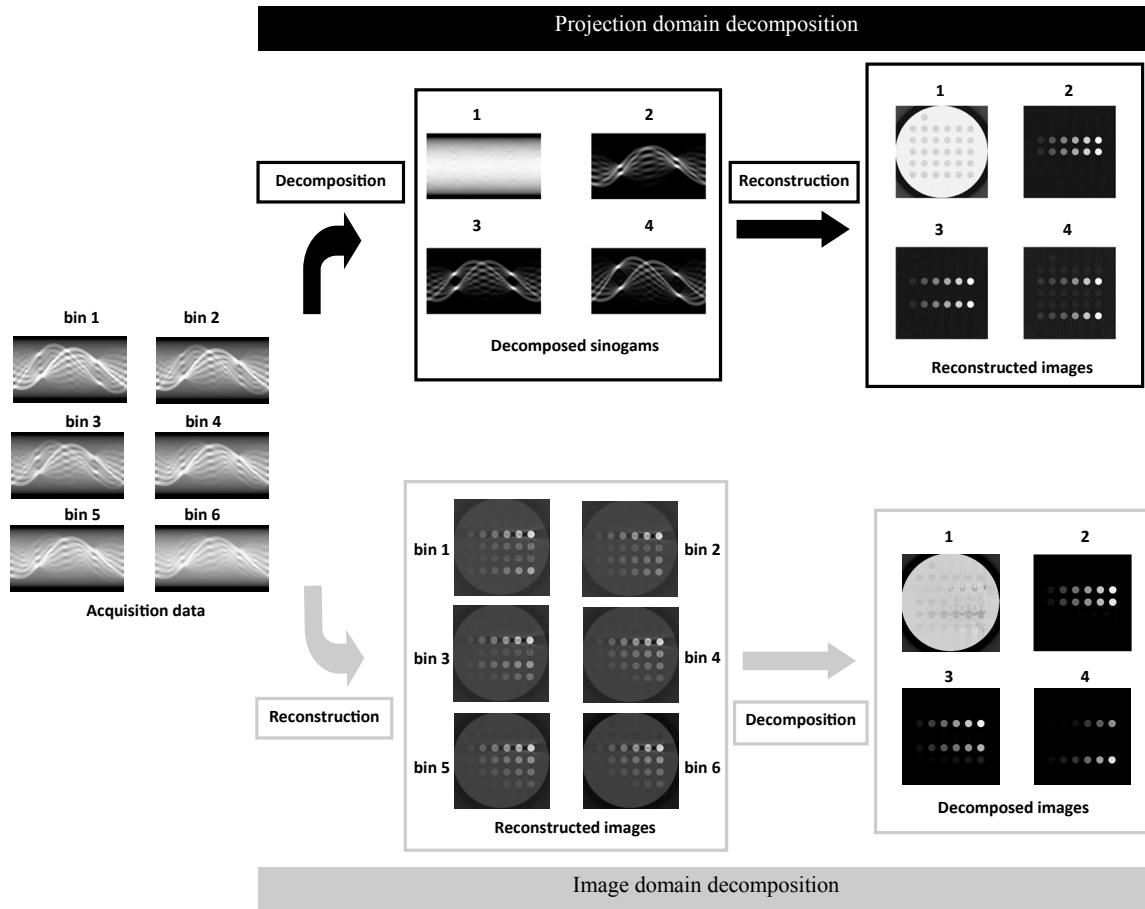


Figure 3: Illustration de la décomposition du domaine de projection et d'image. L'exemple ici suppose que le détecteur CT spectral a 6 bandes d'énergie et donc 6 sinogrammes sont obtenus pour une acquisition. Le premier procédé décompose d'abord les données d'acquisition en  $M$  sinogrammes cibles (ici  $M = 4$  matériaux) en fonction de la localisation, puis effectue une reconstruction sur chaque sinogramme obtenu pour obtenir l'image spatiale finale. La deuxième méthode reconstruit d'abord les images spatiales à partir des données de projection qui correspondent à certaines bandes d'énergie, puis effectue une décomposition en matériaux sur ces données dans le domaine image (i.e. les images spatiales reconstruites).

La décomposition couramment utilisée est basée sur le critère des moindres carrés (LS), nommée proj-LS et méthode ima-LS. Cependant, le problème inverse de la décomposition en matériaux est généralement mal posé et les mesures du CT spectral aux rayons X souffrent de bruits de comptage de photons de type Poisson. Le critère LS standard peut conduire à un sur-ajustement des données de mesure bruitées. Nous avons proposé un critère de moindre log-carré pour la méthode du domaine des projections afin de minimiser les erreurs sur le coefficient d'atténuation linéique: méthode proj-LLS. En outre, afin de

réduire l'effet du bruit et de renforcer la fluidité, nous avons proposé des méthodes de décomposition régularisées par zone respectivement dans les domaines des projections et de l'image reconstruite. La méthode proposée minimise les erreurs quadratiques entre les logarithmes du nombre de photons espéré et mesuré (méthode proj-PR-LLS), ou entre la valeur du coefficient d'atténuation reconstruit et la valeur du coefficient attendu (méthode ima-PR-LS), et en même temps contraint la somme totale des variations (du nombre de photons ou du coefficient d'atténuation) au carré dans les zones.

La Figure 4 résume les méthodes de décomposition en matériaux existantes et proposées qui ont été discutées dans le présent travail.

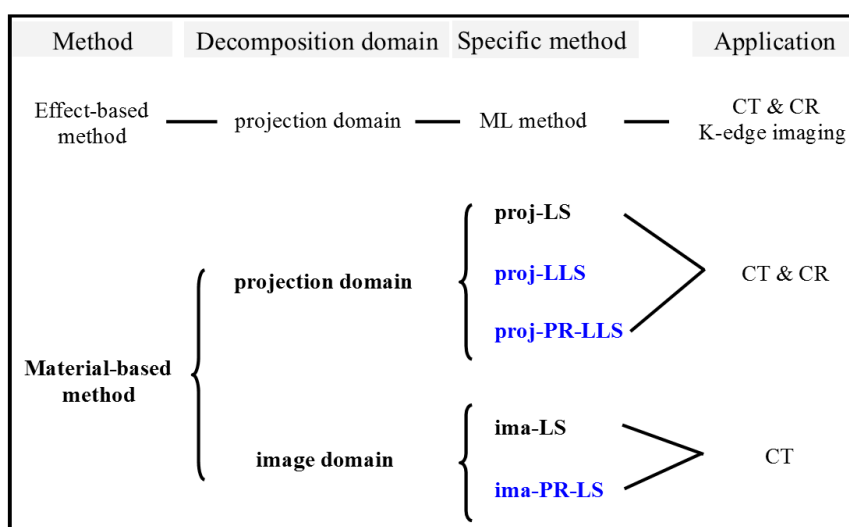


Figure 4: Les méthodes de décomposition en matériaux discutées et proposées (en bleu) dans ce travail de thèse. Le terme CR fait référence à la radiographie spectrale.

### 3 Résultats de décomposition en matériaux pour différentes applications: étude de fantômes

L'objectif de cette partie du travail est d'introduire la méthode de simulation de l'imagerie par rayons X et d'évaluer les méthodes de décomposition dans le domaine des projections proposées à travers l'étude de simulation. Nous simulons le système CT / CR spectral qui possède des capacités de résolution en plusieurs bandes énergétiques en utilisant le logiciel Virtual X-ray Imaging (VXI) [Duvauchelle et al., 2000]. Ce logiciel a été développé à l'INSA de Lyon (France) pour simuler l'imagerie radiographique, radioscopique et tomographique. La simulation est basée sur des techniques de tracé de rayons et s'appuie sur la loi d'atténuation des rayons X de Beer-Lambert. Ciblant une application médi-



cale (imagerie de l'athérosclérose, CT) et une application industrielle (tri des plastiques, radiographie (CR)), nous simulons à travers le logiciel VXI le processus d'imagerie par rayons X avec les deux fantômes correspondants, nous appliquons les méthodes proposées et analysons leurs performances. Pour la première application, nous allons comparer les performances de décomposition de la méthode proj-LS, proj-LLS et proj-PR-LLS et pour la deuxième application, nous utiliserons la méthode proj-PR-LLS que nous complétons par une étape de classification (dénommée proj-PR-LLS-clas). Pour les deux applications de ce chapitre, la CT spectrale ou le processus d'imagerie CR sont simulés avec les paramètres d'acquisition habituellement utilisés dans l'application considérée, par ex. nombre de bandes d'énergie et facteur d'exposition.

Nous comparerons la performance de la méthode proj-PR-LLS et ima-PR-LS, ainsi que l'influence des paramètres d'acquisition sur leur performance dans le prochain chapitre.

### 3.1 Application médicale: identification de l'iode et du calcium

Les maladies cardiovasculaires (MCV) engendrent d'énormes conséquences sanitaires et économiques à l'échelle mondiale et l'athérosclérose est un contributeur majeur des MCV. L'athérosclérose est une maladie dans laquelle l'artère interne se rétrécit en raison de dépôt de plaque. La présence de plaques à l'intérieur des artères coronaires est un facteur de risque grave pour les événements cardiovasculaires indésirables. Les ruptures de plaques vulnérables sont à l'origine d'environ 70% des infarctus aigus du myocarde et des décès coronariens soudains. Il est très important de détecter la présence de plaque et d'évaluer sa vulnérabilité.

Les méthodes existantes peuvent détecter la plaque à haut risque dans une certaine mesure avec des capacités limitées et une évaluation améliorée peut être réalisée par une combinaison de plusieurs méthodes. Cependant, il serait avantageux de trouver une modalité d'imagerie capable d'évaluer en même temps plusieurs caractéristiques de la plaque à haut risque et de permettre une identification avec une meilleure précision. Pour l'inspection de la plaque, l'identification de ses composants est d'une importance significative. Sachant que la CT spectrale aux rayons X possède une capacité de décomposition quantitative en matériaux comparée à l'angiographie conventionnelle par CT, nous étudions la capacité de décomposition des méthodes proposées (méthode proj-LS, proj-LLS et proj-PR-LLS) et évaluons leur performance dans l'identification de l'iode, du calcium et des tissus mous au moyen d'une étude sur le fantôme thoracique humain.

### 3.1.1 Fantôme simulé & géométrie du système

Nous utilisons un fantôme thoracique humain pour simuler les situations in vivo. Les composants et les densités de différents tissus inclus dans le fantôme du thorax (Figure 5 (a)) sont définis selon les publications de White [White et al., 1987] et de la publication 44 de la Commission internationale sur les unités et mesures radiologiques (ICRU44) [ICRU, 1989]. En plus des différents types de tissus corporels, des inserts supplémentaires de solutions de calcium et d'iode avec un diamètre de 6 mm sont placés dans la région du cœur, comme le montre la Figure 5 (b). Les solutions sont à diverses concentrations (calcium: 30, 50, 100, 150, 200 mg/ c, iode: 5, 15, 25, 35, 45 mg/cc).

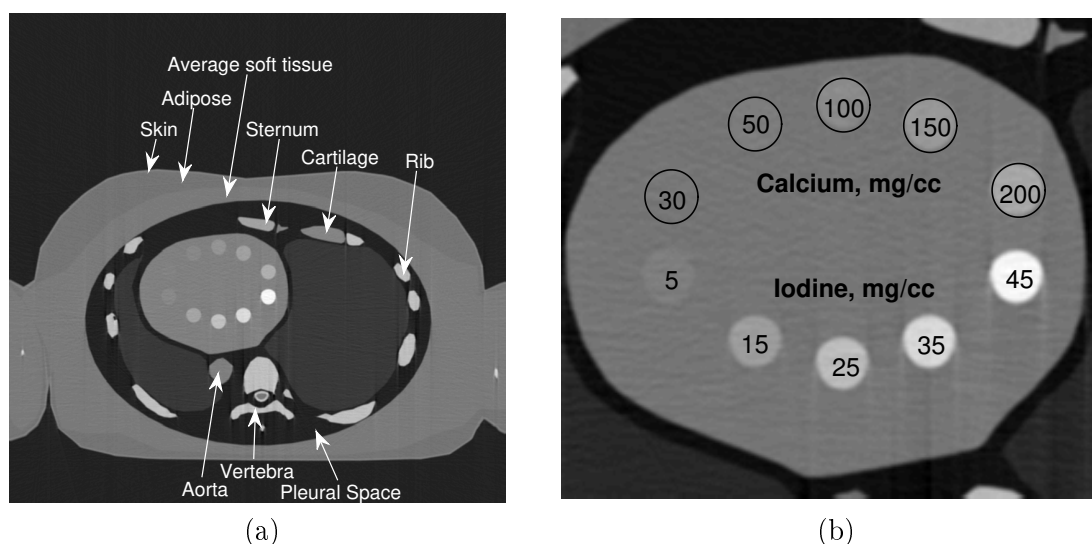


Figure 5: Coupe transversale du fantôme du thorax avec illustration de différents matériaux inclus (a) et de la région du cœur grossie qui contient des inserts de calcium et d'iode avec des concentrations différentes (b).

Le système de CT spectrale aux rayons X simulé utilise un spectre de rayons X de 120 kVp obtenu à partir d'un matériau cible au tungstène sans filtration, l'angle de la cible était de  $17^\circ$  et le courant du tube était de 100 mA. Un détecteur linéaire de tellurure de cadmium (CdTe) de 1000 pixels avec une taille de pixel de  $1 \text{ mm} \times 1 \text{ mm}$  a été utilisé, et sa gamme d'énergie de détection a été réglée de 30 keV à 90 keV avec des bandes d'énergie réparties uniformément. L'efficacité d'absorption du détecteur a été simulée pour un cristal de CdTe de 3 mm d'épaisseur. Le fantôme du thorax a été scanné avec 1200 projections de  $0^\circ$  à  $360^\circ$  et le temps de balayage était de 0.01 s pour chaque projection. Les distances de la source au centre de rotation et du détecteur au centre de rotation étaient respectivement de  $D_{SC}=700 \text{ mm}$  and  $D_{DC}=300 \text{ mm}$ . La Figure 6 illustre la géométrie du système.

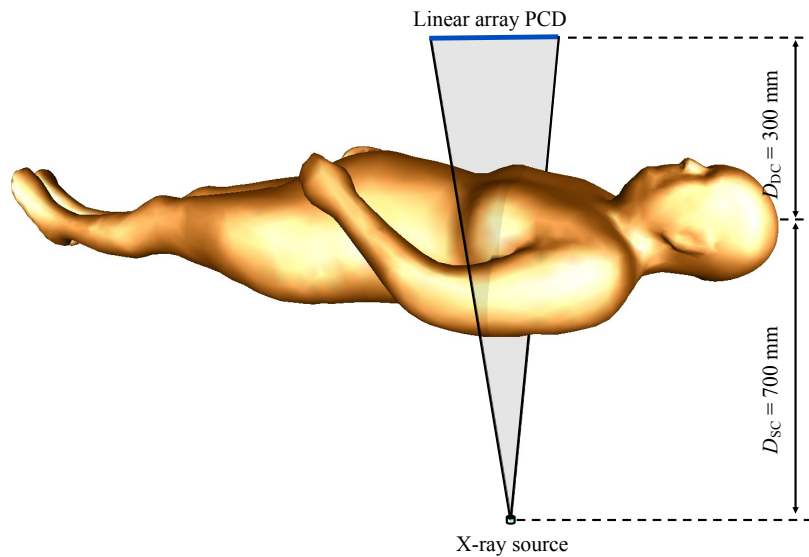


Figure 6: Schéma d'acquisition du CT spectral avec fantôme humain.

### 3.1.2 Résultats de la décomposition

Dans cette application, nous avons choisi le tissu mou, le calcium et l'iode comme base de matériaux pendant la décomposition. Trois méthodes de décomposition de matériaux dans le domaine des projections avec différentes fonctions de coût ont été appliquées: proj-LS, proj-LLS et proj-PR-LLS. La figure 7 montre les images décomposées en utilisant les trois méthodes. On observe que toutes les méthodes donnent la distribution des tissus mous, du calcium et de l'iode:

- La peau, les tissus adipeux, les tissus mous moyens, le cartilage, l'aorte, les poumons et le cœur ne sont visibles que dans l'image des tissus mous. En outre, une partie des os (côtes, vertèbres et sternum) est également présente dans l'image des tissus mous, car les composants des os contiennent non seulement du calcium, mais aussi d'autres éléments comme l'hydrogène et l'oxygène.
- L'image du calcium met bien en évidence les os et les solutions de calcium insérées.
- L'iode est séparée de manière appropriée dans l'image spécifique à l'iode.

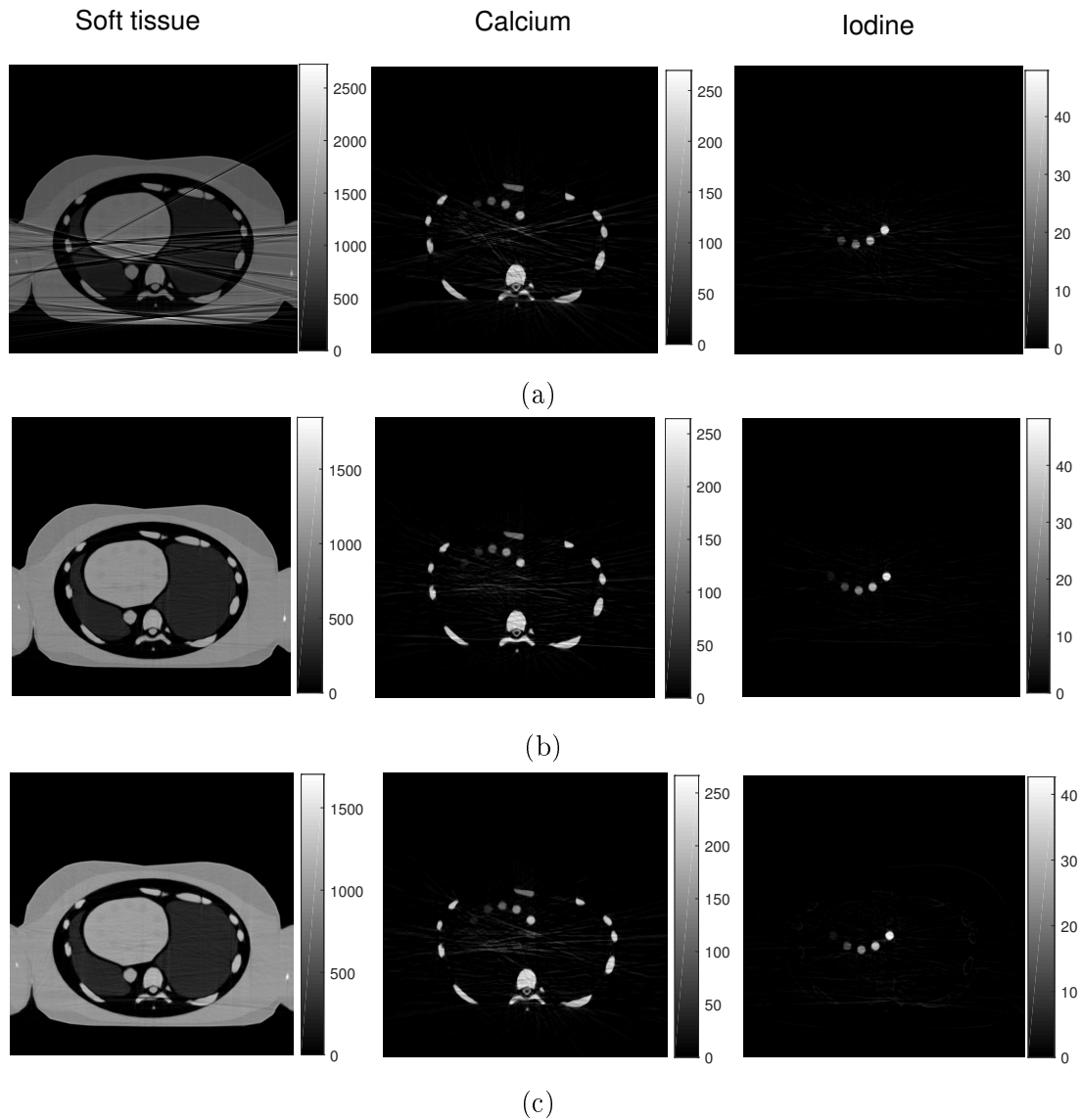


Figure 7: Résultats de la décomposition en matériaux avec la méthode proj-LS (a), la méthode proj-LLS (b) et la méthode proj-PR-LLS (c). Chaque colonne représente la même base de matériaux, i.e. le tissu mou pour la première colonne, le calcium pour la seconde et l'iode pour la troisième.

Pour effectuer une analyse quantitative de la performance des trois méthodes, nous avons calculé les erreurs moyennes (AE) et les rapports de contraste sur bruit (CNR) des solutions décomposées de calcium et d'iode, comme montré dans la Figure 8 et la Figure 9. Les régions d'intérêt (ROI) ont été choisies comme régions d'insertion de calcium ou d'iode dans l'image décomposée correspondante. L'AE est calculée pour chaque ROI en calculant la moyenne des erreurs relatives absolues. Pour le calcul des CNR, nous avons

choisi une région voisine des ROI comme région de fond.

Pour la quantification du calcium, on observe sur les Figures 8 (a) et Figure 9 (a) que la méthode proj-PR-LLS proposée conduit à la meilleure précision de quantification, c'est-à-dire les AE les plus faibles et la meilleure qualité d'image (CNR plus élevé). Pour la détermination de l'iode (Figure 8 (b) et Figure 9 (b)), les deux méthodes proposées ont de meilleures performances que la méthode proj-LS communément utilisée. En comparant la méthode proj-LLS et proj-PR-LLS, nous pouvons observer que la méthode proj-LLS a des erreurs de quantification plus faibles, tandis que la méthode proj-PR-LLS peut générer une image de l'iode avec des CNR plus élevés.

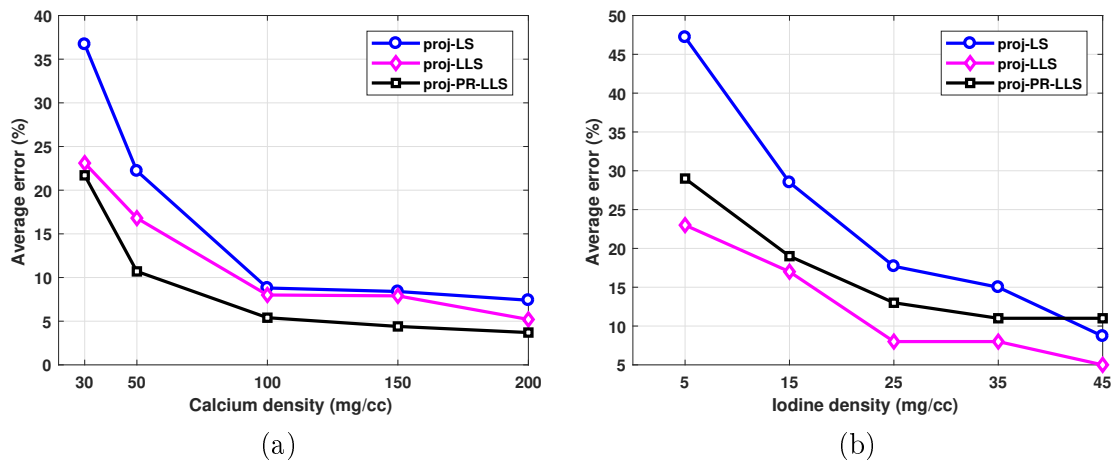


Figure 8: Erreurs moyennes des densités décomposées du calcium (a) et de l'iode (b) en utilisant les méthodes proj-LS, proj-LLS et proj-PR-LLS.

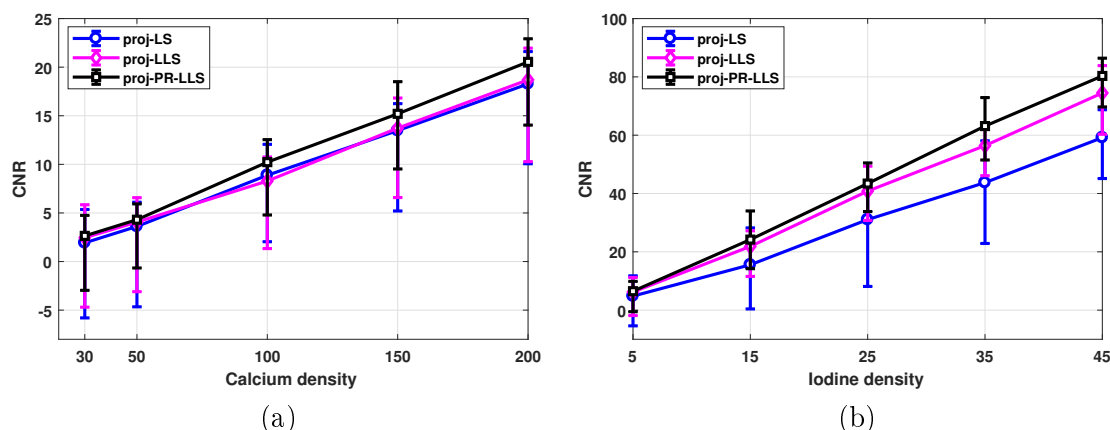


Figure 9: CNR de l'image décomposée du calcium et de l'iode à différentes densités en utilisant la méthode proj-LS, proj-LLS et proj-PR-LLS. Les barres d'erreur représentent la variation du  $CNR_{min}$  à  $CNR_{max}$ .

### 3.1.3 Conclusion and discussion

Motivés par la nécessité de distinguer les compositions de la plaque athérosclérotique, nous avons simulé le processus d'imagerie par CT spectrale avec un fantôme thoracique humain réaliste, et étudié les performances de décomposition en matériaux des trois méthodes présentées dans le chapitre précédent: proj-LS, proj-LLS et proj-PR-LLS. Trois images ont été obtenues en utilisant l'une ou l'autre méthode: image des tissus mous, du calcium et de l'iode. Les résultats ont montré que toutes les méthodes peuvent donner une distribution quantitative des trois matériaux, parmi lesquels l'image des tissus mous contient de la peau, du tissu adipeux, du tissu mou moyen, du cartilage, de l'aorte, du poumon et du coeur; l'image du calcium met bien en évidence les os et les solutions de calcium insérées; L'image de l'iode contient seulement les solutions d'iode insérées. L'analyse quantitative, incluant les erreurs moyennes et les CNR, a démontré que la méthode proj-LLS proposée et la méthode proj-PR-LLS ont une meilleure précision quantitative et une meilleure qualité d'image que la méthode proj-LS couramment utilisée. De plus, la méthode proj-PR-LLS a la capacité d'améliorer les CNR des images décomposées tout en obtenant une meilleure précision quantitative (calcium) ou inférieure mais comparative (iode), en comparaison avec la méthode proj-LLS.

Il y a des améliorations potentielles à notre travail. La dose de rayonnement pour le patient est liée au nombre de projections. Un nombre inférieur de projections peut réduire la dose pour le patient mais également diminuer la qualité de l'image en raison de l'échantillonnage plus clairsemé des données d'imagerie [Van Daatselaar et al., 2004]. Le nombre typique de projections utilisées en CT à faisceau conique dans les applications du

sein, des extrémités et de la tête est de 350 à 450 [Zhao et al., 2014]. Dans la présente étude, 1200 projections ont été utilisées dans le balayage du fantôme simulé pour une meilleure qualité d'image. Ce nombre pourrait conduire à une dose de patient interdite et ceci devrait être considéré dans de futures études.

### 3.2 Application industrielle: tri plastique ABS-RF

Les déchets d'équipements électriques et électroniques (DEEE) ont augmenté rapidement en raison du développement de l'industrie électronique. Ces déchets ont diverses compositions parmi lesquelles les polymères jouent un rôle important. L'acrylonitrile-butadiène-styrène (ABS) est un composant majeur parmi tous les polymères. En raison de la présence d'énergie des EEE, les matériaux en plastique doivent répondre à des normes de sécurité incendie élevées. Cependant, il n'est pas possible de les réaliser avec des polymères purs, donc des retardateurs de flammes (RF) sont ajoutés pour modifier l'inflammabilité des plastiques et augmenter la résistance au feu. Le recyclage des plastiques issus des DEEE est difficile en raison de l'existence des RF (en particulier les RF bromés et chlorés), ce qui pourrait entraîner une pollution environnementale grave. Par conséquent, la technique de tri est importante pour le traitement ultérieur et le recyclage des DEEE afin d'éviter les problèmes environnementaux et de santé majeurs.

Dans le présent travail, nous allons étudier la capacité de décomposition en matériaux de la méthode proj-PR-LLS pour l'imagerie CR spectrale dans l'application de tri des plastiques ABS-RF (c'est-à-dire en radiographie et non pas en tomographie puisque les déchets défilent sur un convoyeur à grande vitesse). En outre, nous développons également une méthode de décomposition basée sur la classification pour cette application spécifique, appelée méthode proj-PR-LLS-clas. Ses performances seront évaluées par rapport à la méthode proj-PR-LLS.

#### 3.2.1 Fantôme simulé & géométrie du système

Comme nous l'avons dit dans la section ci-dessus, l'ABS est un composant majeur parmi tous les polymères utilisés dans les équipements électriques et électroniques, nous l'avons donc choisi comme matériau polymère pour l'investigation. Nous avons également choisi trois types de retardateurs de flamme couramment utilisés, y compris les ignifugeants bromés (Br), chlorés (Cl) et phosphorés (P). Ce sont respectivement le tétrabromobisphénol A (TBBPA), le déchlorane plus (DDC-CO) et le bis diphénylphosphate de résorcinol (RDP). Trois matériaux ABS-RF simulés ont été obtenus en mélangeant chaque RF avec de l'ABS à un pourcentage massique de 15%. Ces choix sont issus d'une étude précédente de CT en bi-énergie menée au laboratoire lors de la thèse de Florian Montagner.

Nous avons simulé un fantôme composé de plusieurs cubes d'une hauteur de 10 mm, d'une largeur de 10 mm et d'épaisseurs différentes. Comme le montre la Figure 10, chaque colonne de cubes est du même matériau (noté en haut) et chaque rangée de cubes est de même épaisseur (notée sur la gauche).

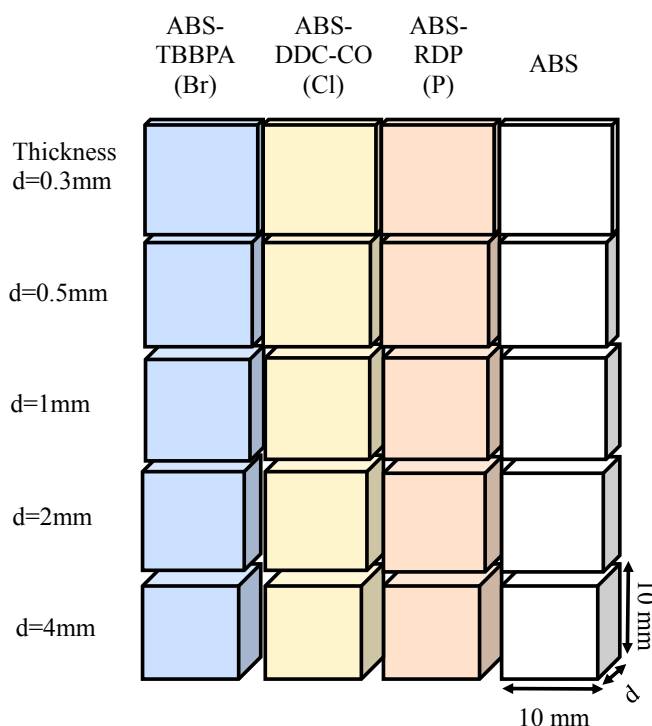


Figure 10: Illustration du fantôme ABS-RF utilisé pour l'imagerie CR spectrale.

Le système simulé utilise un spectre de rayons X de 100 kVp avec un courant du tube de 15 mA. La distance entre la source de rayons X et le centre du fantôme est de 2 m, ce qui est assez loin pour considérer que les rayons X traversant l'objet sont parallèles. Une matrice de détecteurs CdTe de  $90 \times 112$  avec une taille de pixel de  $0.5 \text{ mm} \times 0.5 \text{ mm}$  et une épaisseur de 3 mm a été simulée, et la distance entre le détecteur et le centre du fantôme était de 2 mm. Six bandes d'énergie ont été réglées pour être réparties uniformément de 30 keV à 90 keV. La Figure 11 est une vue schématique du système de CR spectral simulé.



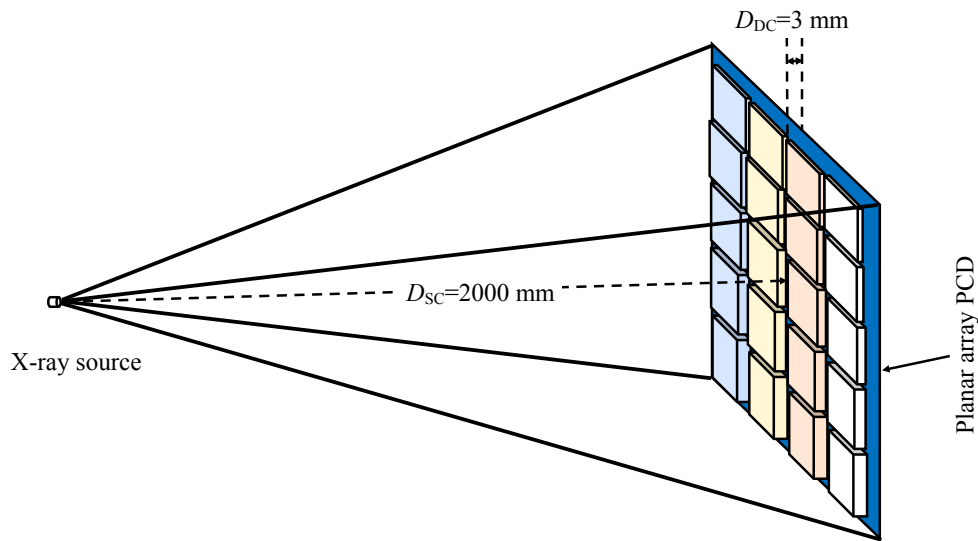


Figure 11: Schéma de la géométrie du système CR. Cette figure n'est qu'une vue schématique simplifiée du système de simulation où les informations dimensionnelles ( $D_{SC}$ ,  $D_{DC}$ , taille du fantôme et du détecteur) ne sont pas à l'échelle réaliste.

### 3.2.2 Résultats de la décomposition de la méthode proj-PR-LLS

Pour cette application, nous avons simulé deux ensembles de données d'acquisition CR spectrales: avec et sans bruit de photons. Nous avons ensuite utilisé la méthode proj-PR-LLS pour décomposer les images radiographiques en trois images de base correspondant à ABS, Br et Cl. La raison pour laquelle on n'a pas choisi P comme base est que P et Cl ont des numéros atomiques trop proches et les expériences ont montré qu'ils peuvent être à peine séparés. Ainsi, nous utilisons Cl comme matériau de base et attendons que P soit également présent dans l'image de base Cl. Nous définissons la taille des zones (patch) à  $2 \times 2$ , et le paramètre de régularisation est noté  $r$  et est ajusté en fonction de la configuration du bruit.

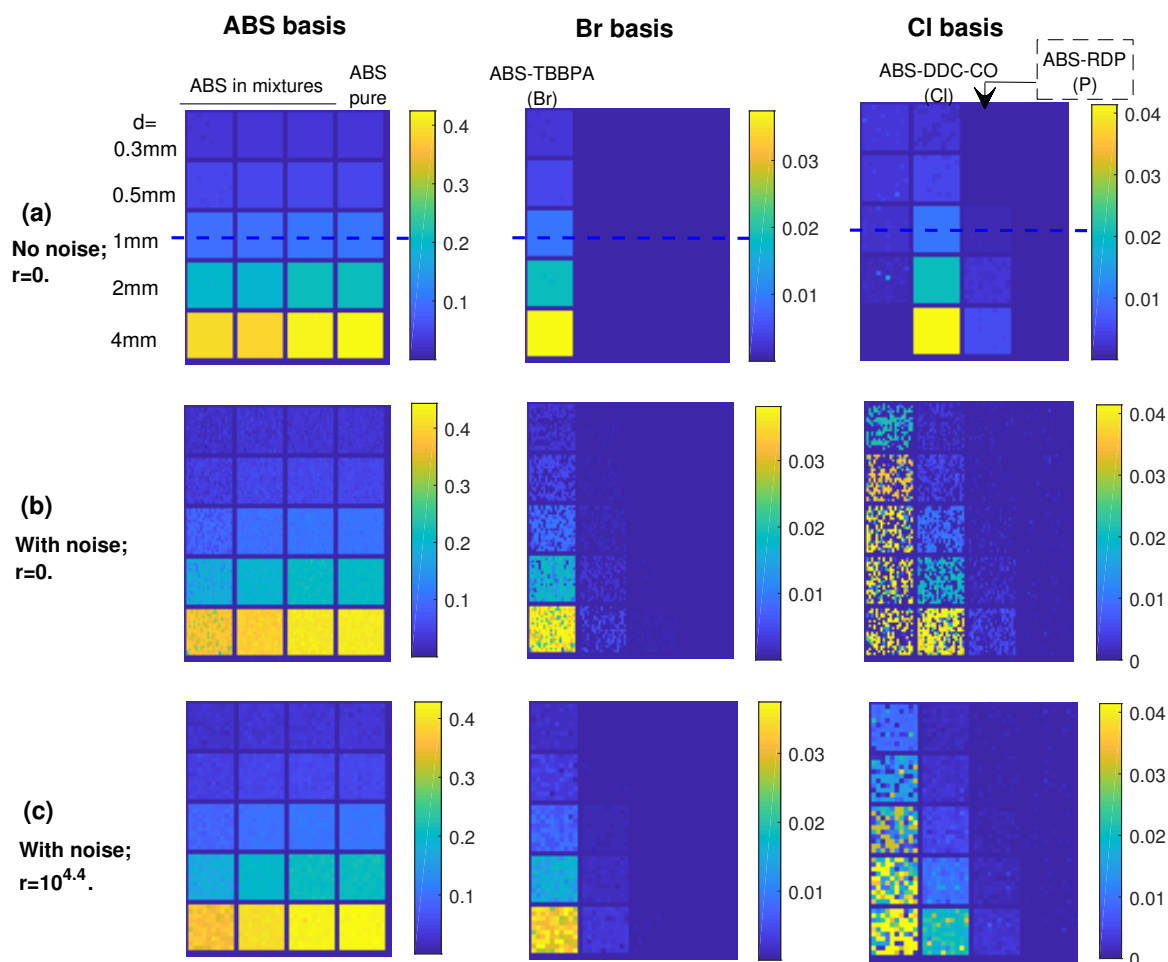


Figure 12: Les résultats de décomposition dans différentes conditions en utilisant la méthode proj-PR-LLS. (a): simulation de CR sans bruit,  $r=0$ ; (b): simulation de CR avec bruit de Poisson,  $r=0$ ; (c): simulation de CR avec bruit de Poisson,  $r=10^{4.4}$ . La première colonne représente la base de l'ABS, la deuxième la base de Br et la troisième la base de Cl. L'échelle de couleur représente le facteur d'atténuation (c'est-à-dire  $\mu \times \text{épaisseur}$ ).

Pour une acquisition simulée sans bruit, nous définissons le paramètre de relaxation  $r$  sur 0, car il n'est pas nécessaire d'appliquer un lissage dans les zones (patches) lorsqu'il n'y a pas de bruit, les résultats de décomposition correspondants sont montrés sur la Figure 12 (a). On observe que tous les cubes sont visibles sur l'image de base ABS, en raison de la présence d'ABS dans les mélanges (ABS-RF) ou ABS pur. Les cubes ABS-TBBPA sont bien séparés et mis en évidence dans l'image de base Br. Lorsque l'épaisseur du cube est faible ( $d=0.3$  et  $0.5$  mm), les cubes ABS-TBBPA et les tubes ABS-DDC-CO sont aussi visibles sur l'image de base Cl; Lorsque l'épaisseur du cube augmente à 1 mm et 2 mm, les trois cubes ABS-RF sont visibles, cependant, l'intensité du signal des cubes ABS-TBBPA

dans l'image de base Cl reste faible; Lorsque  $d = 4$  mm, seuls les cubes ABS-DDC-CO et les cubes ABS-RDP sont visibles dans l'image de base Cl. Pour conclure, dans une situation sans bruit, l'ABS et le Br peuvent être bien identifiés; les performances de détermination des autres RF s'améliorent avec l'épaisseur de l'objet: quand  $d = 4$  mm, les RF contenant Cl et P sont présents dans l'image de base Cl sans diaphonie du matériau ABS-TBBPA, et on peut encore distinguer les deux RF en fonction de leur grande différence de densité.

Lorsque le bruit de Poisson est ajouté pendant la simulation, nous devons reconsidérer le paramètre de relaxation  $r$ . Dans cette situation,  $r$  est déterminé à  $10^{4.4}$  selon la méthode de la courbe en L- Les résultats de la décomposition lorsque  $r = 0$  et  $r = 10^{4.4}$  sont montrés sur la Figure 12 (b) et (c). On peut voir que lorsque  $r = 0$ , les cubes ABS-TBBPA et les cubes ABS-DDC-CO apparaissent à la fois dans l'image de base Br et dans l'image de base Cl, ce qui les rend impossibles à distinguer. De plus, les images décomposées souffrent de bruit intense. Lorsque le paramètre de relaxation passe à  $r = 10^{4.4}$ , les images obtenues sont moins bruitées que celles du premier cas, cependant, la séparation des différents matériaux n'est pas améliorée.

### 3.2.3 Méthode proj-PR-LLS-clas

Les résultats ont montré que la décomposition directement sur la base de 3-matériaux n'est pas assez robuste au bruit. Nous avons donc introduit une procédure de classification-décomposition (méthode proj-PR-LLS-clas) basée sur l'application car nous savons a priori qu'une seule pièce de plastique ne peut contenir 2 RF en même temps. Il est donc raisonnable d'effectuer d'abord deux décompositions à 2 matériaux, puis de choisir le résultat le plus probable. La Figure 13 montre la procédure de cette méthode pour obtenir des valeurs pour une zone.

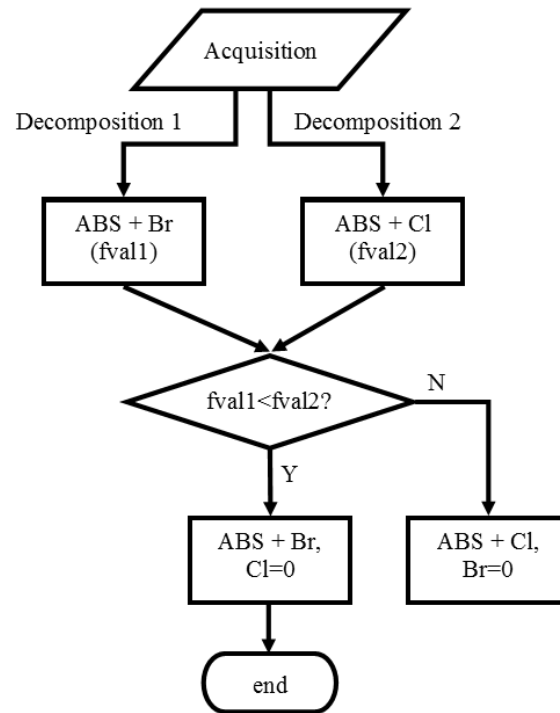


Figure 13: Organigramme de la méthode de décomposition avec classification pour un patch.  $fval1$  et  $fval2$  représentent les valeurs des fonction de coût obtenues à la fin de la décomposition 1 et de la décomposition 2.

### 3.2.4 Résultats de décomposition de la méthode proj-PR-LLS-clas

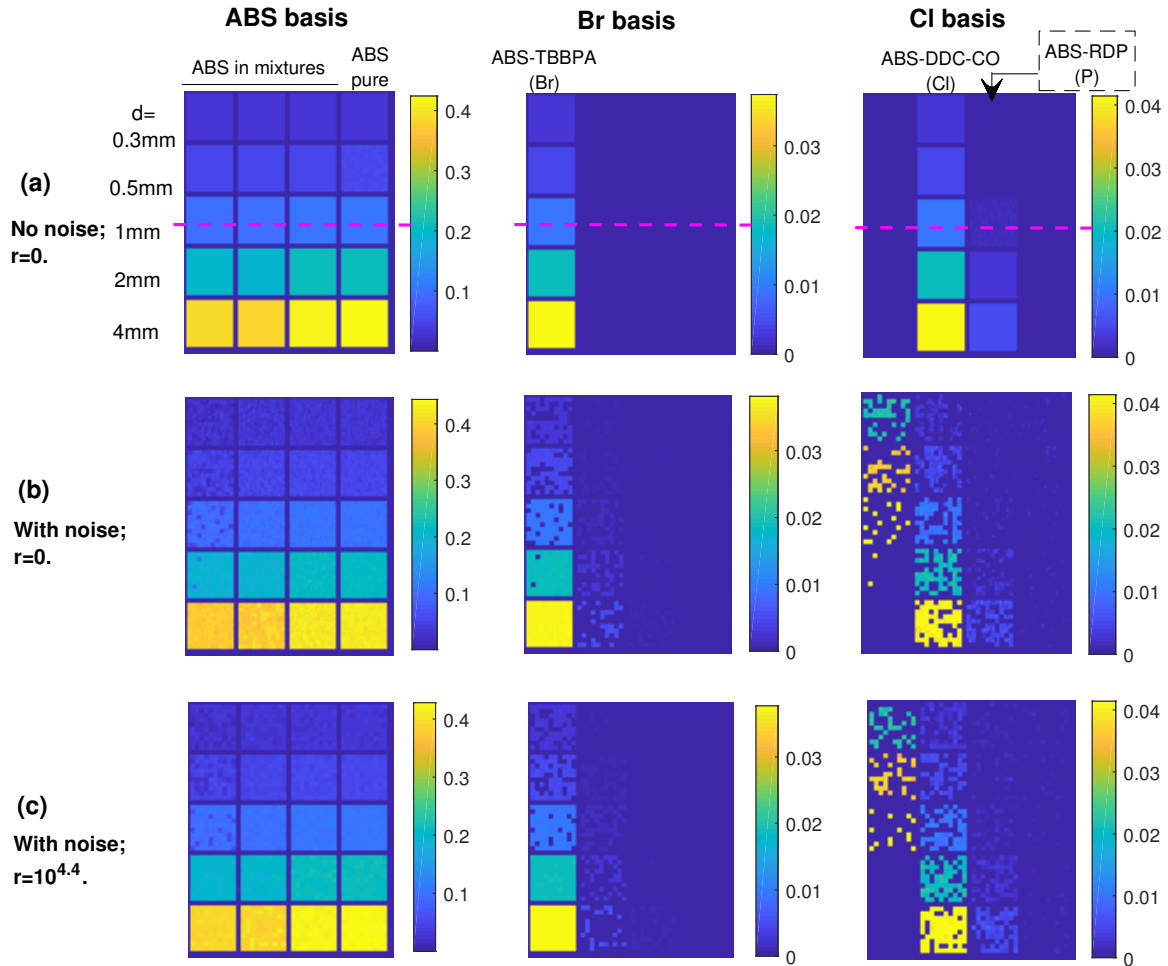


Figure 14: Les résultats de décomposition dans différentes conditions en utilisant la méthode proj-PR-LLS-clas. (a): simulation de CR sans bruit,  $r = 0$ ; (b): simulation de CR avec bruit de Poisson,  $r = 0$ ; (c): simulation de CR avec bruit de Poisson,  $r = 10^{4.4}$ . La première colonne représente la base de l'ABS, la deuxième la base de Br et la troisième colonne la base de Cl.

Dans un état sans bruit (Figure 14 (a)), l'ABS et le RF qui contient du Br peuvent être identifiés à partir des images de base ABS et Br. Pendant ce temps, les cubes de matériaux RF contenant Cl et P apparaissent dans l'image de base Cl, mais ils ont une différence de densité significative pour les cubes de même épaisseur, ils peuvent donc être facilement distingués par l'observateur même si la concentration en RF ou épaisseur de cubes change plus ou moins. Avec le bruit de Poisson simulé, les images décomposées de la méthode proj-PR-LLS-clas ont également une plus grande capacité de séparation que la méthode

proj-PR-LLS. ABS et Br peuvent être identifiés selon l'image de base correspondante. En outre, lorsque l'épaisseur du cube augmente jusqu'à 2 mm et 4 mm, les résultats de la décomposition deviennent beaucoup plus proches de ceux de la condition sans bruit, où ABS et les RF contenant Br, Cl et P peuvent être identifiés en même temps.

### 3.2.5 Conclusion et discussion

Les DEEE ont augmenté rapidement en raison du développement de l'industrie électronique. La technique de tri est importante pour le traitement ultérieur et le recyclage des DEEE afin d'éviter les problèmes environnementaux et sanitaires majeurs. Pour cette application, nous avons simulé l'imagerie CR spectrale avec un fantôme contenant plusieurs cubes de différents matériaux ABS-RF avec différentes épaisseurs, et nous avons étudié la faisabilité de décomposition de différents ABS-FR en utilisant la méthode proj-PR-LLS et proj-PR-LLS-clas. Les résultats montrent que la première méthode n'a pas permis d'identifier les matériaux FR lorsque le bruit de Poisson a été simulé pour l'imagerie CR. Cette dernière méthode, dans un état sans bruit, pourrait distinguer en même temps l'ABS et les RF contenant les éléments Br, Cl et P, avec une quantification de chaque matériau concordant bien avec la valeur théorique. Lorsque le bruit a été ajouté dans la simulation, la méthode proj-PR-LLS-clas peut séparer quatre matériaux en même temps seulement lorsque l'épaisseur du tube est supérieure à 2 mm ce qui est réaliste pour l'application visée.

Il y a certaines limites dans notre travail. Premièrement, les deux méthodes ne sont pas très robustes au bruit lorsque l'épaisseur de l'objet est trop petite, en particulier la méthode proj-PR-LLS. Deuxièmement, la méthode proj-PR-LLS-clas a été proposée en partant du principe que chaque pixel sur l'image radiographique de l'objet contient soit un ensemble de matériaux de base (ABS + Br) ou l'autre (ABS + Cl), de sorte que le matériau n'appartenant pas à la base sélectionnée puisse être mis à 0. La méthode Proj-PR-LLS-clas ne peut pas être appliquée pour une situation où cette condition n'est pas remplie. Troisièmement, la décomposition d'éléments ayant des nombres atomiques similaires (Cl et P), même dans la condition de simulation sans bruit, dépend de leur différence de densité dans la même image. Par conséquent, dans le cas où l'information d'épaisseur des objets est inconnue, ou si les deux matériaux se chevauchent dans la direction des rayons X, la densité décomposée sera largement influencée, conduisant les matériaux à être indiscernables.

## 4 Explorer l'influence de différents paramètres d'acquisition

Nous avons introduit dans le chapitre précédent les performances de décomposition en matériaux de la CT spectrale et de la CR spectrale avec un détecteur de comptage de

photons. Dans les applications ci-dessus, la CT spectrale et le processus d'imagerie CR ont été simulés en utilisant des paramètres d'acquisition actuellement utilisés dans des situations pratiques. Par exemple, le nombre de bandes d'énergie a été fixé à 6 étant donné que la plupart des PCD existants ont de 2 à 8 canaux d'énergie. Dans les applications de l'imagerie médicale, le courant du tube à rayons X et le temps d'exposition ont été fixés à 100 mA·s et 0.01 s / projection, ce qui a entraîné un facteur d'exposition (produit courant du tube et temps d'exposition) de 1 mA·s par projection. Qu'advient-il de la performance de la décomposition en matériaux si on fait varier ces paramètres d'acquisition lors de la simulation?

Le rapport signal sur bruit de la bande d'énergie  $B_i$  défini par le rapport de la moyenne sur l'écart type de mesure est proportionnel à la racine carrée du comptage attendu. Le facteur d'exposition a une influence directe sur le nombre de photons arrivant sur le détecteur, et par conséquent sur le niveau de bruit de l'image. Donc la performance de décomposition sera différente si nous modifions le facteur d'exposition. Pour un spectre de rayons X donné, la largeur de chaque canal d'énergie se rétrécit lorsque nous augmentons le nombre total de bandes d'énergie. Une bande d'énergie étroite limitera le nombre de photons reçus par le détecteur dans chaque bande et entraînera un SNR réduit. Cependant, un plus grand nombre de bandes d'énergie fournit plus de mesures dépendant de l'énergie et apporte une meilleure résolution pour la décomposition du matériau. Par conséquent, en augmentant le nombre de bandes d'énergie, il existe un compromis entre un SNR décroissant et une information spectrale croissante pour la décomposition des matériaux.

Dans le présent travail, nous simulerons l'imagerie par CT spectrale aux rayons X d'un fantôme de poly (méthacrylate de méthyle) (PMMA) rempli de solutions de fer (Fe), de calcium (Ca) et de potassium (K). Dans le but de quantifier le fer par rapport à d'autres matériaux, nous simulons le processus d'acquisition avec différents paramètres, à savoir le facteur d'exposition et le nombre de bandes d'énergie, et étudions leur influence sur la performance de décomposition. Deux méthodes sont utilisées pour cette application: les méthodes de décomposition régularisées par zone dans le domaine de l'image (méthode ima-PR-LLS) et dans le domaine des projections (méthode proj-PR-LS).

#### 4.1 Fantôme simulé & géométrie du système

Nous avons simulé un fantôme PMMA de 80 mm de diamètre. À l'intérieur du fantôme, 31 trous de 6 mm de diamètre ont été remplis avec différentes solutions, comme le montre la Figure 15. Les deux premières rangées représentent des rangées contenant 7 inserts d'eau pure et la troisième rangée correspond à la rangée de mélange. Les trois rangées inférieures contiennent respectivement du fer, du calcium et du potassium dissous dans de l'eau à

différentes concentrations (15-200 mg/cm<sup>3</sup> ou cc). La valeur de densité spécifique pour chaque insert est annotée à l'intérieur de chaque cercle sur la figure avec l'unité de mg/cc. Le symbole '#' marque l'insert de mélange de Fe, Ca, K et d'eau. Par exemple, le premier trou de la rangée de mélange est constitué de 15 mg/cc de fer, 15 mg/cc de calcium et 15 mg/cc de potassium, le second contient 30 mg/cc de fer, 30 mg/cc de calcium et 30 mg/cc de potassium.

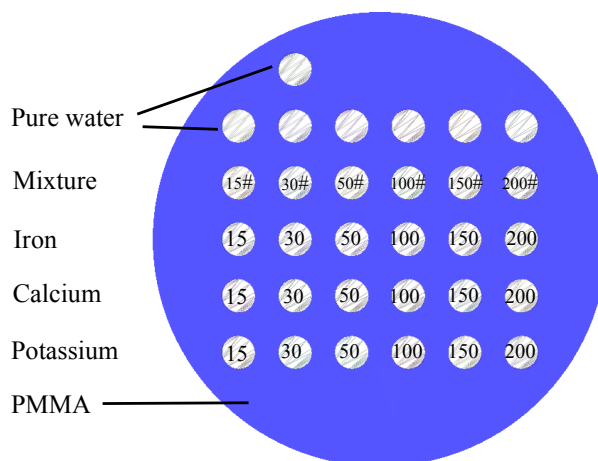


Figure 15: Illustration du fantôme. Chaque rangée contient le même matériau ou les mêmes matériaux dissous dans l'eau à différentes concentrations, les matériaux sont indiqués à gauche et les concentrations sont annotées à l'intérieur de chaque insert sur la figure avec l'unité de mg/cc. Le symbole '#' marque les inserts de mélange qui combinent le fer, le calcium, le potassium et l'eau.

La Figure 16 montre la géométrie du système CT spectral simulé. Le système simulé comprend un détecteur CdTe linéaire de 700 pixels avec une taille de pixel de 0.4 mm × 0.4 mm. L'efficacité d'absorption du détecteur a été simulée pour un cristal de CdTe de 3 mm d'épaisseur. Le spectre de rayons X correspond à une tension de tube de 100kVp. Le fantôme a été scanné avec 1200 projections de 0° à 360°. Les distances de la source au centre de rotation et du détecteur au centre de rotation étaient respectivement de  $D_{SC} = 200$  mm et  $D_{DC} = 400$  mm. Pour étudier l'influence du facteur d'exposition et du nombre de bandes d'énergie, nous définissons différents paramètres d'acquisition: nombre de bandes  $N = 6, 10, 15, 20, 30$  et  $60$ , et facteur d'exposition  $F = 0.025, 0.1, 1, 10$  et  $100$  mA·s par projection. Les bandes d'énergie ont été réparties de manière égale dans la plage d'énergie de détection de 30 keV à 90 keV.



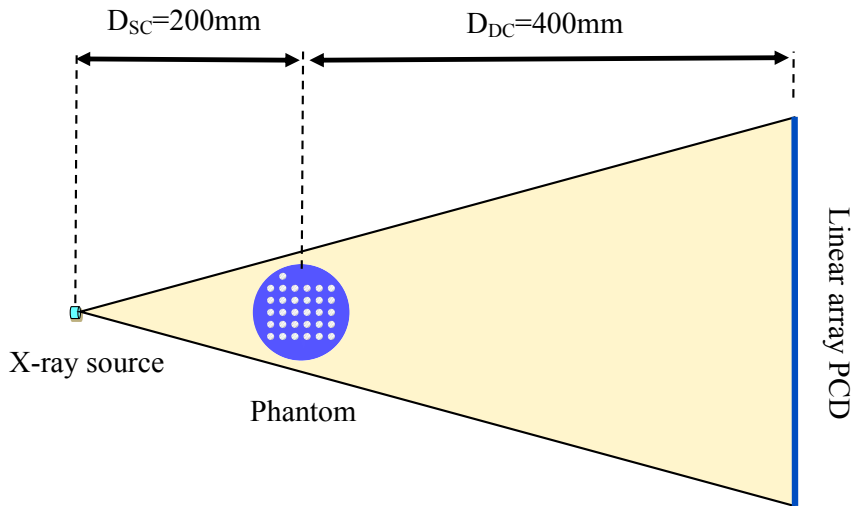


Figure 16: Schéma d'acquisition de CT spectrale.

## 4.2 Résultats de la décomposition

Pour un objet complexe composé de plusieurs matériaux, tous les composants ne peuvent pas être mis dans la base de matériaux. Dans ce cas, l'atténuation provoquée par les composants ayant des numéros atomiques effectifs similaires est censée être représentée par le même matériau de base. Sur la base de cette hypothèse, pour décrire globalement l'ensemble de l'objet, nous choisissons trois matériaux comme base en fonction de leur numéro atomique: matériau léger, matériau médian et matériau lourd. Dans le cas de notre fantôme, le matériau léger correspond au PMMA ou à l'eau, le matériau médian à Ca ou K, le matériau lourd au Fe. Pour améliorer la différence entre les matériaux lourds (Fe) et médians, nous choisissons K comme matériau médian pour les deux méthodes proj-PR-LLS et ima-PR-LS. Cependant, différents matériaux légers sont choisis pour les deux méthodes (PMMA pour proj-PR-LLS et eau pour ima-PR-LS) en raison de leur domaine de décomposition différent. Lorsque nous effectuons une décomposition en matériaux dans le domaine des projections, les données de fonctionnement sont des sinogrammes d'acquisition qui correspondent au nombre de photons transmis pour chaque rayon. Il convient de noter que lorsque le rayon X traverse le fantôme, le PMMA, en tant que porteur de tous les inserts, conduit à la plus grande partie de l'atténuation des rayons X. Par conséquent, nous choisissons le PMMA comme matériau léger pour la méthode proj-PR-LLS. La situation est très différente lorsque nous décomposons dans le domaine de l'image, puisque nous traitons les images reconstruites qui correspondent à la carte des coefficients d'atténuation.

Pour chaque pixel de l'image reconstruite, le coefficient d'atténuation est provoqué par les composants existant dans ce pixel. Considérant que l'eau est le solvant réel du mélange, nous choisissons l'eau comme matériau léger pour la méthode ima-PR-LS.

#### 4.2.1 Méthode proj-PR-LLS

Comme analysé ci-dessus, pour la méthode proj-PR-LLS, les trois matériaux choisis comme base sont le PMMA, le potassium et le fer. Le paramètre de relaxation  $r$  est défini à 1 et la taille de chaque zone est de  $5 \times 5$ . Les résultats ont montré que le fer peut être identifié dans toutes les conditions en utilisant la méthode proj-PR-LLS. Cependant, les performances se différencient beaucoup lorsque les paramètres d'acquisition varient. Deux exemples de résultats sont donnés lorsque  $N=6$ ,  $F=1$  mA·s (Figure 17 (b)), et  $N=60$ ,  $F=10$  mA·s (Figure 17 (c)).

On observe que l'eau et le PMMA sont présents dans l'image de base en PMMA (colonne de gauche). Pour l'image à base de fer (colonne du milieu), on ne peut observer que deux rangées d'inserts, l'un représentant le fer dans le mélange et l'autre le fer dans l'eau, ce qui signifie que le fer est bien séparé des autres matériaux. Pour l'image à base de potassium (colonne de droite), nous observons non seulement les rangées d'inserts qui contiennent du potassium, mais aussi une rangée d'inserts qui contiennent du calcium dans l'eau. Les résultats concordent bien avec notre hypothèse précédente selon laquelle des matériaux ayant des propriétés d'atténuation similaires (potassium et calcium) seront simultanément représentés par la même base. En comparant la Figure 17 (b) et (c), il est évident que les images décomposées de  $N=60$ ,  $F=10$  mA·s sont moins bruitées grâce à un facteur d'exposition plus élevé.

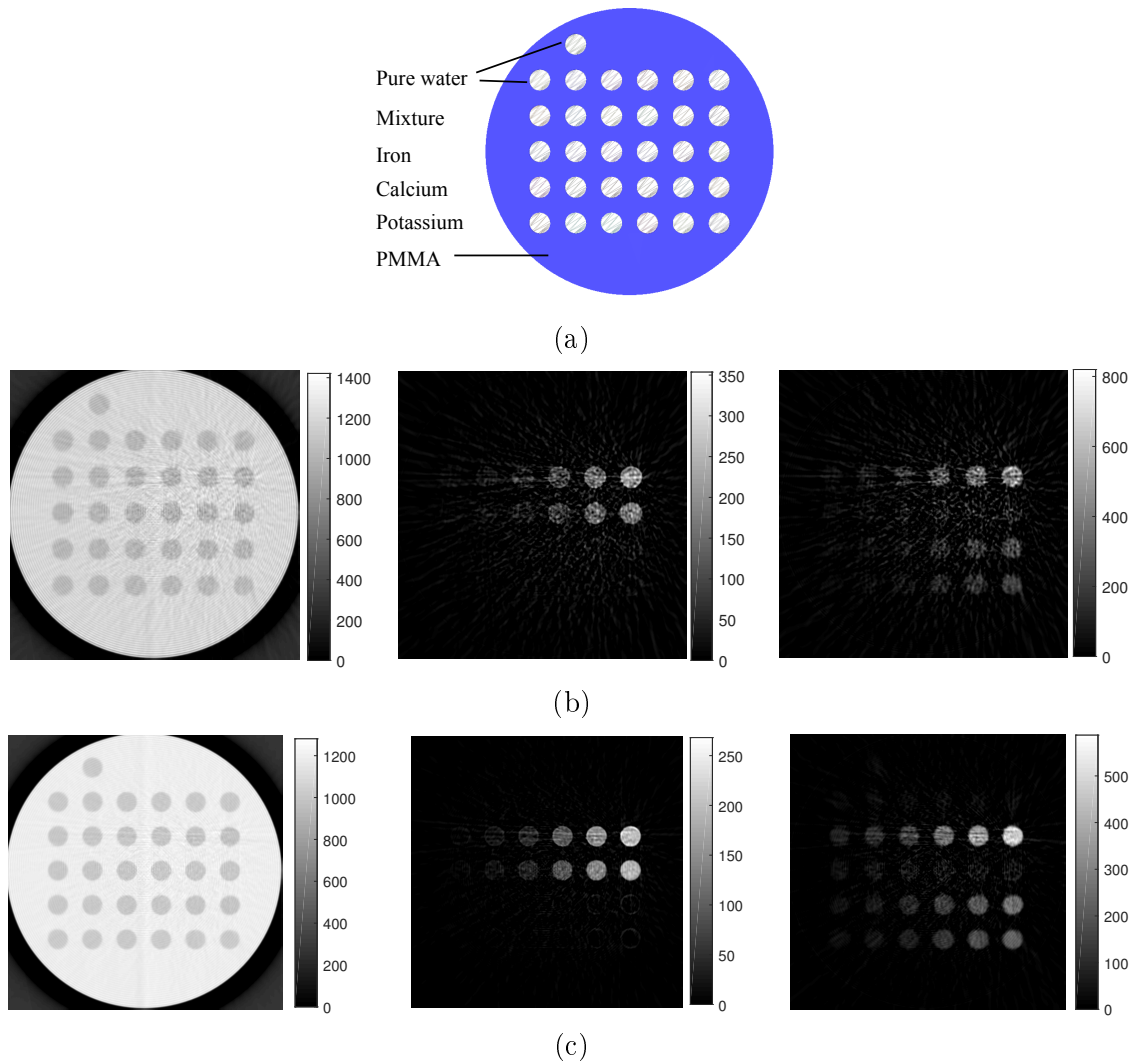


Figure 17: Illustration des composants du fantôme (a) pour mieux comprendre les résultats de la décomposition. Densité décomposée en unité de mg/cc en utilisant la méthode proj-PR-LLS avec paramètres d'acquisition: 6 bandes d'énergie, 1 mA·s par projection pour (b), et 60 bandes d'énergie, 10 mA·s par projection pour (c), où la colonne de gauche représente la base de PMMA, la colonne du milieu le fer, et la colonne de droite le potassium.

La Figure 18 est une illustration complète des erreurs moyennes des concentrations de fer identifiées (dans le mélange) avec tous les différents paramètres d'acquisition. L'erreur de quantification tend à diminuer pour le fer de plus grande concentration. Des performances optimales peuvent être observées pour 200 mg/cc de fer, avec un facteur d'exposition de 100 mA·s, ce qui signifie que l'amélioration de la quantification grâce à un facteur d'exposition plus élevé a une influence majeure, même si le nombre de bandes augmente.

La Figure 19 représente les CNR des images de fer décomposées pour 100 mg/cm<sup>3</sup> de fer. Il est clair que le CNR dépend largement du facteur d'exposition et bénéficie d'un

facteur d'exposition plus élevé. Pour le même facteur d'exposition, le CNR varie en fonction du nombre de bandes d'énergie. Nous pouvons observer que pour un facteur d'exposition plus faible, les performances de décomposition s'améliorent pour un nombre plus faible de bandes d'énergie. Par exemple, lorsque le facteur d'exposition est de 0.025 mA·s, 6 bandes d'énergie conduisent au CNR le plus élevé. Lorsque le facteur d'exposition augmente jusqu'à 100 mA·s, le nombre de bandes d'énergie a peu d'influence sur les performances de CNR.

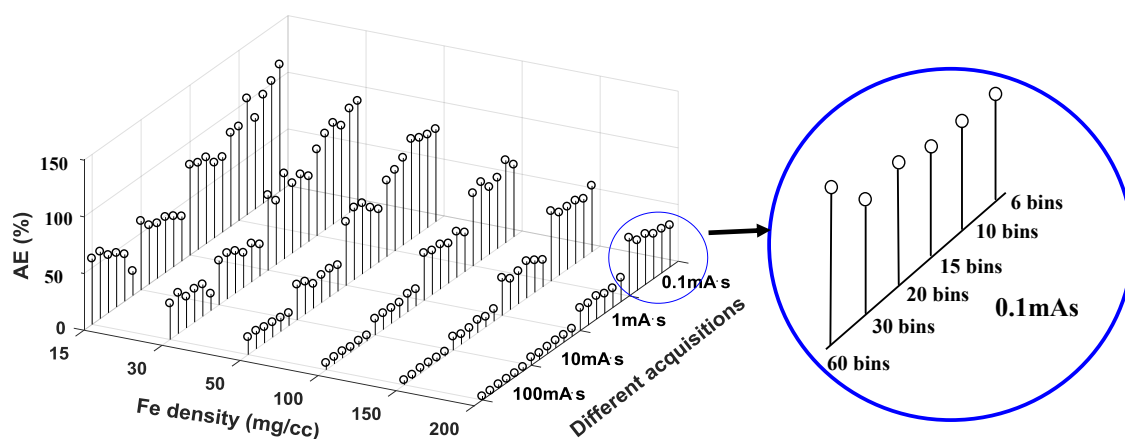


Figure 18: Erreurs moyennes (AE) des concentrations de fer décomposé (dans le mélange) en utilisant la méthode proj-PR-LLS. L'axe des X représente 4 groupes d'acquisitions correspondant à 4 facteurs d'exposition différents  $F$ , dans chacun desquels sont indiqués 6 nombres  $N$  de bandes d'énergie différents: par exemple, pour le groupe supérieur droit,  $(F, N) = (0.1, 6), (0.1, 10), (0.1, 15), (0.1, 20), (0.1, 30), (0.1, 60)$ , puis  $(1, 6), (1, 10), (1, 15)$ , et ainsi de suite. L'axe Y représente différentes concentrations de fer. Les résultats de décomposition avec un facteur d'exposition de 0.025 mA·s ne sont pas présentés dans ce graphique pour des raisons de commodité de lecture.

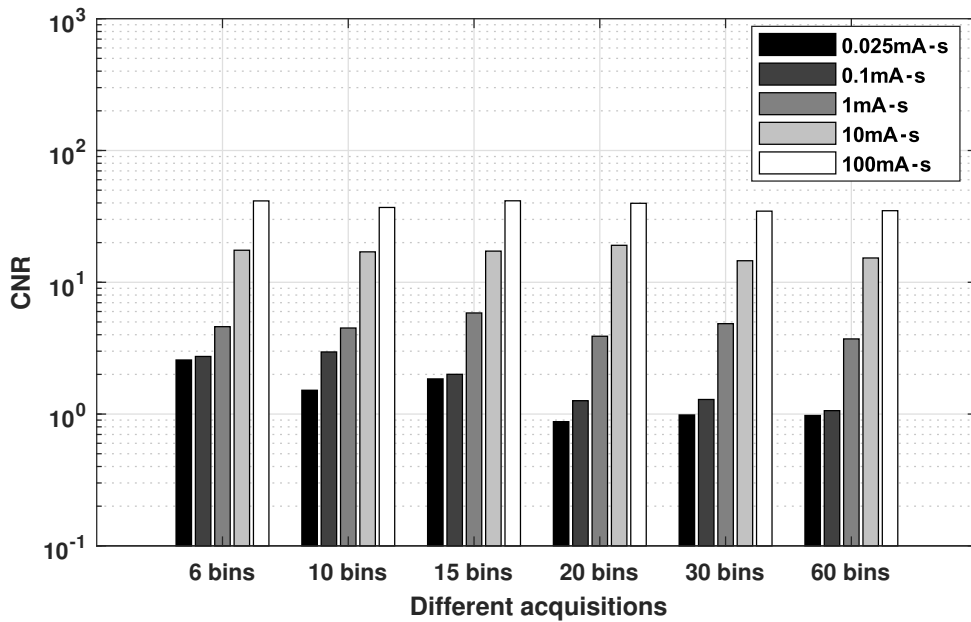


Figure 19: CNR des images de fer décomposées pour 100 mg/cc de fer avec différentes acquisitions utilisant la méthode proj-PR-LLS. Chaque groupe d'acquisitions a le même nombre de bandes d'énergie mais des facteurs d'exposition différents.

#### 4.2.2 Méthode ima-PR-LS

Pour la méthode ima-PR-LS, nous choisissons l'eau, le potassium et le fer comme matériaux de base. Le paramètre de relaxation  $r$  est défini à 1 et la taille de chaque zone pour la régularisation est  $5 \times 5$ . Avec divers paramètres d'acquisition, les résultats de la simulation montrent qu'avec la méthode de décomposition ima-PR-LS, le fer ne peut être séparé du calcium et du potassium que lorsque le nombre de bandes est 60. Nous montrons sur la Figure 20 une décomposition qui a échoué (a)  $N = 6$ , et  $F = 1$  mA·s, et une décomposition réussie (b) lorsque  $N = 60$ , et  $F = 10$  mA·s.

On observe à partir de la Figure 20 (a) que dans l'image à base de fer (milieu), on peut non seulement observer les deux rangées d'inserts qui contiennent réellement du fer, mais aussi les rangées d'inserts contenant du calcium et du potassium qui ne devraient être présents que dans l'image de base de potassium, alors que l'image de base de potassium (à droite) porte à peine l'information. La Figure 20 (b) montre les résultats de la décomposition lorsque  $N = 60$ , and  $F = 10$  mA·s. Une différence évidente peut être observée par rapport à (a). Seulement les deux rangées d'inserts existent dans l'image de base de fer (au milieu), représentant le fer dans le mélange et dans l'eau; tandis que dans l'image du potassium (à droite), les inserts contenant du calcium et du potassium sont bien mis en évidence.

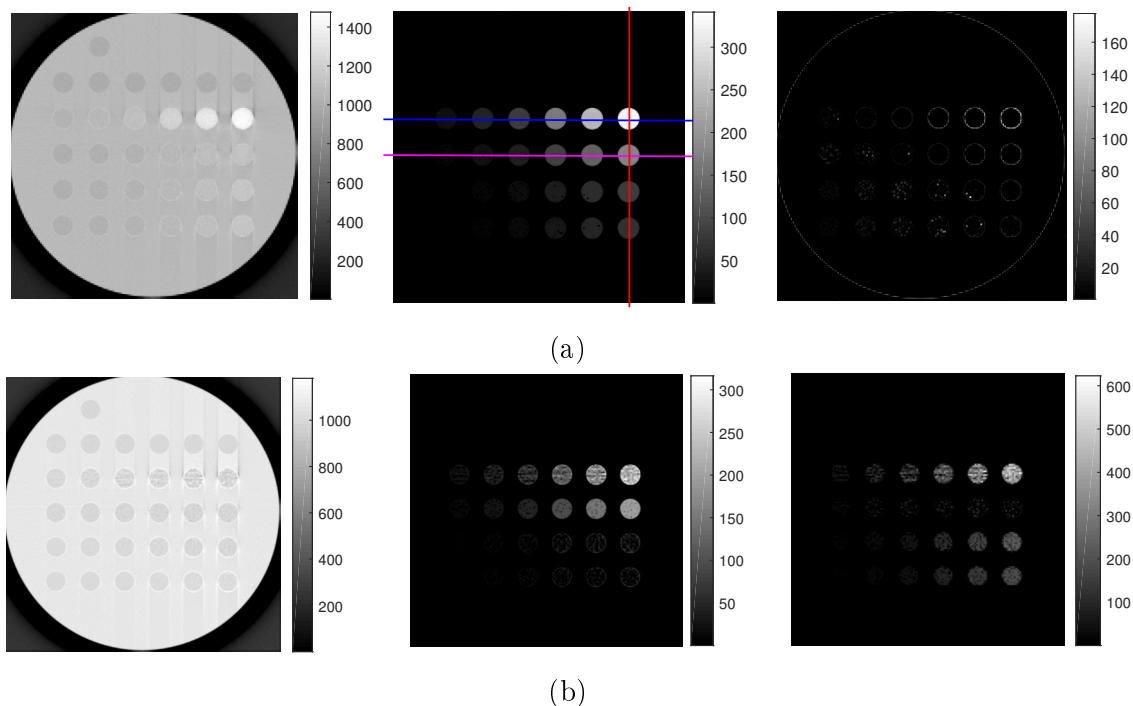


Figure 20: Densité décomposée en unité de  $\text{mg} / \text{cc}$  de base d'eau (colonne de gauche), base de fer (colonne du milieu) et base de potassium (colonne de droite) avec la méthode ima-PR-LS. Paramètres d'acquisition des données: 6 bandes d'énergie, 1  $\text{mA}\cdot\text{s}$  par projection (a), et 60 bandes d'énergie, 10  $\text{mA}\cdot\text{s}$  par projection (b).

Les losanges rouges de la Figure 21 représentent les erreurs moyennes de la concentration de fer identifiée avec des acquisitions de 60 bandes d'énergie et divers facteurs d'exposition en utilisant la méthode ima-PR-LS (on reporte également les valeurs obtenues avec les mêmes paramètres et la méthode proj-PR-LLS déjà représentées à la figure 18 pour comparaison). La précision de la quantification a été améliorée avec l'augmentation du facteur d'exposition et de la concentration du fer. Avec l'acquisition de 100  $\text{mA}\cdot\text{s}$  par projection, l'erreur moyenne de la teneur estimée en fer varie de 35.6% à 9.0% pour les concentrations de 15  $\text{mg}/\text{cc}$  à 200  $\text{mg}/\text{cc}$ . Le CNR des images de fer décomposées pour 100  $\text{mg} / \text{cc}$  de fer varie de 14.1 à 326.0 en augmentant l'exposition dans l'ordre, tandis que les CNR obtenus pour la même acquisition en utilisant la méthode proj-PR-LLS varient de 1.0 à 35.0, Figure 22. Nous pouvons observer qu'avec 60 bandes d'énergie, la méthode ima-PR-LS présente des erreurs moyennes comparables avec la méthode proj-PR-LLS, mais avec des CNR beaucoup plus élevés.

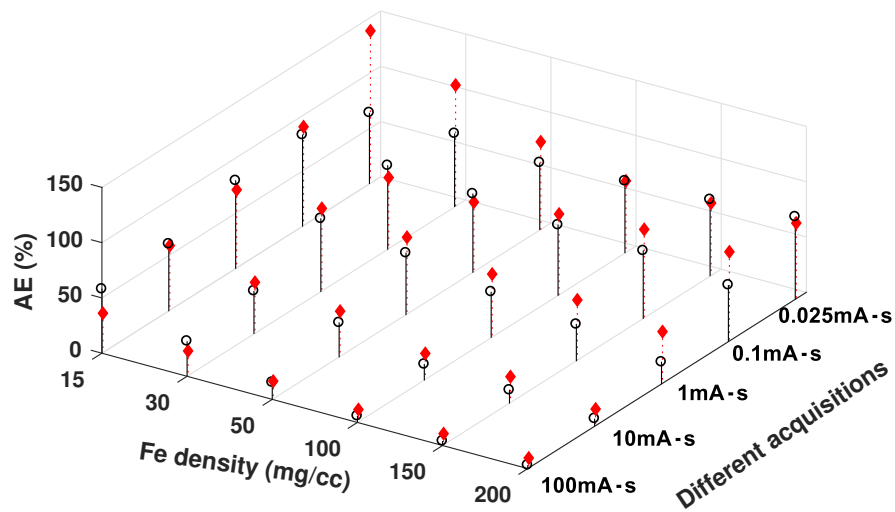


Figure 21: Comparaison des erreurs moyennes des images de fer décomposées obtenues en utilisant la méthode proj-PR-LLS (cercles noirs) et la méthode ima-PR-LS (losanges rouges). Toutes les acquisitions comportent 60 bandes d'énergie mais des facteurs d'exposition différents.

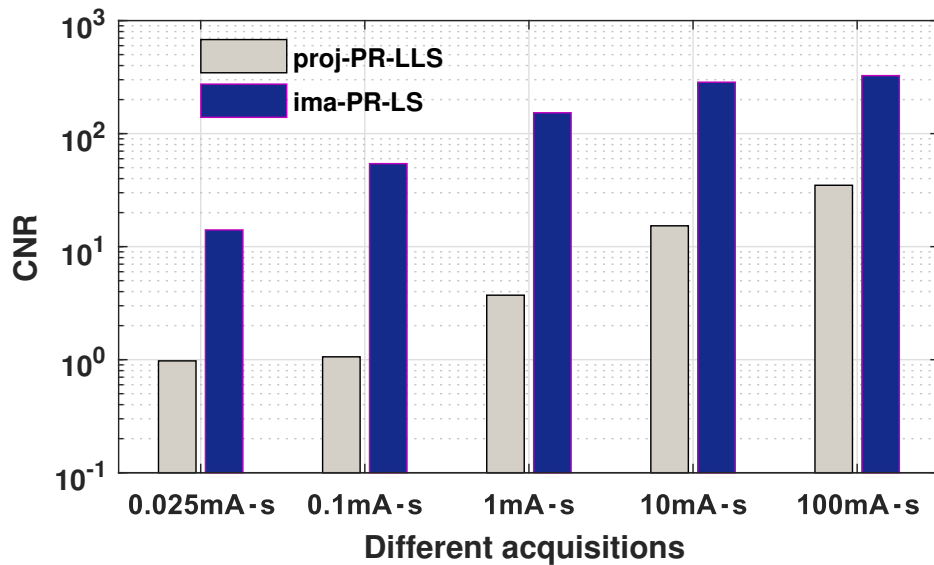


Figure 22: Comparaison CNR des images de fer décomposées pour 100 mg/cc de fer obtenues en utilisant la méthode proj-PR-LLS et la méthode ima-PR-LS. Toutes les acquisitions comportent 60 bandes d'énergie mais des facteurs d'exposition différents.

### 4.3 Conclusion et discussions

Les deux méthodes proj-PR-LLS et ima-PR-LS pour CT spectrale sont capables de discriminer et de quantifier le fer du calcium, du potassium et de l'eau dans certaines conditions. Leurs performances varient avec les paramètres d'acquisition du CT spectral. On peut choisir d'utiliser l'une des deux méthodes selon les contraintes d'acquisition: si le nombre de bandes est important (60 par exemple), on suggère la méthode ima-PR-LS pour la détermination du fer en raison de son CNR plus élevé; sinon, nous suggérons la méthode proj-PR-LLS.

Certains points de la présente étude pourraient être améliorés. Nous avons étudié l'influence du nombre de bandes d'énergie sur la performance de décomposition, au cours de laquelle les bandes étaient supposées uniformément réparties dans la gamme d'énergie de détection. Cependant, la largeur et le placement de chaque bande d'énergie peuvent également influencer la performance de la décomposition du matériau, et ils peuvent être étudiés dans le futur. De même on a fixé la tension maximale du spectre à 100 kVp mais son influence pourrait également être étudiée.

## 5 Conclusion et perspectives

### 5.1 Conclusion

Dans cette thèse, nous avons étudié les méthodes quantitatives de décomposition des matériaux pour la CT spectrale. Les contributions principales du présent travail se concentrent autour de trois aspects: (1) l'étude des méthodes de décomposition en matériaux pour la CT spectrale; (2) validation et évaluation des méthodes proposées par simulation d'applications médicale et industrielle; (3) l'étude de l'influence de différents paramètres d'acquisition, i.e. le facteur d'exposition et le nombre de bandes d'énergie, sur les performances de décomposition.

Avant de commencer ces travaux, nous avons passé en revue les principes de base de la CT spectrale au Chapitre 2. En utilisant le fait que les matériaux ont différentes propriétés d'atténuation des rayons X, un système CT prend des mesures de projections intégrales d'une ligne d'un objet sous différents angles, puis reconstruit l'image en coupe transversale 2D grâce à des calculs mathématiques complexes (respectivement des projections 2D et un volume 3D reconstruit). Les scanners CT conventionnels sont équipés de détecteurs d'intégration d'énergie qui fournissent des informations intégrées de tout le faisceau transmis, tandis que le CT spectral utilise des détecteurs de comptage de photons et est capable d'obtenir des informations spectrales de plusieurs bandes d'énergie avec une seule acquisition. La CT spectrale permet de surmonter de nombreuses limitations des



techniques précédentes et ouvre de nombreuses applications nouvelles, parmi lesquelles la décomposition quantitative des matériaux est le sujet le plus étudié.

Connaissant les principes généraux de la CT spectrale, nous avons mis en place le présent travail en suivant les trois aspects mentionnés ci-dessus:

(1) Méthodes de décomposition des matériaux (Chapitre 3).

Nous avons examiné les méthodes de décomposition des matériaux existantes en deux catégories: les méthodes basées sur les effets et les méthodes basées sur les matériaux. Notre travail était autour de cette dernière famille, où le coefficient d'atténuation linéique est décrit comme les contributions d'une base de matériaux. Par ailleurs, selon le type de données sur lequel l'étape de décomposition fonctionne, nous avons la méthode du domaine des projections et la méthode du domaine de l'image reconstruite. La décomposition couramment utilisée est basée sur le critère des moindres carrés, nommée proj-LS et méthode ima-LS. Cependant, le problème inverse de la décomposition du matériau est généralement mal posé et les mesures de la CT spectrale aux rayons X souffrent de bruits de comptage de photons de Poisson. Le critère LS standard peut conduire à un sur-ajustement des données de mesure bruitées. Nous avons proposé un critère de moindre log-carré pour la méthode du domaine des projection afin de minimiser les erreurs sur le coefficient d'atténuation linéique: méthode proj-LLS. De plus, pour réduire l'effet du bruit et lisser les images, nous avons proposé d'ajouter un terme de régularisation par zones (patch regularisation PR) pour pénaliser la somme des variations carrées dans chaque zone, appelées proj-PR-LLS et ima-PR-LS.

(2) Validation et évaluation par simulation (Chapitre 4).

La performance des méthodes de décomposition de matériaux dans le domaine des projections proposées a été validée par l'imagerie spectrale à rayons X simulée. La simulation a été réalisée avec le logiciel VXI pour des applications médicale et industrielle:

- Application médicale: identification de l'iode et du calcium. Pour distinguer les compositions de la plaque d'athérosclérose, nous avons simulé l'imagerie par CT spectrale d'un fantôme thoracique humain avec les bruits réalistes. Des solutions supplémentaires de calcium et d'iode avec différentes concentrations ont été placées à l'intérieur du fantôme. Trois méthodes de décomposition ont été étudiées: proj-LS, proj-LLS et proj-PR-LLS. En décomposant les données d'acquisition en trois matériaux de base: l'iode, le calcium et le tissu mou, toutes les méthodes peuvent obtenir des distributions de densité des matériaux de

base correspondants. Cependant, la méthode proj-LLS proposée et la méthode proj-PR-LLS ont une meilleure précision quantitative et une meilleure qualité d'image que la méthode proj-LS communément utilisée en fonction de leurs erreurs moyennes et des CNR.

- Application industrielle: tri plastique ABS-RF. Bien que nous ayons discuté des méthodes de décomposition basées sur l'imagerie CT spectrale, il est vrai que les méthodes de décomposition dans le domaine des projections peuvent être appliquées pour l'imagerie par radiographie (CR) spectrale. Dans ce cas, nous avons étudié la capacité de décomposition en matériaux de la méthode proj-PR-LLS proposée pour l'imagerie CR spectrale dans l'identification de différents matériaux ABS-RF (RF: RF bromé, RF chloré et RF phosphoré). Les résultats montrent que la décomposition directement dans la base 3-matières (ABS + Br + Cl) n'est pas assez robuste au bruit. Pour améliorer la performance, nous avons proposé une méthode proj-PR-LLS-clas qui ajoute une étape de la classification à la procédure de décomposition. L'idée de classification est basée sur cette application spécifique car en réalité, chaque matière plastique ne contient qu'un seul type de RF. Par conséquent, il est raisonnable de décomposer d'abord en deux matériaux (ABS + Br et ABS + Cl), puis de choisir celui ayant la valeur de fonction coût plus petite comme résultat final. Cette méthode a amélioré la séparation entre Br et Cl par rapport à la méthode proj-PR-LLS. Pour la simulation avec les bruits réalistes, lorsque l'épaisseur du fantôme est favorable, l'ABS et les RF contenant Br, Cl et P peuvent être identifiés en même temps.

### (3) Influence de différents paramètres d'acquisition (Chapitre 5).

Nous avons simulé l'imagerie par CT spectrale d'un fantôme de PMMA avec des solutions de Fe, Ca et K à différentes concentrations pour étudier l'influence du facteur d'exposition et du nombre de bandes d'énergie sur la performance de la décomposition en matériaux. Les simulations ont été effectuées dans diverses conditions d'acquisition en faisant varier le nombre de bandes d'énergie ( $N = 6, 10, 15, 20, 30$  et  $60$ ) et les facteurs d'exposition par projection ( $F = 0,025, 0,1, 1, 10$  et  $100$  mA·s). Les performances de la méthode proj-PR-LLS et de l'ima-PR-LS ont été étudiées.

La méthode de décomposition de Proj-PR-LLS nous a permis de discriminer le fer du calcium, du potassium et de l'eau dans toutes les conditions. Selon le graphique du CNR, pour un facteur d'exposition plus faible, les performances de décomposition tendent à bénéficier d'un nombre inférieur de bandes d'énergie. La méthode de décomposition Ima-PR-LS est beaucoup plus sensible au nombre de classes d'énergie

que la méthode proj-PR-LLS. Le fer dans le mélange n'a pas été séparé du calcium et du potassium quand  $N = 6, 10, 15, 20$  et  $30$ . Le seul cas réussi est apparu quand  $N = 60$ .

En conclusion, les deux méthodes proj-PR-LLS et ima-PR-LS pour la CT spectrale sont capables de discriminer et de quantifier le fer du calcium, du potassium et de l'eau dans certaines conditions. Leurs performances varient avec les paramètres d'acquisition du CT spectral. On peut choisir d'utiliser l'une des deux méthodes selon les contraintes d'acquisition: si le nombre de bandes est important (60 par exemple), on suggère la méthode ima-PR-LS pour la détermination du fer en raison de son CNR plus élevé; sinon, nous suggérons la méthode proj-PR-LLS.

## 5.2 Perspectives

Nous avons présenté dans les parties précédentes la performance de décomposition des méthodes proposées et l'influence de différents paramètres d'acquisition à travers des validations simulées. Dans cette section, plusieurs améliorations potentielles seront discutées comme suit.

- Sur la simulation.

L'efficacité d'absorption du détecteur de comptage de photons à base de CdTe a été simulée dans le présent travail. Cependant, notre simulation a supposé une résolution d'énergie de détecteur parfaite de sorte que tous les photons puissent être comptés correctement dans la bande d'énergie correspondante. En pratique, la fonction de réponse du détecteur du faisceau monochromatique a un large spectre et la résolution en énergie est limitée. Par conséquent, la résolution énergétique du détecteur devrait être prise en compte dans le futur.

- Sur les méthodes de décomposition.

- Nous avons utilisé la reconstruction FBP tout au long du présent travail pour des raisons de coût de calcul. Cependant, la reconstruction itérative a le potentiel de réduire le bruit et d'améliorer la qualité de l'image. Il sera intéressant de remplacer la reconstruction FBP par la méthode itérative si la condition de temps de calcul est autorisée.

- Pour les méthodes régularisées par zone proposées (proj-PR-LLS et ima-PR-LS), plusieurs paramètres doivent être choisis: taille de patch ( $np_r \times np_c$ ) et paramètre de relaxation ( $r$ ) Nous avons utilisé une taille de zone unique pour chaque application, et son influence sur la performance de décomposition doit

être étudiée. Quant à  $r$ , il a été choisi visuellement, sauf pour l'application du tri plastique, où nous avons appliqué la méthode de la courbe en L à une certaine région sur les images radiographiques, et utilisons le  $r$  approché pour toutes les zones. Cependant,  $r$  devrait changer pour différentes zones puisque le niveau de bruit varie. Par conséquent, une amélioration supplémentaire doit être effectuée pour la sélection du paramètre de relaxation par zone.

- Validation expérimentale.

L'évaluation des méthodes proposées dans cette thèse est basée sur l'imagerie spectrale à rayons X simulée, qui est différente des données expérimentales réelles. Une validation expérimentale supplémentaire sera envisagée dans les travaux futurs.



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# Chapter 1

## General introduction

### Contents

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## 1.1 Problem statement and objective

X-ray computed tomography (CT) is first introduced in the 1970s by Cormack and Hounsfield, for which they were awarded the Nobel Prize for Physiology or Medicine in 1979. This invention showed the possibility to invasively give high quality cross-sectional images of object with multiple-angle measurements and more or less complex computations. Afterwards, the advancement of X-ray CT has greatly benefited from developed reconstruction algorithms, advanced computer technology and technological improvements of detectors and sources. It now has wide applications in medical, industrial, material, aerospace and geology fields.

It is known that the conventional CT with single X-ray tube and energy integrating detector measures the total attenuation of an object over the entire spectrum. However, various compositions of object respond differently to a particular energy of the incoming radiation. Making use of such property, we can distinguish different components of the object. In the past years, numerous technologies of X-ray CT have been proposed, including dual-energy CT (DECT) and spectral CT. DECT has limited ability in material decomposition by producing two data sets corresponding to two different x-ray spectra. In contrast, spectral CT employs photon counting detectors (PCDs) to obtain more complete spectral information: the transmitted photons can be discriminated corresponding to selected energy bins with one single acquisition. In this way, multiple materials can be simultaneously identified. A number of material decomposition methods have been reported and different experimental systems are under development for spectral CT. However, most researches focus on the imaging of contrast agents with high atomic numbers ( $Z$  number), such as iodine, gadolinium and gold, which have unique K-edges within detection energy range. It is much more difficult to distinguish those having low atomic numbers, especially when their  $Z$  numbers are close.

Some of the material decomposition methods proposed for spectral CT imaging can also be applied to PCD-based spectral computed radiography (CR). Targeting on one medical application of spectral CT (atherosclerosis imaging) and one industrial application of spectral CR (plastic sorting), our objective is to develop material decomposition methods to improve the imaging quality of these two applications:

- Medical application: atherosclerosis imaging. Atherosclerosis is a disease in which the inside artery narrows due to the build-up of plaques. Plaques inside the coronary arteries are a serious risk factor for adverse cardiovascular events. The ruptures of vulnerable plaques are the cause of about 70 % of fatal acute myocardial infarctions and sudden coronary deaths. Discrimination of plaque compositions is very important in the identification of high-risk plaques.
- Industrial application: plastic sorting. Waste electrical and electronic equipments (WEEE) have been increasing rapidly due to the development of electronic industry. They contain various compositions among which polymers occupy an important part. Due to the presence of electronic power of electrical and electronic equipment (WEEE), the plastic materials should meet high fire safety standards. However, it is not possible to realize with pure polymers, therefore flame retardant (FR) are added to change flammability of plastics and increase the fire resistance. Recycling of plastics from WEEE is challenging because of the existence of FRs (especially

the brominated and chlorinated FRs), which might result in serious environmental pollution. Therefore, the sorting technique is important for subsequent treatment and recycling of WEEE to avoid major environmental and health problems.

At this primary stage of the proposed new research, it is hard to obtain the experimental data due to the non-existence of physical or commercial spectral CT systems. Simulation is then an efficient, cost-effective and feasible way to address the problem. Therefore, we will study the material decomposition methods, evaluate their performance through simulations in view of the above-mentioned applications, and further investigate the influence of different acquisition parameters on material decomposition performance.

## 1.2 Main contributions

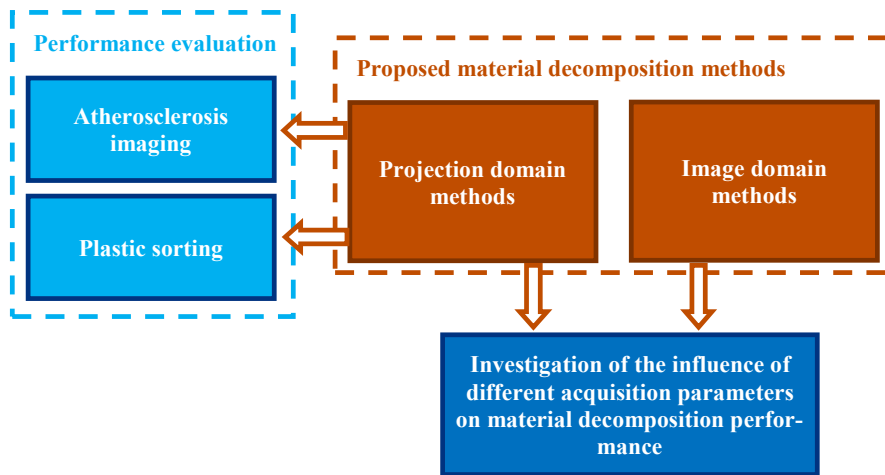


Figure 1.1: Contributions of the present work.

The main contributions of this thesis include: the proposal of new material decomposition methods, the validation and assessment of the proposed methods through simulated spectral CT or CR imaging, and the investigation of the influence of different acquisition parameters on material decomposition performance, as illustrated in Figure 1.1. In the following, we detail the contributions following the three aspects.

- Material decomposition methods (Chapter 3).
  - General understanding. Making use of multi-energy information, spectral CT has the potential to discriminate different components inside the object. Many material decomposition methods have been proposed and different experimental spectral CT systems are under development. According to the type of data on which the decomposition step operates, the methods can be divided into projection domain method and image domain method. The former, also called pre-reconstruction decomposition method, firstly decomposes projection data

into several desired components (i.e. materials), and then applies independently reconstruction to each component to obtain their respective distribution in space. The latter, also known as post-reconstruction method, operates on conventionally reconstructed CT images corresponding to different energy bins and it obtains the concentration of target materials using linear matrix inversion.

- Proposed methods. The commonly used objective function to solve this problem is based on least squares criterion, which minimizes the errors between expected and measured number of photons (projection domain method) or the errors between expected and reconstructed attenuation coefficients (image domain method). However, the inverse problem of material decomposition is usually ill-posed and the X-ray spectral CT measurements suffer from Poisson photon counting noises. The standard least squares objective function can lead to overfitting to the noisy measurement data. Therefore, we have proposed a least log-squares criterion for projection domain method to minimize the errors on linear attenuation coefficient. Furthermore, we have proposed to add a regularization term to penalize the sum of the square variations of the decomposed images, in order to reduce the effect of noise and enforce smoothness. The proposed patchwise regularized method is applied to both projection domain and image domain decomposition.
- Validation and assessment via simulation (Chapter 4).
  - Simulation of spectral X-ray imaging. Virtual X-ray imaging (VXI) software is used to simulate the spectral X-ray CT and CR imaging of specific phantoms. The simulation is based on ray-tracing techniques together with the X-ray attenuation law.
  - Medical application. A realistic computational human thorax phantom has been built for the simulation of spectral CT imaging. Three projection domain methods, including the proposed ones, have been applied for the identification of soft tissue, iodine and calcium. Their performance are compared in terms of the average error and contrast-to-noise ratio.
  - Industrial application. The spectral CR imaging of a phantom with multiple cubes containing different plastic materials has been simulated. We have used the proposed decomposition methods to identify the type of flame retardant contained in each cube in order to achieve plastic sorting.
- Influence of different acquisition parameters (Chapter 5).

We have investigated the influence of different acquisition parameters, i.e., exposure factor and the number of energy bins, on material decomposition performance through a phantom study for iron determination. We have simulated spectral CT imaging of the phantom with different settings of exposure factor (0.025, 0.1, 1, 10 and 100 mA·s per projection) and number of energy bins (6, 10, 15, 20, 30 and 60), and have compared the material decomposition performance of image domain and projection domain methods with the simulated data.

### 1.3 Organization of thesis

The thesis manuscript is organized as follows:

In Chapter 2, entitled “**General principles of spectral CT**”, the principles of the interactions of X-rays with matter are introduced, including photoelectric absorption, Compton scattering and pair production; the principles of X-ray CT are described, including conventional energy integrated CT, dual-energy CT and spectral CT.

In Chapter 3, entitled “**Material decomposition methods**”, a review of the existing material decomposition methods for spectral CT is presented. Based on the existing methods, we have proposed patchwise regularized decomposition methods in both projection domain and image domain.

In Chapter 4, entitled “**Material decomposition results for different applications: phantoms study**”, the X-ray spectral imaging simulation procedure is detailed and the decomposition results of proposed methods are demonstrated through phantom study for both medical and industrial applications.

In Chapter 5, entitled “**Exploring the influence of different acquisition parameters**”, a series of spectral CT acquisitions have been simulated with different parameters and the influence of these parameters on material decomposition performance of the proposed methods is investigated.

In Chapter 6, entitled “**Conclusion and perspectives**”, a brief summary of the main results, the conclusions and future perspectives are presented.



## Chapter 2

# General principles of spectral CT

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## 2.1 Interactions of X-rays with matter

In 1895, the German physicist Röntgen was investigating the glow that occurred during electric discharges inside an evacuated glass tube. During his experiments, he was surprised to notice that a screen coated with crystals of barium platinocyanide started to glow. The screen happened to be in his laboratory for the detection of ultraviolet radiation. In the following days, he carried out a series of tests and finally confirmed the existence of the mysterious rays [Cierniak, 2011]. He published his discovery in 1896 [Röntgen, 1896] with an enclosed X-ray picture of the hand of his wife Bertha (Figure 2.1), which clearly showed her bones in fingers and the wedding ring. His publication showed the possibility of non-invasive imaging of internal features and soon spread over the world. A lot of research was carried out on X-rays quickly and devices were built to take X-ray pictures. To reward this remarkable discovery, Röntgen was awarded the first Nobel Prize in Physics.

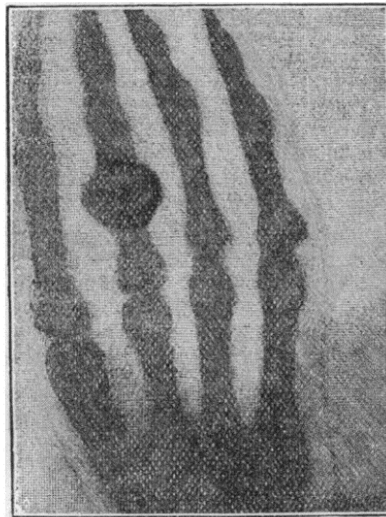


Figure 2.1: The X-ray picture of the hand of Röntgen's wife, retrieved from his original publication [Röntgen, 1896].

X-ray is a form of electromagnetic radiation that has extremely short wavelength and high frequency. Most X-rays have a wavelength ranging from 0.01 to 10 nanometers, corresponding to frequencies in the range about  $10^{16}$  to  $10^{20}$  Hz and energies in the range about 10 eV to 100 MeV. Figure 2.2 shows the wavelength, frequency and energy of electromagnetic spectrum. It can be observed that X-rays have high energy among the spectrum.

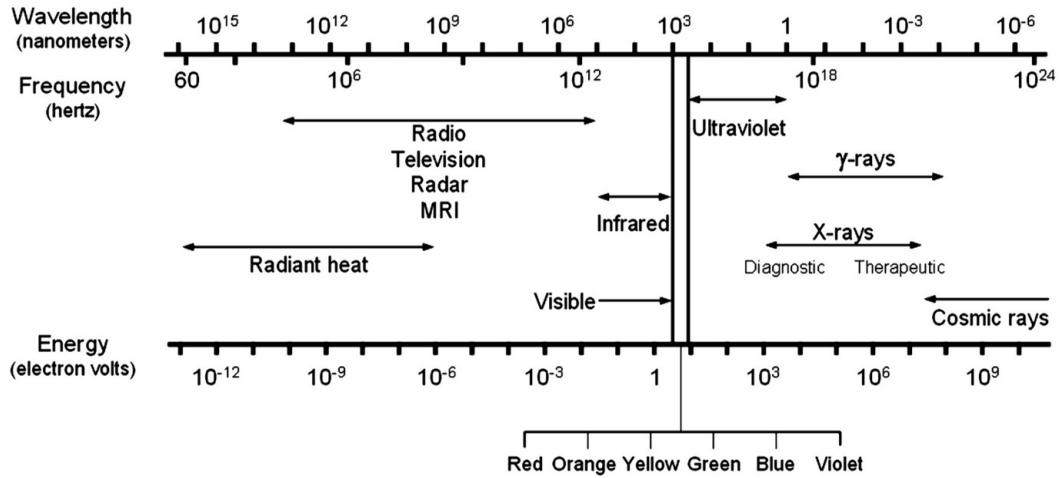


Figure 2.2: The electromagnetic spectrum, presented as a function of wavelength, frequency, and energy, retrieved from [Seibert, 2004].

The X-ray imaging approaches, including X-ray radiography and CT are based on the principle that the primary beam attenuates when it passes through the object. The number of photons decreases progressively in this process. According to Beer-Lambert law, the attenuation of a monochromatic X-ray beam in a homogeneous medium can be expressed as:

$$\Phi(x) = \Phi_0 \exp(-\mu x), \quad (2.1)$$

where the  $\Phi_0$  is the primary X-ray photon fluence,  $\Phi(x)$  is the attenuated photon fluence with respect to traveling distance of  $x$  in the medium,  $\mu$  is the linear attenuation coefficient.

Another important parameter mass attenuation coefficient  $\mu_m$ , is defined by:

$$\mu_m = \mu / \rho, \quad (2.2)$$

where  $\rho$  is material density.  $\mu_m$  has unit of centimeters squared per gram. Each element has its unique mass attenuation coefficient curve, making it possible to distinguish different components of a mixture object.

There are three principal X-ray interactions with matters that account for the total attenuation. They are photoelectric absorption  $\mu^{\text{pe}}$ , Compton scattering  $\mu^{\text{C}}$ , and pair production  $\mu^{\text{pp}}$  [Barrett and Swindell, 1996]. In fact, there is another effect that occurs when the X-ray interacts with the matter: Rayleigh scattering, also known as coherent scattering. It is an elastic interaction between a photon and an atom, where the photons direction is changed by a small angle but its energy is not. The scattered photons are mainly in the forward direction and the probability of this event occurring is low. Therefore it has little effect on the attenuation coefficient. Thus the overall attenuation coefficient  $\mu^{\text{tot}}$  and  $\mu_m^{\text{tot}}$  can be considered as the sum of photoelectric absorption, Compton scattering and pair production:

$$\mu^{\text{tot}} = \mu^{\text{pe}} + \mu^{\text{C}} + \mu^{\text{pp}}, \quad (2.3)$$

and

$$\mu_m^{\text{tot}} = \mu_m^{\text{pe}} + \mu_m^{\text{C}} + \mu_m^{\text{pp}}. \quad (2.4)$$



The following sections will introduce the detailed mechanism of photoelectric absorption, Compton scattering and pair production.

### 2.1.1 Photoelectric absorption

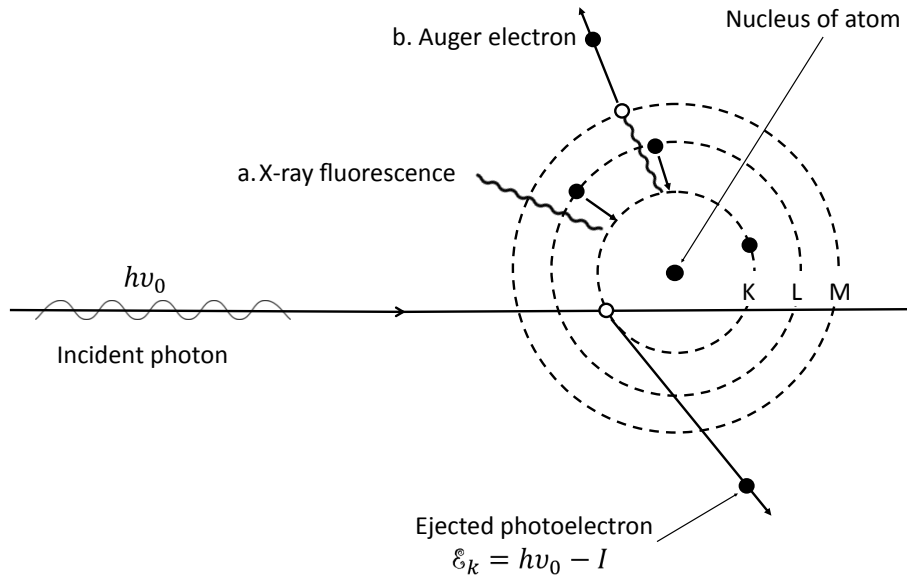


Figure 2.3: During the photoelectric event, the incident photon is annihilated. Part of its energy is consumed by ionization of atom and the rest is given to ejected photoelectron as its kinetic energy. The transfer of electron from outer shell to inner shell to fill in the vacancy created by photoelectron will generate either a. X-ray fluorescence, or b. Auger electron. Figure is inspired by [Barrett and Swindell, 1996].

In photoelectric effect, the incident photon with energy of  $h\nu_0$  interacts with a target atom, its energy is totally absorbed by the atom by ionization and imparting kinetic energy  $\mathcal{E}_k$  to the ejected photoelectron:

$$h\nu_0 = \mathcal{E}_k + I, \quad (2.5)$$

where  $I$  is the ionization potential, also called binding energy needed for a particular electron to be involved in a photoelectric event. Photoelectric interaction will occur only when the incident photon has energy that is equal to or greater than  $I$ . A photon having an energy just above the binding energy of the electron is more likely to be absorbed than a photon having an energy just below this binding energy, causing a sudden change in the attenuation coefficient of the atom, called "edge". A K-shell interaction is approximately four to five times more probable than an L-shell interaction if both interactions are energetically allowed.

As analyzed in the above, when the photoelectric event occurs, a vacancy is created in the particular shell, which makes the electronic structure of the atom unstable. The electron from outer shell will transfer to fill this vacancy and create characteristic X-ray

lines. The energy of the line is equal to the difference in binding energies of the two shells. This will generate either X-ray fluorescence or an Auger electron (by transferring the energy of X-ray line to another electron which is then emitted).

The linear attenuation contributed by photoelectric absorption  $\mu^{\text{pe}}$  is given by experiments as:

$$\mu^{\text{pe}} \approx k \frac{Z^m}{(h\nu_0)^n} \frac{\rho}{A}, \quad (2.6)$$

where  $k$  is a constant depending on the shell involved,  $Z$  is the atomic number and  $A$  is the atomic weight,  $m$  and  $n$  are parameters that varies slowly with  $Z$  and  $\nu_0$ . A useful estimation for parameter  $m$  and  $n$  is given as  $m = 4$  and  $n = 3$ , making Equation (2.6) into

$$\mu^{\text{pe}} = k \frac{Z^4}{(h\nu_0)^3} \frac{\rho}{A}. \quad (2.7)$$

We can see that  $\mu^{\text{pe}}$  increases with atomic number and material density and is negatively related with energy of incident photon.

### 2.1.2 Compton scattering

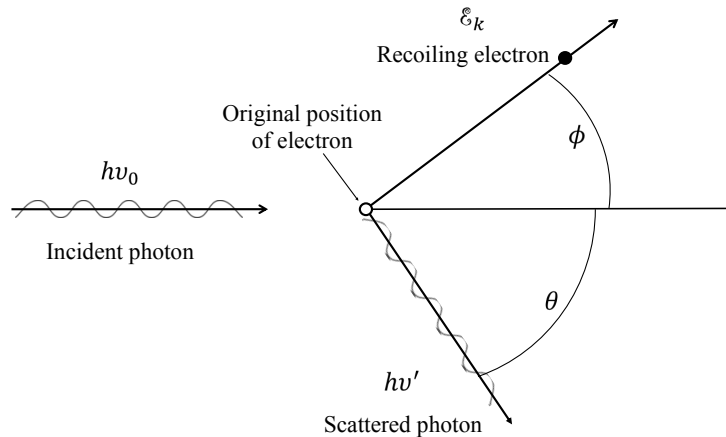


Figure 2.4: The mechanism of Compton scattering: incident photon is scattered, its energy and direction change and a recoiling electron is ejected. Figure is inspired by [Barrett and Swindell, 1996].

When the incident photon has energy that is much more than the binding energy, Compton scattering occurs. In Compton effect, the incident photon is scattered by a free electron. It deviates from the original direction by angle  $\theta$  and passes part of energy  $\mathcal{E}_k$  to the recoiling electron, recoil angle noted as  $\phi$  (See Figure. 2.4 ).

With  $\alpha = h\nu_0/m_0c^2$  ( $m_0c^2 = 0.511\text{meV}$ ), the scattered photon with the remaining energy  $h\nu'$  can be given by:

$$h\nu' = h\nu_0(1 + \alpha - \alpha\cos\theta)^{-1}. \quad (2.8)$$

Collision cross section  $\sigma$  is defined as the cross sectional area presented by the attenuating material to the incident beam. It describes the probability that an incident photon will experience a collision with material, and furthermore be attenuated. The relationship between collision cross section and linear attenuation coefficient can be expressed as:  $\sigma = \mu/n$ ,  $n$  is the number of attenuating particles per cubic centimeter.

$$\mu = \sigma n. \quad (2.9)$$

Klein and Nishina firstly deduce the formula of collision cross section for Compton scattering  $\sigma^C$ :

$$f_{\text{KN}} = \frac{\sigma^C}{\sigma_0} = \frac{3}{4} \left[ \frac{2(1+\alpha)^2}{\alpha^2(1+2\alpha)} + \frac{\ln(1+2\alpha)}{\alpha} \left( \frac{1}{2} - \frac{1+\alpha}{\alpha^2} \right) - \frac{1+3\alpha}{(1+2\alpha)^2} \right], \quad (2.10)$$

where  $f_{\text{KN}}$  is Klein and Nishina function,  $\sigma_0 = 8\pi r_0^2$  is the cross section for classical Thomson scattering,  $r_0 = e^2/(m_0c^2) = 2.818 \times 10^{-13}\text{cm}$ .

The electron density  $n_e$  ( $\text{cm}^{-3}$ ) in terms of Avogadro's number  $N_0$  ( $6.02 \times 10^{23} \text{mol}^{-1}$ ) is:

$$n_e = N_0 \rho Z/A. \quad (2.11)$$

Assume that all atomic electrons take part in the Compton scattering, then the linear attenuation coefficient caused by Compton effect is:

$$\mu^C = n_e \sigma^C = (\sigma_0 N_0 \rho Z/A) f_{\text{KN}}. \quad (2.12)$$

It can be seen that Compton scattering correlates mainly with the density of materials, while the type of atom, especially when the atomic number is low, has little impact since  $Z/A \approx 0.5$ .

### 2.1.3 Pair production

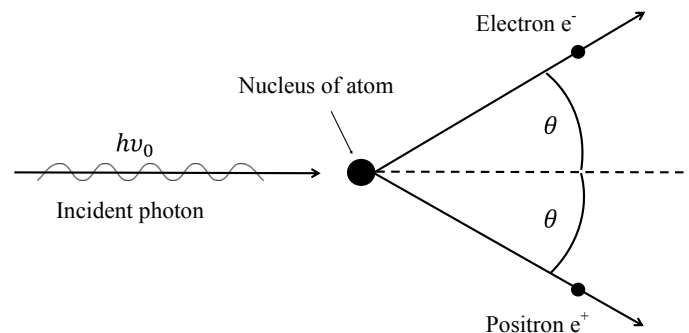


Figure 2.5: The mechanism of pair production: incident photon is annihilated, an electron-positron pair is generated. Figure is inspired by [Barrett and Swindell, 1996].

In a pair production effect, the incident photon interacts with the nucleus and convert its energy into an electron-positron pair. Suppose the kinetic energy of the electron and

positron as  $\mathcal{E}_{e^+}$  and  $\mathcal{E}_{e^-}$ , the photon must have higher energy than the sum of the rest mass energies of the electron and positron ( $2 \times 0.511\text{MeV} = 1.022\text{MeV}$ ), since:

$$h\nu_0 = \mathcal{E}_{e^+} + \mathcal{E}_{e^-} + 1.022\text{MeV}. \quad (2.13)$$

According to the complicated calculations thorough quantum electrodynamics in the form of Feynman diagrams, the collision cross section for pair production  $\sigma^{pp}$  is approximately positively related with  $Z^2$ , and it increases with the incident photon energy.

#### 2.1.4 Total attenuation coefficient

From previous analysis, the total attenuation coefficient can be considered sum of those three major interactions. It depends on the density, atomic number of materials, and also depends on the energy of incident photon. Figure. 2.6 takes water as an example to illustrate the relationship of photoelectric absorption, Compton scattering, pair production and total attenuation coefficient corresponding to photon energy.

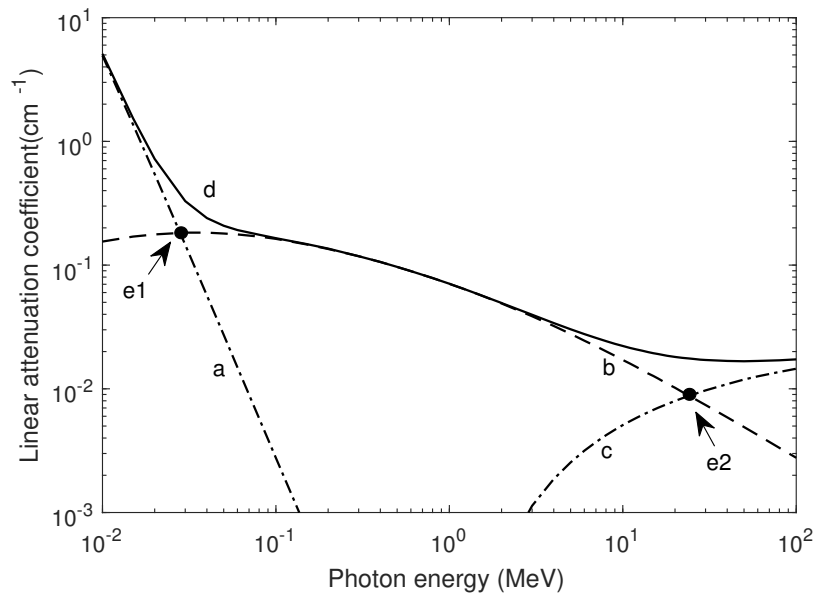


Figure 2.6: Energy dependence of linear attenuation coefficient (water): a. photoelectric absorption  $\mu^{\text{pe}}$ ; b. Compton scattering  $\mu^{\text{C}}$ ; c. pair production  $\mu^{\text{pp}}$ ; d. total attenuation coefficient  $\mu^{\text{tot}}$ . Points e1 and e2 are energies where  $\mu^{\text{pe}} = \mu^{\text{C}}$  and  $\mu^{\text{C}} = \mu^{\text{pp}}$ . Data taken from database XGAM [Berger and Hubbell, 1987].

For each atom, there is a particular energy where  $\mu^{\text{pe}} = \mu^{\text{C}}$  and another energy where  $\mu^{\text{C}} = \mu^{\text{pp}}$  (Figure. 2.6, point e1 and point e2). By plotting the relationship of atomic number and those particular energies, we can get a general view of the dominant regions of each attenuating process, see Figure. 2.7. It is observed that pair production dominates only when photon energy is extremely high, above approximately 10 Mev. For lower energy which are commonly used in diagnostic CT, photoelectric effect and Compton scattering

are the main attenuation factors. Photoelectric effect dominates most of the high-Z atoms and Compton scattering has major influence on low-Z materials.

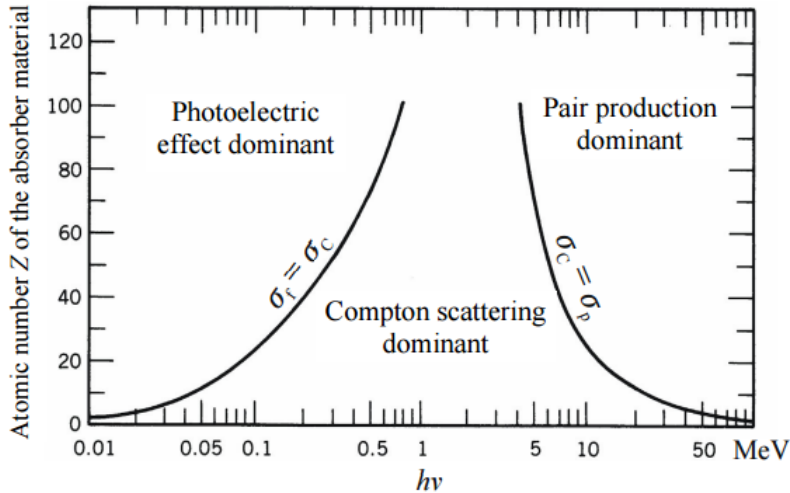


Figure 2.7: Dominant regions of three kinds of X-ray interactions with matter. Figure retrieved from website [Nuclear, 2018].

## 2.2 Conventional X-ray computed tomography

### 2.2.1 Historical background

After X-ray has been discovered, numerous research has been carried out for seeking new imaging modality. Many efforts have been done on planar X-ray radiography to produce 2D projections of objects situated between X-ray source and the detector. However, it is difficult to distinguish the overlapping components caused by the projection, such as the overlapping soft tissues and bones in physical scan. The introduction of X-ray computed tomography (CT) turned to be the right solution for this problem.

Based on the theory that materials have different attenuation properties to X-ray, CT scanners take measurements of integral projections of an object from different angles and then reconstruct the 2-D cross-sectional image through more or less complex computations. Figure 2.8 shows the mechanics of CT imaging, the basic components are X-ray source, object and detector.

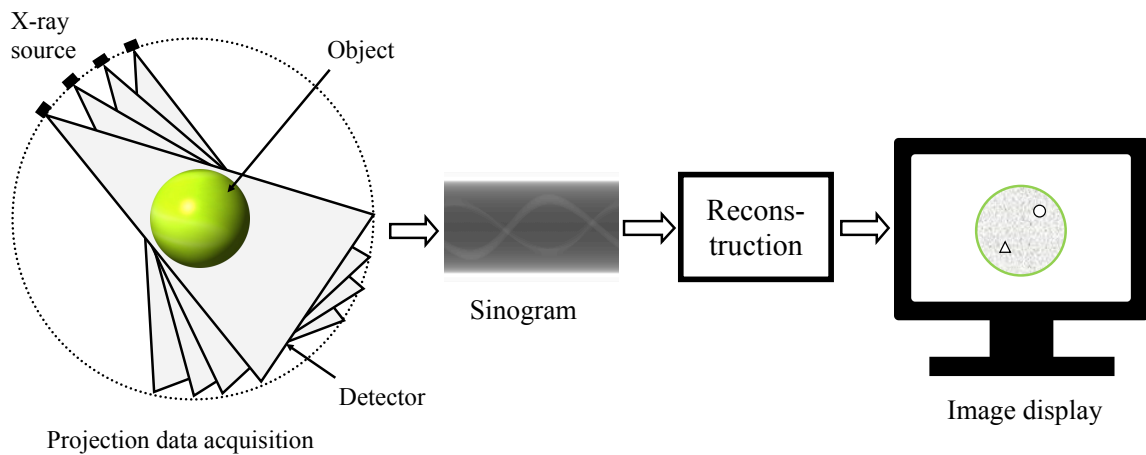


Figure 2.8: The mechanics of CT imaging: cross sectional image is reconstructed from projection data measured from multiple angles.

The basic mathematical principles behind the reconstruction of CT images was proposed by the Austrian mathematician Radon. In 1917, he proposed the famous Radon transform which transforms a function into its line integrals over particular lines, and also provided the inverse Radon transform which can be used to reconstruct images from a number of projections [Radon, 1917, Radon, 1986]. In 1963, a South African American physicist Cormack introduced a method to find the real function in a finite region of a plane given its line integrals along all straight lines intersecting the region, he also pointed out that this method can be used to determine 2 dimensional X-ray attenuation coefficients [Cormack, 1963]. However, he never considered of putting his theory into practice.

During the 1960s and early 1970s, there were a lot of researchers who dedicated on the development of CT technology [Kalender, 2006], including Oldendorf [Oldendorf, 1961], Kuhl and Edwards [Kuhl and Edwards, 1963], Bracewell and Riddle [Bracewell and Riddle, 1967], Gordon [Gordon et al., 1970], Bates and Peters [Bates and Peters, 1971]. The most important breakthrough was made by an English electrical engineer Hounsfield. In 1971, he invented the first X-ray CT scanner, the EMI Mark I, and installed it at the Atkinson Morleys Hospital in Wimbleton (see Figure 2.9 (a)). The first patient examination using this CT scanner took place in the same year and the obtained images revealed the presence of cyst formation (Figure 2.9 (b)) [Hounsfield, 1973, Ambrose, 1973].

The great success of the first head CT scanner instantly attracted numerous neurologists, radiologists, physicists, engineers and data processing specialists, they started to work on the algorithms of CT reconstruction and the interpretation of CT images. Commercial manufacturers like General Electric (GE), Siemens and Philips soon joined in the race to seize more market for this fresh but prospective technology. The number of CT scanners increased from 60 in 1974 to more than 10000 in 1980 [Kalender, 2006]. To reward the great achievements of Hounsfield, he was awarded the Nobel Prize for Physiology or Medicine in 1979 along with Cormack.

Afterwards, the advancement of X-ray CT has greatly benefited from developed recon-

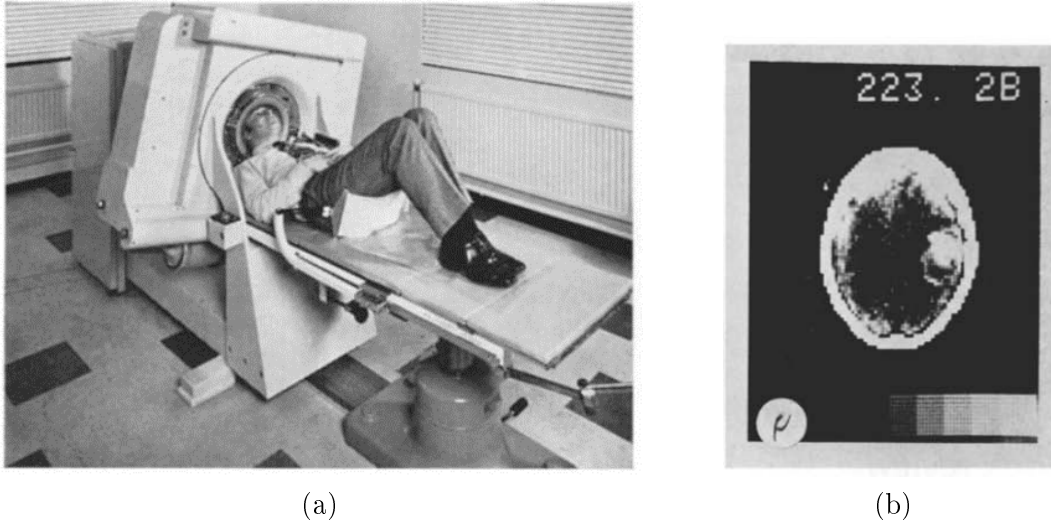


Figure 2.9: The EMI Mark I scanner (a), and the cross sectional image of brain (b).

struction algorithms, advanced computer technology and improved manufacture technique. The introduction of spiral (helical) CT in 1990 [Kalender et al., 1990] is another important step in the development of CT scanners. Spiral scan mode made it possible to continuously scan the extended volumes without interscan delay. The advantages of speed and continuity offered improved CT applications, such as the imaging of the lung within one breathhold. In 1998, multi-slice CT was proposed [Klingenbeck-Regn et al., 1999, Hu, 1999], even larger volume coverage in shorter scan times and improved longitudinal resolution became feasible [Ulzheimer and Flohr, 2009]. Later on, the 8-slice [Kachelrieß et al., 2000], 16-slice [Flohr et al., 2002b, Flohr et al., 2002a], 64-slice (2004, GE, Philips and Toshiba), 256-slice and 320-slice (2007, Philips and Toshiba) spiral CT scanner were implemented successively. It is striking to see how much the CT technology has evolved since its first introduction several decades ago.

X-ray CT was firstly invented for medical application, and it is now an important medical imaging tool for preventive medicine and the display of lesions. For example, a cardiac CT scan for calcium scoring gives pictures of the coronary arteries to determine plaques, or contrast (usually iodine) enhanced heart scan to assess the extent of occlusion in the coronary arteries. CT is also used in the applications outside medical area. For example, defects detection in lumber [Funt and Bryant, 1987], exploration of coal [Mathews et al., 2017], inspection of fiber reinforced polymer [Schilling et al., 2005, Kastner et al., 2010] and geology engineering [Mees et al., 2003]. For convenience, the term “CT” in this thesis is used solely to refer to X-ray computed tomography.

### 2.2.2 X-ray source

X-ray can be generated through the Bremsstrahlung process. We can accelerate the electrons in a vacuum tube with a high voltage  $U_{acc}$ , and then stop the high velocity electron with a metal target (usually tungsten, alloy of rhenium and tungsten, molybdenum or copper). The deceleration of electrons will lead to the emission of Bremsstrahlung, where

the lost kinetic energy is converted into photons with continuous spectrum. The generated photons can be in any directions and their maximum energy will be  $E_{\max} = eU_{\text{acc}}$ , the kinetic energy of electrons. For example, if the tube voltage is 100 kV, the generated X-rays will have energy up to 100 keV. In addition, the low-energy photons have weak penetration, they are likely to be fully absorbed by large object (like human) and can not arrive the detector, thus they contribute to patient dose but not to the image production. Therefore, the low-energy photons are usually removed by a filter in front of the X-ray tube before irradiating any object [Walsh, 2014].

On the other hand, the incident electrons can also interact with the orbital electrons. When an orbital electron is knocked out of the inner shell of the target metal atom, the electron from higher energy levels will fill the inner shell vacancy, resulting in emission of X-ray. Usually the transitions are from upper shells into K shell (called K lines), into L shell (called L lines). The wavelength of X-rays emitted through this process depends on the type of metal material and the energy gap between the respective electron orbital shells. Thus the X-rays have several specific discrete energies, called characteristic X-ray. Figure 2.10 shows the X-rays generated from a tungsten anode tube with voltage of 150 kV, the Bremsstrahlung emission and characteristic X-rays can be observed in this spectrum.

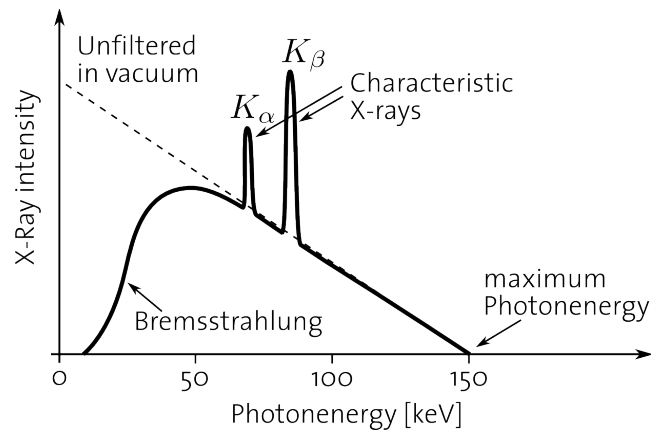


Figure 2.10: Spectrum of a tungsten X-ray source with tube voltage of 150 kV. The Bremsstrahlung emission, characteristic X-rays and the filtering of the lower-energy part are clearly shown in the spectrum. Figure retrieved from website [Cattin, 2016]

The intensity of emitted X-rays are determined by photon flux and the energy of photons. The photon flux is defined as the number of photons per second per unit area and it is proportional to the tube current. The photon counting process has Poisson distribution, that is the variance of photon counting equals the expected counting. The signal-to-noise ratio defined by the ratio of mean to standard deviation of the counting is proportional to the square root of the expected counting. Thus increasing the photon flux will gain more signal quality.

### 2.2.3 Energy integrating detector

Conventional CT devices are equipped with energy integrating detectors which provide integrated information of all the transmitted beam. Two types of energy integrating de-



tectors prevail: scintillator-based detector and semiconductor-based detector.

Scintillator-based detector consists of three essential layers: scintillator layer, photodiode layer and a substrate to provide the mechanical and electrical infrastructure [Shefer et al., 2013]. The physical principles are illustrated in 2.11. When the X-rays interact with the scintillator, photons are absorbed predominantly via the photoelectric effect, and a number of electron-hole pairs are created. After some time the recombination of electrons with holes will result in the emission of photons within visible range [Nikl, 2006]. The choices of scintillator materials include sodium iodide [NaI(Tl)] and cesium iodide [CsI(Tl)], (doped with thallium as activator) bismuth germanium oxide (BGO), cadmium tungstate ( $\text{CdWO}_4$ ), or polycrystalline ceramic rare-earth scintillators [Wang, 2015]. The emitted visible lights by the scintillator are then converted into electric current in the photodiode layer.

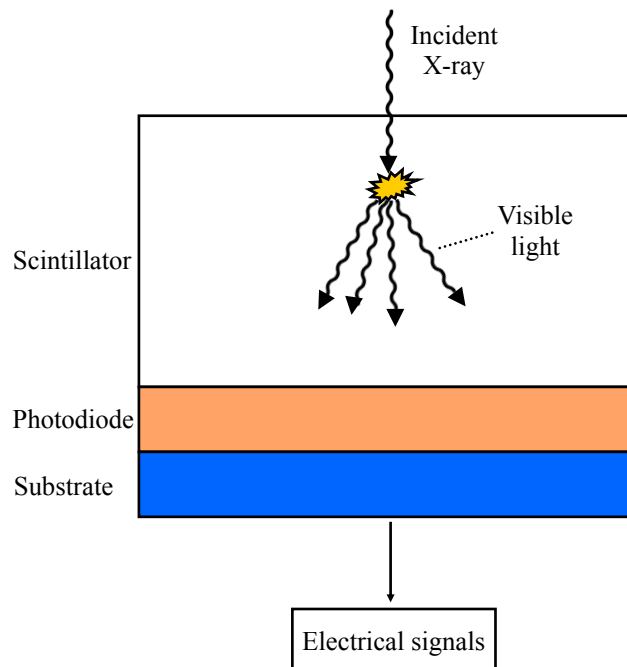


Figure 2.11: Schematic description of a scintillator-based detector.

Another type of detector is the room-temperature semiconductor detectors. Traditional semiconductors include silicon (Si) and germanium (Ge), but there has been increasing demand in detectors based on compound semiconductors, among which the cadmium telluride (CdTe) and cadmium zinc telluride (CdZnTe) detectors are the most promising. Figure 2.12 illustrates the mechanics of the semiconductor detector. The interaction of X-rays with the semiconductor material creates electron-hole pairs. The number of electron-hole pairs is proportional to the photon energy. The electrons move to the anode direction and the holes move to the cathode direction. The moving charge carriers induce the signals on the electrodes. The charge signals are then processed and recorded by the integrating application-specific integrated circuit (ASIC) [Del Sordo et al., 2009]. The major advantage

of room-temperature semiconductor detectors over scintillator detectors is that they have better overall quantum efficiency and their disadvantage is the lower stability especially in high-flux conditions [Wang, 2015].

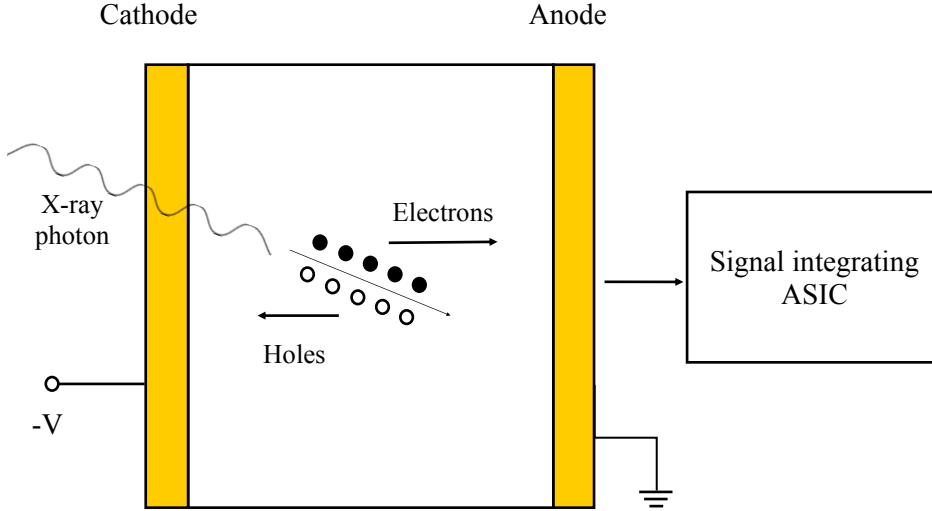


Figure 2.12: Mechanics of the room-temperature semiconductor detector.

#### 2.2.4 CT image reconstruction

Image reconstruction is an important step to retrieve the cross sectional attenuation coefficients from the measured X-ray data, which is the transmitted beam intensity along a line between X-ray source and detector. For monochromatic X-ray source of energy  $E$ , the measurement can be written as a function of the attenuation coefficients:

$$I(E) = I_0(E) \exp\left(-\int_L \mu_E(x, y) ds\right), \quad (2.14)$$

where  $I(E)$  is the measured intensity and  $I_0(E)$  is the intensity coming from the X-ray source,  $\mu_E(x, y)$  is the linear attenuation coefficient of the object at location  $(x, y)$ . Figure 2.13 represents the case where a parallel beam is used, in which  $\theta$  and  $t$  are polar coordinates of the path that the X-ray beam crosses through the object, like in Figure 2.13 is. Thus the line integration of the  $\mu_E(x, y)$  is:

$$P_{E,\theta}(t) = \int_{(\theta,t)line} \mu_E(x, y) ds = -\ln \frac{I(E)}{I_0(E)}. \quad (2.15)$$

In practical cases, the X-rays are polychromatic. However, the Equation (2.15) is also applied and this yields artifacts in the CT reconstruction due to beam hardening since we usually ignore the influence of different photon energies. For the following part in this section, we will omit the energy dependent variable  $E$ , since it does not contribute to the method of reconstruction.

We generalize  $\mu(x, y)$  with  $f(x, y)$ , the path that the X-ray crosses in the object can be given by:

$$x \cos \theta + y \sin \theta = t. \quad (2.16)$$

Thus Equation (2.15) can be rewritten as:

$$P_{\theta}(t) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} f(x, y) \delta(x \cos \theta + y \sin \theta - t) dx dy, \quad (2.17)$$

where  $\delta$  is the Dirac delta function.  $P_{\theta}(t)$  is called the Radon transform of function  $f(x, y)$ .  $P_{\theta}(t)$  is physically the projection of  $f(x, y)$  along the line which is in direction  $\theta$  and has distance  $t$  from the origin of coordinate. If we fix  $\theta$  and change  $t$  to all different values, we will obtain a set of projection data in direction  $\theta$ ; If we change  $\theta$  at the same time we will obtain sets of projection data from different directions, that is called sinogram.

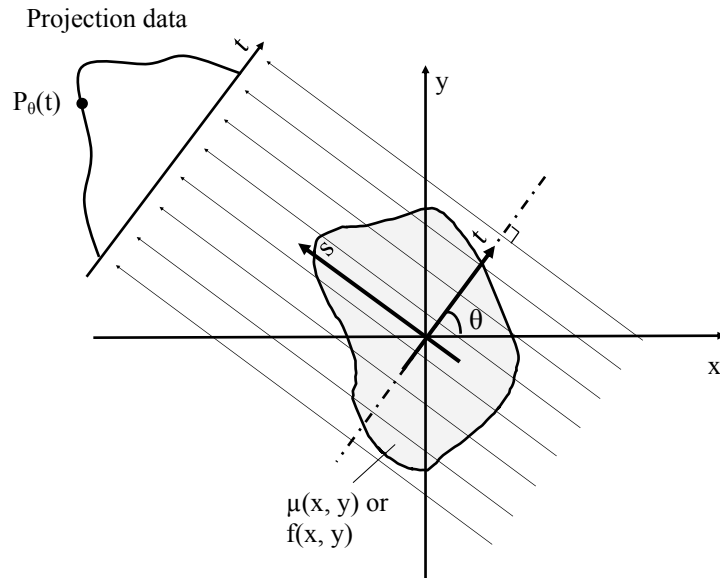


Figure 2.13: Parallel projections  $P_{\theta}(t)$  of object  $f(x, y)$  for angle  $\theta$ .

To reconstruct  $\mu(x, y)$  from  $P_{\theta}(t)$ , there are two main categories of methods, analytical reconstruction and iterative reconstruction. The principle are reviewed in the book of Kak [Kak and Slaney, 1988]. The most common algorithm in the analytical reconstruction category is the filtered back-projection (FBP) method.

### Filtered back-projection reconstruction method

We rotate the original coordinate system by angle  $\theta$ , can change  $(x, y)$  into  $(t, s)$ , the transform can be expressed as:

$$\begin{bmatrix} t \\ s \end{bmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \quad (2.18)$$

In the  $(t, s)$  coordinate system, we do a Fourier transform to  $P_\theta(t)$ :

$$S_\theta(w) = \int_{-\infty}^{+\infty} P_\theta(t) e^{-j2\pi w t} dt = \int_{-\infty}^{+\infty} \left[ \int_{-\infty}^{+\infty} f(t, s) ds \right] e^{-j2\pi w t} dt. \quad (2.19)$$

According to Equation (2.18), the above formula can be written as:

$$S_\theta(w) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} f(x, y) e^{-j2\pi w(x \cos \theta + y \sin \theta)} dx dy. \quad (2.20)$$

Make  $u = w \cos \theta$ ,  $v = w \sin \theta$ , then the right-hand side of Equation (2.20) is a two-dimensional Fourier transform at spatial frequency of  $(u, v)$ :

$$S_\theta(w) = F(w \cos \theta, w \sin \theta) = F(u, v). \quad (2.21)$$

The above equation indicates that the Fourier transform of the original object on radial lines can be determined by the Fourier transform of the projections at different angles. This is called the central or Fourier slice theorem ( or projection-slice theorem). Figure 2.14 illustrates the Fourier slice theorem.

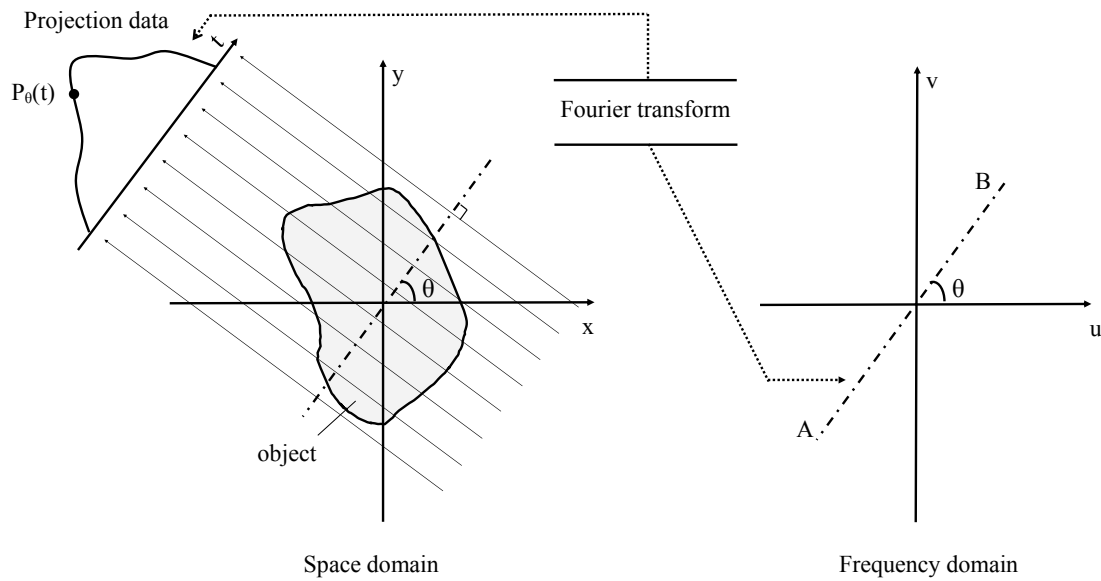


Figure 2.14: The Fourier slice theory: the Fourier transform of a set of projections along angle  $\theta$  equals the Fourier transform of the object along the line  $AB$ .

Fourier slice theorem is the basis of FBP algorithm. From Equation (2.20) and (2.21), we know that:

$$f(x, y) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} F(u, v) e^{j2\pi(ux+vy)} du dv. \quad (2.22)$$

Substitute coordinates  $u$  and  $v$  in frequency domain with  $w$  and  $\theta$  in polar coordinate system, we have:

$$\begin{aligned}
 f(x, y) &= \int_0^{2\pi} \int_0^{+\infty} F(w, \theta) e^{j2\pi(x \cos \theta + y \sin \theta)} w \, dw \, d\theta \\
 &= \int_0^{\pi} \int_0^{+\infty} F(w, \theta) e^{j2\pi(x \cos \theta + y \sin \theta)} w \, dw \, d\theta \\
 &\quad + \int_0^{\pi} \int_0^{+\infty} F(w, \theta + \pi) e^{j2\pi[x \cos(\theta + \pi) + y \sin(\theta + \pi)]} w \, dw \, d\theta.
 \end{aligned} \tag{2.23}$$

Since

$$F(w, \theta + \pi) = F(-w, \theta). \tag{2.24}$$

equation (2.23) can be written as:

$$f(x, y) = \int_0^{\pi} \left[ \int_{-\infty}^{+\infty} F(w, \theta) |w| e^{j2\pi(x \cos \theta + y \sin \theta)} \, dw \right] d\theta. \tag{2.25}$$

We substitute the two-dimensional Fourier transform  $F(w, \theta)$  of object with the Fourier transform of the projection data at angle  $\theta$ , and the above equation can be expressed as:

$$\begin{aligned}
 f(x, y) &= \int_0^{\pi} \left[ \int_{-\infty}^{+\infty} S_{\theta}(w) |w| e^{j2\pi(x \cos \theta + y \sin \theta)} \, dw \right] d\theta \\
 &= \int_0^{\pi} Q_{\theta}(x \cos \theta + y \sin \theta) \, d\theta,
 \end{aligned} \tag{2.26}$$

where

$$Q_{\theta}(x \cos \theta + y \sin \theta) = Q_{\theta}(t) = \int_{-\infty}^{+\infty} S_{\theta}(w) |w| e^{j2\pi t} \, dw. \tag{2.27}$$

Equation (2.27) indicates that the original projection data  $P_{\theta}(t)$  is firstly transformed into frequency domain  $S_{\theta}(w)$ , then  $S_{\theta}(w)$  is multiplied by filter  $|w|$ , and the result is transformed into  $Q_{\theta}(t)$  by the inverse Fourier transform. Therefore  $Q_{\theta}(t)$  is considered as "filtered projections". Equation (2.27) indicates that the filtered projections  $Q_{\theta}(t)$  are "back-projected". Through integration of  $\theta$ , the filtered projections of all directions are smeared back for the determination  $f(x, y)$ .

The filtering step can also be done in space domain using convolution:

$$Q_{\theta}(t) = \int_{-\infty}^{+\infty} P_{\theta}(t') h(t - t') \, dt', \tag{2.28}$$

where kernel  $h(t)$  is the inverse Fourier transform of  $|w|$ . In fact, the inverse transform of  $|w|$  does not exist since it is not square integrable. Since the projection data is sampled, the filter only needs to match  $|w|$  at the sampling points. Also, in practice the energy contained in high frequency is negligible, the filter can be made bandlimited. Suppose the  $W$  is the maximum frequency, and according to the sampling theorem, the sampling interval is  $\tau = 1/2W$ . Bandlimited filter can be expressed as:

$$H(w) = |w| b_w(w), \tag{2.29}$$

where

$$b_w(w) = \begin{cases} 1 & |w| < W \\ 0 & \text{otherwise.} \end{cases} \quad (2.30)$$

The corresponding filter kernel of  $H(w)$  is:

$$h(n\tau) = \begin{cases} \frac{1}{4\tau^2}, & n = 0 \\ 0, & n \text{ even} \\ -\frac{1}{n^2\pi^2\tau^2}, & n \text{ odd.} \end{cases} \quad (2.31)$$

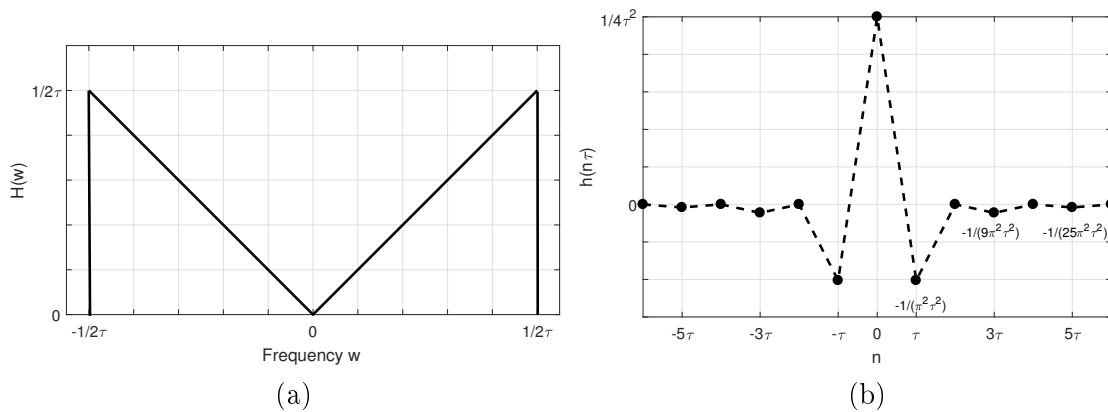


Figure 2.15: The bandlimited filter response (a), and the corresponding impulse response (b).

Function  $H(w)$  and function  $h(n\tau)$  are shown in Figure 2.15. In practice, a modified filter will be used to weaken the higher frequencies and obtain better image quality. This can be achieved by a simple multiplicative window such as a Hamming window.

In practice, fan beam CT is more common than parallel CT. The X-ray source radiates fan-shaped beam and a number of detectors are put opposite to detect the transmitted photons. They rotate together to generate a set of projections. Two types of fan beam projections exist, like discussed in [Kak and Slaney, 1988]: the equiangular interval projections and the equispaced interval projections. The former applies for conditions where the detectors are put to sample the projections by equiangular intervals; and the latter is for the condition where the detectors are positioned with equal space along a straight line (see Figure 2.16). In our research, the spectral CT imaging system accords with the latter one, therefore we will discuss the FBP reconstruction algorithm in this situation.

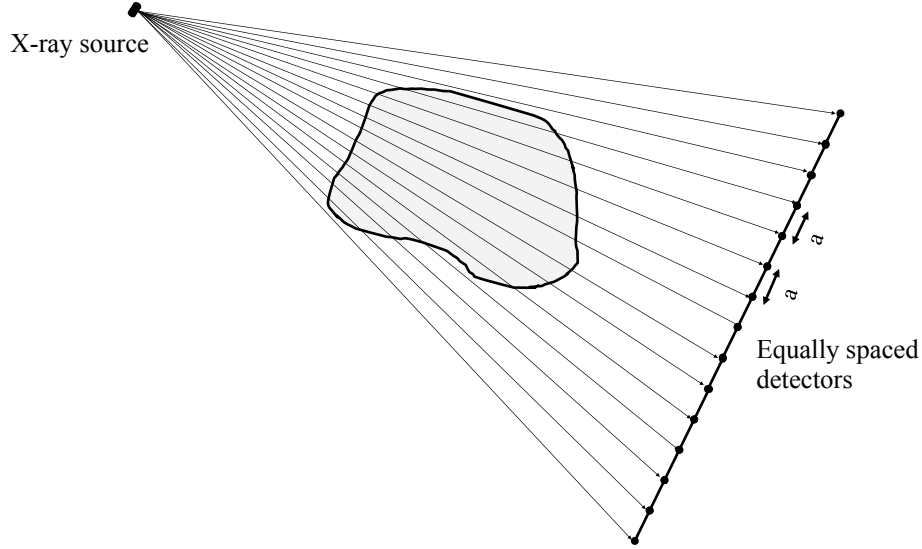


Figure 2.16: Fan beam projections where the detectors are positioned with equal space along a straight line.

We assume that the projection data acquired from Figure 2.16 is  $R_\beta(s)$ , and its relationship with the parallel projections  $P_\theta(t)$  can be derived from Figure 2.17:

$$t = s \cos \gamma = \frac{sD}{\sqrt{s^2 + D^2}} \quad (2.32)$$

$$\theta = \beta + \gamma = \beta + \tan^{-1} \frac{s}{D}. \quad (2.33)$$

Similarly with Equation 2.26, the reconstruction algorithm can be derived for fan beam CT imaging as:

$$R'_\beta(s) = R_\beta(s) \frac{D}{\sqrt{D^2 + s^2}} \quad (2.34)$$

$$g(s) = \frac{1}{2} h(s) \quad (2.35)$$

$$Q_\beta(s) = R'_\beta(s) * g(s) \quad (2.36)$$

$$f(r, \phi) = \int_0^{2\pi} \frac{1}{U^2} Q_\beta(s') d\beta, \quad (2.37)$$

where  $r$  and  $\phi$  are polar coordinates of a pixel on the object,  $s'$  is the value of  $s$  for the ray that passes through the pixel  $(r, \phi)$  under consideration, and  $U$  is the ratio between distance  $D$  and the distance from the source to the projection of point  $(r, \phi)$  onto the central ray:

$$U = \frac{D + r \sin(\beta - \phi)}{D} \quad (2.38)$$

$$s' = D \frac{r \cos(\beta - \phi)}{D + r \sin(\beta - \phi)}. \quad (2.39)$$

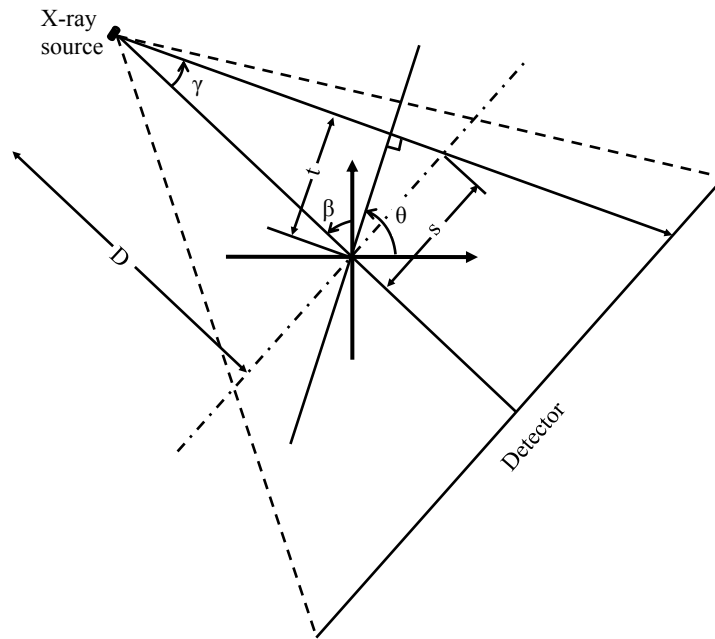


Figure 2.17: Parameters used in the derivation of the reconstruction method for equispaced fan beam CT imaging.

### Iterative reconstruction method

Another category of image reconstruction for X-ray CT is iterative reconstruction method. This method begins with an initial image assumption, and compares it to measured values while making adjustments until the two are in agreement. by the following different steps:

- ① Set the reconstruction image an initial value  $f^{(0)}$ ;
- ② Calculate the forward projection of the  $f^{(k-1)}$  (for the first iteration  $k = 1$ , the second iteration  $k = 2$ , and so on);
- ③ Compare the difference between real measured data and calculated projection by step ②;
- ④ Correct reconstruction image by back-projection and obtain  $f^{(k)}$ ;
- ⑤ Increase  $k$  by 1 ( $k = k + 1$ ) and repeat step ②, ③ and ④ until the stopping criterion is satisfied ;

The initial image  $f^{(0)}$  is arbitrary, but usually we make it 0, or an image reconstructed by another method such as FBP. The stopping criterion can either be the maximum number of iterations, or the small enough update of current image estimate , or the predefined quality criterion [Beister et al., 2012]. A set of iterative reconstruction methods has been proposed, such as the algebraic reconstruction technique (ART) [Gordon et al., 1970],



simultaneous iterative reconstruction technique (SIRT) [Gilbert, 1972], simultaneous algebraic reconstruction technique (SART) [Andersen and Kak, 1984], maximum likelihood expectation-maximization (ML-EM) algorithm [Shepp and Vardi, 1982], and so on. Here we introduce in detail the most basic and popular ART method.

In ART reconstruction, the projection process of CT imaging system can be represented by:

$$b_i = \sum_j a_{i,j} f_j, \quad (2.40)$$

where  $b_i$  is the integration data measured with the  $i_{\text{th}}$  ray (total number of rays  $M = \text{No. rotation angles} \times \text{No. detectors}$ );  $a_{i,j}$  is the weighting factor that represents the contribution of the  $j_{\text{th}}$  voxel to ray  $i$ ;  $f_j$  is the attenuation coefficient of voxel  $j$  in our case. Therefore, we have:

$$A\mathbf{f} = \mathbf{b}, \quad (2.41)$$

where  $A = a_{i,j}$  is the system matrix,  $\mathbf{f} = [f_1, f_2, \dots, f_N]$  is the image vector where  $N$  is the total number of voxels in the reconstruction image, and  $\mathbf{b} = [b_1, b_2, \dots, b_M]$  is the measurement vector. To solve  $\mathbf{f}$ , the Kaczmarz method [Kaczmarz, 1993] is applied and the following iterative formula is obtained:

$$\mathbf{f}^{(k)} = \mathbf{f}^{(k-1)} + \lambda_{k-1} \frac{b_i - \mathbf{f}^{(k-1)} \mathbf{a}_i^T}{\mathbf{a}_i \mathbf{a}_i^T} \mathbf{a}_i, \quad (2.42)$$

where  $k$  is the number of iterations and  $\lambda_{k-1}$  is the relaxation parameter,  $i = k \bmod M + 1$ ,  $\mathbf{a}_i$  is a vector made of the  $i_{\text{th}}$  row of  $A$ .

Compared to analytical FBP method, iterative reconstruction has advantage to reduce noise and improve image quality by integrating various physical models and incorporating prior information. It outperforms FBP method especially with sparse and incomplete data. The most serious disadvantage of iterative reconstruction is its huge computational costs, since each iteration involves forward projections. Computing power may not be sufficient for complicated modeling, such as in the case of fine volumetric image reconstruction, dual-energy or spectral CT data processing, extreme large matrix sizes will be used and great demands on computational speed will be requested. For this reason iterative reconstruction techniques are not yet suitable for scanning patients in acute situations [Opie, 2013].

## 2.3 X-ray spectral CT

### 2.3.1 Introduction

We have discussed in the above the principles of conventional CT imaging. The X-ray sources in use nowadays consists in a spectrum of energies. However, the conventional energy-integrating detector sums up all the energy information and thus gives lower energy photons which carries contrast information less weight than higher energy photons (Figure 2.18 (a)). The reconstructed image corresponds to the linear attenuation coefficients at a single average energy. Spectral information is not fully utilized in this case and

contrast between different materials is lost. Spectral CT appears to make advantage of multi-energy information passed through the object to improve CT imaging.

The concept of energy-resolving CT has been discussed since the invention of CT. In the landmark CT paper [Hounsfield, 1973] of Hounsfield, he proposed to take CT scans with the same slice of material at two different voltages to determine atomic number of materials. In 1976, Alvarez and Macovski proposed to extract energy-dependent information by representing the total attenuation with functions corresponding to photoelectric and Compton effect, and the energy-independent parts of the two effects were then reconstructed respectively [Alvarez and Macovski, 1976]. In 1977, Riederer et al. presented their work of selective iodine imaging by CT scans using three heavily filtered X-ray beams [Riederer and Mistretta, 1977]. Material selective imaging using dual-energy scan also extended to X-ray radiographic imaging [Brody et al., 1981, Lehmann et al., 1981].

Following the above concept, a variety of dual-energy CT (DECT) systems were built for energy-resolving imaging. There are currently three main techniques for achieving DECT. The first one is called rapid kilovoltage switching technique, where the voltage of X-ray tube is switched rapidly to produce two X-ray beams with different energies for scanning at every other projection during the whole scan, and its principle is shown in Figure 2.18 (b). The second one is dual-source CT technique where two X-ray tubes and two corresponding detectors are equipped in the CT system to simultaneously acquire two set of data for the same slice. These two techniques both use different X-ray spectra and their principles are shown in Figure 2.18 (b). The third is dual-layer (sandwich) detector technique, which still uses energy-integrating detector, but two sets of scintillation arrays and photodiodes stacked on top of each other, so that the lower-energy photons are absorbed by the top scintillator array, while the higher-energy photon penetrates the top layer and are absorbed by the bottom scintillator array [Nasirudin, 2015], see Figure 2.18 (c). DECT has limited ability in material decomposition by producing two datasets corresponding to two different X-ray spectra of the same anatomic region [Danad et al., 2015]. The potential of using DECT to detect the distribution of materials in vivo attracted much investigation [Fischer et al., 2011, Hazirolan et al., 2008, Luo et al., 2015, Panta et al., 2015]. Take an essential element for human body iron as an example: Hazirolan et al. applied DECT to the detection of myocardial iron deposition in Thalassaemia patients; the measured myocardial DECT density values showed strong negative correlation with MRI T2\* values [Hazirolan et al., 2008]. Luo et al. also proved the diagnostic potential of DECT in liver iron content determination using virtual iron content imaging with fifty-six patients suspected of having liver iron overload [Luo et al., 2015]. However, DECT is unable to give the accurate concentration of iron except for the correlated Hounsfield Unit (HU) values and usually requires relatively high dose levels.

Different from DECT, spectral CT employs photon counting detectors (PCDs) and is able to obtain spectral information of several energy bins with single acquisition, see Figure 2.18 (d). Spectral CT technology became available only within the recent years. Thanks to the development of detector technology, PCDs were realized to extract multi-energy information. The first commercial photon-counting system was introduced for mammography in 2003 [Åslund et al., 2007]. Several major manufacturers were also involved in the investigation of energy-resolved CT. In 2013, Philips introduced the IQon Spectral CT, which is the world's first spectral detector CT. Spectral CT imaging has the potential to overcome many limitations of the previous techniques and apply for many new applications. It can

improve X-ray CT by reducing dose, enable artifacts correction, permit K-edge imaging using high-Z contrast agents and provide quantitative material decomposition. Spectral CT is getting more and more attention and has become a research hotspot.

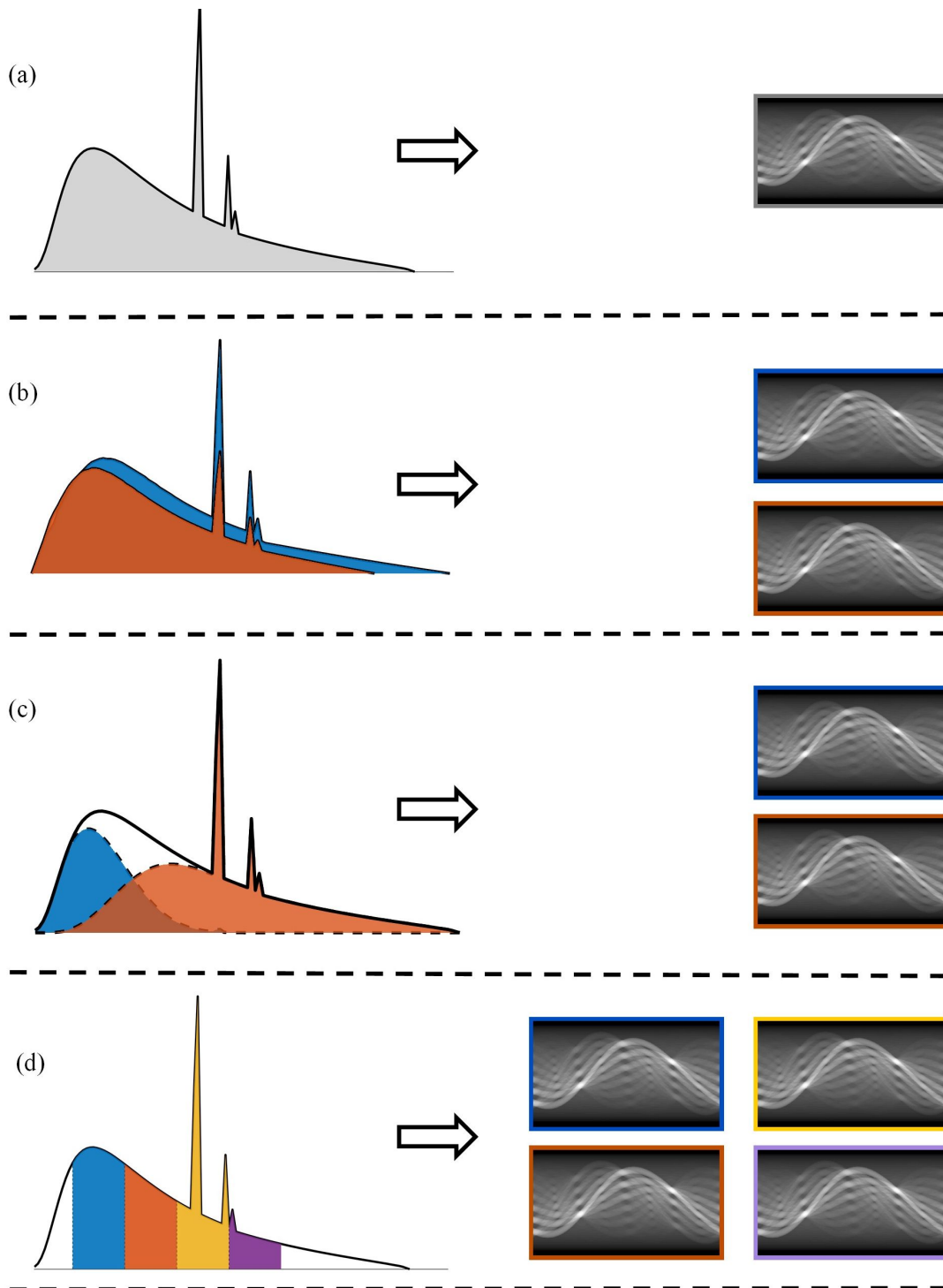


Figure 2.18: Data acquisition from different CT systems: conventional CT system where integrating detectors acquire one single sinogram (a); DECT using rapid kilovoltage switching technique or dual-source technique (b) or dual-layer detector technique (c) acquiring two set of projection data; spectral CT system (d) with photon counting detectors acquire several datasets of selected energy bins.

### 2.3.2 Photon counting detector

Photon counting detector is the most essential part of the spectral CT system. PCDs have the ability to discriminate transmitted photons corresponding to selected energy bins in order to obtain spectral information with one data acquisition.

Figure 2.19 illustrates the principle of the PCD. It consists of two parts, a sensor and an electronic part of application-specific integrated circuit (ASIC). The principle of the sensor is the same as the semiconductor based integrating detector that we have discussed in 2.2.3: firstly, the X-rays interact with the semiconductor material, and result in a number of electron-hole pairs; then the electrons and the holes move to the opposite directions, the anode and the cathode respectively; the moving charge carriers induce the signals on the electrodes. The charge signals are then passed to the electronic part (the photon counting ASIC): a preamplifier and a shaper convert the charge signals into pulses with amplitudes proportional to the incident photons energies, then the comparators divide the pulses into different pre-selected bins according to their amplitudes, the counters record the total number of pulses for each bin and output the counting signal.

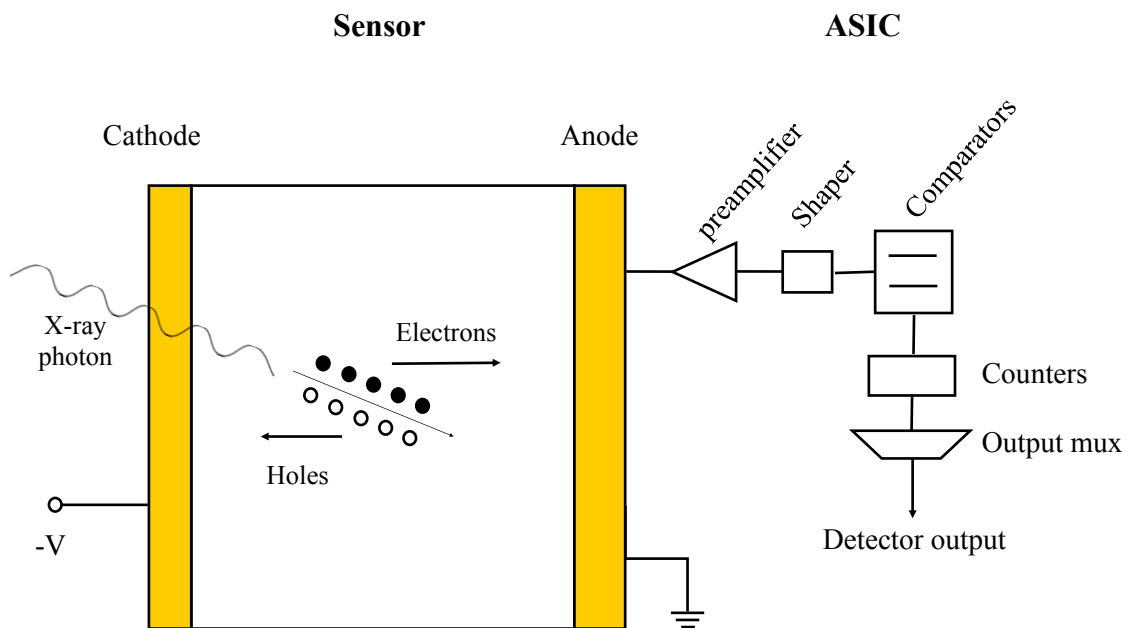


Figure 2.19: Principle of the photon counting detector.

The most common semiconductor material used for PCD is silicon (Si). Si is a well available material that has mature technique for high-quality and high-purity manufacture, it also have high charge-collection efficiency. The main disadvantage is that silicon has relative lower atomic number (14). From Figure 2.7 we can derive that Compton scattering dominates most of the energies during X-ray interactions with silicon. This fact degrades the energy response since not all the photon energy is deposited to electrons in Compton scattering. Materials with higher atomic number and larger photoelectric cross section are much preferred. CdTe and CZT are two most promising materials which benefit from

high atomic number, high density and wide band width. The main challenge of CdTe and CZT material based PCD is the limited commercial availability of high-quality crystals. Table 2.1 gives a comparison of several PCDs.

The main advantage of PCD over energy integrating detectors is the eliminated electronic noise. By setting a low-energy threshold that is above the highest amplitude of the noise, electronic noise can be excluded from being counted. In this way, low-dose and low-energy benefits with higher image quality. Furthermore, instead of being less weighted, low-energy photons can be counted in order to bring valuable information, e.g. more contrast to the image. However, PCDs are not flawless, the measurement of PCDs may deviate from the truth for several reasons [Taguchi and Iwanczyk, 2013]:

- Pulse pileup. When several photon interactions occur at the same time, multiple pulses may be piled up and be counted as one event, resulting in wrong recorded energy and counts loss.
- Charge sharing. When the generated electron charge cloud reaches the anode near the pixel boundary, they maybe divided and counted by the neighboring pixels to a smaller energy level.
- K-escape X-rays. X-ray fluorescence or Auger electrons may be generated during the photoelectric effect, as we have discussed in 2.1.1. The fluorescent X-ray photons can either be absorbed by the PCD pixel with the primary interaction again, be detected by an adjacent pixel, or leave the PCD completely.
- Compton scattering. The photon energy is not fully transmitted to electrons, resulting in energy loss.
- Charge trapping. The electron or hole is trapped by a trapping center and is thermally re-emitted with a delay. This will result in lower-energy counting.
- Polarization and long-term reliability.

Table 2.1: Comparison of different PCDs. This table is not a complete list of all available PCDs and is only for comprehensive review.

Index	Name	Manufacturer	Material	Pixel number	Pixel size ( $\mu\text{m} \times \mu\text{m}$ )	No. of energy thresholds	Maximum count rate (Mcps/pixel)	Energy resolution
1	MEXC (Refs group 1) <sup>1</sup>	Gamma Medica Ideas, Northridge, California	CdTe	1×1024	380×160	6	1-2	NA
2	DXMCT-1 (Refs group 2) <sup>2</sup>	DxRay Inc, Northridge, California	CdTe	16×16	1000×1000	2	6	4.75% (5.8 keV FWHM @ 122 KeV)
3	DXMCT-2 (Refs group 3) <sup>3</sup>	DxRay Inc, Northridge, California	CZT	16×16	500×500	4	20	7 keV FWHM @ 60 KeV
4	Siemens 2010 (Refs group 4) <sup>4</sup>	Siemens AG, Forchheim, Germany	CdTe	64×64	225×225	4	NA	NA
5	MicroDose SI (Refs group 5) <sup>5</sup>	Sectra Mamea AB, Solna, Sweden	Si strip	NA	50×50	2	NA	12%-26%
6	Medipix3 (Refs group 6) <sup>6</sup>	CERN, Geneva, Switzerland	CMOS	256×256	55×55 110×110	1, 2, 4, 8	0.145-0.21	NA
7	C10413 (Refs group 7) <sup>7</sup>	Hamamatsu Photonics, Japan	CdTe	1×64	800×500	5	2	≤15% FWHM @ 122 KeV

<sup>1</sup> Reference group 1 [Feuerlein et al., 2008, Schlomka et al., 2008, Pan et al., 2012]<sup>2</sup> Reference group 2 [Barber et al., 2009, Iwanczyk et al., 2009]<sup>3</sup> Reference group 3 [Barber et al., 2013]<sup>4</sup> Reference group 4 [Kappler et al., 2010, Kappler et al., 2012]<sup>5</sup> Reference group 5 [Fredenberg et al., 2010a, Fredenberg et al., 2010b]<sup>6</sup> Reference group 6 [Ballabriga et al., 2011, Ballabriga et al., 2006, Gimenez et al., 2011, Zaimon, 2012]<sup>7</sup> Reference group 7 [Alessio and MacDonald, 2013, Hamamatsu, 2014]

### 2.3.3 Applications of spectral CT imaging

As we have introduced in 2.3.1, spectral CT discriminate transmitted photons corresponding to selected energy bins and obtain spectral information with one data acquisition. This technique enables us to overcome many limitations of the conventional CT techniques and opens up many new application possibilities. Quantitative material decomposition is the hottest topic for spectral CT, including K-edge imaging of contrast materials and selective imaging of other previously indistinguishable materials. Other applications include energy weighting and virtual monochromatic imaging to improve image quality.

#### Quantitative material decomposition

The X-ray attenuation for different materials varies from each other. With the spectral information of transmitted photons, it is possible to discriminate different components of object. As we have said before, in 1976, Alvarez and Macovski proposed to extract energy-dependent information by represent the total attenuation with functions correspond to photoelectric and Compton effect, and the energy-independent parts of the two effects were then reconstructed [Alvarez and Macovski, 1976]. The reconstructed photoelectric image provides composition information of object while the reconstructed Compton image provides mass density information of object. In 2007, Roessl and Proksa developed this idea by adding the K-edge terms on the photoelectric and Compton effect decomposition formula and gadolinium was discriminated from normal tissues in the thorax phantom in their simulation study [Roessl and Proksa, 2007]. Their results were further validated by CT system experiments where the contrast agents (gadolinium and iodine) were well quantified [Schlomka et al., 2008]. This technique was named K-edge imaging and it enables multi-agent imaging [Roessl et al., 2011, Butler et al., 2011, Boone et al., 2014, Pan et al., 2010, Si-Mohamed et al., 2017, Lee et al., 2016b, Lee et al., 2016a].

There is less research about the quantification ability of materials that lack K-edge properties within the detection energy range, which is more challenging. Le et al. proposed a calibrated least squares fitting technique to decompose hydroxyapatite and iodine by a simulation study [Le and Molloy, 2011]. Based on this work, Alessio et al. made further improvement and their decomposition results with carotid endarterectomy specimens suggested the presence of water, lipid, and calcium deposits in the plaque walls [Alessio and MacDonald, 2013]. Zainon et al. used small animal spectral micro-CT with Medipix3 detector (thresholds: 10, 16, 22 and 28keV) to scan the carotid atherosclerotic plaque; water-like, calcium-like and lipid-like tissues were well separated according to histology comparison, but iron was not distinguished from calcium [Zainon, 2012].

Detailed material decomposition methods will be introduced in Chapter 3.

#### Energy weighting

There are mainly three weighting cases in CT imaging: integrating, counting and energy weighting. The first case uses weighting factors that are proportional to the energy of photon; the second case sums up the number of interacting photons with constant weighting factor; and in the third case, the energy-bin data are weighted by energy dependent factor to obtain better contrast-to-noise ratio (CNR) and signal-to-noise Ratio (SNR) [Carramate et al., 2011]. By giving lower-energy data more weight, the dose efficiency is effectively



improved and enables a higher CNR at a constant patient dose, or a lower dose at a constant CNR [Berglund et al., 2014]. Energy weighting can be performed both in projection domain or image domain data. In the research of Giersch et al., by using weighting factor  $E^{-3}$ , the SNR can be enhanced by up to from 1.3 to 1.9 or reduce the dose by factor of 2.5 without losing image quality [Giersch et al., 2004]. An “image-based” weighting method by Schmidt shows that the CNR is improved by factors of 1.0 to 1.3 compared to photon-counting weighting with negligible beam-hardening artifacts [Schmidt, 2009].

### Virtual monochromatic imaging

We have discussed in 2.1 the principles of X-ray interactions with matter. There are limited number of interaction effects and their energy dependence have all been represented. Therefore through the energy-resolving imaging, virtual monochromatic images can be calculated in the projection domain or in the image domain. Such monochromatic images have the advantage to improve spectral CNR, since the low-energy attenuation carries more contrast. For example, in intra-hepatic and extra-hepatic portal veins imaging, 51 keV monochromatic images provide the best CNR that is 100% higher than the polychromatic images [Zhao et al., 2012]. Hard X-rays attenuate less than soft X-rays, thus monochromatic images of higher energy have the potential to reduce beam-hardening [Neuhaus et al., 2017, Yu et al., 2012] and metal artifacts [Wang et al., 2013]. Another application of monochromatic imaging is to characterize materials. For example, when comparing a set of monochromatic images at lower energies, the iodine and calcium can be separated since the attenuation of iodine changes greatly around its K-edge (33.17 keV) while that of calcium is quite flat. Therefore the CNR of contrast-enhanced imaging can be improved by choosing an energy slightly above the absorption edge of the contrast agent.

## 2.4 Summary

This chapter presents the general principles of spectral CT, including the following sections:

1. Interactions of X-rays with matter. X-ray is a form of electromagnetic radiation that has extremely short wavelength and high frequency. It was discovered in 1895 by Röntgen. The research on new imaging modality using X-rays started since its discovery. Those research are based on the attenuation property of X-rays when passes through the object. There are three major X-ray interactions with matters that account for the total attenuation: photoelectric absorption, Compton scattering and pair production. Their mechanisms are introduced in detail.
2. Principles of conventional X-ray CT. The first CT scanner was invented by Hounsfield in 1971. The CT scanner takes measurements of integral projections of an object from different angles and then reconstructs the 2-D cross-sectional image through complex mathematics computations. The basic components are X-ray source, object and detector. Currently used energy integrating detectors include scintillator-based and semiconductor-based detector. The most important step in CT imaging is image reconstruction, which retrieves the cross sectional attenuation coefficients from the measured X-ray data. There are two main categories of methods, analytical reconstruction (FBP reconstruction) and iterative reconstruction. Iterative reconstruction

has the potential to reduce noise and improve image quality, but it is not applicable for widely used practical applications due to huge computation costs.

3. Principles of spectral X-ray CT. Spectral CT employs photon counting detectors and is able to obtain spectral information of several energy bins with single acquisition. This technology became available only within the recent years thanks to the development of detector technology. PCDs are semiconductor based detectors that have the ability to discriminate transmitted photons corresponding to selected energy bins. Spectral CT imaging enables to overcome many limitations of the previous techniques and opens up many new applications. Quantitative material decomposition is the most investigated topic for spectral CT, including K-edge imaging of contrast materials and selective imaging of other previously indistinguishable materials. Other applications include energy weighting and virtual monochromatic imaging to improve image quality.



## Chapter 3

# Material decomposition methods

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## 3.1 State of the art

Making use of multi-energy information, spectral CT has the potential to discriminate different components inside the object. Many material decomposition methods have been proposed and different experimental systems are under development for spectral CT. According to the formulation of the decomposition, there are mainly two kinds of methods. The first is effect-based decomposition, also called K-edge imaging, where the attenuation is considered as a linear combination of the photoelectric effect, Compton effect and extended K-edge components if there are materials with their K-edge within the CT energy range. The second is material-based method, which describes the linear attenuation coefficient by the contributions of a basis of materials.

### 3.1.1 Effect-based decomposition / K-edge imaging

K-edge is the binding energy of the K shell electron of an atom. Generally, the attenuation coefficient decreases with photon energy, but there is a sudden increase at the photon energy just above the binding energy since the probability of the photoelectric effect occurring is much higher than the energy below this binding energy. There exists also L-edge which corresponds to the binding energy of L shell electrons. Figure 3.1 illustrates the energy dependence of X-ray attenuation coefficient for iron (a) and iodine (b), where can be clearly seen the K-edges of the two materials as well as the L-edges of iodine. A K-shell interaction is approximately four to five times more probable than an L-shell interaction if both interactions are energetically allowed, thus we consider only the K-edge here. It should be notice that the K-edge of iron appears at a quite small energy (7.11 keV) that is usually outside the energy range of PCD, therefore we define such lighter materials that lack K-edge properties within the detection energy range as “non-K-edge material”, and those having K-edge absorption within the energy range as “K-edge material”. Generally, K-edge materials are much easier to be quantified because of their unique attenuation coefficient.

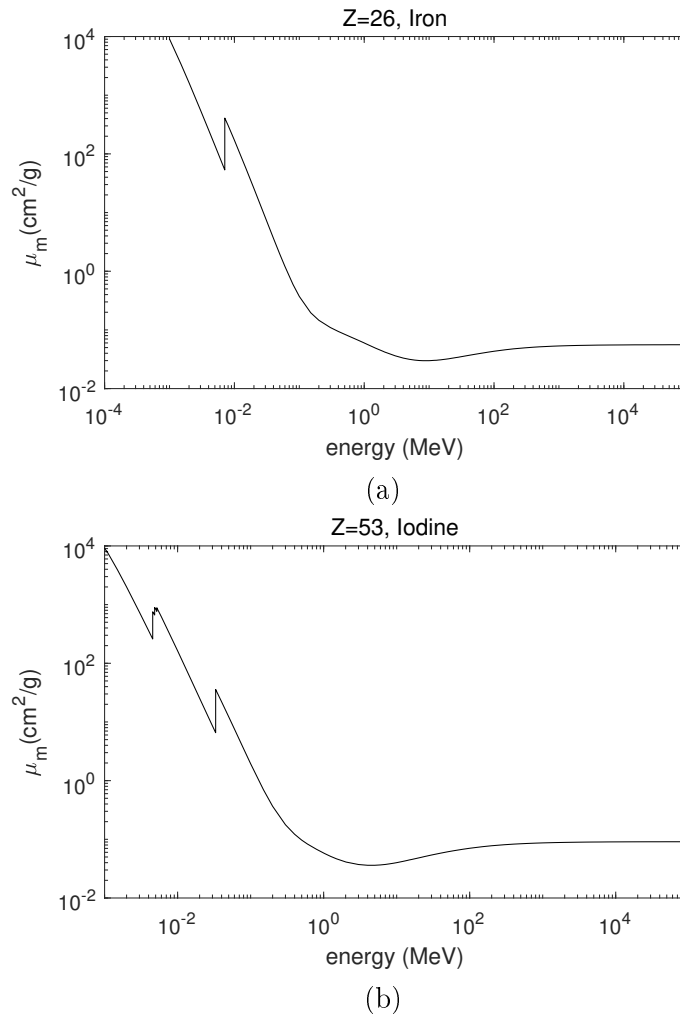


Figure 3.1: Energy dependence of X-ray attenuation coefficient for iron (a) and iodine (b). K-edge of iron appears at 7.11 keV; iodine K-edge at 33.17 keV. L-edges of iodine : L-I 5.19 keV, L-II 4.85 keV and L-III 4.56 keV. Data taken from [Hubbell and Seltzer, 2004].

The detector absorption efficiency is denoted as  $D(E)$  and we assume that the photon counting detector allows energy-resolving measurements in  $N$  energy bins with ideal energy resolution. According to Beer-Lambert law, the expected number of photons  $\lambda_i$ , in energy bin  $B_i$  ( $i=1, 2, \dots, N$ ) can be expressed as

$$\lambda_i = \sum_{E=E_s(i)}^{E_f(i)} D(E) N_0(E) \exp\left[-\int \mu(\vec{x}, E) ds\right], \quad (3.1)$$

where  $E_s(i)$  and  $E_f(i)$  denote the start and final energies of bin  $B_i$ ,  $N_0(E)$  is the number of photons in the initial spectrum at energy  $E$ ,  $\mu(\vec{x}, E)$  represents linear attenuation coefficient of the object at location  $\vec{x}$  and energy  $E$ . It is noticed that there is a location-dependent integral and an energy-dependent sum in this formula, which correspond respectively to the two variables  $\vec{x}$  and  $E$  on which  $\mu(\vec{x}, E)$  depends. Therefore,

if we transform  $\mu(\vec{x}, E)$  into the sum of the products of energy-dependent term  $f_\alpha(E)$  and location-dependent term  $a_\alpha(\vec{x})$ , it will be easier to calculate the integral and the sum separately. We then write

$$\mu(\vec{x}, E) = \sum_{\alpha=1}^M a_\alpha(\vec{x}) f_\alpha(E), \quad (3.2)$$

where  $M$  denotes the number of terms in use. Generally,  $a_\alpha(\vec{x})$  describes the physico-chemical or quantity property (depending on the concrete formulation of Equation (3.2)) of the unknown object and  $f_\alpha(E)$  is a known function that varies with energy. In the work of [Roessl and Proksa, 2007],  $\mu(\vec{x}, E)$  is taken as the combination of photoelectric absorption, Compton scattering and extra K-edge components if there is any K-edge material in the object, making Eq. (3.2) into

$$\mu(\vec{x}, E) = a_{\text{ph}}(\vec{x}) f_{\text{ph}}(E) + a_{\text{Co}}(\vec{x}) f_{\text{KN}}(E) + \sum_{\alpha=1}^{M-2} \rho_\alpha(\vec{x}) \mu_{\text{m}\alpha}(E), \quad (3.3)$$

where  $a_{\text{ph}}(\vec{x})$  and  $a_{\text{Co}}(\vec{x})$  represent location dependency of photoelectric absorption and Compton scattering, respectively.  $f_{\text{ph}}(E)$  denotes the cross section of photoelectric absorption that can be approximated by  $E^{-3}$ , see Equation (2.6).  $f_{\text{KN}}(E)$  is the cross section of Compton scattering, namely Klein-Nishina function, see Equation (2.10).  $\rho_\alpha(\vec{x})$  denotes the density of K-edge material  $\alpha$  at point  $\vec{x}$  and  $\mu_{\text{m}\alpha}(E)$  the mass attenuation coefficient of K-edge material  $\alpha$  at energy  $E$ .  $(M - 2)$  represents the number of K-edge materials inside the object.

Substituting Equation (3.2) into Equation (3.1), we have

$$\begin{aligned} \lambda_i(A_\alpha) &= \sum_{E=E_s(i)}^{E_t(i)} D(E) N_0(E) \exp\left[-\int \sum_{\alpha=1}^M a_\alpha(\vec{x}) f_\alpha(E) ds\right] \\ &= \sum_{E=E_s(i)}^{E_t(i)} D(E) N_0(E) \exp\left[-\sum_{\alpha=1}^M f_\alpha(E) \int a_\alpha(\vec{x}) ds\right] \\ &= \sum_{E=E_s(i)}^{E_t(i)} D(E) N_0(E) \exp\left[-\sum_{\alpha=1}^M f_\alpha(E) A_\alpha(sx, sy)\right], \end{aligned} \quad (3.4)$$

with

$$A_\alpha(sx, sy) = \int a_\alpha(\vec{x}) ds, \quad (3.5)$$

where  $A_\alpha(sx, sy)$  is the line integral of location-dependent parameter  $a_\alpha(\vec{x})$  along the measured projection path,  $(sx, sy)$  represents the location of the measured projection in the sinogram, with  $sx$  denoting detector pixels and  $sy$  denoting measurement angles. To estimate  $A_\alpha(sx, sy)$ , maximum-likelihood (ML) method is used in [Roessl and Proksa, 2007, Schlomka et al., 2008]. Firstly suppose the detected number of photons  $M_i$  form a

set of independent Poisson random variables, then the likelihood function as the possibility of measurement result ( $M_1 = m_1, M_2 = m_2, \dots, M_N = m_N, \dots$ ) can be calculated:

$$P(m_1, \dots, m_N | \lambda_1(A_\alpha), \dots, \lambda_N(A_\alpha)) = \prod_{i=1}^N \frac{\lambda_i(A_\alpha)^{m_i}}{m_i!} e^{-\lambda_i(A_\alpha)}. \quad (3.6)$$

For computational convenience in seeking the extremum, Equation (3.6) is simplified by applying a negative logarithm operator on both sides and dropping the term that is unrelated to  $A_\alpha$ . Then calculating the negative logarithm likelihood function, we will obtain:

$$\begin{aligned} L(A_\alpha) &= -\ln [P(m_1, \dots, m_N | \lambda_1(A_\alpha), \dots, \lambda_N(A_\alpha))] \\ &= \sum_{i=1}^N [\lambda_i(A_\alpha) + \ln m_i! - m_i \ln \lambda_i(A_\alpha)] \\ &\cong \sum_{i=1}^N [\lambda_i(A_\alpha) - m_i \ln \lambda_i(A_\alpha)]. \end{aligned} \quad (3.7)$$

By minimizing the above negative log-likelihood function, the line integral of object density  $A_\alpha$  can be solved. As we can see in Equation (3.5),  $A_\alpha$  is the line integral of  $a_\alpha$ , thus  $a_\alpha$  can be obtained by applying a conventional reconstruction on  $A_\alpha$ .

The K-edge imaging technology enables specific imaging of high-Z K-edge materials, such as iodine bismuth, gold and gadolinium. These materials are good candidates of contrast agents. In the work of Feuerlein, a partially occluded stent was simulated by using a calcified plaque isoattenuated to a surrounding gadolinium chelate solution. By K-edge imaging, the separated gadolinium image clearly shows perfused lumen of vessel [Feuerlein et al., 2008]. In the work of Pan et al., fibrin-specific bismuth-enriched K-edge nanocolloid (nanoK (Bi)) particles are well enhanced in both spectral CT scans of a blood vessel phantom and carotid artery endarterectomy specimens [Pan et al., 2010]. Cormode et al. made *in vivo* experiments using rabbits after injections of gold nanoparticles and iodinated contrast agent, their results show that gold and iodine distributions are clearly differentiated [Cormode et al., 2017].

### 3.1.2 Material-based decomposition

There is actually another commonly used standard to categorize the material decomposition methods for spectral CT. According to the type of data on which the decomposition step operates, the methods can be divided into projection domain method and image domain method. The former, also called pre-reconstruction decomposition method, decomposes projection data into several desired components (i.e. materials), and then applies independently reconstruction to each component to obtain their respective distribution in space. The latter, also known as post-reconstruction method, operates on conventionally reconstructed CT images corresponding to different energy bins to obtain the concentration of target materials using linear matrix inversion, see figure 3.2. Both methods have their advantages and disadvantages, depending on different situations.



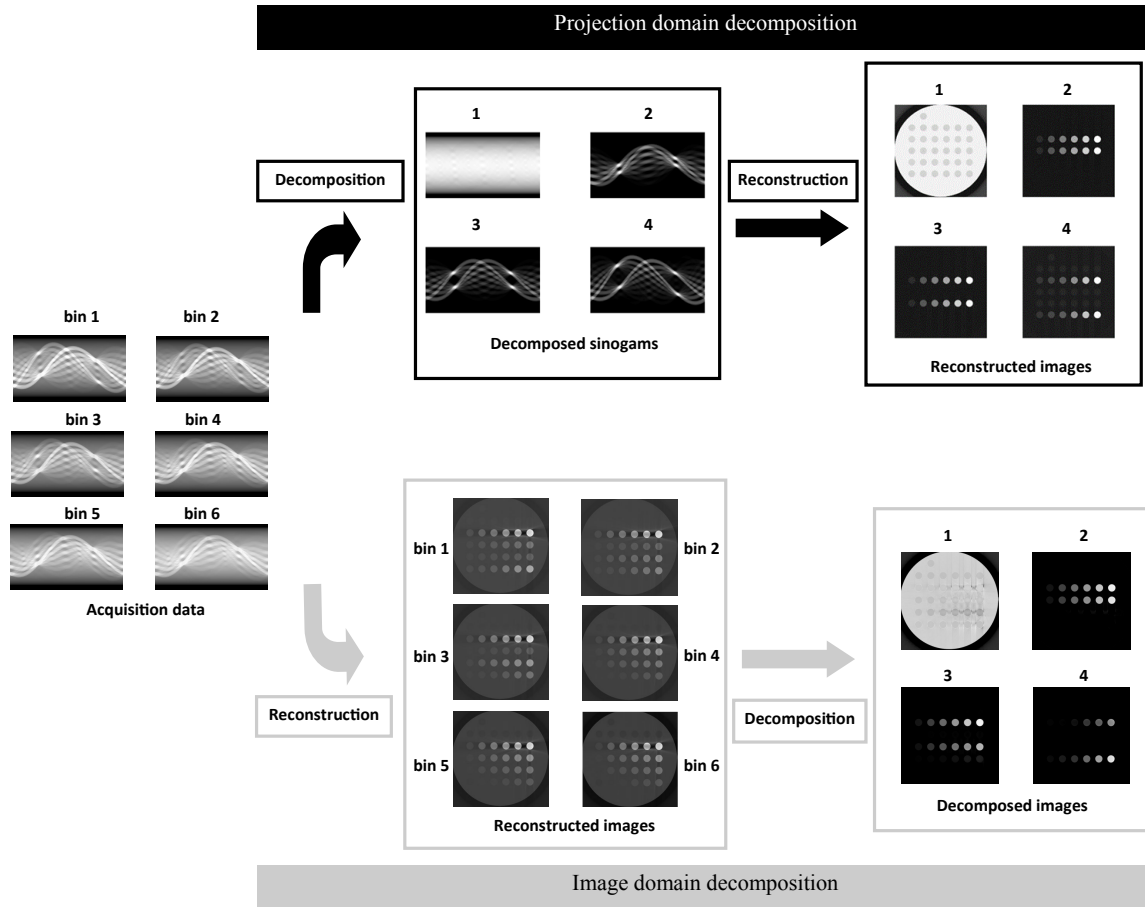


Figure 3.2: Illustration of projection domain decomposition and image domain decomposition. The example here assumes that the spectral CT has 6 energy bins and 6 sinograms are obtained for one acquisition. The former method firstly decomposes acquisition data into  $M$  location-dependent target sinograms ( $M = 4$ ) in this case, and then perform a reconstruction on each obtained sinogram to get the final spatial image. Image domain method firstly reconstructs the spatial images from their respective projection data corresponding to a given energy bin, and then performs material decomposition on these image domain data (i.e. the reconstructed spatial images).

The K-edge imaging presented in 3.1.1 is actually a projection domain method since it processes directly the projection data. We know from K-edge imaging that only the K-edge materials with relatively high atomic number can be discriminated using the projection domain method. However, in practice, non-K-edge materials are more commonly encountered. Lighter atoms, such as iron, calcium and potassium, usually have much lower K-edge energy that is beyond the detection energy range. In this situation, K-edge imaging method can not distinguish them, nor give any quantitative information since their attenuations are all included and mixed in photoelectric absorption and Compton scattering. Therefore, another version of formula Equation (3.2) should be considered to describe linear attenuation coefficient in terms of a basis of  $M$  materials. We will develop

the material-based method in two situations: projection domain decomposition and image domain decomposition.

### Projection domain material-based method

We have introduced that the attenuation coefficient can be considered as the linear combination of the basis material mass attenuation coefficients weighted by their densities. So we have

$$\begin{aligned}\mu(\vec{x}, E) &= \rho_1(\vec{x})\mu_{m1}(E) + \rho_2(\vec{x})\mu_{m2}(E) + \dots + \rho_M(\vec{x})\mu_{mM}(E) \\ &= \sum_{\alpha=1}^M \rho_{\alpha}(\vec{x})\mu_{m\alpha}(E),\end{aligned}\quad (3.8)$$

where  $\rho_{\alpha}(\vec{x})$  denotes the density of material  $\alpha$  at point  $\vec{x}$ . Material  $\alpha$  is not exclusive to K-edge materials, but also applicable for lighter materials.  $\mu_{m\alpha}(E)$  designates the mass attenuation coefficient of material  $\alpha$  at energy  $E$ , which can be found in NIST database [Hubbell and Seltzer, 2004].  $M$  should be smaller than or equal to  $N$ , otherwise the problem will be under-determined and an infinite number of solutions exist if there are no other equality constraints. The types of materials chosen for decomposition depend on the application and prior knowledge of the scanned objects.

Similarly with Equation (3.4), by substituting Equation (3.8) into Eq. (3.1), we have

$$\begin{aligned}\lambda_i &= \sum_{E=E_s(i)}^{E_f(i)} D(E)N_0(E) \exp\left[-\int \sum_{\alpha=1}^M \rho_{\alpha}(\vec{x})\mu_{m\alpha}(E) ds\right] \\ &= \sum_{E=E_s(i)}^{E_f(i)} D(E)N_0(E) \exp\left[-\sum_{\alpha=1}^M \mu_{m\alpha}(E) \int \rho_{\alpha}(\vec{x}) ds\right] \\ &= \sum_{E=E_s(i)}^{E_f(i)} D(E)N_0(E) \exp\left[-\sum_{\alpha=1}^M \mu_{m\alpha}(E)P_{\alpha}(sx, sy)\right],\end{aligned}\quad (3.9)$$

with

$$P_{\alpha}(sx, sy) = \int \rho_{\alpha}(\vec{x}) ds, \quad (3.10)$$

where  $P_{\alpha}(sx, sy)$  is the line integral of object density  $\rho_{\alpha}(\vec{x})$  along the measured projection path. Normally the objective function used to estimate  $P_{\alpha}(sx, sy)$  is the least squares (LS) method:

$$P_{\alpha} = \arg \min_{P_{\alpha}} \sum_{i=1}^N [\lambda_i(P_{\alpha}) - m_i]^2, \quad (3.11)$$

where  $m_i$  is the measured number of photons in energy bin  $B_i$ . After  $P_{\alpha}$  is obtained, we can apply conventional reconstructions to get the density distribution of target materials. We denote this method as proj-LS method.

### Image domain material-based method

Unlike projection domain method, decomposition in image domain works on conventionally reconstructed images  $\mu(i, \vec{x})$  for each energy bin  $B_i$ , which represents energy-resolved linear attenuation coefficient. Similarly to Equation (3.8),  $\mu(i, \vec{x})$  is considered to be the linear combination of mass attenuation coefficients  $\mu_{m\alpha}(i)$  within one energy bin  $B_i$  weighted by the concentration of material  $\rho_\alpha(\vec{x})$ :

$$\begin{aligned}\mu(\vec{x}, i) &= \rho_1(\vec{x})\mu_{m1}(i) + \rho_2(\vec{x})\mu_{m2}(i) + \dots + \rho_M(\vec{x})\mu_{mM}(i) \\ &= \sum_{\alpha=1}^M \rho_\alpha(\vec{x})\mu_{m\alpha}(i).\end{aligned}\quad (3.12)$$

The main difference between Equation (3.12) and Equation (3.8) is that  $\mu_{m\alpha}(i)$  denotes the mass attenuation coefficient of material  $\alpha$  within energy bin  $B_i$ , instead of a punctual fixed energy value. It is not trivial to determine the exact  $\mu_{m\alpha}(i)$  values since precisely it correlates not only with energy, but also with unknown object properties. A simplified formula to determine the effective mass attenuation coefficient of one energy bin from punctual energy values is defined by [Le and Molloy, 2011]:

$$\mu_{m\alpha}(i) = \frac{\sum_{E=E_s(i)}^{E_t(i)} N_0(E)\mu_{m\alpha}(E)}{\sum_{E=E_s(i)}^{E_t(i)} N_0(E)}.\quad (3.13)$$

By writing the location vector  $\vec{x}$  into two-dimensional coordinates  $(x, y)$ , the density distribution of material  $\alpha$  can be expressed as  $\rho_\alpha(x, y)$ . And the least squares minimization to estimate  $\rho_\alpha(x, y)$  can be written as

$$\rho_\alpha(x, y) = \arg \min_{\rho_\alpha} \sum_{i=1}^N [\hat{\mu}(x, y, i) - \sum_{\alpha=1}^M \rho_\alpha(\vec{x})\mu_{m\alpha}(i)]^2,\quad (3.14)$$

where  $\hat{\mu}(x, y, i)$  represents the estimated linear attenuation coefficient corresponding to energy bin  $B_i$  from conventionally reconstructed images. This method is in image domain and is based on LS criterion, thus we call it ima-LS method.

Material-based decomposition has wider applications and also presents the potential to be optimized. Le and Molloy used a calibrated least squares fitting technique in image domain to quantify calcium and iodine [Le and Molloy, 2011] for breast imaging. To assess tissue composition of atherosclerotic plaque, Alessio and MacDonald used weighted least-squares method, which assumes that the materials are limited at a certain location to only those contained in one of the pre-selected classes. Therefore, this method firstly segments the image into pre-selected classes, then decomposes the pixel into corresponding materials contained in the class [Alessio and MacDonald, 2013]. Zeng et al. proposed a reconstruction method that uses penalized weighted least-squares scheme incorporating the structure tensor total variation regularization to gain better material decomposition quality [Zeng et al., 2016]. Ducros et al. uses a regularized weighted least squares Gauss-Newton algorithm to decompose the spectral X-ray projection images of a thorax phantom into soft tissue, bone and gadolinium bases [Ducros et al., 2017].

## 3.2 Patchwise regularized decomposition

In the present work, material-based method is preferred according to our application. The commonly used objective function which is based on LS criterion (Equation (3.11) and (3.14)) directly minimizes the errors between expected and measured number of photons or the errors between expected and reconstructed attenuation coefficients. However, the inverse problem of material decomposition is usually ill-posed and the X-ray spectral CT measurements suffer from Poisson photon counting noises. The standard least squares objective function can lead to overfitting to the noisy measurement data. We then propose to add a regularization term to penalize the sum of the square variations of the decomposed images, in order to reduce the effect of noise and enforce smoothness.

### 3.2.1 Projection domain

For projection domain decomposition, Equation (3.11) gives the objective function to solve the density integrals of different materials by minimizing the square errors between expected number of photons  $\lambda_i$  and measured number of photons  $m_i$  for all energy bins. According to Beer-Lambert law, the number of transmitted photons is negatively exponential to the attenuation coefficient. Instead of minimizing directly the difference of number of photons, we propose a least log-squares (LLS) criterion, as given in Equation (3.15). A natural logarithm operator is placed on  $\lambda_i$  and  $m_i$ , which makes them inversely related to the linear attenuation coefficient. Therefore Equation (3.15) has a physical meaning of minimizing the errors on linear attenuation coefficient.

$$P_\alpha(sx, sy) = \arg \min_{P_\alpha(sx, sy)} \sum_{i=1}^N [\ln(\lambda_i(P_\alpha^C)) - \ln(m_i^C)]^2. \quad (3.15)$$

Material decomposition using the above LLS criterion is called proj-LLS method. Based on proj-LLS method, we further propose a patchwise regularized least log-squares (proj-PR-LLS) method. Firstly, the sinograms from acquisition are divided into patches with the size of  $np \times np$ . The decomposition is performed patch by patch by minimizing the following objective function:

$$P_\alpha^C(sx, sy) = \arg \min_{P_\alpha^C(sx, sy)} \left\{ \sum_{(sx, sy) \in C} \sum_{i=1}^N [\ln(\lambda_i(P_\alpha^C)) - \ln(m_i^C)]^2 + rR(P_\alpha^C) \right\}, \quad (3.16)$$

where  $P_\alpha^C(sx, sy)$  represents  $P_\alpha(sx, sy)$  when  $(sx, sy)$  is inside patch  $C$ .  $r$  denotes the relaxation parameter.  $R(P_\alpha^C)$  is the regularization term used to reduce the effect of noise and enforce smoothness. Figure 3.3 illustrates the decomposition process for patch  $C$ . The objective function is composed of two parts, the squared residuals from acquisition data and the regularization term from the target decomposed data, both parts are calculated within the same patch  $C$ . By minimizing this objective function, the density integrals of target materials in patch  $C$  can be decomposed. Then we go on with the next patch until all the patches are traversed. After obtaining  $P_\alpha(sx, sy)$  for each material, FBP reconstruction is applied to get materials' density distribution.

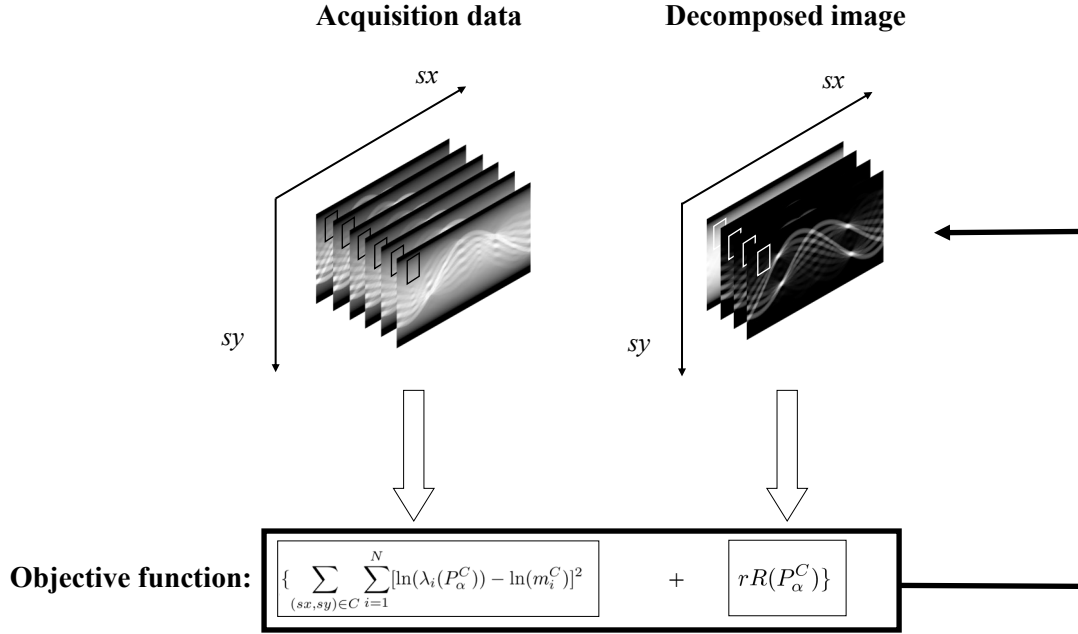


Figure 3.3: Illustration of the proj-PR-LLS method for patch  $C$ . Patch  $C$  is noted by rectangular regions in the acquisition sinograms and the decomposed images. The objective function is calculated by summing up the squared residuals from acquisition data and the regularization term from the target decomposed data. Decomposed images in patch  $C$  are obtained by minimizing the objective function.

$R(p_\alpha^C)$  in this work is considered as the sum of the  $L2$  regularizations of gradient images of  $P_\alpha^C$ :

$$\begin{aligned}
 R(P_\alpha^C) &= \sum_{\alpha=1}^M \|\nabla P_\alpha^C\|_2^2 \\
 &= \sum_{\alpha=1}^M \sum_{\substack{(sx,sy) \in C \\ (sx-1,sy) \in C \\ (sx,sy-1) \in C}} \{ [P_\alpha^C(sx, sy) - P_\alpha^C(sx-1, sy)]^2 \\
 &\quad + [P_\alpha^C(sx, sy) - P_\alpha^C(sx, sy-1)]^2 \}. \quad (3.17)
 \end{aligned}$$

This regularization term enforces patchwise smoothness and can reduce the effect of noise.

### 3.2.2 Image domain

We have introduced in 3.1.2 the commonly used image domain material decomposition method, which can be summarized into two steps: firstly, reconstruct conventional (spatial) images of linear attenuation coefficients from the acquired projection data corresponding to different energy bins; then perform material decomposition on the reconstructed images.

Equation (3.14) gives a standard least squares objective function minimizing the square errors between expected and reconstructed linear attenuation coefficients. To improve image quality, we propose to use the patchwise regularized least-squares (ima-PR-LS) method for the estimation of  $\rho_\alpha(x, y)$ :

$$\rho_\alpha^C(x, y) = \arg \min_{\rho_\alpha^C(x, y)} \left\{ \sum_{(x, y) \in C} \sum_{i=1}^N [\hat{\mu}^C(x, y, i) - \sum_{\alpha=1}^M \rho_\alpha^C(x, y) \mu_{m\alpha}(i)]^2 + rR(\rho_\alpha^C) \right\}, \quad (3.18)$$

where  $\rho_\alpha^C(x, y)$  is the density of material  $\alpha$  when its location  $(x, y)$  is inside patch  $C$ .  $r$  denotes the relaxation parameter.  $R(\rho_\alpha^C)$  is the regularization term. Similarly to Equation 3.17,  $R(\rho_\alpha^C)$  is the sum of the  $L2$  regularizations of gradient images of material density  $\rho_\alpha^C$ :

$$\begin{aligned} R(\rho_\alpha^C) &= \sum_{\alpha=1}^M \|\nabla \rho_\alpha^C\|_2^2 \\ &= \sum_{\alpha=1}^M \sum_{\substack{(x, y) \in C \\ (x-1, y) \in C \\ (x, y-1) \in C}} \{[\rho_\alpha^C(x, y) - \rho_\alpha^C(x-1, y)]^2 \\ &\quad + [\rho_\alpha^C(x, y) - \rho_\alpha^C(x, y-1)]^2\}. \end{aligned} \quad (3.19)$$

Formula (3.18) minimizes the square errors between reconstructed attenuation coefficient value and expected coefficient value given by Equation (3.12), and at the same time constrains the total sum of squared variations within patches.

Figure 3.4 is an illustration of the ima-PR-LS method. The reconstructed images are divided into location-dependent small patches. At the same time, the decomposed images are also supposed to have the same division. For patch  $C$ , the objective function consists of two parts, squared residuals of the reconstructed linear attenuation coefficients and regularization term of the decomposed images. Material density within patch  $C$  can be obtained by minimizing this objective function. By repeating the decomposition process for all patches, we can get the whole density distribution of all materials.

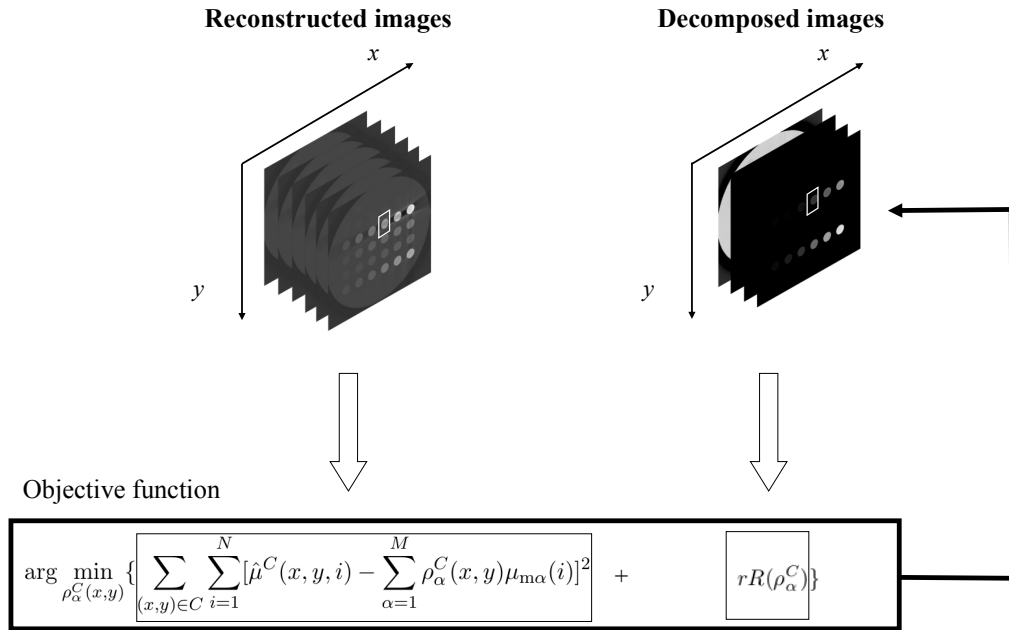


Figure 3.4: Illustration of the image domain decomposition process based on a patchwise regularized least squares criterion for patch  $C$ . Patch  $C$  is denoted by the rectangular regions in the reconstructed or decomposed images. The objective function is calculated by summing up the squared residuals and the regularization term from the target decomposed data. Decomposed images in patch  $C$  is obtained by minimizing the objective function.

### 3.3 Summary

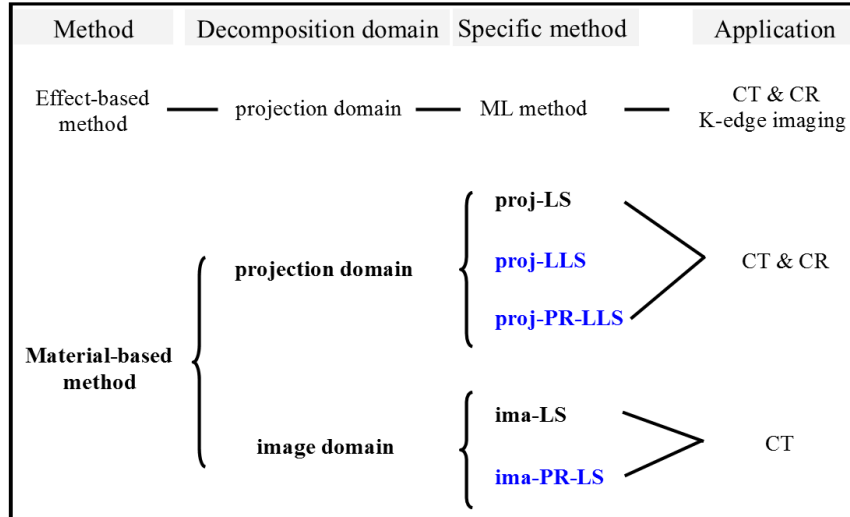


Figure 3.5: The material decomposition methods discussed and proposed (in blue) in this chapter. The term “CR” in refers to computed radiography.

In this chapter, we have described in detail the existing and proposed material decomposition methods for X-ray spectral CT, as illustrated in Figure 3.5.

According to the formulation of the decomposition, the existing material decomposition methods can be divided into two categories. The first is effect-based decomposition, also called K-edge imaging, where the attenuation is considered as a linear combination of the photoelectric effect, Compton effect and extended K-edge components if there are materials with their K-edge within the CT energy range. The second is material-based method, which views the linear attenuation coefficient as the contributions of a basis of materials. For the material-based method, we have introduced the least squares based decomposition in projection domain (proj-LS method) and in image domain (ima-LS method). The former method decomposes projection data into several desired components, and then applies independent reconstruction to each component to obtain the distribution of materials. The latter operates on conventionally reconstructed CT images corresponding to different energy bins to obtain the concentration of target materials using linear matrix inversion.

Based on the existing methods, we have investigated the material-based approaches. We have proposed a least log-squares criterion for projection domain method to minimize the errors on linear attenuation coefficient: proj-LLS method. Furthermore, to reduce the effect of noise and enforce smoothness, we proposed patchwise regularized decomposition methods in both projection domain and image domain. The proposed methods minimize the square errors between the logarithmic expected and measured number of photons (proj-PR-LLS method), or between the reconstructed attenuation coefficient value and expected coefficient value (ima-PR-LS method), and at the same time constrains the total sum of squared variations within patches. The reason for having applied regularization to small patches instead of the whole image is to avoid huge computation cost. However, the



patchwise regularized can cause “pattern” defects where gray difference may exist between adjacent patches. This defect along with the computation cost of ima-PR-LS and proj-PR-LLS methods will be discussed in Chapter 5.

Although the above decomposition methods have been demonstrated in the case of spectral CT, the projection domain methods can also be applied to spectral computed radiography (CR) which is based on the PCD. Thus, as a first step, we will analyze in Chapter 4 the performance of projection domain methods only through spectral CT and CR imaging for medical and industrial applications. Then, in Chapter 5, We will compare projection and image domain methods and explore the influence of acquisition parameters on material decomposition performance.

## Chapter 4

# Material decomposition results for different applications: phantoms study

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## 4.1 Introduction

The objective of this chapter is to introduce the simulation method of X-ray imaging and to evaluate the proposed projection domain material decomposition methods through the simulation study. Around these two points, firstly we will present the spectral CT simulation method based on Virtual X-ray imaging (VXI) software. Secondly, targeting on a medical application (atherosclerosis imaging, CT) and an industrial application (plastic sorting, computed radiography (CR)), we will simulate through VXI software the X-ray imaging process with two corresponding phantoms, apply the proposed methods and analyze their performance. For the former application, we will compare the decomposition performance of the proj-LS, proj-LLS and proj-PR-LLS method and for the latter application, we will use proj-PR-LLS method and a further developed proj-PR-LLS-clas method.

For both applications in this chapter, the spectral CT or CR imaging process are simulated with currently used acquisition parameters, e.g. number of energy bins and exposure factor. We will compare the performance of proj-PR-LLS and ima-PR-LS method, and investigate the influence of these parameters on their performance in Chapter 5.

## 4.2 Simulation of spectral X-ray imaging

### 4.2.1 Basic principles

We simulate the spectral CT/CR system which has multiple energy bin resolving capability using Virtual X-ray imaging (VXI) software [Duvauchelle et al., 2000]. VXI software was developed at INSA Lyon (France) to simulate the radiographic, radiosopic and tomographic imaging. The simulation is based on ray-tracing techniques together with the X-ray attenuation law.

Figure 4.1 illustrates the basic principle of simulation technique used in VXI. The X-rays are emitted by the source towards the object and pixelized detector. The object consists of different small voxels. Each ray interacts with a set of voxels when crossing the object and then the transmitted number of photons is detected by the detector. For the given detector pixel  $K$  in Figure 4.1, consider the ray  $SK$  between source point  $S$  and detector  $K$ , the expected number of photons  $N(E)$  that arrive at pixel  $K$  is calculated by Beer-Lambert law:

$$N(E) = N_0(E)\Delta\Omega \exp \left[ \sum_{\alpha} -\mu_{\alpha}(E)x_{\alpha} \right], \quad (4.1)$$

where  $N_0(E)$  is the emitted number of photons with energy  $E$  from the X-ray source per solid angle unit;  $\Delta\Omega$  is the corresponding solid angle of ray  $SK$ , which is proportional to the size of pixel  $K$ ;  $\mu_{\alpha}(E)$  represents the linear attenuation coefficient of material  $\alpha$  at energy  $E$  and  $x_{\alpha}$  the total path length through the material  $\alpha$ . Photons scattered inside the object or the detector are not taken into account in the present simulation study.

VXI software allows the users to define a set of parameters for their own applications. Figure 4.2 illustrates the simulated imaging chain. The users can define the geometry of the source including shape, size and position, the spectrum and photon flux. Beam parameters enable, if need be, collimators to be taken into account. Object geometry allows import of standard Computer-aided Design (CAD) files and definition of various

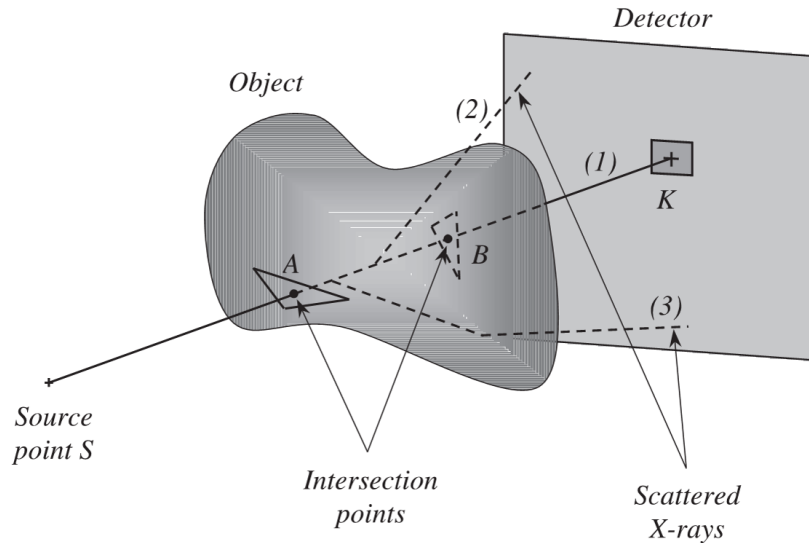


Figure 4.1: Illustration of the simulation principles. The ray  $SK$  intersects two meshes at points  $A$  and  $B$ . Geometrical calculations enable the attenuation path length  $AB$  to be determined. Ray (1): transmitted photons. Ray (2) and (3): scattered photons. Figure is retrieved from [Duvauchelle et al., 2000].

materials. Detector parameters enable the simulation of detectors with different geometries (pixel size/number, position and energy channels) and detecting modes (counting mode counts the total detected number of photons; integration mode records the total absorbed energy by detector; spectro mode counts the arriving photons into corresponding predefined energy bins). In addition to all these geometry parameters, we can also control the movements of samples to simulate the rotation of CT imaging and acquire a number of tomographic projection images.

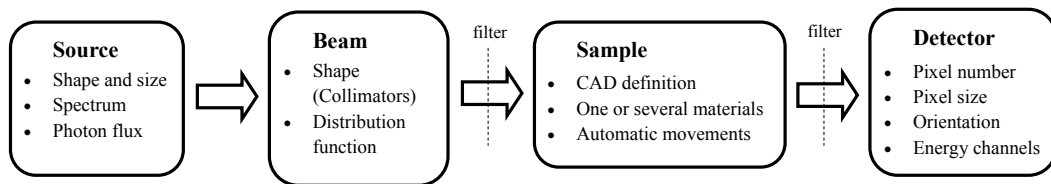


Figure 4.2: Illustration of the simulated imaging chain. Every box in this figure corresponds to a section of the simulation software, in which several parameters are adjustable. Figure is retrieved from [Duvauchelle et al., 2000].

#### 4.2.2 X-ray source generation

In this software, multiple properties of X-ray source can be defined. Our simulation was carried out with point X-ray sources based on Birch & Marshall model [Birch and Marshall,

1979]. Figure 4.3 shows two spectra used in the present study: both were computed for tungsten target material without filtration, the target angles were  $17^\circ$  and the tube voltage were respectively 100kVp and 120kVp. The beam shapes were chosen to be isotropic. Other parameters like position and tube current were set respectively according to specific applications.

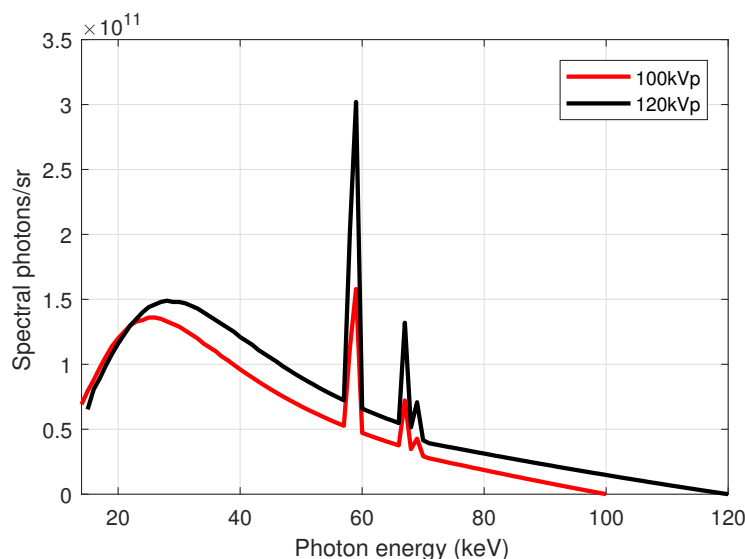


Figure 4.3: The X-ray spectra are computed based on Birch & Marshall model for tungsten target material without filtration, the target angles were  $17^\circ$  and the tube voltage were set to be 100kVp and 120kVp.

### 4.2.3 Sample definition

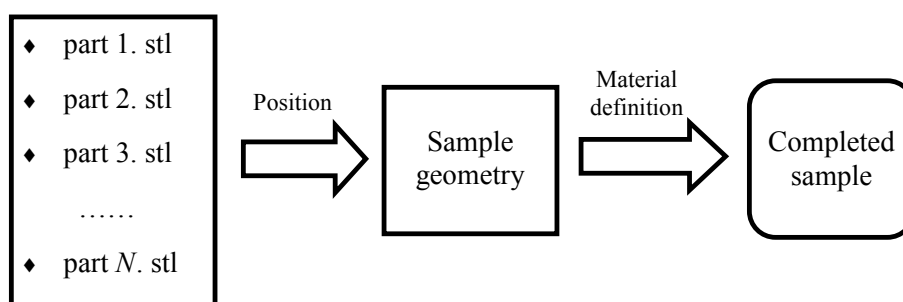


Figure 4.4: Scheme of sample definition process: geometry of each part of the sample is designed separately, then assembled together to obtain the sample geometry, finally we can define the material for each part of sample to get the completed sample.

The definition of sample in VXI includes geometry definition and material definition. VXI accepts standard CAD files to describe the geometry of object. For the present work, the 3D objects were designed in CAD with stereolithographic (STL) format and

then were imported into VXI. For an object consisting of several parts, each part can be handled independently in CAD and then all parts can be assembled in VXI by giving them different positions. After having the sample geometry, another step is to define the material for each part of sample. VXI allows chemical compound or mixture material definition by assigning the constituent elements with different atomic percentages or mass percentages. Take water ( $\text{H}_2\text{O}$ ) as an example, we can define this material either by assigning atomic percentages 66.67% and 33.33% or mass percentages 11.19% and 88.81% to hydrogen (H) and oxygen (O). Figure 4.4 illustrates the entire sample definition process.

#### 4.2.4 Detector definition

Detector geometry can be determined by defining the number and size of pixels of the detector. It is also possible to define the detector material (chemical composition, density, thickness) as well as the position and orientation of the detector plane. Targeted on the simulation of photon counting detector, we choose the spectro mode, and characterize the number of detector energy bins and the starting/final energy of detecting energy range in order to allows counting the arriving photons into corresponding pre-defined energy bins to simulate the spectral X-ray imaging process.

#### 4.2.5 Noise condition

During our simulation, photon noise was simulated for spectral CT/CR imaging. We will discuss in the following content the photon noise for polychromatic beam in photon counting mode, how we simulate it for spectral X-ray imaging and the influence of the number of photons on the signal-to-noise ratio.

For monochromatic beam of energy  $E$ , the raw data coming from photon-counting process has Poisson distribution [Ochi, 1990, Hasinoff, 2014]. Denoting the expected number of photons as  $\lambda_E$  and the measurement as  $m_E$ , then the probability of detecting  $m_E$  photons can be calculated by

$$m_E \sim \text{Poisson}(\lambda_E), p(m_E) = \frac{e^{-\lambda_E} \lambda_E^{m_E}}{m_E!}. \quad (4.2)$$

Poisson distribution has the property that its variance  $\sigma_E^2$  equals the expected counting  $\lambda_E$ , as given by

$$\sigma_E^2 = \lambda_E. \quad (4.3)$$

This indicates that the photon noise depends on the expected number of photons  $\lambda_E$  and that its standard deviation increases with the square root of  $\lambda_E$ . When it comes to polychromatic beam, as in the spectral CT/CR imaging process, the detected number of photons  $m_i$  for one energy bin  $B_i$  is a sum of all the photons in that energy bin range

$$m_i = \sum_{E=E_s(i)}^{E=E_f(i)} m_E, \quad (4.4)$$

where  $E_s(i)$  and  $E_f(i)$  are the starting and final energies of bin  $B_i$ . Since  $m_E (E = E_s(i), \dots, E_f(i))$  are independent variables that obey the Poisson distribution, the expected value  $\lambda_i$  and variance  $\sigma_i^2$  can be calculated

$$\lambda_i = \sum_{E=E_s(i)}^{E=E_f(i)} \lambda_E, \quad (4.5)$$

$$\sigma_i^2 = \sum_{E=E_s(i)}^{E=E_f(i)} \sigma_E^2 = \sum_{E=E_s(i)}^{E=E_f(i)} \lambda_E. \quad (4.6)$$

It can be noticed that  $m_i$  also has Poisson distribution:  $m_i \sim \text{Poisson}(\lambda_i)$ . When  $\lambda_i$  is greater than about 20, the Poisson distribution can be approximated by the Gaussian distribution with the mean and variance of  $\lambda_i$ , and the approximation improves as  $\lambda_i$  increases. In this case, we have

$$m_i \sim N(\lambda_i, \lambda_i). \quad (4.7)$$

Therefore, we can simulate the photon-counting process by adding a Gaussian noise to the expectation:

$$m_i = \lambda_i + \sigma_i G = \lambda_i + \sqrt{\lambda_i} G, \quad (4.8)$$

where  $G \sim N(0, 1)$  is a standard normal distribution.

The signal-to-noise ratio (SNR) can be defined by the ratio of mean to standard deviation of the measurement [Schroeder, 1999, Bushberg et al., 2003]

$$SNR_i = \frac{\lambda_i}{\sigma_i} = \frac{\lambda_i}{\sqrt{\lambda_i}} = \sqrt{\lambda_i}. \quad (4.9)$$

The above equation indicates that the SNR of the detected signal in each energy bin is proportional to the square root of the expected counting. Consequently, image noise in spectral CT or CR is influenced by the number of photons falling inside each energy bin. Increasing the number of energy bins  $N$  could bring better resolution for material decomposition, but can also increase image noise. The trade-off between hiring more energy bins and augmenting SNR needs to be considered [Leng et al., 2011]. Another factor that directly influences the number of photons arriving on the detector is the exposure factor (milliamperes $\times$ time). Therefore, in the present work, we investigated the influence of these two factors on the performance of material determination methods, details will be presented in Chapter 5.

### 4.3 Decomposition quality assessment

The performance of material decomposition was evaluated by the average density, average error and the contrast-to-noise ratio (CNR) [Leng et al., 2015].

#### 4.3.1 Average density

For a region of interest (ROI) on the decomposed image, the average density  $\bar{\rho}_{ROI}$  can be defined by averaging all values computed after material decomposition in that region:

$$\bar{\rho}_{ROI} = \frac{\sum_{j=1}^J \rho_j}{J}, \quad (4.10)$$



where  $\rho_j$  denotes the calculated density of pixel  $j$ , and  $J$  the total number of pixels within that ROI.

### 4.3.2 Average error

Average error  $AE_{\text{ROI}}$  (%) represents the mean value of absolute relative errors of the ROI, with respect to theoretical density  $t_j$ :

$$AE_{\text{ROI}} = \frac{1}{J} \sum_{j=1}^J \frac{|\rho_j - t_j|}{t_j}. \quad (4.11)$$

### 4.3.3 Contrast-to-noise ratio

To calculate the CNR of the region of interest, we choose another region on the neighboring background area and denote it as BG. The mean density and the standard deviation (i.e. image noise) of the BG region can be denoted respectively as  $\bar{\rho}_{\text{BG}}$  and  $SD_{\text{BG}}$ . The CNR is then given by:

$$\text{CNR} = \frac{\bar{\rho}_{\text{ROI}} - \bar{\rho}_{\text{BG}}}{SD_{\text{BG}}}. \quad (4.12)$$

As in our case,  $\rho_{\text{ROI}}$  should be greater than  $\rho_{\text{BG}}$ , we therefore define the minimum and maximum CNR for the same ROI and BG as:

$$\text{CNR}_{\min} = \frac{\rho_{\text{ROImin}} - \rho_{\text{BGmax}}}{SD_{\text{BG}}}. \quad (4.13)$$

$$\text{CNR}_{\max} = \frac{\rho_{\text{ROImax}} - \rho_{\text{BGmin}}}{SD_{\text{BG}}}. \quad (4.14)$$

## 4.4 Medical application: iodine and calcium identification

### 4.4.1 Medical context

Cardiovascular disease (CVD) produces immense health and economic burdens globally and atherosclerosis is a major contributor for CVD [Benjamin et al., 2017]. Atherosclerosis is a disease in which the inside artery narrows due to the build up of plaque. Plaques inside the coronary arteries is a serious risk factor for adverse cardiovascular events. The ruptures of vulnerable plaques are the cause of about 70% of fatal acute myocardial infarctions and sudden coronary deaths [Naghavi et al., 2003]. It is of great importance to detect the plaque and assess its vulnerability.

A high-risk plaque (HRP) usually demonstrates a large lipid-rich necrotic core that occupies a large proportion of the plaque, a thin fibrous cap with accumulated macrophages behind it, increased plaque inflammation, neovascularization, luminal stenosis and so on [Moreno, 2010]. The commonly used invasive coronary imaging methods include intravascular ultrasound (IVUS), optical coherence tomography (OCT) and near infrared spectroscopy (NRIS) [Sandfort et al., 2015]. Contrast-enhanced IVUS examination enables visualization of neovascularity of the atherosclerotic plaque and associated adventitial vasa vasorum [Feinstein, 2006]; the fibrous cap thickness can be assessed by OCT and the lipid

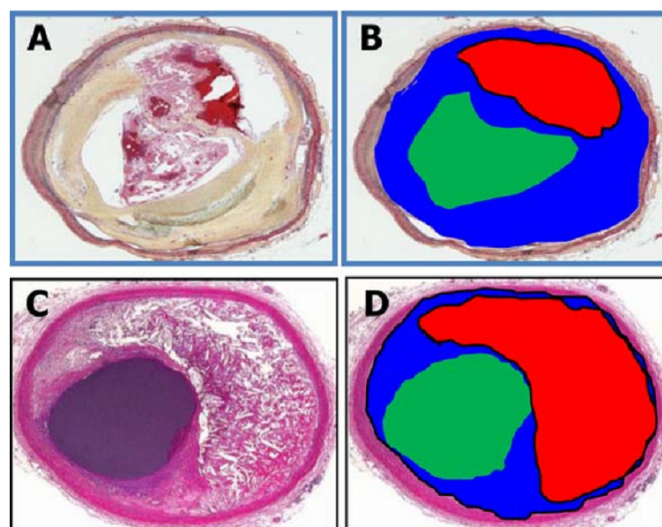


Figure 4.5: Histopathological characteristics of a ruptured plaque (A, B) and the plaque which is prone to disruption (C-D). In images B and D, the plaque area has been colored blue, the lumen in green and the necrotic core in red. The larger the plaque area and the larger the necrotic core size, the higher is the likelihood of plaque vulnerability. Figure retrieved from [Narula, 2009].

content of plaques can be assessed by NIRS [Moreno et al., 2002]. Noninvasive methods include magnetic resonance imaging (MRI) and radionuclide imaging, such as single photon emission computed tomography (SPECT) or positron emission tomography (PET). MRI can demonstrate the coronary vessel lumen and characterizes the coronary vessel wall [Macedo et al., 2008, Miao et al., 2009]; Technetium-99m-labelled ( $^{99m}\text{Tc}$ ) SPECT has the ability to detect the presence of inflammation in carotid plaques [Sun et al., 2014]; PET imaging can track plaque inflammation using  $^{18}\text{F}$ -fluorodeoxy glucose (FDG) [Rudd et al., 2008]. All methods can detect the HRP to some extent with limited abilities and improved evaluation can be performed by a combination of multiple methods. However, it will be favorable to find one imaging modality which can evaluate multiple characteristics of HRP at the same time and enable identification with better accuracy.

Computed tomography angiography (CTA) is an X ray computed tomography technique used to visualize arterial and venous vessels throughout the body. The patient is injected with contrast agent (usually iodinated contrast) and then the heart is scanned using a high speed CT scanner. There has been increasing interest in using CTA for atherosclerosis imaging. The multi-slice CT (MSCT) with conventional energy integrating detector has been widely implemented clinically and many research has been done to investigate its potential to detect coronary plaques. Preliminary studies show that MSCT can not only characterize lumen stenosis, but also quantify plaque volume and the extent of vessel wall re-modeling, and depict tissue density according to different X-ray attenuating properties of each structure [Leber et al., 2005, Cademartiri et al., 2006, Voros et al., 2011]. Its performance for HRP detection has been validated by comparing with IVUS and OCT [Voros et al., 2014, Nakazato et al., 2014]. However, MSCT characterizes composition

of plaques depending on the absolute attenuation values, which are easily influenced by multiple parameters: lumen attenuation, body mass index of the patient, and contrast to noise ratio of the images.

Dual-energy CT (DECT) can obtain additional spectral information compared with conventional energy integrating CT and has the potential to improve plaque imaging by enhancing identification of plaque compositions. Barreto et al. showed that DECT is able to characterize atherosclerotic plaques and distinguish calcified plaques from noncalcified plaques by comparison of attenuations at two tube voltages [Barreto et al., 2008]. Tran et al. used DECT to identify the iodinated contrast and hydroxyapatite ( $\text{HA}$ ,  $\text{Ca}_5(\text{PO}_4)_3(\text{OH})$ ), results show that DECT can detect and differentiate between contrast medium and calcified tissues, but its accuracy is dependent on the CT density of tissues and limited when CT attenuation is low [Tran et al., 2009]. Bhavane et al. performed atherosclerosis imaging in mice with liposomal-iodine nanoparticle contrast agent to localize macrophage cells, and identified iodine and calcium concentration map based on DECT material decomposition [Bhavane et al., 2013].

X-ray spectral CT obtains spectral information corresponding to different energy bins with single acquisition. It outperforms DECT with better material decomposition ability and shorter scan time, i.e. reduced radiation dose. Previous CTA studies have shown the limited ability to identify calcification of plaque and iodinated contrast agent which is used to assess stenotic narrowing. In the present study, we will investigate the decomposition ability of the methods (proj-LS, proj-LLS and proj-PR-LLS method) discussed in Chapter 3, and evaluate their performance in the identification of iodine, calcium and soft tissues through a computational human thorax phantom study.

#### 4.4.2 Computational human thorax phantom

We use a computational human thorax phantom to simulate the *in vivo* situations. The geometry of the thorax phantom comes from VHP-Female v.2.2, which is a platform-independent full-body computational human model [Noetscher et al., 2015]. This 3D CAD model contains up to 270 parts, 45 individual muscles, three body shells and so on, all extracted from open-source Visible Human Project - Female dataset of the National Library of Medicine. Figure 4.6 is an illustration of this model, where the geometries of different organs, bones, muscles, tissues, vessels can be clearly seen.

Our simulation needs only the thorax part of the full-body model and the blue line in Figure 4.6 denotes the location of the slice being scanned in our simulation. To build a complete thorax phantom, geometry information is not enough. Material components of different parts included in the thorax phantom are of the same importance. The organ and tissue-specific elemental compositions have been published in Publication 44 of International Commission on Radiological Units and Measurements (ICRU44) [ICRU, 1989] and earlier publications by White [White et al., 1987]. Based on these researches, we defined the components and densities of different tissues included in the thorax phantom shown in Figure 4.7 (a). Table 4.1 is a list of this information.

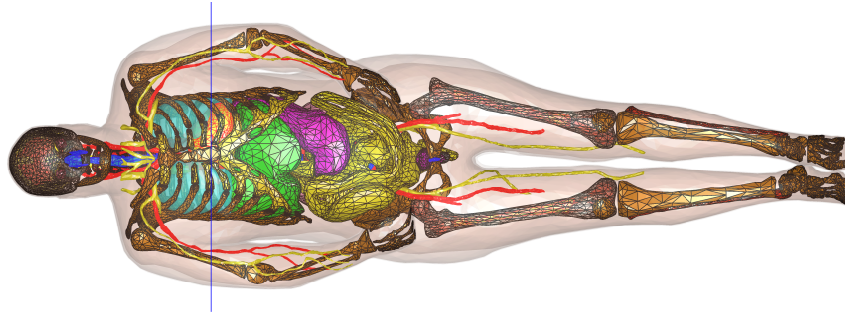


Figure 4.6: Illustration of VHP-Female v2.2 model. Geometries of different body parts have been described in this model, including the organs, bones, muscles, tissues, vessels and so on. The blue line in this figure denotes the slice that is scanned during our later simulation.

Table 4.1: Elemental compositions and mass densities of body tissues included in the thorax phantom.

Body tissue	Elemental composition (% by mass)					Density (kg/m <sup>3</sup> )
	H	C	N	O	Others	
Lung	10.3	10.5	3.1	74.9	Na(0.2); P(0.2); S(0.3); Cl(0.3); K(0.2)	1050
Heart	10.3	12.1	3.2	73.4	Na(0.1); P(0.1); S(0.2); Cl(0.3); K(0.2); Fe(0.1)	1060
Average soft tissue	10.6	30.8	2.4	55.5	Na(0.1); P(0.1); S(0.2); Cl(0.1); K(0.2)	1010
Adipose	11.4	59.8	0.7	27.8	Na(0.1); S(0.1); Cl(0.1)	950
Skin	10	20.4	4.2	64.5	Na (0.2); P(0.1); S(0.2); Cl(0.3); K(0.1)	1090
Sternum	7.8	31.6	3.7	43.8	Mg(0.1);P(4.0);S(0.2); Cl(0.1); K(0.1); Ca(8.5); Fe(0.1)	1250
Cartilage	9.6	9.9	2.2	74.4	Na(0.5); P(2.2); S(0.9); Cl(0.3)	1100
Ribs	6.4	26.3	3.9	43.6	Na(0.1);Mg(0.1); P(6.0); S(0.3); Cl(0.1); K(0.1); Ca(13.1)	1410
Aorta (blood)	10.2	11	3.3	74.5	Na(0.1); P(0.1); S(0.2); Cl(0.3); K(0.2); Fe(0.1)	1060
Vertebra	6.3	26.1	3.9	43.6	Na(0.1); Mg(0.1); P(6.1); S(0.3); Cl(0.1); K(0.1); Ca(13.3)	1420

Besides different kinds of body tissues, extra inserts of calcium and iodine solutions with diameter of 6 mm are placed within the heart region, as shown in Figure 4.7 (b).

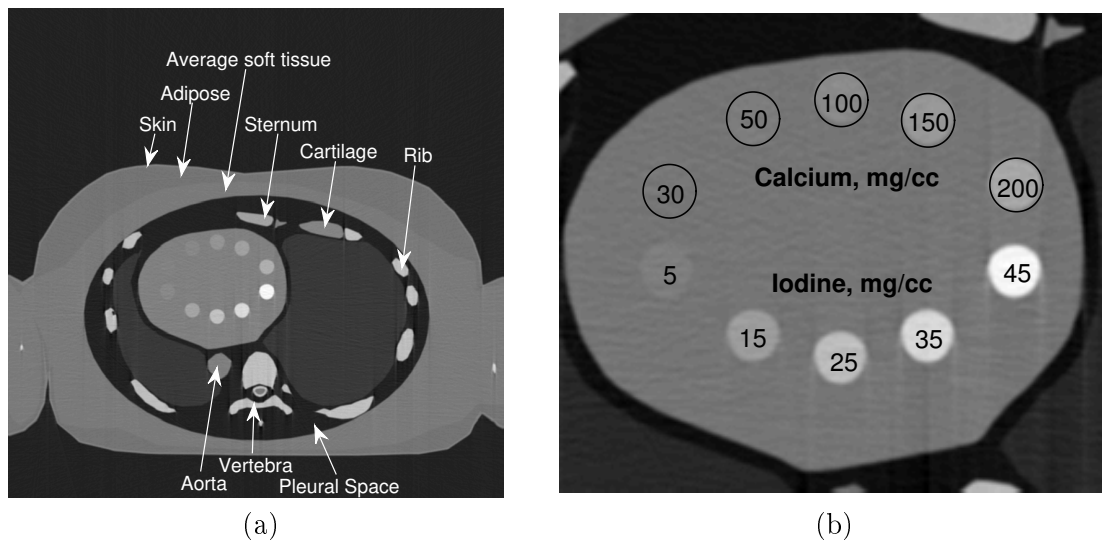


Figure 4.7: Cross section of the thorax phantom with illustration of different material types included (a) and the magnified heart region that contains extra calcium and iodine inserts with different concentrations (b).

Different inserts are with various concentrations (calcium: 30, 50, 100, 150, 200 mg/cc; iodine: 5, 15, 25, 35, 45 mg/cc) as denoted in Figure 4.7 (b). All solutions are a mixture of calcium or iodine with water.

#### 4.4.3 System geometry

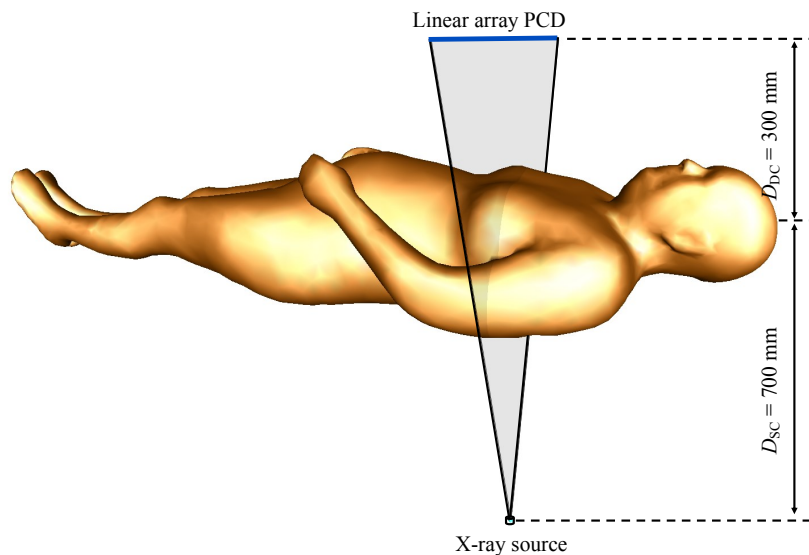


Figure 4.8: Scheme of spectral CT acquisition with computational human phantom.

The simulated X-ray spectral CT system hired a 120kVp X-ray spectrum from tungsten target material without filtration, the target angle was  $17^\circ$  and tube current was 100mA, as show in Figure 4.3. A linear cadmium telluride (CdTe) detector of 1000 pixels with pixel size of  $1\text{mm}\times 1\text{mm}$  was used, and its detecting energy range was set from 30keV to 90keV with evenly distributed 6 energy bins. The absorption efficiency of the detector was simulated for a 3 mm thick CdTe crystal. The thorax phantom was scanned with 1200 projections from  $0^\circ$  to  $360^\circ$  and the scan time was 0.01 s for each projection. The distances of source to the center of rotation and detector to the center of rotation were  $D_{SC} = 700$  mm and  $D_{DC} = 300$  mm respectively. Figure 4.8 illustrates the system geometry.

#### 4.4.4 Results

In this application, we chose soft tissue, calcium and iodine as material basis during decomposition. Three projection domain material decomposition methods with different objective functions were applied:

- ① proj-LS method, corresponding to objective function in Equation (3.11).
- ② proj-LLS method, corresponding to objective function in Equation (3.15).
- ③ proj-PR-LLS method, corresponding to objective function in Equation (3.16). Patch size was set to be  $2 \times 2$  and relaxation parameter was chosen to be 1.

Figure 4.9 shows the decomposed images using the three methods. It is observed that all methods give the distribution of soft tissue, calcium and iodine:

- Skin, adipose, average soft tissue, cartilage, aorta, lung and heart tissues are visible only in the soft tissue image. Besides, part of the bones (ribs, vertebra and sternum) is also present in soft tissue image, because the components of bones contain not only calcium, but also other elements like hydrogen and oxygen.
- Calcium image well highlights bones and inserted calcium solutions
- Iodine is separated appropriately in the iodine-specific image.

We can observe obvious streak artifacts in the decomposed soft tissue image using proj-LS method, which is caused by individual acquisition pixels where few photons were detected and high noise resulted in visible measurement errors. This situation is much better when using the proj-LLS and proj-PR-LLS method.

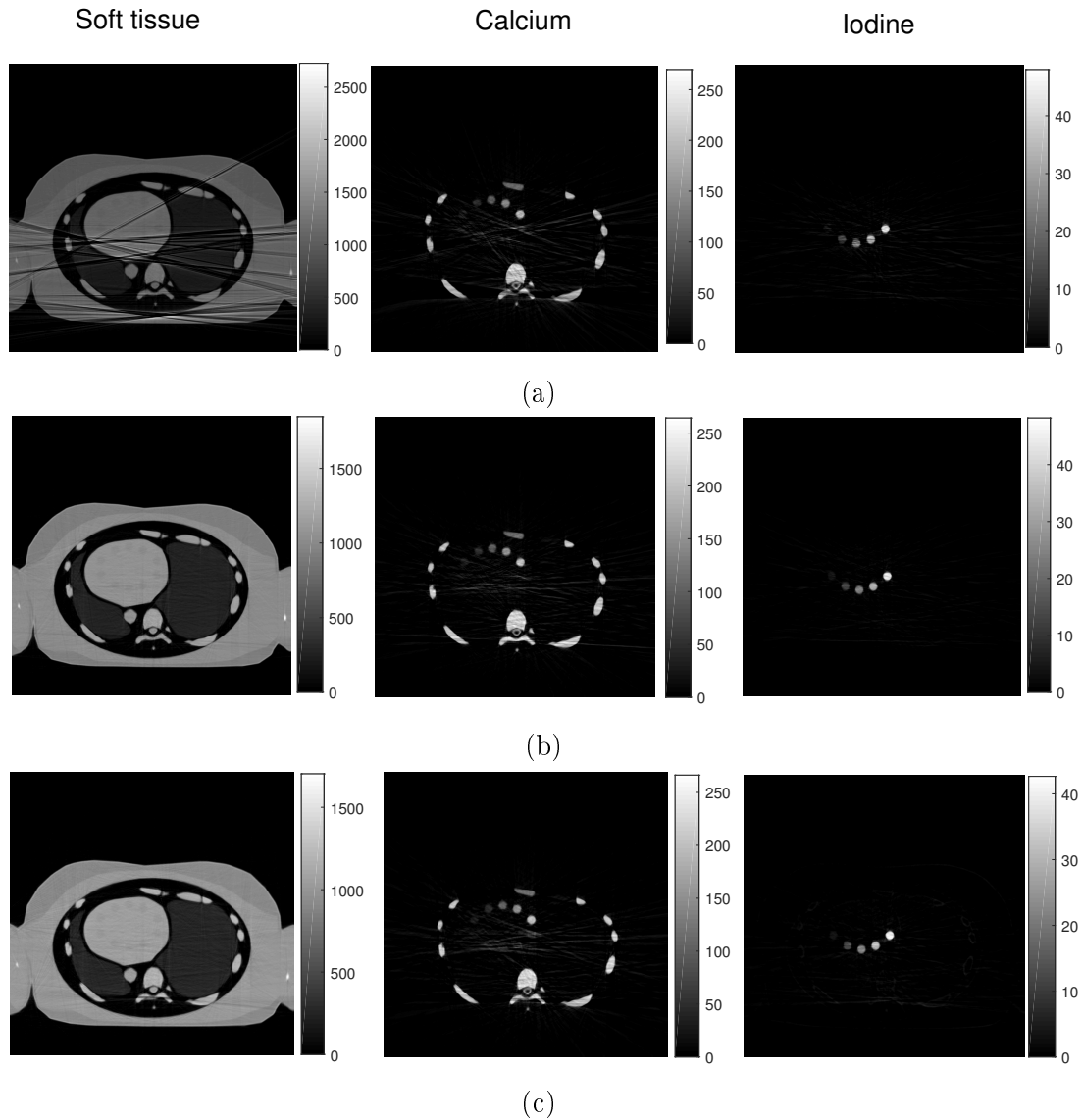


Figure 4.9: Material decomposition results of proj-LS method (a), proj-LLS method (b) and proj-PR-LLS method (c). Each column represents the same material basis, i.e. soft tissue for the first column, calcium for the second and iodine for the third.

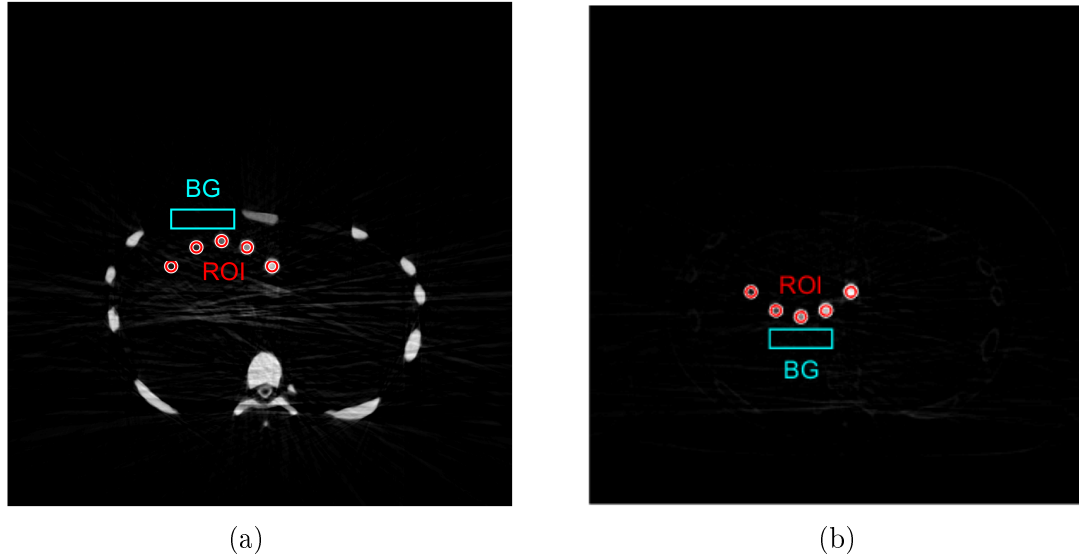
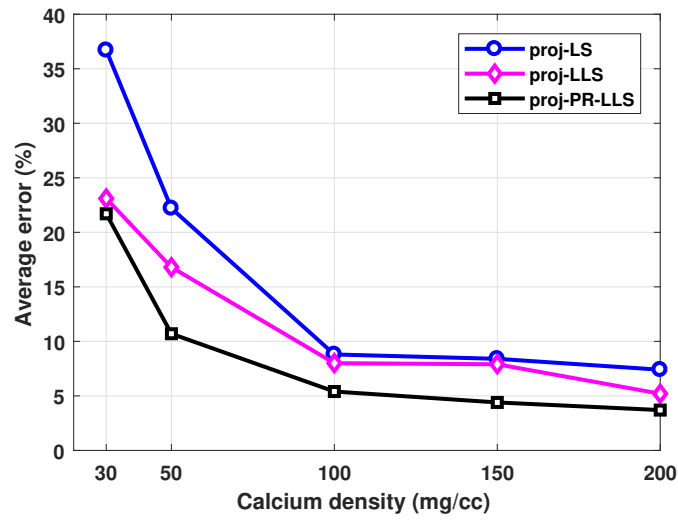


Figure 4.10: Illustration of the ROI and BG regions chosen for quantitative analysis of calcium (a) and iodine (b). The red circles represent ROI and the cyan circles BG regions.

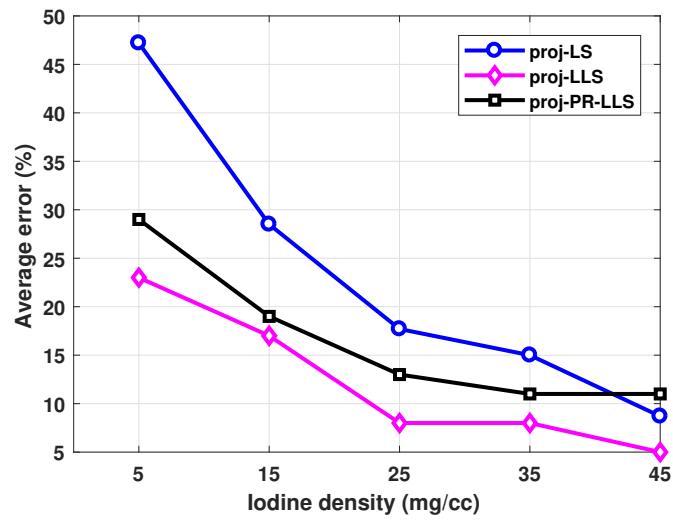
To make a quantitative analysis of the performance of the three methods, we calculated the average errors (AEs) and CNRs of the decomposed calcium and iodine solutions, as shown in Figure 4.11 and Figure 4.12. ROIs were chosen as regions of calcium or iodine insert in the corresponding decomposed image (Figure 4.10 red circles). AE is calculated for each ROI by averaging the absolute relative errors using Equation (4.11). For the calculation of CNRs, we chose a region neighboring to the ROIs as the BG region (Figure 4.10 cyan circles), and determined CNRs according to Equation (4.14).

For the quantification of calcium, it is observed from Figure 4.11 (a) and Figure 4.12 (a) that the proposed proj-PR-LLS method has the best quantification accuracy, i.e. lowest AEs and best image quality, i.e. highest CNRs. For the determination of iodine (Figure 4.11 (b) and Figure 4.12 (b)), the proposed two methods have better performance than the commonly used proj-LS method. Comparing proj-LLS and proj-PR-LLS method, we can observe that proj-LLS method has lower quantification errors, while proj-PR-LLS method can generate iodine image with higher CNRs.



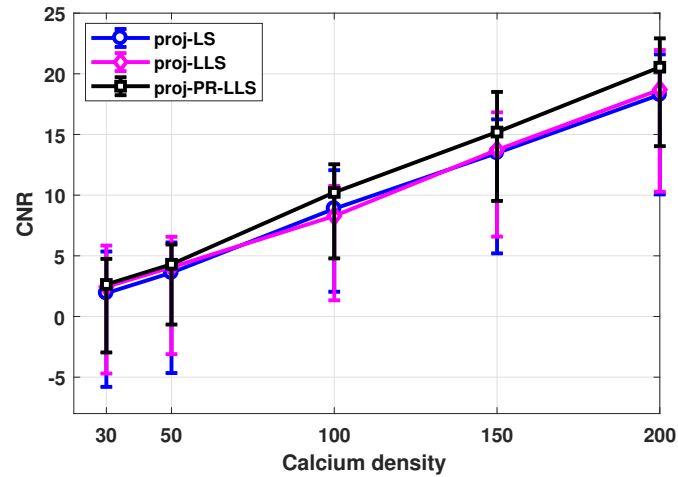


(a)

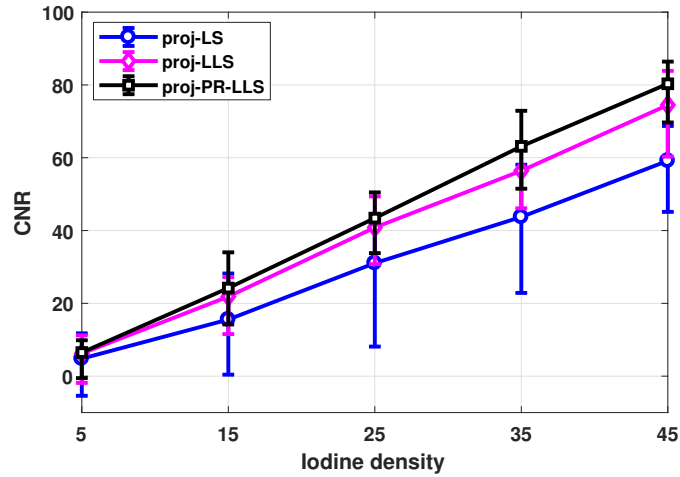


(b)

Figure 4.11: Average errors of decomposed densities of calcium (a) and iodine (b) using proj-LS, proj-LLS and proj-PR-LLS methods.



(a)

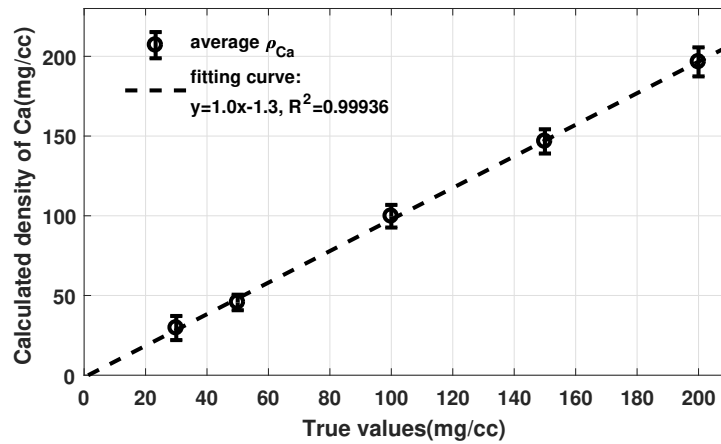


(b)

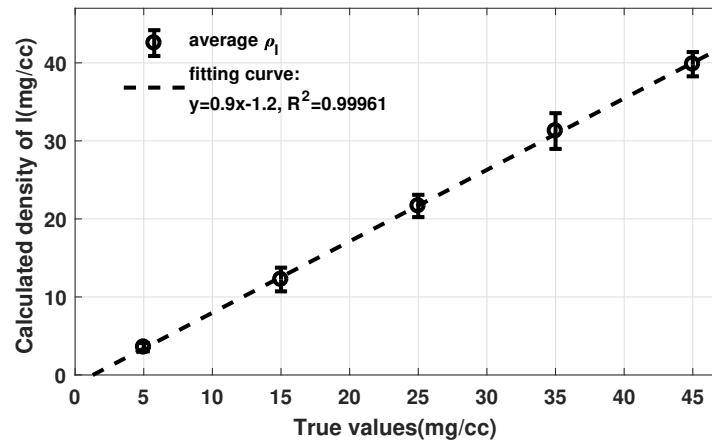
Figure 4.12: CNRs of decomposed calcium and iodine image at different densities using proj-LS, proj-LLS and proj-PR-LLS method. The error bars represent the variation of CNR from  $CNR_{min}$  to  $CNR_{max}$ .

By all the above analysis, we can conclude that our proposed proj-LLS and proj-PR-LLS method have better decomposition performance than the commonly used proj-LS method. Moreover, proj-PR-LLS method has the ability to enhance CNRs of decomposed images while obtaining better (calcium) or inferior but comparative (iodine) quantitative accuracy, when comparing with proj-LLS method.

Figure 4.13 illustrates the relationships between calculated average density within each insert and the known true values of calcium and iodine using proj-PR-LLS method. Good linear relationship can be noticed, the slopes of the fitting curves are around 1 and the constant intercepts are very small, indicating that the measured densities of calcium and iodine are close to true values.



(a)



(b)

Figure 4.13: Comparison of the decomposed average density of calcium (a) and iodine (b) with true values using proj-PR-LLS method. The error bars indicate the standard deviation of decomposed density.

For visual benefits, Figure 4.14 demonstrates the color overlay image using three decomposed material images shown in Figure 4.9 (c). The color overlay process was realized by setting the pixels with densities higher than 30 mg/cc in calcium image into red, the pixels with densities higher than 4 mg/cc in iodine image into green, and finally overlaying the two colors on the soft tissue image. Obvious streak artifacts can be observed in Figure 4.14, because there exists individual acquisition pixels where few photons were detected and high noise resulted in visible measurement errors after reconstruction, and the coloring process by setting a threshold made this artifact more obvious.

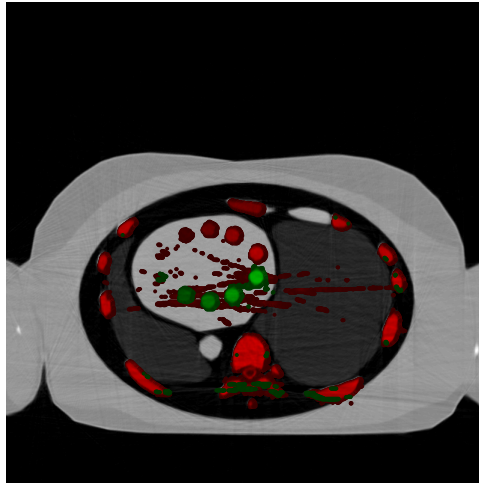


Figure 4.14: Color overlay image of soft tissues(gray), calcium (red) and iodine (green).

#### 4.4.5 Conclusion and discussion

Motivated by the need to distinguish compositions of atherosclerotic plaque, we simulated spectral CT imaging process with a realistic computational human thorax phantom, and investigated the material decomposition performance of the three methods introduced in Chapter 3: proj-LS, proj-LLS and proj-PR-LLS method. Three images were obtained using either method: soft tissue, calcium and iodine image. Results showed that all methods can give quantitative distribution of three materials, among which soft tissue image contains skin, adipose, average soft tissue, cartilage, aorta, lung and heart tissues; calcium image well highlights bones and inserted calcium solutions; iodine image contains only the inserted iodine solutions. Quantitative analysis, including average errors and CNRs demonstrated that the proposed proj-LLS method and proj-PR-LLS method have better quantitative accuracy and better image quality than the commonly used proj-LS method. Moreover, proj-PR-LLS method has the ability to enhance CNRs of decomposed images while obtaining better (calcium) or inferior but comparative (iodine) quantitative accuracy, when comparing with proj-LLS method.

There are potential improvements to our work. Radiation dose to patient is related to the number of projections. A lower number of projections can reduce patient dose but will also decrease image quality due to the sparser sampling of imaging data [Van Daatselaar et al., 2004]. The typical number of projections used by cone beam CT in applications of the breast, extremities, and head scans are 350-450 [Zhao et al., 2014]. In the present study, 1200 projections were used in the simulated phantom scan for better image quality. This number could lead to a prohibited patient dose and this should be considered in future studies.

## 4.5 Industrial application: ABS-FR plastic sorting

### 4.5.1 Industrial context

Waste electrical and electronic equipment (WEEE) has been increasing rapidly due to the development of electronic industry. In European Union, the amount of WEEE generated in 2005 is 9 million tonnes and this number is supposed to grow to 12 million by 2020 [Beigbeder et al., 2013, EuropeanCommission, 2018]. WEEE covers a wide variety of products such as lamps, hairdryers, computers, TV-sets, fridges and cell phones. This kind of waste contains various compositions among which polymers play an important part [Cui and Forssberg, 2003]. Acrylonitrile-butadiene-styrene (ABS) is a major component among all the polymers. The other polymers includes ABS/polycarbonate (PC) alloys, high-impact polystyrene (HIPS), polypropene (PP), poly(vinyl chloride) (PVC), and so on [Barthes et al., 2012]. Due to the presence of electronic power of EEE, the plastic materials should meet high fire safety standards. However, it is not possible to realize with pure polymers, therefore flame retardant (FR) are added to change flammability of plastics and increase the fire resistance [Peeters et al., 2014]. There are mainly four categories of FRs: (a) halogenated organic compounds (e.g., brominated aromatic compounds, chlorinated paraffins and alicyclic compounds), (b) phosphorus compounds (e.g., organophosphates, halophosphates, phosphine oxides and red phosphorus), (c) nitrogen-based compounds and (d) Inorganic salts [Fromme et al., 2016].

Recycling of plastics from WEEE is challenging because of the existence of FRs (especially the brominated and chlorinated FRs), which might result in serious environmental pollution. Therefore, the sorting technique is important for subsequent treatment and recycling of WEEE to avoid major environmental and health problems. Multiple techniques were applied for the plastics identification, such as: Near-infrared (NIR) analysis, Raman absorption spectrometry (RAS), Fourier-transform infrared (FTIR), sliding spark spectroscopy (SSSP), X-Ray fluorescence (XRF), X-Ray computed radiography (CR), and dual Energy computed radiography (DECR) [Peeters et al., 2014].

CR technique measures the absorption of X-ray beam through objects. For materials with similar thickness, it is possible to separate them according to their attenuation nature to X-rays. Material with higher density and larger atomic number tends to absorb more photons. This method can differentiate metal and non-metal materials or lead and barium glasses. However, it is not possible to distinguish materials with similar attenuation properties. DECR provides extra spectral information for material decomposition. Research of using DECR for multi-material identification can be found in waste management [Mesina et al., 2007, Montagner, 2012, Gundupalli et al., 2017]. For example, Duvillier et al. plotted the log-measurement using DECR, polyethylene and PVC can be separated from the curves [Duvillier et al., 2018].

As we have introduced before, photon counting detector is able to obtain spectral information of several energy bins with single acquisition. It provided current CT technology with stronger material decomposition ability. However, the PCDs are not restricted to CT imaging, but can also be applied to CR. As we have mentioned in Chapter 2, the first commercial photon-counting system was introduced for mammography [Åslund et al., 2007], which is an application of X-ray transmission imaging. Furthermore, the proposed patchwise regularized method in projection domain process directly the attenuated X-ray

information, and can be applied for CR imaging. In the present work, we will investigate the material decomposition ability of proj-PR-LLS method for spectral CR imaging in application for ABS-FR plastic sorting. Furthermore, we also develop a classification based decomposition method for this specific application, named proj-PR-LLS-clas method. Its performance will be evaluated in comparison with proj-PR-LLS method.

#### 4.5.2 ABS-FRs phantom

As we have said in the above section, ABS is a major component among all the polymers used by the electrical and electronic equipments, thus we selected it as the polymer material for investigation. We also chose three kinds of commonly used flame retardants, including the brominated (Br), chlorinated (Cl) and phosphorus (P) FRs. They are respectively tetrabromobisphenol A (TBBPA), dechlorane plus (DDC-CO) and resorcinol bis(diphenyl phosphate) (RDP). Three ABS-FR materials were obtained by mixing each FR with ABS at mass percentage of 15%. Information of these materials is summarized in Table 4.2.

Table 4.2: Components of three ABS-FR materials used for the phantom.

Material(ABS-FR)	ABS-TBBPA	ABS-DDC-CO	ABS-RDP
Density of material $\rho$ (mixture)	1060 mg/cm <sup>3</sup>	1060 mg/cm <sup>3</sup>	1060 mg/cm <sup>3</sup>
Chemical formula of FR	C <sub>15</sub> H <sub>12</sub> Br <sub>4</sub> O <sub>2</sub>	C <sub>18</sub> H <sub>12</sub> Cl <sub>12</sub>	C <sub>30</sub> H <sub>24</sub> O <sub>8</sub> P <sub>2</sub>
Mass % ( $\omega$ ) of FR	15%	15%	15%
Mass % ( $\omega$ ) of Br, Cl and P, respectively	8.82%	9.76%	1.62%
$\rho_{\text{eff}}^*$ of Br, Cl and P, respectively	93.5 mg/cm <sup>3</sup>	103.5 mg/cm <sup>3</sup>	17.2 mg/cm <sup>3</sup>

\* :  $\rho_{\text{eff}}$  is the effective density calculated by  $\rho_{\text{eff}}(\alpha) = \rho(\text{mixture}) \times \omega(\alpha)$ .

For example,  $\rho_{\text{eff}}(\text{Br}) = \rho(\text{mixture}) \times \omega(\text{Br}) = 1060 \times 8.82\% = 93.5 \text{ mg/cm}^3$ ;

$\rho_{\text{eff}}(\text{ABS}) = \rho(\text{mixture}) \times \omega(\text{ABS}) = 1060 \times (1 - 15\%) = 901 \text{ mg/cm}^3$ .

We simulated a phantom composed of multiple cubes with height of 10 mm, width of 10 mm and different thicknesses. As shown in Figure 4.15, each column of cubes are of the same material (denoted on the top) and each row of cubes are of the same thickness (denoted on the left). Figure 4.16 shows the mass attenuation coefficients of the components contained in the phantom: ABS, Br, Cl and P, which will be used to distinguish different ABS-FR material.

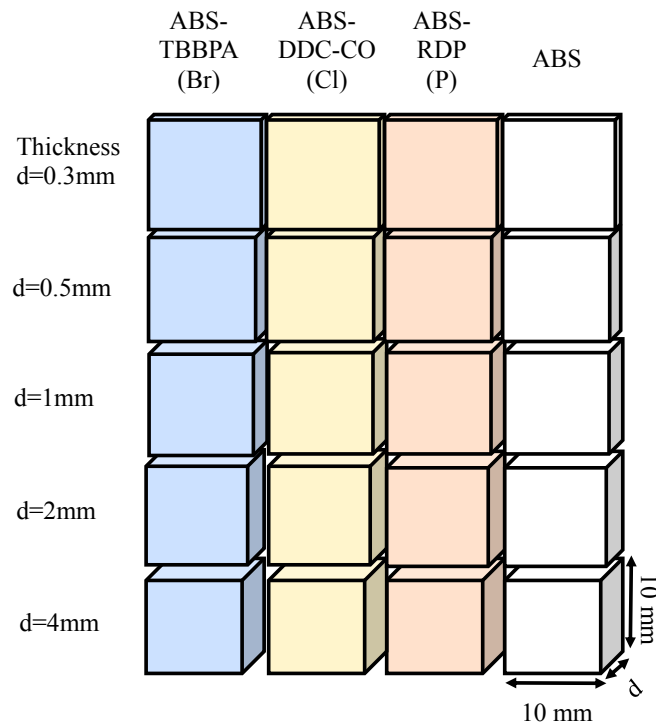


Figure 4.15: Illustration of the ABS-FR phantom used for spectral CR imaging. Materials of these cubes are introduced in Table 4.2.

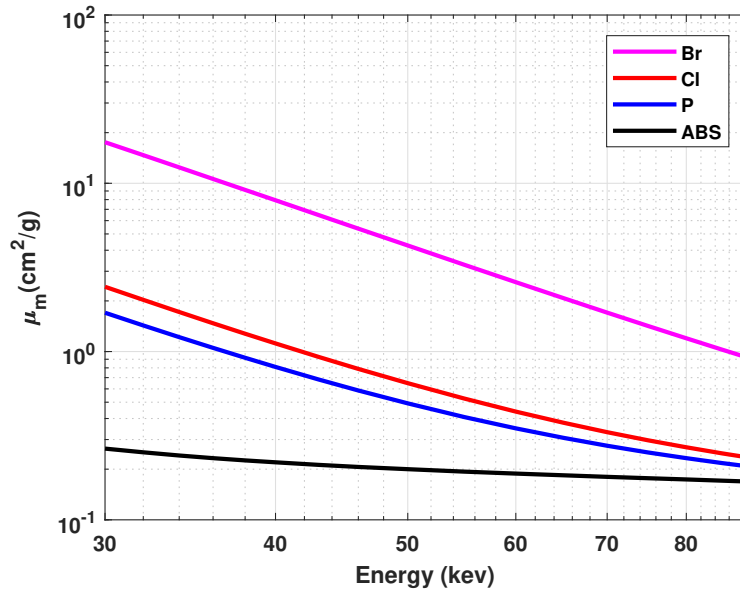


Figure 4.16: Mass attenuation coefficients ( $\mu_m$ ) of components (ABS, Br, Cl and P) contained in this phantom within the detecting energy range from 30 keV to 90 keV.  $\mu_m$  of ABS is calculated according to formula  $\mu_m = \sum_{\alpha} \omega_{\alpha} \mu_{m\alpha}$ , with  $\omega_{\alpha}$  and  $\mu_{m\alpha}$  representing the weight fraction and mass attenuation coefficient of each element  $\alpha$  of the compound. Data taken from [Hubbell and Seltzer, 2004].

We will use projection domain decomposition method for this application, where the final calculated values  $P_{\alpha}$  for material  $\alpha$  are the line integral of material density  $\rho_{\alpha}$  (Equation 3.10). In this case, with known thickness  $d$  of each cube, theoretical values for  $P_{\alpha}$  at position  $(sx, sy)$  of the transmitted image can be given by

$$P_{\alpha}(sx, sy) = d(sx, sy) \times \rho_{\alpha}(sx, sy), \quad (4.15)$$

where  $\rho_{\alpha}$  equals the effective density calculated in Table 4.2. Table 4.3 lists the theoretical values of  $P_{\alpha}$  for material ABS, Br, Cl and P at various thicknesses.

Table 4.3: Theoretical values of  $P_{\alpha}$  (unit: mg/cm<sup>2</sup>) for each material. Material ABS has two columns of values, the first is *ABS pure*, which corresponds to the material of the 4<sup>th</sup> column of cubes in the phantom shown in Figure 4.15, and *ABS in mixture* corresponds to the ABS components in the other cubes of Figure 4.15.

Thickness	ABS (Pure)	ABS in mixtures	Br in ABS-TBBPA	Cl in ABS-DDC-CO	P in ABS-RDP
0.3 mm	31.80	27.03	2.81	3.11	0.52
0.5 mm	53.00	45.05	4.68	5.18	0.86
1 mm	106.00	90.10	9.35	10.35	1.72
2 mm	212.00	180.20	18.70	20.70	3.44
4 mm	424.00	360.40	37.40	41.40	6.88



### 4.5.3 System geometry

The simulated system uses the 100 kVp X-ray spectrum in Figure 4.3 with tube current of 15 mA. The distance from X-ray source to phantom center is 2000 mm, which is far enough to consider the X rays passing through the object as parallel. A  $90 \times 112$  CdTe detector array with pixel size of  $0.5 \text{ mm} \times 0.5 \text{ mm}$  and thickness of 3 mm was simulated, and the distance of detector to phantom center was 3 mm. Six energy bins were set to be evenly distributed from 30 keV to 90 keV. Figure 4.17 is a schematic view of the simulated spectral CR system.

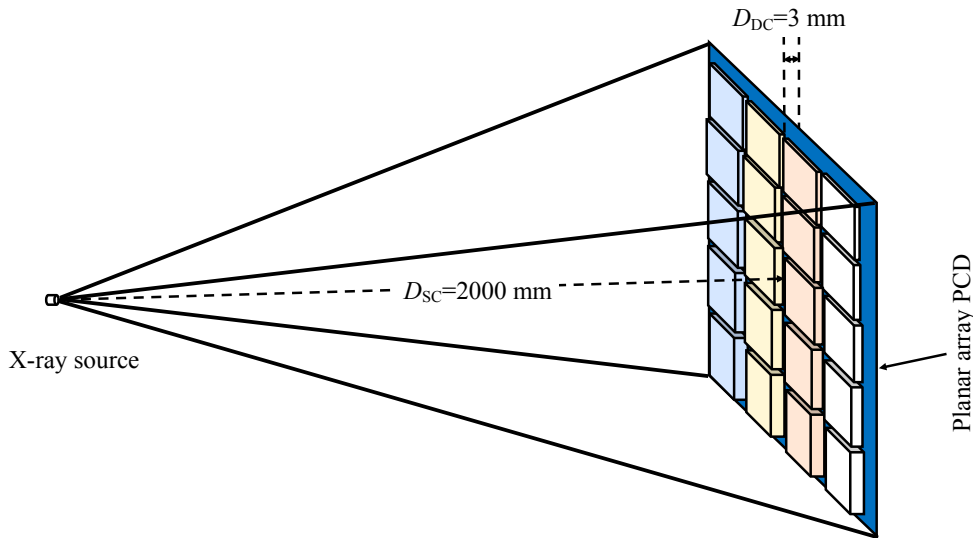


Figure 4.17: Scheme of spectral CR system geometry. This figure is only a simplified schematic view of the simulation system where the dimensional information ( $D_{SC}$ ,  $D_{DC}$ , size of phantom and detector) is not in realistic scale.

### 4.5.4 Decomposition results of proj-PR-LLS method

For this application, we have simulated two sets of spectral CR acquisition data: with and without photon noise. Then we used proj-PR-LLS method to decompose the radiographic images into three basis images corresponding to ABS, Br and Cl. The reason for having not selected P as the basis is that P and Cl have too close atomic numbers and experiments showed that they can be barely separated. Thus we use Cl as basis material and expect that P will also be present in the Cl basis image. We set the patch size to be  $2 \times 2$ .

For simulated acquisition without noise, we set the relaxation parameter  $r$  to 0 since it is not necessary to enforce smoothness within patches when no noise exists, corresponding decomposition results are shown in Figure 4.18 (a). It is observed that all cubes are visible in the ABS basis image, due to the presence of ABS in either mixtures (ABS-FR) or pure ABS. The ABS-TBBPA cubes are well separated and highlighted in the Br basis image. When cube thickness  $d = 0.3$  and  $0.5$  mm, the ABS-TBBPA cubes and ABS-DDC-CO tubes are visible in the Cl basis image; When cube thickness increases to 1 mm and 2 mm, all three ABS-FR cubes are visible, however, the signal intensity of ABS-TBBPA cubes

in the CI basis image decreases compared to those with smaller thickness; When  $d = 4$  mm, only ABS-DDC-CO cubes and ABS-RDP cubes are visible in the CI basis image. To conclude, in noise-free situation, ABS and Br can be well identified; the determination performance of other FRs improves with object thickness: when  $d = 4$  mm, the FRs containing Cl and P are present in the CI basis image without cross-talk of ABS-TBBPA material, one can further distinguish the two FRs according to their large density difference.

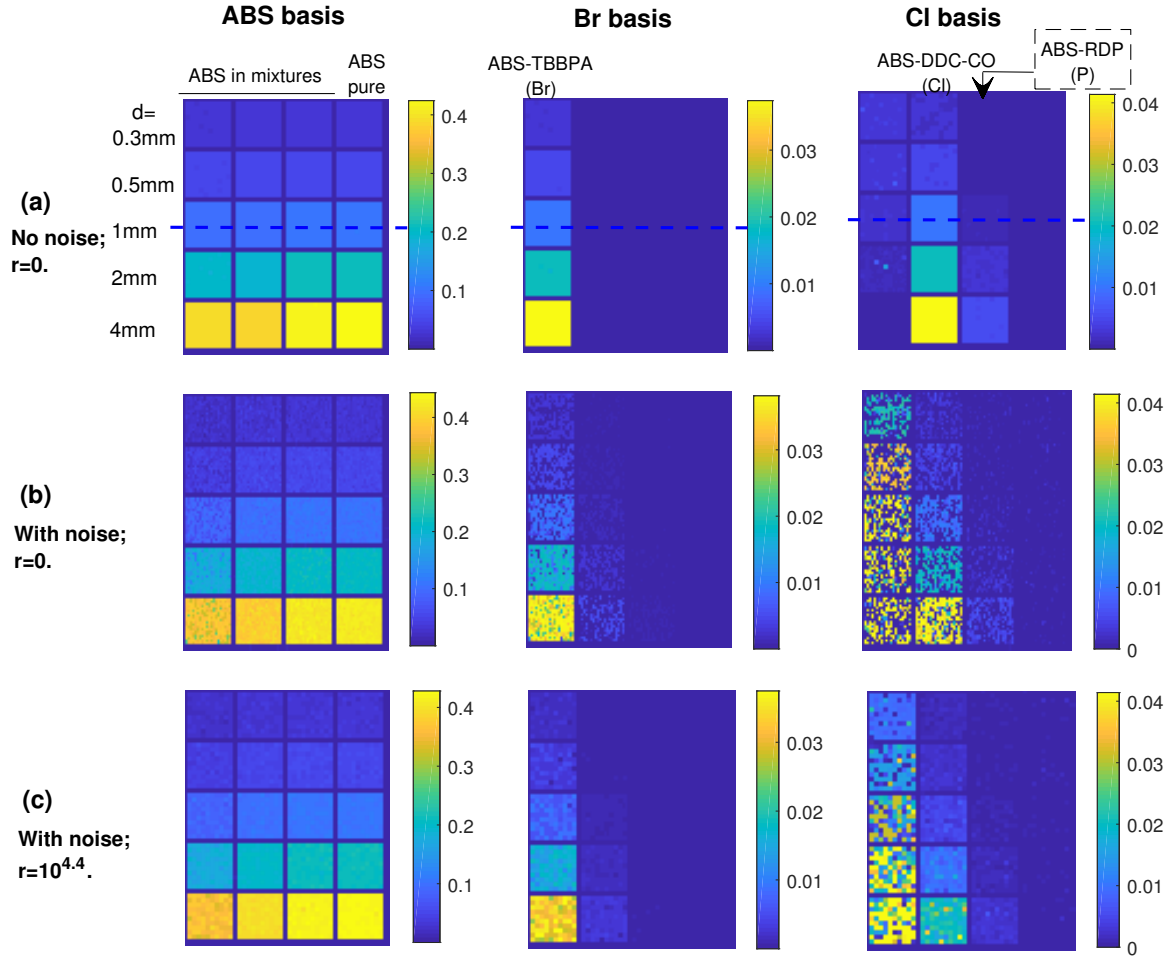


Figure 4.18: Decomposition results under different conditions using proj-PR-LLS method. (a): simulation of CR without noise,  $r = 0$ ; (b): simulation of CR with Poisson noise,  $r = 0$ ; (c): simulation of CR with Poisson noise,  $r = 10^{4.4}$ . The first column represents ABS basis, second column Br basis, and third column CI basis image. The dash lines on images of (a) mark the position where 1-D profiles are plotted in later analysis.

When Poisson noise is added during the simulation, we need to reconsider the relaxation parameter  $r$ .  $r$  is determined as  $10^{4.4}$  in this situation according to the L-curve criterion. Some details of  $r$  selection using the L-curve method are introduced in Appendix section. The decomposition results when  $r = 0$  and  $r = 10^{4.4}$  are shown in Figure 4.18 (b) and (c). It can be seen that when  $r = 0$ , the ABS-TBBPA cubes and ABS-DDC-CO cubes appears

in both Br basis image and Cl basis image, making them impossible to be distinguished. Moreover, the decomposed images suffers from heavy noise. When the relaxation parameter changes to  $r = 10^{4.4}$ , the obtained images are less noisy than those in the former case, however, the separation of different materials is not enhanced.

#### 4.5.5 Proj-PR-LLS-clas method

We have shown in the above section the decomposition results using proj-PR-LLS method. Its performance is not satisfying, especially when Poisson noise is added during the simulation. To improve this situation, we develop another method based on proj-PR-LLS method.

As we have introduced, the objective of this application is to separate the ABS materials with and without flame retardant, and further identify the type of flame retardant. In industrial applications, each plastic material contains only one type of FR and no overlapping exists between samples we perform CR inspection. Thus ideally, one pixel on the radiographic image of our phantom should either be identified as Br or Cl if it contains FR. Specifically for this application, we develop a classification-based (proj-PR-LLS-clas) decomposition method.

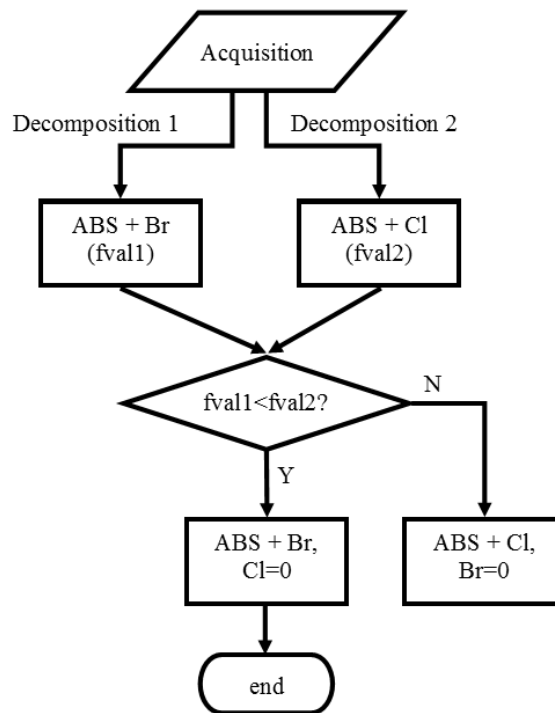


Figure 4.19: Flowchart of the decomposition method with classification for one patch.  $fval1$  and  $fval2$  represent the cost function values obtained at the end of decomposition 1 and decomposition 2.

Figure 4.19 shows the procedure of this method to obtain values for one patch. Instead of the 3-material (ABS, Br and Cl) decomposition using proj-PR-LLS method, the first

step of proj-PR-LLS-clas method is to perform two independent decompositions which decompose the data into 2-material basis (ABS + Br, and ABS+Cl); then by comparing the cost function values (fval1 and fval2) at the end of each decomposition, one of the two decompositions is chosen for this patch. For example, if  $fval1 > fval2$ , we choose the results of the decomposition which decompose the data into ABS and Br, consequently, the values of Cl in this patch will be set to 0. After all patches being considered, full images of ABS, Br and Cl will be obtained.

#### 4.5.6 Decomposition results of proj-PR-LLS-clas method

Figure 4.20 shows the decomposition results of proj-PR-LLS-clas method with the same condition as proj-PR-LLS method, whose results has been shown in Figure 4.18.

In noise-free condition (Figure 4.20 (a)), ABS and Br contained FR can be identified from the ABS and Br basis images. Meanwhile, the cubes of FR materials containing Cl and P appear in the Cl basis image, but they have significant density difference for cubes with the same thickness, therefore, they can be easily distinguished by the observer even if the concentration of FRs or thickness of cubes changes more or less. Figure 4.21 gives the 1-D profiles along dash lines in Figure 4.18 (a) and 4.20 (a), the comparison between theoretical density integrals ( $P_\alpha$  in Table 4.3) of 3 basis materials and our calculations using two methods is illustrated. It is observed that the proj-PR-LLS-clas method has higher consistence with true values than the other one, especially for the Cl basis curve, where ABS-TBBPA cubes are mistaken as Cl contained FR by proj-PR-LLS method.

With simulated Poisson noise, the decomposed images of proj-PR-LLS-clas method also has higher material separation ability than those of proj-PR-LLS method. When  $r = 0$ , it can be observed from Figure 4.20 (b) that the ABS-TBBPA cubes are indicated in the Br basis image, with some mistakenly appeared pixels of the ABS-DDC-CO cubes. This situation is improved obviously when we use  $r = 10^{4.4}$ : less pixels of ABS-DDC-CO cubes appears in the Br basis image of Figure 4.20 (c). Besides, comparing the Cl basis images of (b) and (c), (c) is closer to the Cl basis image of (a), especially when cube thickness  $d = 2$  mm and 4 mm where only the ABS-DDC-CO cubes and ABS-RDP cubes are highlighted. Therefore, a good choice of relaxation parameter can improve the decomposition performance.

To conclude, the proj-PR-LLS-clas method has better material decomposition ability than proj-PR-LLS for this application, no matter when Poisson noise is or is not considered in the simulation. ABS and Br contained FR can be identified according to corresponding basis image. Furthermore, when the cube thickness increases to 2 mm and 4 mm, the decomposition results become much closer to those of noise-free condition, where ABS and the FRs containing Br, Cl and P can be identified at the same time.

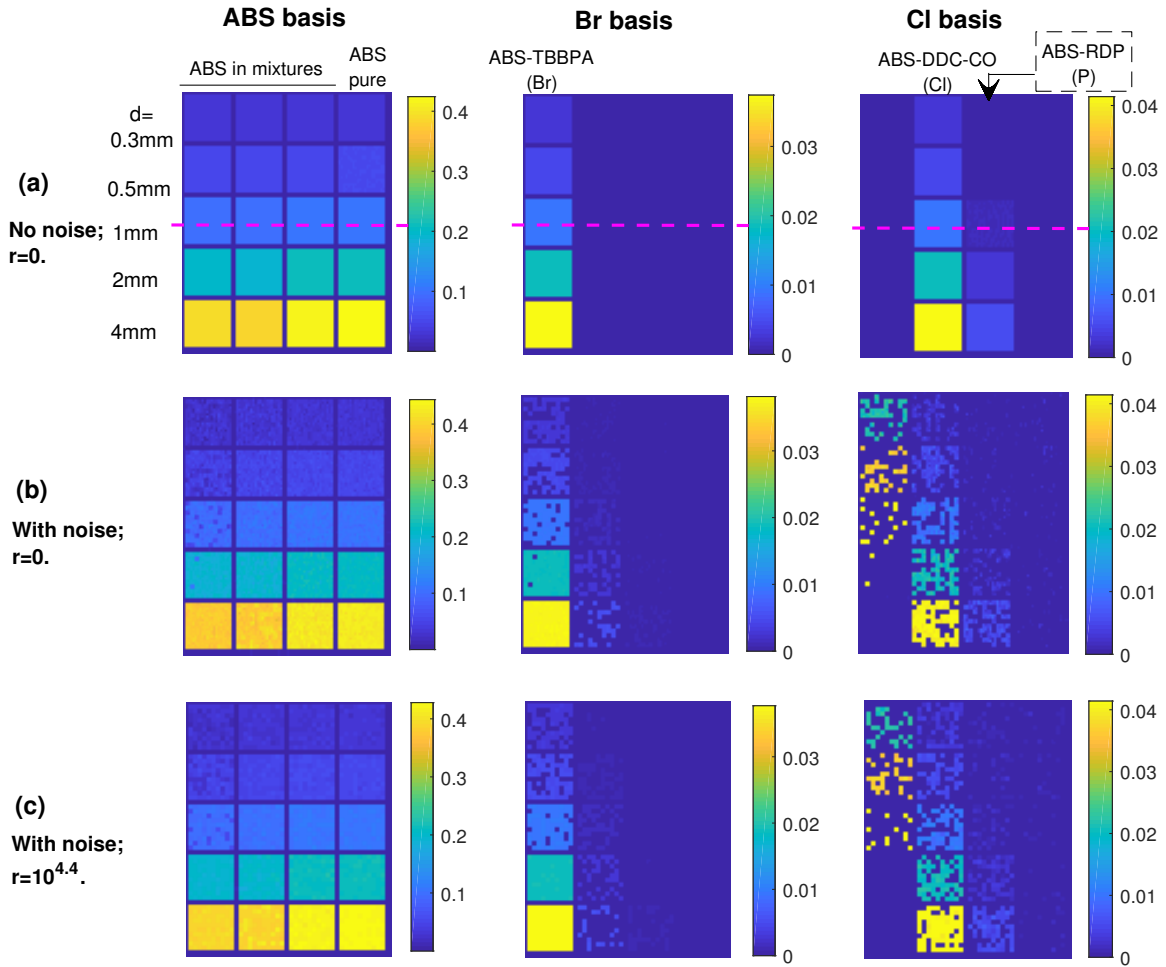


Figure 4.20: Decomposition results under different conditions using proj-PR-LLS-clas method. (a): simulation of CR without noise,  $r = 0$ ; (b): simulation of CR with Poisson noise,  $r = 0$ ; (c): simulation of CR with Poisson noise,  $r = 10^{4.4}$ . The first column represents ABS basis, second column Br basis, and third column Cl basis image. The dash lines on images of (a) mark the position where 1-D profiles are plotted in later analysis.

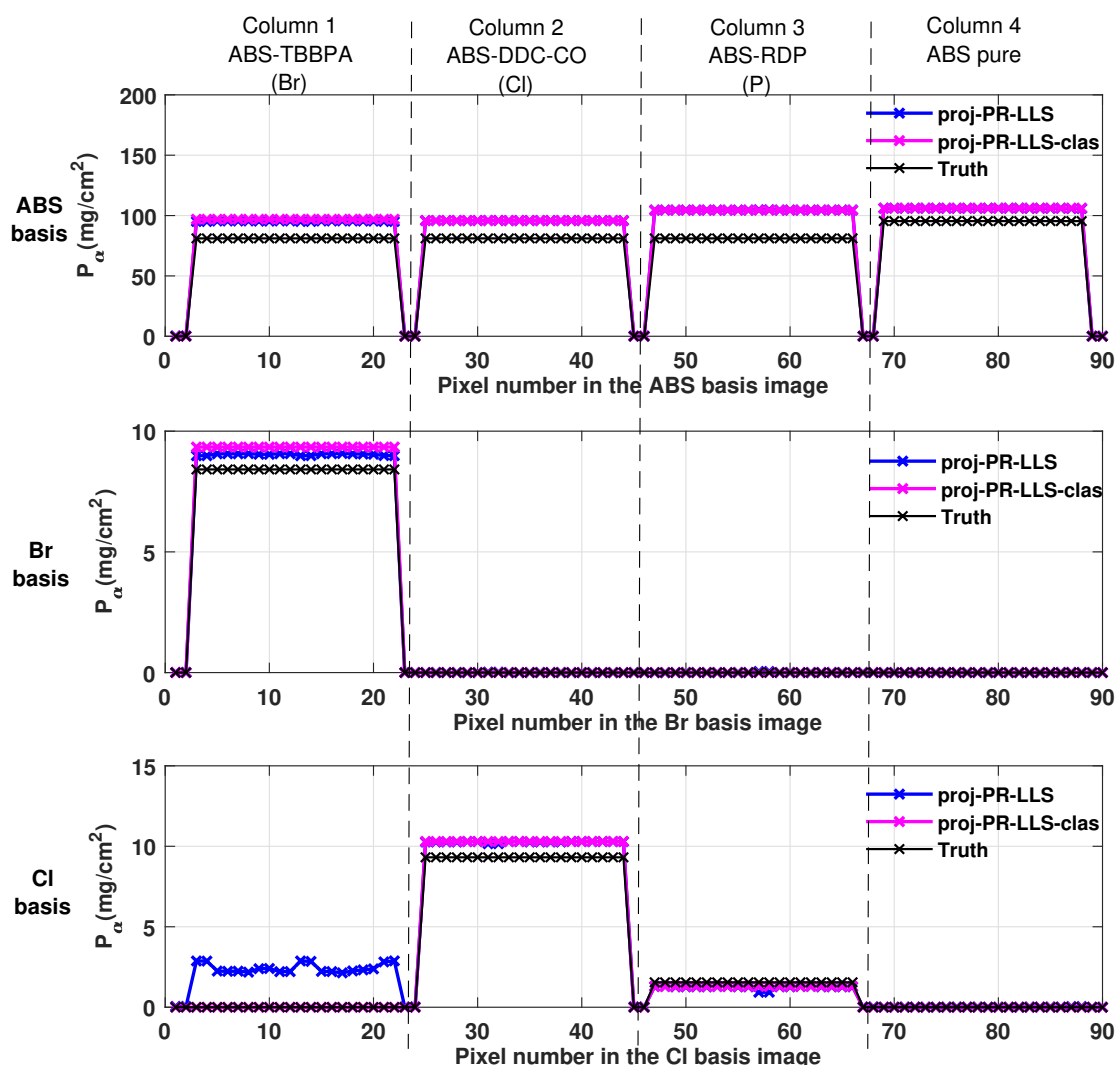


Figure 4.21: Performance comparison of proj-PR-LLS method and proj-PR-LLS-clas method in noise-free condition: 1-D profiles along the dash lines in Figure 4.18 and 4.20. ABS basis (top), Br basis (middle) and Cl basis (bottom). Black curves represent the theoretical density integrals of basis materials ( $P_\alpha$  for thickness of 1 mm in Table 4.3) if the decomposition is perfect, blue curves represent calculated values using method without classification and magenta curve using method with classification.

#### 4.5.7 Conclusion and discussion

WEEE has been increasing rapidly due to the development of electronic industry. The sorting technique is important for subsequent treatment and recycling of WEEE to avoid major environmental and health problems. For this application, we have simulated the spectral CR imaging with a phantom containing multiple cubes of different ABS-FR materials with various thicknesses, and have investigated the decomposition feasibility of different ABS-

FRs using the proj-PR-LLS method and proj-PR-LLS-clas method. Results show that the former method failed to identify the FR materials when Poisson noise was simulated for CR imaging. The latter method, in noise-free condition, could distinguish ABS and the FRs containing element Br, Cl and P at the same time, with quantification of each material agreeing well with the theoretical value. When noise was added in the simulation, the proj-PR-LLS-clas method can separate four materials at the same time only when the tube thickness is as large as 2 mm or 4 mm.

There are certain limitations in our work. Firstly, the two methods are not very robust to noise when the object thickness is too small, especially the proj-PR-LLS method. Secondly, proj-PR-LLS-clas method has been proposed under the premise that each pixel on the radiographic image of object contains either one set of basis materials (ABS+Br) or the other (ABS+Cl), so that the material not belonging to the selected basis can be put 0. Proj-PR-LLS-clas method can not be applied for situation where this premise is not met. Thirdly, the decomposition of elements with similar atomic numbers (Cl and P), even in the noise-free condition of simulation, depends on their density difference in the same image. Therefore, in case where the thickness information of objects is unknown, or the two materials overlap in the X-ray direction, the decomposed density will be largely influenced, leading the materials to be indistinguishable.

## 4.6 Summary

In this chapter, we have presented the spectral CT/CR simulation method using the VXI software. The simulation is based on ray-tracing techniques together with the X-ray attenuation law. The users can define parameters of the X-ray source, object and detector for their own applications. Furthermore, spectro mode of detector allows counting the arriving photons into corresponding pre-defined energy bins to simulate the spectral X-ray imaging process.

With VXI software, we have simulated spectral X-ray imaging with different phantoms, and investigated the material decomposition performance of the methods proposed in Chapter 3 for medical and industrial applications:

1. Medical application: iodine and calcium identification. To distinguish compositions of atherosclerotic plaque, we have simulated spectral CT imaging of a computational human thorax phantom with realistic noise and investigated the material decomposition performance of three methods: proj-LS, proj-LLS and proj-PR-LLS method. Results show all methods can give quantitative distribution of iodine, calcium and soft tissues respectively, among which the proposed proj-LLS method and proj-PR-LLS method have better quantitative accuracy and better image quality than the commonly used proj-LS method.
3. Industrial application: ABS-FR plastic sorting. In addition to spectral X-ray CT, we have also investigated the material decomposition ability of the proposed proj-PR-LLS method for spectral CR imaging in the identification of different ABS-FR materials. Results show that the decomposition directly in the 3-material basis is not enough robust to noise. Thus we have introduced a classification-decomposition procedure (proj-PR-LLS-clas method) based on the application because we know a

priori that one piece of plastic contain can not contain 2 FRs at the same time. So it is reasonable to firstly perform two decompositions in 2-materials basis and then choose the more likely one to be the final result. This method has enhanced the separation between Br and Cl compared to proj-PR-LLS method. For simulation with realistic noise, when the thickness of phantom is favorable, ABS and the FRs that contain Br, Cl and P can be identified at the same time.





## Chapter 5

# Exploring the influence of different acquisition parameters

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## 5.1 Introduction

We have described in the previous chapter the material decomposition performance of X-ray spectral CT and spectral CR with photon counting detector. In the above applications, the spectral CT and CR imaging process were simulated using acquisition parameters commonly used in practical situations. For example, the number of energy bins was set to 6 considering that most existing PCDs (Table 2.1) have 2 to 8 bins. In medical imaging applications (atherosclerosis imaging), the X-ray tube current and exposure time were set to be 100 mA and 0.01 s/projection, resulting in an exposure factor (tube current and time product) of 1 mA·s per projection. What will be the performance of material decomposition if we vary these acquisition parameters during the simulation?

As indicated by Equation 4.9 and recalled here

$$SNR_i = \frac{\lambda_i}{\sigma_i} = \frac{\lambda_i}{\sqrt{\lambda_i}} = \sqrt{\lambda_i}, \quad (5.1)$$

the signal-to-noise ratio of energy bin  $B_i$ , defined by the ratio of mean ( $\lambda_i$ ) to standard deviation ( $\sigma_i$ ) of measurement, is proportional to the square root of the expected counting. The exposure factor has a direct influence on the number of photons arriving at the detector, and consequently on the level of image noise. Therefore, we believe that the decomposition performance should be different if we change the exposure factor.

For a given X-ray spectrum, the width of each energy bin narrows when we increase the total number of energy bins, as illustrated in Figure 5.1. A narrow energy bin will limit the number of photons received by the detector in each bin and result in decreased SNR. However, larger number of energy bins provides more energy dependent measurements and brings better resolution for material decomposition. Therefore, by increasing the number of energy bins, there exists a trade-off between decreasing SNR and increasing spectral information for material decomposition.

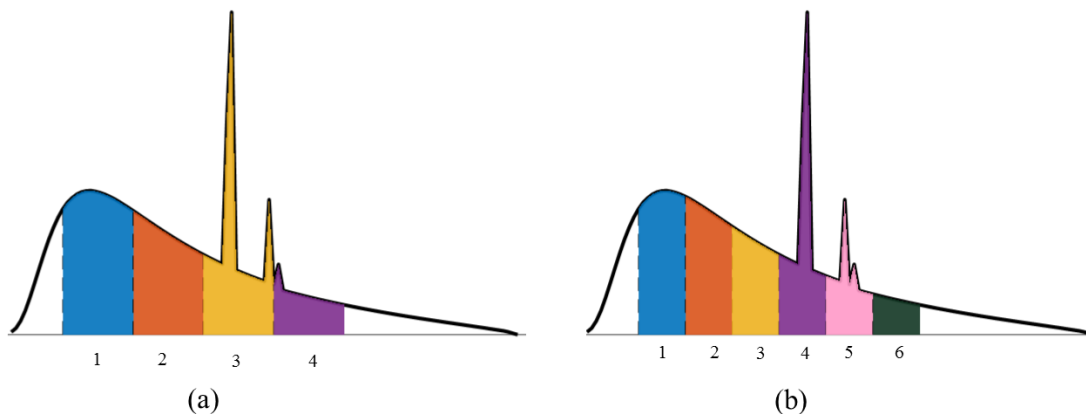


Figure 5.1: Illustration of spectral CT acquisition with 4 (a) and 6 (b) energy bins for the same X-ray spectrum.

In the present work, we will simulate X-ray spectral CT imaging of a poly(methyl methacrylate) (PMMA) phantom filled with iron (Fe), calcium (Ca) and potassium (K)

solutions. With the objective of quantifying iron from other materials, we simulate the acquisition process with different parameters, i.e. exposure factor and number of energy bins, and investigate their influence on the decomposition performance.

## 5.2 Method and material

### 5.2.1 Medical context

Iron is a micronutrient essential for adequate erythropoietic function, oxidative metabolism and cellular immune response to bacterial infection. Disorders in iron, such as iron deficiency or overload, are important risk factors for heart diseases such as coronary artery disease and heart failure [Von Haehling et al., 2015, Muñoz et al., 2011]. There are different methods for the evaluation of tissue iron content, which can be classified into two categories: invasive techniques and noninvasive techniques. Invasive techniques include biopsy and serum ferritin level. Noninvasive techniques include superconducting quantum interference device (SQUID) and MRI [Mavrogeni, 2009, Ibrahim and Bowman, 2014]. However, these existing techniques all have their own limitations. Biopsy is an invasive procedure that may cause bleeding from the incision site, pain and infections, also it is limited by sampling errors since iron is not uniformly distributed inside organs [Yoon et al., 2015]. Serum ferritin test is less invasive, but it can be easily influenced by many factors such as inflammation, infection, hepatic dysfunction, ascorbate deficiency, hemolysis, and ineffective erythropoiesis [Crosby, 1976]. SQUID is particularly more accurate for liver iron content (LIC) determination but not for other organs [Kolnagou et al., 2009]. MRI is a useful imaging tool for the diagnosis of iron deposition, but has very long scan time and inability to quantify iron concentration greater than 300 mol/g due to susceptibility and rapid signal decay artifacts [Ibrahim and Bowman, 2014, Fischer et al., 2011]. Therefore, it is necessary to develop new techniques for tissue iron content determination.

In the past years, numerous technologies of DECT and spectral CT were developed, and their clinical applications were increasingly investigated [Fredenberg, 2017]. As we have mentioned, DECT has limited ability in material decomposition by producing two datasets corresponding to two different X-ray spectra of the same anatomic region [Danad et al., 2015]. The potential of using DECT to detect the distribution of iron in tissues was investigated [Fischer et al., 2011, Hazirolan et al., 2008, Luo et al., 2015, Panta et al., 2015]. Hazirolan et al. applied DECT to the detection of myocardial iron deposition in Thalassaemia patients; the measured myocardial DECT density values showed strong negative correlation with MRI T2\* values [Hazirolan et al., 2008]. Luo et al. also proved the diagnostic potential of DECT in LIC determination using virtual iron content imaging with fifty-six patients suspected of having liver iron overload [Luo et al., 2015]. However, DECT is unable to give the accurate concentration of iron except for the correlated Hounsfield Unit (HU) values and usually requires relatively high dose levels.

Unlike DECT, spectral CT employs PCD and is able to obtain spectral information of several energy bins with single acquisition. Its ability in material decomposition has been discussed in previous chapters, including K-edge material and non-K-edge material determination. Iron, as a non-K-edge material within diagnostic X-ray energy range (10 keV-150keV), is more challenging to be distinguished. Zainon et al. used small animal spectral micro-CT with Medipix3 detector (thresholds: 10, 16, 22 and 28keV) to scan

the carotid atherosclerotic plaque; water-like, calcium-like and lipid-like tissues were well separated according to histology comparison, but iron was not distinguished from calcium [Zainon, 2012]. Li et al. developed an image domain material decomposition algorithm which depends on an empirical calibration with various concentrations of the chosen basis materials, and experimental validation was performed for the decomposition of calcium chloride ( $\text{CaCl}_2$ ) and iron chloride ( $\text{FeCl}_3$ ). The results showed that  $\text{CaCl}_2$  and  $\text{FeCl}_3$  can be separated while the performance is subject to energy threshold configuration of acquisition [Li et al., 2015].

To summarize the literature survey, various methods exist for iron content evaluation, but with different limitations. At the same time, many material decomposition methods have been proposed and different experimental systems are under development for spectral CT. However, there is a lack of feasibility analysis and method comparison for the use of spectral CT for iron content determination. Therefore, the present study aims to investigate the ability of spectral CT to quantitatively separate iron from other elements like calcium and potassium, by using the proposed patchwise regularized decomposition methods in image domain (proj-PR-LLS method) and in projection domain (ima-PR-LS method).

### 5.2.2 Simulated phantom & system geometry

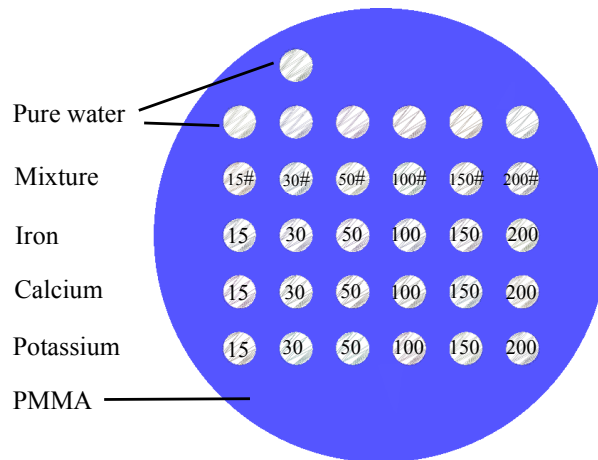


Figure 5.2: Phantom illustration. Each row contains the same material or materials soluted by water at different concentrations, types of material are indicated on the left hand and concentrations are annotated inside each insert on the figure with unit of mg/cc. Symbol ‘#’ marks the mixture inserts which combine iron, calcium, potassium and water together.

We simulated an 80mm-diameter PMMA phantom for scanning. Inside the phantom, 31 insert holes with diameter of 6mm were filled with different solutions, as shown in Figure 5.2. The first two rows represent pure water rows that contain 7 inserts of pure water, and the third row correspond to the mixture row. The 3 bottom rows contain respectively iron, calcium and potassium soluted by water at different concentrations (15-200mg/cc). Specific density value for each insert is annotated inside each circle on the figure with unit of mg/cc. Symbol ‘#’ marks the mixture insert of iron (Fe), calcium

(Ca), potassium (K) and water. For example, the first hole of the mixture row consists of 15mg/cc iron, 15mg/cc calcium and 15mg/cc potassium, the second one contains 30mg/cc iron, 30mg/cc calcium and 30mg/cc potassium, and so on.

Figure 5.3 shows the mass attenuation coefficients of different materials contained in this phantom within the detection energy range, i.e. 30 keV-90keV. It can be observed that all materials are without K-edge, and those with close atom numbers like Ca and K, water and PMMA have similar attenuation properties, making them difficult to be separated from each other. In this case, the attenuation caused by either of the component is supposed to be represented by the same basis material.

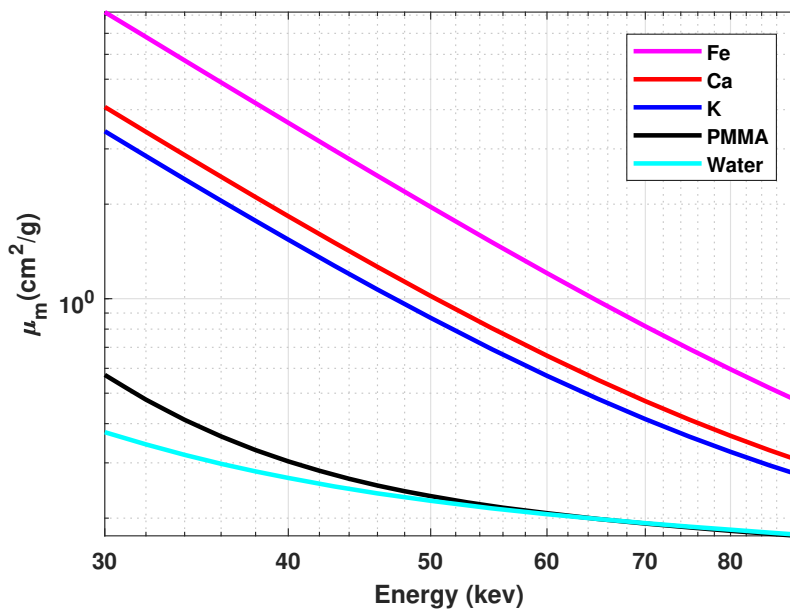


Figure 5.3: Mass attenuation coefficients ( $\mu_m$ ) of the 5 materials (Fe, Ca, K, PMMA and water) contained in this phantom within the detecting energy range from 30 keV to 90 keV. Data taken from [Hubbell and Seltzer, 2004].

Figure 5.4 shows the system geometry of the simulated spectral CT system. The simulated system hired a linear CdTe detector of 700 pixels with pixel size of 0.4mm×0.4mm. The absorption efficiency of the detector was simulated for a 3 mm thick CdTe crystal. The X-ray spectrum has tube voltage of 100kVp (spectrum shown in Figure 4.3). Phantom was scanned with 1200 projections from 0° to 360°. The distances of source to the center of rotation and detector to the center of rotation were  $D_{SC} = 200$  mm and  $D_{DC} = 400$  mm, respectively. To investigate the influence of exposure factor and number of energy bins, we set different acquisition parameters: number of energy bins  $N = 6, 10, 15, 20, 30$  and 60, and exposure factor  $F = 0.025, 0.1, 1, 10$  and 100 mA·s per projection. Energy bins were equally distributed within the detection energy range from 30 keV to 90 keV.

After obtaining the simulation data with various acquisition parameters, we performed material decomposition using the two methods proposed in Chapter 3: proj-PR-LLS method and ima-PR-LS method. Their performance is evaluated in terms of average

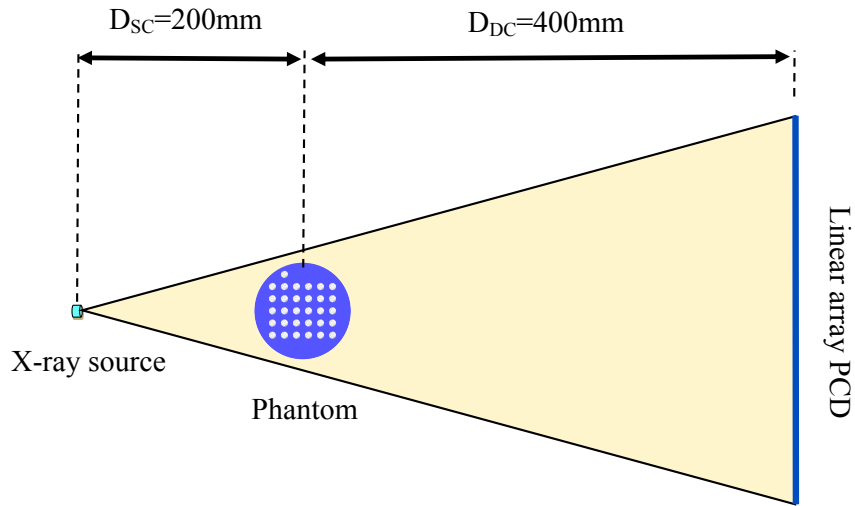


Figure 5.4: Scheme of spectral CT acquisition.

error and CNR. To calculate the CNR of decomposed iron image, a circular region of interest (ROI) of 5 mm diameter is placed at the location of the 100 mg/cc mixture insert (Figure 5.5). Another circular ROI of the same size is placed in a neighboring background area.

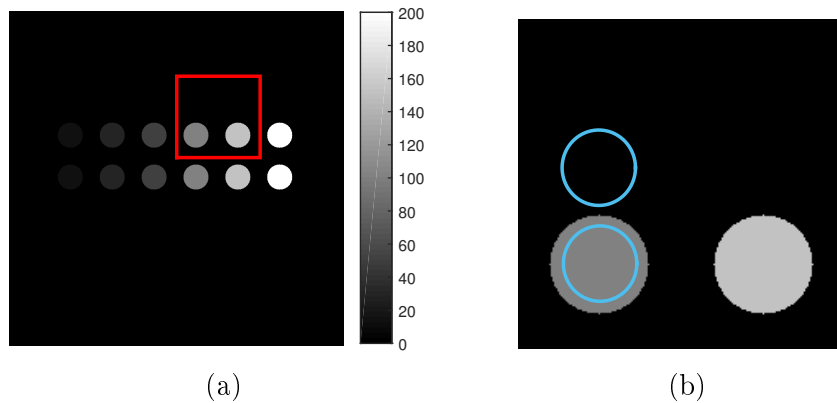


Figure 5.5: Ground truth image of iron density distribution (a) and zoomed view of the red rectangle region (b). The circular regions of interest are placed over the 100mg/cc mixture solution and its neighboring background.

### 5.3 Results

As mentioned in Chapter 3, the number of basis materials must be equal to or smaller than the number of energy bins. Therefore, for a complex object composed of multiple materials,

all the components can not be put in the material basis. In this case, the attenuation caused by components having similar effective atom numbers  $Z_{\text{eff}}$  are supposed to be represented by the same basis material. Based on this hypothesis, to comprehensively describe the whole object, we choose three materials as basis according to their atomic numbers: light material, median material and heavy material. In the case of our phantom, according to Figure 5.3, the light material corresponds to PMMA or water, median material Ca or K, heavy material Fe. To enhance the difference between heavy (Fe) and median materials, we choose K as median material for both proj-PR-LLS and ima-PR-LS methods. However, different light materials are chosen for the two methods (PMMA for proj-PR-LLS and water for ima-PR-LS) because of their different decomposition domain. When we perform material decomposition in projection domain, the handled data are acquired sinograms which correspond to the transmitted number of photons of each ray. It should be noticed that when the X-ray passes through the phantom, PMMA, as a carrier of all inserts, contributes to most of the X-ray attenuation. Therefore, we select PMMA as the light material for proj-PR-LLS method. The situation is much different when we decompose in image domain, since we deal with the reconstructed images which corresponds to the attenuation coefficients map. For each pixel of the reconstructed image, the attenuation coefficient is caused by the components present in that pixel. Considering that water is a good solvent that is more likely to exist in the mixture than PMMA, we choose water as the light material for ima-PR-LS method.

### 5.3.1 Proj-PR-LLS method

As analyzed before, for proj-PR-LLS method, the three materials chosen as basis material are PMMA, potassium and iron. Relaxation parameter  $r$  is set to be 1 and the size of each patch is  $5 \times 5$ . The results have shown that, iron can be identified in all conditions using proj-PR-LLS method. However, the performance changes a lot when the acquisition parameters vary. Two examples of the decomposition results are shown in Figure 5.6 and 5.7 when  $N=6$ ,  $F=1$  mA·s and  $N=60$ ,  $F=10$  mA·s.

It is observed in Figure 5.6 that water and PMMA are present in the PMMA basis image (left column). For the iron basis image (middle column), we can only observe two rows of inserts, one representing iron in the mixture and the other iron in water, which means that iron is well separated from other materials. For the potassium basis image (right column), we observe not only the rows of inserts that contain potassium, but also a row of inserts which contain calcium in water. The results agree well with our previous hypothesis that materials with similar attenuation properties (potassium and calcium) will be simultaneously represented by the same basis. Comparing Figure 5.6 (b) and (c), it is obvious that the decomposed images of  $N=60$ ,  $F=10$  mA·s are less noisy thanks to higher exposure factor.



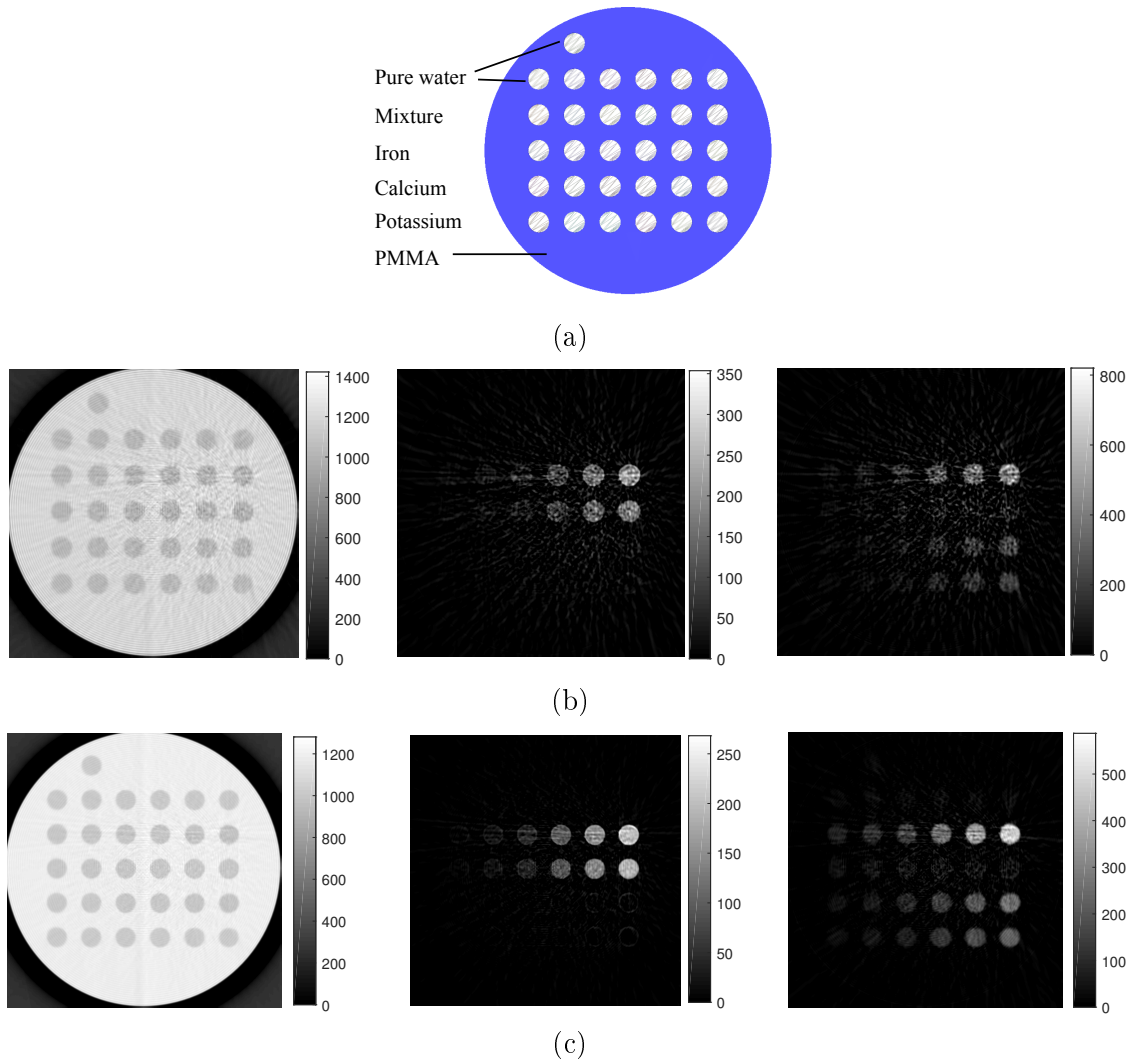


Figure 5.6: Components illustration of phantom (a) to better understand the decomposition results. Decomposed density in unit of mg/cc using the proj-PR-LLS method with acquisition parameters: 6 energy bins, 1 mA-s per projection for (b), and 60 energy bins, 10 mA-s per projection for (c), where the left column represents PMMA basis, middle column iron basis and right column potassium basis.

To make a quantitative analysis, we calculated the average density  $\bar{\rho}_{ins}$  of each measured iron and potassium insert, the relationship between  $\bar{\rho}_{ins}$  and true values is shown in Figure 5.7. The corresponding error bar for each average measurement indicates the variability of data. The fitting curves of  $\bar{\rho}_{ins}$  at different concentrations against the theoretical values  $t_{ins}$  showed very good linear properties. For iron (Figure 5.7 (a) and (c)), no matter when it was soluted in the mixture or in water, the slopes of fitting curves were almost 1, and the intercepts were considerably small, meaning that the quantification was quite accurate. For potassium (Figure 5.7 (b) and (d)), the calculated concentrations in mixture inserts were almost two times the values in water inserts, caused by the fact that calcium was also classified into potassium basis. When comparing Figure 5.7 (c), (d) with

(a), (b), we can observe smaller error bars, which indicate that the decomposed images have lower noise level thanks to higher exposure factor.

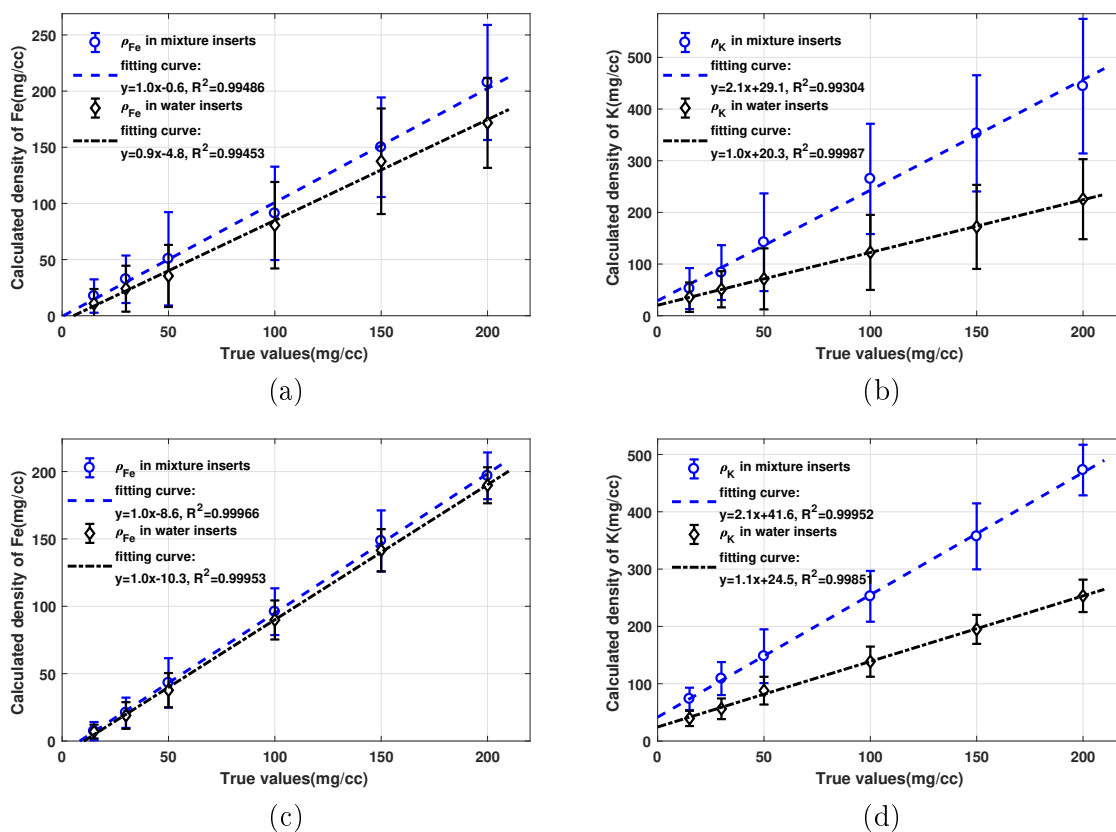


Figure 5.7: Comparison of the decomposed average density with true values by proj-PR-LLS method: iron (a) and potassium (b) when acquisition parameters are 6 energy bins, 1 mA·s per projection; iron (c) and potassium (d) when acquisition parameters are 60 energy bins, 10 mA·s per projection. The error bars indicate the standard deviation of decomposed density.

Figure 5.8 is a comprehensive illustration of the average errors of identified iron (in the mixture) concentrations with all different acquisition parameters. Quantification error tends to decrease for iron of larger concentration. Optimal performance can be observed for 200 mg/cc iron, with exposure factor of 100 mA·s, which means that the improvement of quantification thanks to a higher exposure factor has a major influence, even if the number of energy bins increases.

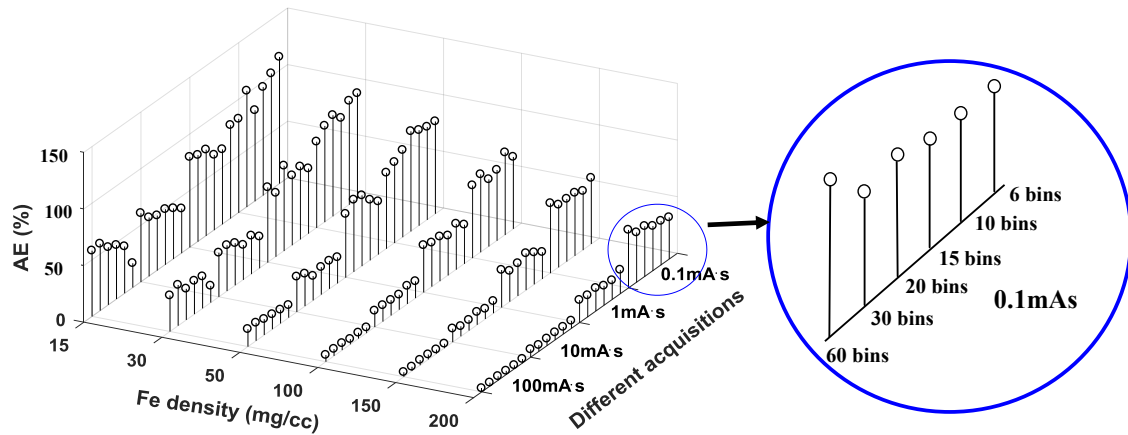


Figure 5.8: Average errors (AE) of decomposed iron (in the mixture) concentrations using proj-PR-LLS method. X-axis represents 4 groups of acquisitions corresponding to 4 different exposure factors  $F$ , in each of which are indicated 6 different numbers of energy bins  $N$ : for example, for the top right group,  $(F, N) = (0.1, 6), (0.1, 10), (0.1, 15), (0.1, 20), (0.1, 30), (0.1, 60), (1, 6), (1, 10), (1, 15)$ , and so on. Y-axis represents different iron concentrations. Decomposition results with exposure factor of  $0.025 \text{ mA}\cdot\text{s}$  are not presented in this plot for the sake of reading convenience.

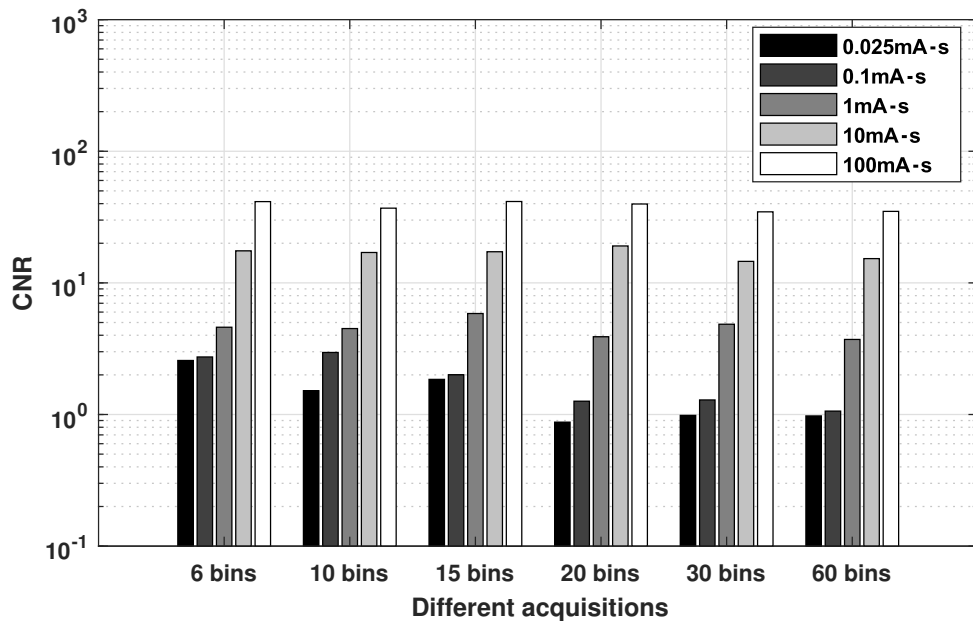


Figure 5.9: CNRs of decomposed iron images for  $100 \text{ mg/cc}$  of iron with different acquisitions using proj-PR-LLS method. Each group of acquisitions has the same number of energy bins but different exposure factors.

Figure 5.9 plots the CNRs of the decomposed iron images for 100 mg/cc of iron. Clearly the CNR depends largely on the exposure factor and it benefits from a higher exposure factor. For the same exposure factor, the CNR varies with the number of energy bins. We can observe that for lower exposure factor, decomposition performance tends to benefit from a lower number of energy bins. For example, when the exposure factor is 0.025 mA·s, 6 energy bins gain the highest CNR. When exposure factor keeps increasing to 100 mA·s, the number of energy bins has little influence on the CNR performance.

### 5.3.2 Ima-PR-LS method

For ima-PR-LS method, we choose water, potassium and iron as basis materials. Relaxation parameter  $r$  is set to be 1 and the size of each patch for regularization is  $5 \times 5$ . With various acquisition parameters, the simulation results show that with ima-PR-LS decomposition method, iron can be separated from calcium and potassium only when the number of energy bins is 60. We show in Figure 5.10 one failed decomposition (a) when  $N=6$ , and  $F=1$  mA·s, and one successful decomposition (b) when  $N=60$ , and  $F=10$  mA·s.

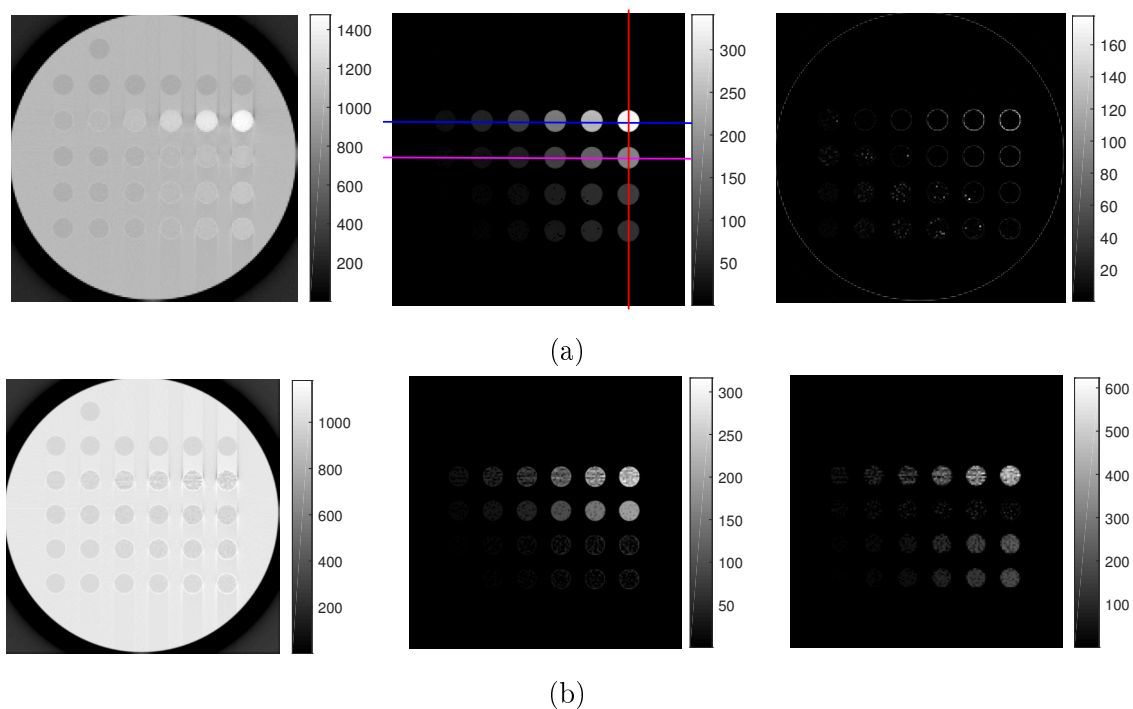


Figure 5.10: Decomposed density in unit of mg/cc of water basis (left column), iron basis (middle column) and potassium basis (right column) by ima-PR-LS method. Data acquisition parameters: 6 energy bins, 1 mA·s per projection (a), and 60 energy bins, 10 mA·s per projection (b). The red, blue and magenta lines on the iron basis image mark the position where 1-D profiles are plotted in later analysis.

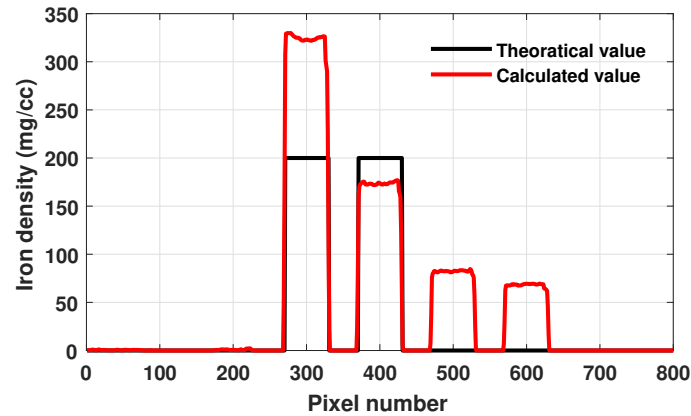


Figure 5.11: 1-D profiles along the red line in Figure 5.10 (a): black curve represents theoretical values, red curve represents measured values.

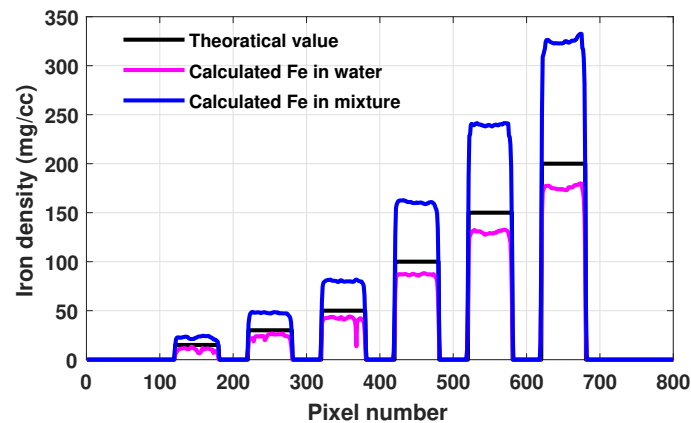
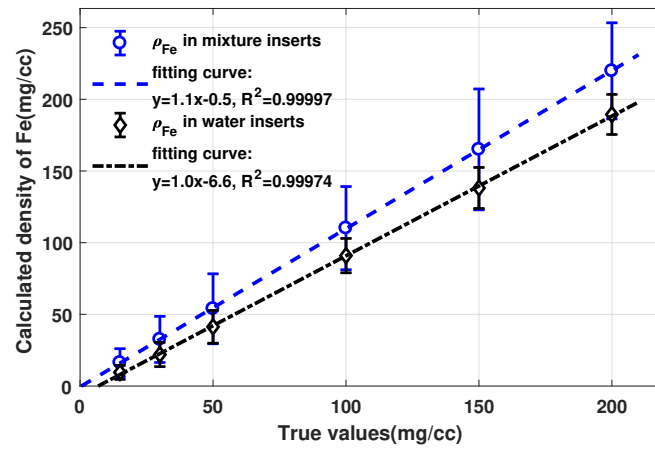


Figure 5.12: 1-D profiles along the blue and magenta lines in Figure 5.10 (a): black curve represents theoretical values, magenta curve iron/water inserts and blue curve mixture inserts.

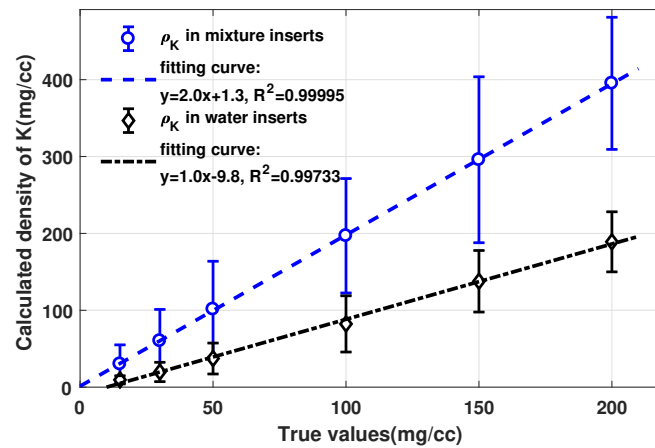
It is observed from Figure 5.10 (a) that the water basis image (left) that PMMA and water (first 7 inserts) are present. Moreover, in regions of inserts containing different solutions where water is supposed to be separated, the density is higher than expected, i.e. density of water 1000 mg/cc, especially for the row of mixture inserts. In iron basis image (middle), we can not only observe the two rows of inserts that really contain iron, but also the rows of inserts containing calcium and potassium which are supposed to be present in the potassium basis image, however, the potassium basis image (right) carries barely information. Figure 5.11 is the 1-D profile along the red line in Figure 5.10, theoretical values are given by the black curve. We can see extra peaks around the 500th and 600th pixel where calcium and potassium are contained. Therefore, iron is not separated from calcium and potassium in this case. Figure 5.12 is the 1-D profile along the blue and magenta lines in Figure 5.10. It can be observed that the measured iron density in the

Fe/water inserts agrees well with the theoretical value while the number is much higher for iron in mixture inserts, caused by the fact that calcium and potassium are mistaken as iron. In conclusion, with the acquisition parameters of  $N=6$  and  $F=1$  mA·s, the proposed patchwise regularized method in image domain is able to separate iron from water, but fails to separate iron from calcium and potassium.

Figure 5.10 (b) shows the decomposition results when  $N=60$ , and  $F=10$  mA·s. Obvious difference can be observed when comparing with Figure 5.10 (a). Only two rows of inserts exist in the iron basis image (middle) of Figure 5.10 (b), representing iron in the mixture and in water; for the potassium basis image (right), inserts containing calcium and potassium are highlighted. Figure 5.13 gives the relationship between  $\bar{\rho}_{ins}$  of Fe/K and the true values. Similarly to those obtained by proj-PR-LLS method in Figure 5.7, good linear properties can be observed; for iron soluted in the mixture or in water, the slopes of fitting curves were almost 1, and the intercepts were considerably small; for potassium, the calculated concentrations in mixture inserts were almost two times the values in water inserts, caused by the fact that calcium was also classified into potassium basis.



(a)



(b)

Figure 5.13: Relationship between calculated and true densities in the case of iron (a) and potassium (b) with true values by ima-PR-LS method. Data acquisition parameters: 60 energy bins, 10 mA·s per projection.

The red diamonds in Figure 5.14 represent the average errors of the identified iron concentration with acquisitions of 60 energy bins and various exposure factors using ima-PR-LS method. Quantification accuracy was improved with the increase of the factor of exposure and iron density. With the acquisition of 100mA·s per projection, the average error of the estimated iron content varies from 35.6% to 9.0% for the concentrations from 15 mg/cc to 200 mg/cc. The CNR of the decomposed iron images for 100 mg/cc of iron varies from 14.1 to 326.0 when increasing exposure in the order, while the CNRs obtained for the same acquisition using proj-PR-LLS method vary from 1.0 to 35.0, as shown in Figure 5.15. We can observe that with 60 energy bins, ima-PR-LS method exhibits comparable average errors with proj-PR-LLS method, but with much higher CNRs.

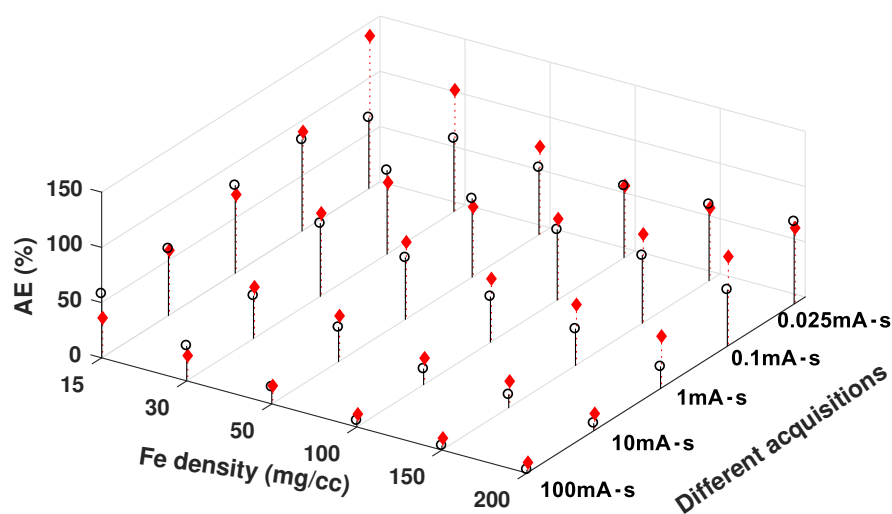


Figure 5.14: Average errors comparison of decomposed iron images obtained using proj-PR-LLS method (black circles) and ima-PR-LS method (red diamonds). All acquisitions are with 60 energy bins but different exposure factors.

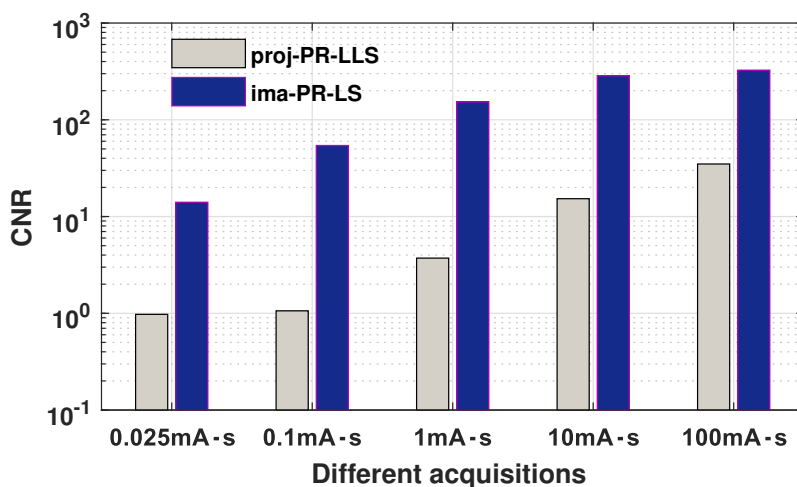


Figure 5.15: CNRs comparison of decomposed iron images for 100 mg/cc of iron obtained using proj-PR-LLS method and ima-PR-LS method. All acquisitions are with 60 energy bins but different exposure factors.

Figure 5.16 demonstrates the computational time of proj-PR-LLS and ima-PR-LS methods for different acquisitions. The computation time is measured on a computer with processor Intel Core i5 and 8 GB RAM. The software platform used was Matlab R2017a. It can be observed that the computation time of proj-PR-LLS method depends largely on the number of energy bins while the exposure factor has little influence. With the same acquisition parameters ( $N = 60$  and the same  $F$ ), ima-PR-LS method takes



much shorter time than proj-PR-LLS method.

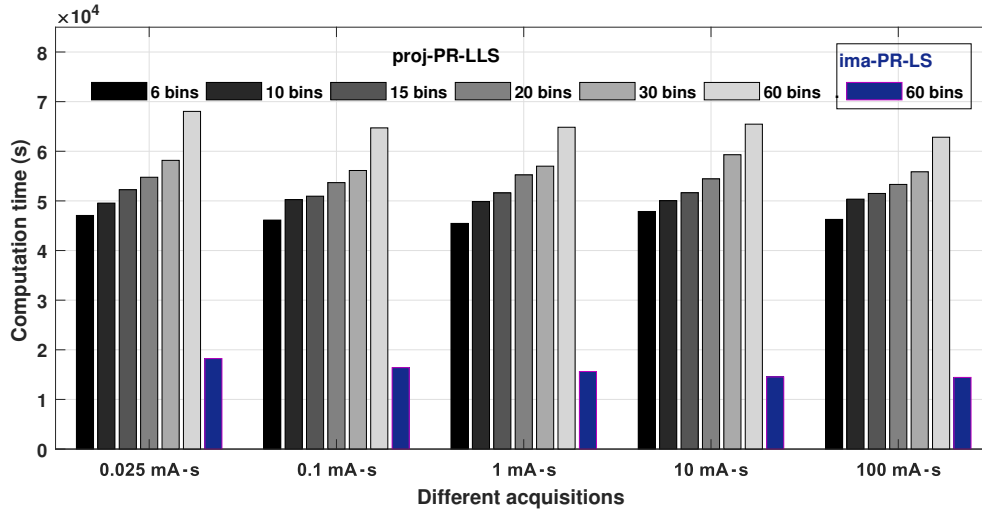


Figure 5.16: Computation time of proj-PR-LLS and ima-PR-LS methods for different acquisitions: exposure factor  $F$  from 0.025 to 100 mA·s, energy bins  $N$  from 6 to 60 for proj-PR-LLS method and  $N = 60$  for ima-PR-LS method.

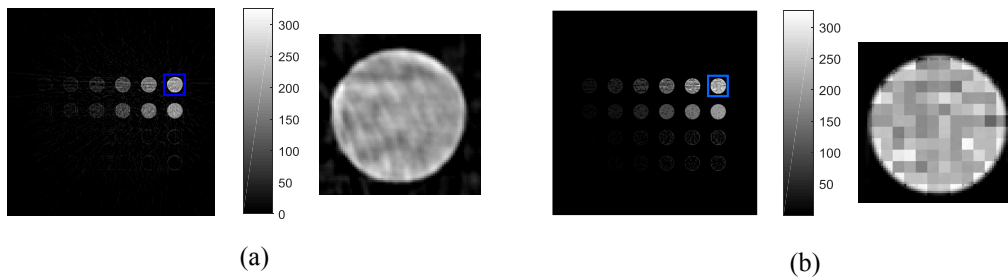


Figure 5.17: Zoomed views of the decomposed iron images ( $N = 60$ ,  $F = 10$  mA·s) obtained by proj-PR-LLS (a) and ima-PR-LS (b) methods to show the “pattern” defects caused by patchwise regularization.

## 5.4 Conclusion and discussion

To investigate the influence of exposure factor and number of energy bins on the performance of material decomposition, we have simulated spectral CT imaging of a PMMA phantom with Fe, Ca and K solutions at different concentrations. The simulations were done under various acquisition conditions by varying the number of energy bins (6, 10, 15, 20, 30 and 60) and exposure factors per projection (0.025, 0.1, 1, 10 and 100 mA·s). Then we performed material decomposition using proj-PR-LLS method and ima-PR-LS method, which have been proposed in Chapter 3.

Proj-PR-LLS decomposition method enabled us to discriminate iron from calcium, potassium and water under all conditions. According to the CNR plot, for lower exposure factor, decomposition performance tends to benefit from a lower number of energy bins. This finding agrees with the theoretical analysis that low dose acquisition suffers from more serious noise problem (Equation (5.1)), and that the more the energy bins, the more serious this problem is. We can employ the detector with an appropriate number of energy bins, depending on the acquisition parameter.

Ima-PR-LS decomposition method is much more sensitive to the number of energy bins than proj-PR-LLS method. Iron in the mixture was not separated from calcium and potassium when  $N = 6, 10, 15, 20$  and  $30$ . The only successful case appeared when  $N = 60$ . The possible reason is that this method considers material decomposition as a linear inverse problem, where the effective mass attenuation coefficients  $\mu_m(i)$  of each energy bin  $B_i$  form its coefficient matrix. However,  $\mu_m(i)$  was estimated by Equation (3.13) and this estimation has brought deviations to the true coefficient matrix. The larger the number of energy bins, the more accurate the estimated coefficient  $\mu_m(i)$  is and the less deviation it causes. With 60 energy bins, ima-PR-LS method outperforms the other approach, with higher CNRs. In the case  $N = 60$  and  $F = 100\text{mA}\cdot\text{s}$ , the average errors of estimated iron content varied from 35.6% to 9.01% for the concentrations from 15mg/cc to 200 mg/cc.

We have mentioned in Chapter 3 that the proposed patchwise decomposition may cause “pattern” defect, which can be observed in the zoomed views in Figure 5.17. For image domain method, this defect exist in the form of patch effect, where gray difference can be observed from one patch to another (Figure 5.17 (b)); for projection domain method, “pattern” defect exist in the form like ring artifact (Figure 5.17 (a)) since the image is obtained by applying FBP reconstruction to the decomposed sinogram.

Beam hardening is a well-known effect in X-ray CT scan, which expresses the phenomenon that the polychromatic X-ray beam becomes “harder” when it passes through the object, due to the attenuation of lower energy photons and the presence of only higher energy photons. Some research showed that spectral CT imaging has the ability to correct beam hardening by projection domain material decomposition [Roessl and Proksa, 2007], or by virtual monochromatic imaging technique [Neuhaus et al., 2017, Yu et al., 2012]. Image domain decomposition works on reconstructed images of different energy bins, where beam hardening artifacts can be introduced by conventional reconstructions. Wider energy bin width (small number of energy bins) leads to heavier beam hardening. When the number of energy bins increases to 60 in our case, the beam hardening effect can be considered negligible (as the variation of the attenuation coefficient in one keV is negligible).

Both proj-PR-LLS and ima-PR-LS methods for spectral CT are able to discriminate and quantify iron from calcium, potassium and water under certain conditions. Their performances vary with the acquisition parameters of spectral CT. One can choose to employ one of the two methods according to the acquisition constraints: if the number of energy bins is large (60 for example), we suggest ima-PR-LS method for iron determination in view of its higher CNR and shorter running time; otherwise, we suggest the proj-PR-LLS method.

Certain points of the present study could be improved. We have investigated the influence of the number of energy bins on the decomposition performance, during which the bins were assumed to be evenly distributed within the detecting energy range. However, the width and placement of each energy bin can also influence the performance of material

decomposition, and they can be investigated in the future.

# Chapter 6

## Conclusion and perspectives

### Contents

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## 6.1 Conclusion

In this thesis, we have studied the quantitative material decomposition methods for spectral CT. As mentioned in Chapter 1, the main contributions of the present work lie in three aspects: (1) study of the material decomposition methods for spectral X-ray CT; (2) validation and assessment of the proposed methods via simulation for medical and industrial applications; (3) investigation of the influence of different acquisition parameters, i.e. exposure factor and number of energy bins, on material decomposition performance.

Before presenting the achievements of the present thesis work, the basic principles of spectral CT have been reviewed in Chapter 2. Based on the fact that materials have different attenuation properties to X-ray, CT scanners take measurements of integral projections of an object from different angles and then reconstruct the 2-D cross-sectional image through more or less complex computations. Conventional CT devices are equipped with energy integrating detectors which provide integrated information of all the transmitted beam while spectral CT employs photon counting detectors and is able to obtain spectral information of several energy bins with single acquisition. Spectral CT enables us to overcome many limitations of the conventional CT techniques and opens up many new application possibilities, among which quantitative material decomposition is the hottest topic.

Acquainted with the general principles of spectral CT, we set up the present work following the above-mentioned three aspects:

(1) Material decomposition methods (Chapter 3).

We have classified existing material decomposition methods in two categories: effect-based and material-based methods. Our work was around the latter one, where the linear attenuation coefficient is described as the contributions of a basis of materials. Meanwhile, according to the type of data on which the decomposition operates, we have investigated the projection domain method and the image domain method. The commonly used decomposition is based on least square criterion, named proj-LS and ima-LS method. However, the inverse problem of material decomposition is usually ill-posed and the X-ray spectral CT measurements suffer from Poisson photon counting noises. The standard LS criterion can lead to overfitting to the noisy measurement data. We have proposed a least log-squares criterion for projection domain method to minimize the errors on linear attenuation coefficient: proj-LLS method. Furthermore, to reduce the effect of noise and enforce smoothness, we have proposed to add a patchwise regularization term to penalize the sum of the square variations within each patch, giving rise to the proj-PR-LLS and ima-PR-LS methods.

(2) Validation and assessment via simulation (Chapter 4).

The performance of the proposed projection domain material decomposition methods has been validated through simulated spectral X-ray imaging. The simulation was realized with VXI software for medical and industrial applications:

- Medical application: iodine and calcium identification. To distinguish compositions of atherosclerotic plaque, we have simulated spectral CT imaging of a

computational human thorax phantom with realistic noise. Extra calcium and iodine solutions with different concentrations were placed inside the phantom. Three material decomposition methods have been investigated: proj-LS, proj-LLS and proj-PR-LLS methods. By decomposing the acquired data into three basis materials, iodine, calcium and soft tissues, all methods enable us to obtain the density distributions of the corresponding basis materials. However, the proposed proj-LLS method and proj-PR-LLS method exhibit better accuracy and better image quality than the commonly used proj-LS method in terms of their average errors and CNRs.

- Industrial application: ABS-FR plastic sorting. Although the material decomposition methods were demonstrated in case of spectral CT imaging, the projection domain decomposition methods can also be applied to PCD-based spectral CR imaging. For the latter, we have investigated the material decomposition ability of the proposed proj-PR-LLS method for spectral CR imaging in order to identify different ABS-FR materials (FRs: brominated FR, chlorinated FR and phosphorus FR). The results show that the decomposition directly in the 3-material basis (ABS+ Br+Cl) is not enough robust to noise. To improve the performance, we proposed a proj-PR-LLS-clas method which integrates classification into the decomposition procedure. The idea of classification is based on the fact that each plastic material contains only one type of FR. Therefore, it is reasonable to decompose firstly in 2-material basis (ABS+Br and ABS+Cl), and then choose the one with smaller objective function values as the final results. This method has enhanced the separation between Br and Cl compared to proj-PR-LLS method. For simulation with realistic noise, when the thickness of phantom is large enough, ABS and the FRs that contain Br, Cl and P can be identified at the same time.

(3) Influence of different acquisition parameters (Chapter 5).

We have simulated spectral CT imaging of a PMMA phantom with Fe, Ca and K solutions at different concentrations to investigate the influence of exposure factor and number of energy bins on the performance of material decomposition. The simulations were done under various acquisition conditions by varying the number of energy bins ( $N = 6, 10, 15, 20, 30$  and  $60$ ) and exposure factors per projection ( $F = 0.025, 0.1, 1, 10$  and  $100\text{mA}\cdot\text{s}$ ). The performance of proj-PR-LLS method and ima-PR-LS has been studied.

Proj-PR-LLS decomposition method enabled us to discriminate iron from calcium, potassium and water under all conditions. According to the CNR plot, for lower exposure factor, decomposition performance tends to benefit from lower number of energy bins. Ima-PR-LS decomposition method is much more sensitive to the number of energy bins than proj-PR-LLS method. Iron in the mixture was not separated from calcium and potassium when  $N = 6, 10, 15, 20$  and  $30$ . The only successful case appeared when  $N = 60$ .

To conclude, both proj-PR-LLS and ima-PR-LS methods for spectral CT are able to discriminate and quantify iron from calcium, potassium and water under certain conditions. Their performances vary with the acquisition parameters of spectral CT.

One can choose to employ one or the other depending on acquisition constraints: if the number of energy bins is large (60 for example), we suggest ima-PR-LS method for iron determination in view of its higher CNR; otherwise, we suggest the proj-PR-LLS method.

## 6.2 Perspectives

We have presented in the previous parts the decomposition performance of the proposed methods, and the influence of different acquisition parameters on the methods. Several potential improvements can be carried out in the future.

- On the simulation
  - The absorption efficiency of the CdTe-based photon counting detector has been simulated in the present work. However, our simulation has assumed a perfect detector energy resolution so that all the photons can be correctly counted for the corresponding energy bin. In practice, the detector response function of monochromatic beam has a broad spectrum and the energy resolution is limited. Therefore, the detector energy resolution should be considered in the future.
  - Our simulation was based on the Beer Lambert law only, i.e. without scattered photons though VXI software allows simulation with first order scattering at a cost of much longer simulation time. Therefore, taking scattering into consideration for the simulation will be a step forward to see if it has an influence on the decomposition performance.
  - State of the art PCDs have defects including pulse pileup, charge sharing, K-escapes, Compton scattering and so on, which were not simulated in our study and can be improved in the future as published by others. In the work of [Taguchi et al., 2010, Alvarez, 2014], pulse pileup effect has been modeled by analytical formalism. Furthermore, in the work published by CEA-LETI [Montémont et al., 2006], a model of the semiconductor detector has been developed which included other defects such as charge sharing, K-escapes and Compton scattering in the detector response matrix.
- On the decomposition methods
  - We have used FBP reconstruction throughout the present work for sake of computation cost. However, iterative reconstruction has potential to reduce noise and improve image quality. It would be interesting to replace FBP reconstruction with iterative methods if computational condition is allowed.
  - For the proposed patchwise regularized methods (proj-PR-LLS and ima-PR-LLS), several parameters need to be chosen: patch size ( $np_r \times np_c$ ) and relaxation parameter ( $r$ ). We have used single patch size for the whole image of each application, further study can be revolved around a zone-wise patch size. For example, we take the low energy bin image and apply a segmentation process to detect the homogeneous zones and detail zones, then we define large

patch sizes for the former and small patch size for the latter. As for  $r$ , it has been chosen heuristically through visual inspection, except for the application of plastic sorting, where we have applied L-curve method to a certain region on the radiographic images, and used the approximated  $r$  for all patches. However,  $r$  should change for different patches since the noise level varies. Therefore, further improvement could be done concerning the selection of patchwise relaxation parameter.

- Experimental validation

The evaluation of the proposed methods in this thesis was based on simulated spectral X-ray imaging, which is different from real experimental systems. A Philips spectral CT prototype has been installed at imaging center CERMEP (Centre d'Etude et de Recherche Multimodal Et Pluridisciplinaire) in Lyon. It can detect and quantify a variety of atoms including iodine, gadolinium, gold and bismuth using K-edge technique, and also enables to enhance the contrast-to-noise ratio of images by virtual monochromatic imaging technique. However, the raw data are not available now for processing. Further experimental validation on real spectral CT data will be considered in the future.

### 6.3 Author's publications

#### Journal papers:

- Ting Su, Valérie Kaftandjian, Philippe Duvauchelle, and Yuemin Zhu. "A spectral X-ray CT simulation study for quantitative determination of iron." *Nuclear Instruments and Methods in Physics Research Section: A*, 2018, 894:39-46 (Published)
- Bingqing Xie, Ting Su, Valérie Kaftandjian, Pei Niu, Feng Yang, Marc Robini, Yuemin Zhu, Philippe Duvauchelle. "Material Decomposition in X-ray Spectral CT Using Multiple Constraints in Image Domain." *Journal of Nondestructive Evaluation*. (Under review)

#### Conference papers:

- Ting Su, Valérie Kaftandjian, Philippe Duvauchelle, Philippe Douek, and Yuemin Zhu. "Quantitative material decomposition method for spectral CT imaging." 7th Conference on Industrial Computed Tomography (iCT 2017), Leuven, Belgium, Feb 2017. (Published)
- Ting Su, Valérie Kaftandjian, Philippe Duvauchelle, and Yuemin Zhu. "Material decomposition for spectral X-ray CT: application to calcium and iodine identification." 2017 IEEE Nuclear Science Symposium and Medical Imaging Conference (IEEE NSS/NIC 2017), Atlanta, USA, Oct 2017. (Published)
- Ting Su, Valérie Kaftandjian, Philippe Duvauchelle, and Yuemin Zhu. "Plastic sorting by X-ray radioscopy with photon counting detector." 12th European Conference on Non-Destructive Testing (ECNDT 2018), Gothenburg, Sweden, June, 2018 (Accepted)



- Bingqing Xie, Ting Su, Valérie Kaftandjian, Philippe Duvauchelle, Pei Niu, Marc Robini, and Yuemin Zhu. “Image Domain Local Joint Sparse Material Decomposition in Spectral CT.” 8th Conference on Industrial Computed Tomography (iCT 2018), Wels, Austria, Feb 2018. (Published)

# Appendix

## Determination of $r$ with L-curve method (section 4.5)

The L-curve is a log-log plot of the norm of a regularized solution versus the norm of the corresponding residual, where the “corner” of the curve corresponds to the selected relaxation parameter [Hansen, 1999]. For proj-PR-LLS decomposition method, the solution norm and residual norm correspond to the objective function value and  $R(P_\alpha^C)$  value in Equation 3.16. We choose a region of interest on the radiographic image for the determination of  $r$ , which is shown in Figure A.1.

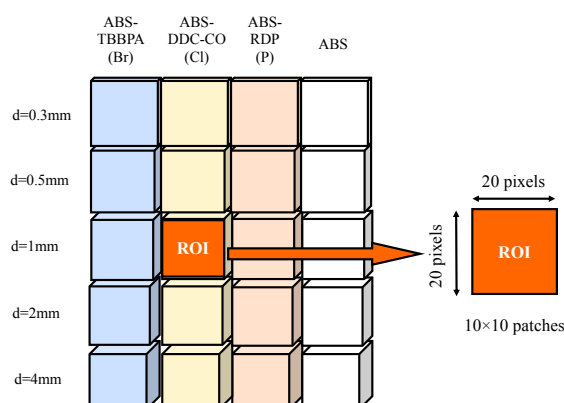


Figure A.1: Illustration of ROI for the determination of  $r$ .

The ROI contains  $20 \times 20$  pixels. Known that the patch size has been set to  $2 \times 2$ , there are  $10 \times 10 = 100$  patches within the ROI. For a given  $r$ , we define the solution norm and residual norm as the average values calculated for these 100 patches. We plotted the L-curve with  $r$  varying from  $10^{-10}$  to  $10^{10}$ , as shown in Figure A.2 (a). It is observed that the “corner” exists between  $r = 10^4$  and  $r = 10^5$ . Further more, we plotted the same curve for a set of  $r$  between  $10^4$  and  $10^5$ , Figure A.2 (b). From this figure, we select  $r = 10^{4.4}$  as the relaxation parameter for all patches when using proj-PR-LLS method for material decomposition.

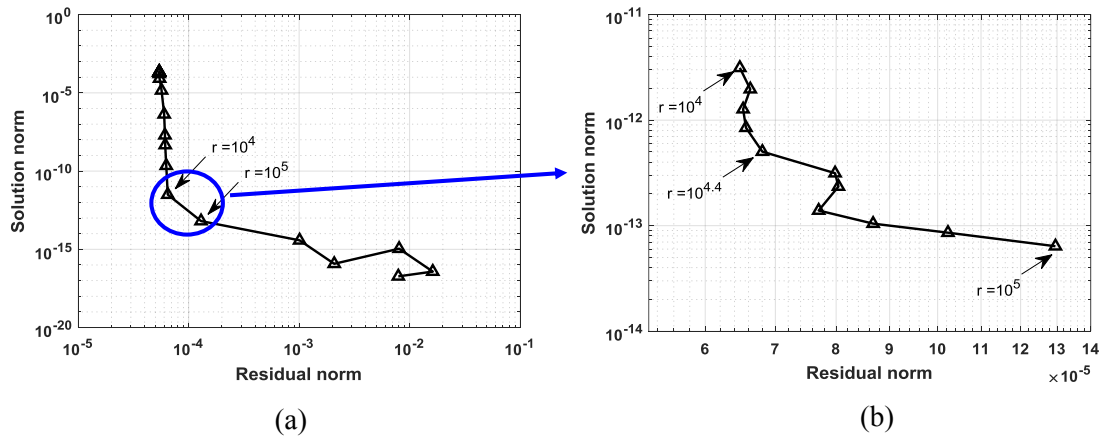


Figure A.2: The L-curve with  $r$  varying from  $10^{-10}$  to  $10^{10}$  (a), and from  $10^4$  to  $10^5$  (b).

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# Abbreviations

**ABS** Acrylonitrile-butadiene-ctyrene

**AE** Average Error

**BG** Background Region

**CNR** Contrast-to-noise Ratio

**CR** Computed Radiography

**CT** Computed Tomography

**DDC-CO** Dechlorane Plus

**DECT** Dual-energy Computed Tomography

**FBP** Filtered Back-projection

**FR** Flame Retardant

**LS** Least Squares

**PCD** Photon Counting Detector

**PMMA** Poly(Methyl Methacrylate)

**RDP** Resorcinol Bis(Diphenyl Phosphate)

**ROI** Region of Interest

**SNR** Signal-to-noise Ratio

**TBBPA** Tetrabromobisphenol A

# Main Symbols

$\mu$  Linear attenuation coefficient

$\mu_m$  Mass attenuation coefficient

$\rho$  Density

$E$  Energy

$D(E)$  Detector absorption efficiency

$\alpha$  Type of material

$i$   $i$ th energy bin

$\lambda_i$  Expected number of photons in the  $i$ th energy bin

$P_\alpha$  Density integral of material  $\alpha$

$Z$  Atomic number

$r$  Relaxation parameter

$d$  Thickness

$N$  Number of energy bins

$F$  Exposure factor



## FOLIO ADMINISTRATIF

### THESE DE L'UNIVERSITE DE LYON OPEREE AU SEIN DE L'INSA LYON

NOM : SU  
(avec précision du nom de jeune fille, le cas échéant)

DATE de SOUTENANCE : 28/06/2018

Prénoms : Ting

TITRE : Méthodes de décomposition quantitative des matériaux pour la tomographie spectrale aux rayons X

NATURE : Doctorat

Numéro d'ordre : 2018LYSEI056

Ecole doctorale : Electronique, électrotechnique, automatique (EEA)

Spécialité : Traitement du Signal et de l'Image

#### RESUME :

La tomographie (CT) aux rayons X joue un rôle important dans l'imagerie non invasive depuis son introduction. Au cours des dernières années, de nombreuses avancées technologiques en tomographie par rayons X ont été observées, notamment la CT spectrale, qui utilise un détecteur à comptage de photons (PCD) pour discriminer les photons transmis correspondant à des bandes d'énergie sélectionnées afin d'obtenir une information spectrale.

La CT spectrale permet de surmonter de nombreuses limitations des techniques précédentes et ouvre de nombreuses applications nouvelles, parmi lesquelles la décomposition quantitative des matériaux est le sujet le plus étudié. Un certain nombre de méthodes de décomposition des matériaux ont été rapportées et différents systèmes expérimentaux sont en cours de développement pour la CT spectrale. Selon le type de données sur lequel l'étape de décomposition fonctionne, nous avons les méthodes du domaine des projections (décomposition avant reconstruction) et les méthodes du domaine de l'image reconstruite (décomposition après reconstruction).

La décomposition couramment utilisée est basée sur le critère des moindres carrés, nommée proj-LS et méthode ima-LS. Cependant, le problème inverse de la décomposition du matériau est généralement mal posé et les mesures du CT spectral aux rayons X souffrent de bruits de comptage de photons de Poisson. Le critère des moindres carrés peut conduire à un surajustement des données de mesure bruitées. Dans le présent travail, nous avons proposé un critère de moindre log-carré pour la méthode du domaine de projection afin de minimiser les erreurs sur le coefficient d'atténuation linéaire: méthode proj-LLS. De plus, pour réduire l'effet du bruit et lisser les images, nous avons proposé d'ajouter un terme de régularisation par patch pour pénaliser la somme des variations au carré dans chaque zone pour les décompositions des deux domaines, nommées proj-PR-LLS et ima -PR-LS méthode.

Les performances des différentes méthodes ont été évaluées par des études de simulation avec des fantômes spécifiques pour différentes applications: (1) Application médicale: identification de l'iode et du calcium. Les résultats de la décomposition des méthodes proposées montrent que le calcium et l'iode peuvent être bien séparés et quantifiés par rapport aux tissus mous. (2) Application industrielle: tri des plastiques avec ou sans retardateur de flamme. Les résultats montrent que 3 types de matériaux ABS avec différents retardateurs de flamme peuvent être séparés lorsque l'épaisseur de l'échantillon est favorable.

Enfin, nous avons simulé l'imagerie par CT spectrale avec un fantôme de PMMA rempli de solutions de Fe, Ca et K. Différents paramètres d'acquisition, c'est-à-dire le facteur d'exposition et le nombre de bandes d'énergie, ont été simulés pour étudier leur influence sur la performance de décomposition pour la détermination du fer.

MOTS-CLÉS : Tomographie, Rayons X, CT spectrale, Détecteur à comptage des photons, Décomposition de matériaux, Simulation

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