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Anna Mira

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THÈSE

Pour obtenir le grade de

DOCTEUR DE LA COMMUNAUTE UNIVERSITE GRENOBLE ALPES

Spécialité : **BIS – Biotechnologie, instrumentation, signal et imagerie pour la biologie, la médecine et l'environnement**

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Présentée par

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préparée au sein du **Laboratoire Techniques de L'Ingénierie Médicale et de la Complexité - Informatique, Mathématiques et Applications** en collaboration avec **GE Healthcare**. dans **l'École Doctorale Ingénierie pour la santé la Cognition et l'Environnement**.

Modélisation biomécanique du sein pour l'évaluation de la compression et de la perception d'inconfort en mammographie.

Thèse soutenue publiquement le **5 Juillet 2018** devant le jury composé de :

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Breast biomechanical modeling for the evaluation of the compression and the discomfort perception in mammography.

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ABSTRACT

Contexte La mammographie est une modalité d'imagerie médicale à faible dose permettant la détection du cancer mammaire à un stade précoce. Lors de l'examen, le sein est comprimé entre deux plaques afin d'uniformiser son épaisseur et d'étaler les tissus. Cette compression améliore la qualité clinique de l'examen mais elle est également source d'inconfort chez les patientes. Bien que la mammographie soit la méthode de dépistage la plus efficace du cancer du sein, l'inconfort ressenti peut dissuader les femmes de passer cet examen. Par conséquent, une technique alternative de compression du sein prenant en compte le confort de la patiente, en plus de l'amélioration de la qualité d'image, présente un grand intérêt.

Méthodes Dans ce travail, nous avons proposé un nouvel environnement de simulation permettant l'évaluation de différentes techniques de compression du sein. La qualité de la compression a été caractérisée en termes de confort de la patiente, de la qualité d'image et de la dose glandulaire moyenne délivrée. Afin d'évaluer la déformation du sein lors de la compression, un modèle biomécanique par éléments finis du sein a été développé. Ce dernier a été calibré et évalué en utilisant des volumes IRM d'une volontaire dans trois configurations différentes (sur le dos, le ventre et de côté). Par ailleurs, la qualité d'image a été évaluée en utilisant un environnement de simulation d'imagerie auparavant validé pour la simulation de l'acquisition d'images en mammographie.

Résultats La capacité de notre modèle biomécanique à reproduire les déformations réelles des tissus a été évaluée. Tout d'abord, la géométrie du sein dans les trois configurations a été estimée en utilisant des matériaux Néo-Hookeens pour la modélisation des tissus mous. Les propriétés mécaniques des différents constituants du sein ont été estimés afin que les géométries du sein dans les positions couché sur le ventre et couché soient les plus proches possibles des mesures. La distance de Hausdorff entre les données estimées et les données mesurées est égale à 2.17 mm en position couché sur le ventre et 1.72 mm en position couché sur le dos. Le modèle a ensuite été évalué dans une troisième configuration sur le

côté, avec une distance de Hausdorff étant alors égale à 6,14 *mm*. Cependant, nous avons montré que le modèle Néo-Hookeen ne peut pas décrire intégralement le comportement mécanique riche des tissus mous. Par conséquent, nous avons introduit d'autres modèles de matériaux basés sur la fonction d'énergie de Gent. Cette dernière hypothèse a permis de réduire l'erreur maximale dans la configuration couché sur le ventre et dos incliné d'environ 10 *mm*.

Le couplage entre la simulation de la mécanique du sein et la simulation d'acquisition d'image nous ont permis d'effectuer deux études préliminaires. Dans la première étude, les différences entre les pelotes de compression standard rigide et flex ont été évaluées. Selon les simulations effectuées, l'utilisation de la pelote flex pour la compression du sein a le potentiel d'améliorer le confort de la patiente sans affecter la qualité de l'image ou la dose glandulaire moyenne.

Dans la seconde étude, l'impact du positionnement du sein sur la mécanique globale de la compression mammaire a été étudié. Nos simulations confirment que rapprocher la pelote de compression de la cage thoracique peut augmenter l'inconfort de la patiente. Selon les données estimées, pour une même épaisseur du sein sous compression, la force appliquée au sein peut être s'accroître de 150 %.

Conclusion L'estimation réaliste de la géométrie du sein pour différentes configurations sous l'effet de la gravité, ainsi que les résultats conformes aux descriptions cliniques sur la compression du sein, ont confirmé l'intérêt d'un environnement de simulation dans le cadre de nos études.

Mots clés Mammographie, compression mammaire, confort du patient, modèle biomécanique

Background Mammography is a specific type of breast imaging that uses low-dose X-rays to detect breast cancer at early stage. During the exam, the woman's breast is compressed between two plates in order to even out the breast thickness and to spread out the soft tissues. This compression improves the exam quality but can also be a source of discomfort. Though mammography is the most effective breast cancer screening method, the discomfort perceived during the exam might deter women from getting the test. Therefore, an alternative breast compression technique considering the patient comfort in addition to an improved clinical image quality is of large interest.

Methods In this work, a simulation environment allowing the evaluation of different breast compression techniques was put forward. The compression quality was characterized in terms of patient comfort, image quality and average glandular dose. To estimate the breast deformation under compression, a subject-specific finite element biomechanical model was developed. The model was calibrated and evaluated using MR images in three different breast configurations (supine, prone and supine tilted). On the other hand, image quality was assessed by using an already validated simulation framework. This framework was largely used to mimic image acquisitions in mammography.

Findings The capability of our breast biomechanical model to reproduce the real breast deformations was evaluated. To this end, the geometry estimates of the three breast configurations were computed using Neo-Hookean material models. The subject specific mechanical properties of each breast's structures were assessed, to get the best estimates of the supine and prone configurations. The Hausdorff distances between the estimated and the measured geometries were equal to 2.17 mm and 1.72 mm respectively. Then, the model was evaluated using a supine tilted configuration with a Hausdorff distance of 6.14 mm . However, we have shown that the Neo-Hookean strain energy function cannot fully describe the rich mechanical behavior of breast soft tissues. Therefore, alternative material models based on the Gent strain energy function were proposed. The latter assumption reduced the maximal error in supine tilted breast configuration by about 10mm .

The coupling between the simulations of the breast mechanics and the X-ray simulations allowed us to run two preliminary studies. In the first study, the differences between standard rigid and flex compression paddles were assessed. According to the performed simulations, using the flex paddle for breast compression may improve the patient comfort without affecting the image quality and the delivered average glandular dose.

In the second study, the impact of breast positioning on the general compression mechanics was described. Our simulations confirm that positioning the paddle closer to the chest wall is suspected to increase the patient discomfort. Indeed, based on the estimated data, for the same breast thickness under compression, the force applied to the breast may increase by 150%.

Conclusion The good results we obtained for the estimation of breast deformation under gravity, as well as the conforming results on breast compression quality with the already

ABSTRACT

published clinical statements, have shown the feasibility of such studies by the means of a simulation framework.

Keywords Mammography, breast compression, patient comfort, biomechanical model

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GENERAL PROBLEM STATEMENT

Today, mammography is the primary imaging modality for breast cancer screening and plays an important role in cancer diagnosis. Subtle soft-tissue findings and microcalcifications that may represent early breast cancer are visualized by means of X-rays images. After investigation, the abnormal findings are taken up for further evaluation.

A standard mammography protocol always includes breast compression prior to image acquisition. Woman's breast is compressed between two plates until a nearly uniform breast thickness is obtained. The breast flattening improves diagnostic image quality and reduces the absorbed dose of ionizing photons. However, the discomfort and pain induced by this compression procedure might deter women from attending a mammography. Fleming et al. [46] showed in a 2500 women panel study that 15% of those who skipped the second appointment cited an unpleasant or painful first mammogram.

An important improvement concerning the patient comfort could be achieved with the emergence of Full-Field Digital Mammography (FFDM). Due to the improved detector capabilities, digital mammography became better in terms of image quality and radiation dose than Film-Screen Mammography. The use of Automatic Exposure Control (AEC) allowed to estimate the acquisition parameters providing the optimal image quality and average glandular dose for a given breast thickness and glandularity.

Subsequently, there is an opportunity to leverage the potential of the recent imaging technologies by developing alternative breast compression techniques. The new techniques have to consider the patient comfort in addition to an improved image quality and a reduced ionizing radiation dose. This may imply another paddle geometry or peculiar material properties as well as distinct compression paddle positioning.

The goal of this PhD thesis was to develop a simulation environment able to characterize the impact of the paddle design on the patient comfort and its repercussion on the mammography image quality and average glandular dose. Due to the complexity of in-vivo clinical studies, a realistic simulation framework is of a large interest. To this end, the following tasks were considered.

- To develop a biomechanical breast model taking into consideration the subject-specific breast geometry and tissues' mechanical properties.
- To evaluate this biomechanical breast model.
- To model the breast deformations under compression.
- To integrate the corresponding deformable breast phantom into the image acquisition simulation framework.
- To compute compression quality measures able to characterize the differences between various breast compression techniques in terms of patient comfort, image quality and average glandular dose.

Using the developed tools, two studies could be performed.

- To assess the differences between standard rigid and flex paddles in terms of patient comfort, image quality and average glandular dose for two different breast volumes.
- To assess the breast positioning impact on compression mechanics and patient comfort, considering one breast volume and one paddle model.

TECHNICAL APPROACH

To study the impact of the paddle design on the compression quality, a simulation framework was developed. The breast mechanics and patient comfort were addressed by the means of finite element modeling (ANSYS¹). On the other hand, the image quality could be assessed by using an image simulation framework modeling the X-rays propagation through matter during acquisition of a mammography image (CatSim²).

First, to develop a subject-specific breast model, the MR images of two volunteers in three distinct positions (supine, prone and supine tilted) were acquired. The MRI volumes were processed (ITK³/ VTK⁴/ CamiTK⁵) and segmented (ITK-Snap⁶). Then, the processed images were used to extract the 3D surfaces of the breast, compatible with ANSYS Mechanical meshing software. The breast geometries were discretized using tetrahedral solid elements and were the subjects of hyper-elastic quasi-static simulations. An exhaustive optimization process was performed to determine the subject-specific tissues mechanical properties as well as the corresponding breast stress-free configuration. The model was developed and calibrated such as the best estimates of supine and prone breast configurations were obtained. The model accuracy was assessed in terms of Hausdorff distance between the measured and estimated breast surfaces in supine tilted configuration.

Once the model was created and evaluated, it was used to quantify the breast compression quality. To this end, different finite element models of the paddle were developed with peculiar assumption on their flexibility and degrees of freedom. For each simulation of breast compression, the patient comfort was associated with the internal tissues stress/strain distribution and the pressure range at the skin surface. The mean average dose was computed using the model proposed by Dance et al. [30] for the corresponding

¹<https://www.ansys.com/>

²Milioni de Carvalho P. 2014, PhD thesis

³<https://itk.org/>

⁴<https://www.vtk.org/>

⁵<http://camitk.imag.fr/>

⁶<http://www.itksnap.org>

breast thickness was derived from finite element simulations. The compressed breast geometry was then imported into the image simulation software (CatSim) together with an embedded set of virtual microcalcifications. Synthetic projections were then generated and the signal to noise ratio as well as the signal-difference to noise ratio were computed to characterize the resulting image quality.

THESIS OVERVIEW

This manuscript is divided into six major chapters. **Chapter 1**, describes the clinical background required for a good understanding of our work. Both internal and external structure of the breast are described. The role of regular screening for breast cancer is discussed with a list of involved medical imaging technologies.

Chapters 2 and 3 are focused on breast biomechanical modeling. **Chapter 2** provides a brief introduction to the continuum and contact mechanics and describes the finite element numerical method able to solve such problems. This chapter provides also a review on biomechanical modeling of the breast. Successes and failures of experiments reported in the literature, to determine the tissues material properties and breast stress-free geometry, are discussed. The most advanced biomechanical models are listed with their corresponding errors with reference to real breast deformations. **Chapter 3** describes the breast biomechanical model we have proposed and the multi-loading gravity simulations that we performed to evaluate the model. First, the patient data acquisition as well as the required image pre-processing operations are presented. The optimal mesh size for such simulations is determined. Then, the model sensitivity to different boundary conditions and constitutive parameters is studied. The best modeling techniques of the main anatomical structures, such as the suspensory ligaments and the pectoral fascia, are selected. The results of the optimization process allowing to estimate the subject specific mechanical properties of breast tissues and stress-free geometry are presented. Finally, the model fidelity to the real deformations, as measured in MR images of the breast in three different configurations, is discussed.

Chapters 4 and 5 are focused in breast deformation under compression modeling, as well as on the assessment of the compression quality in mammography. **Chapter 4** describes the breast compression process and its associated mechanics as recorded during real mammography acquisitions. The role of tissues compression in mammography as well as the current gold standards for image quality and average glandular dose are discussed. The last proposed technologies dealing with patient comfort and pain reducing techniques are outlined with their impact on patient comfort. In **Chapter 5**, two studies on breast

compression quality are described. First, the finite element models of standard compression paddles are provided with the corresponding assumptions on their dynamics. The computed compression force and breast thickness are compared to the corresponding parameters issued from real mammography exams underwent by the volunteers. The derived adjustments of tissues constitutive models are provided. The details for mammography images simulation and breast phantom creation are also discussed. Next, the metrics of image quality, average glandular dose and patient comfort are defined and used to compare the compression quality between different paddle models and different paddle positions.

Finally, **Chapter 6** summarizes the work reported on this manuscript and generalizes the corresponding results. Perspectives and directions for future work are also provided.

ETHICS AND FUNDING

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The two involved volunteers agreed to participate in a pilot study approved by an ethical committee, MammoBio MAP-VS pilot study.

CLINICAL BACKGROUND

The aim of this chapter is to provide the required clinical background on breast cancer screening and diagnosis for a good understanding of the global aim and relevance of the present work.

First, the breast evolution from early to the adult ages is described, with a detailed characterization of internal and external adult breast structures. To explain the intra-individual variation of breast mechanical and structural properties, hormonal changes during the menstrual cycle, pregnancy or menopause are presented. Next the cancer edogenesis is described and the most common cancer types are characterized. Finally, different modalities for breast imaging are presented with their underlying technical principles as well as their relevance for breast cancer regular screening.

1.1 Breast anatomy

Internal and external breast structures will be repeatedly referenced in the following work, therefore their detailed description including mechanical properties and their localization is needed. Although the breast anatomy seems to be simple and easy to understand, a detailed analysis of breast embryogenesis is requested for a better localization of the supporting breast tissues. The breast support matrix is a structure of high interests when modeling breast mechanics.

1.1.1 Breast embryogenesis

The breast is a modified skin gland which starts to develop at the embryonic stage from the epidermis and dermis. During the sixth fetal month, from 12 to 20 solid cords of epithelial cells are growing down into the dermis (Figure 1.1.a-b). Later, these cords evolve into lactiferous ducts and alveoli (Figure 1.1.c-d). Thus, near birth, a simple network of branching ducts is already developed in the pectoral area [131].

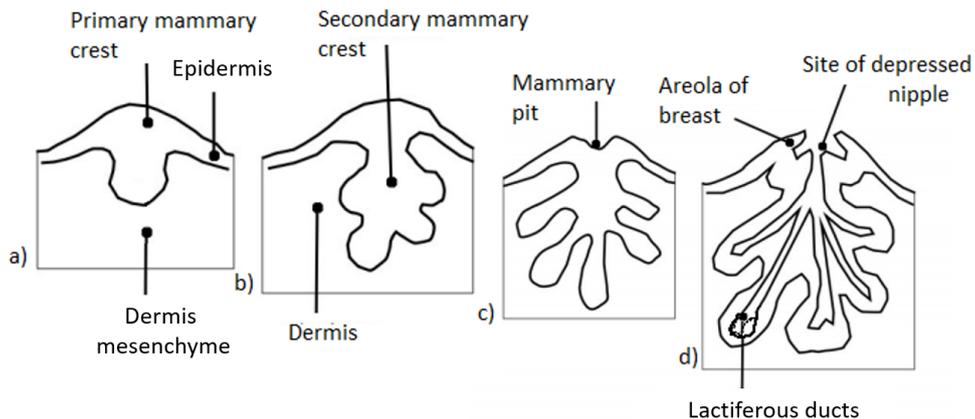


Figure 1.1: Breast embryogenesis: stages of formation of the duct system. The ectoderm is responsible for duct system and alveoli, the mesenchyme is responsible for the connective tissue and vessels [131].

The glandular lobes, generally remain underdeveloped until puberty (13 to 18 years). Under hormonal stimulation, the breast buds, due to the development of the mammary glands and increased deposition of fatty tissue, become palpable discs beneath the nipple. The ducts grow into the soft tissue and the lobular differentiation begins [83].

Kopans D.B. [83] analyzed the breast development sequence in the subcutaneous tissues. According to the author, the evolution of the breast within the fascial system is unclear, with two possible evolution paths:

- (A) The superficial fascia splits in two layers forming the deep and the superficial fascia. The mammary gland appears between these two layers (Figure 1.2.A).

(B) The elongating ducts retracts the superficial fascia. The mammary gland are enveloped by the superficial fascia (Figure 1.2.B)

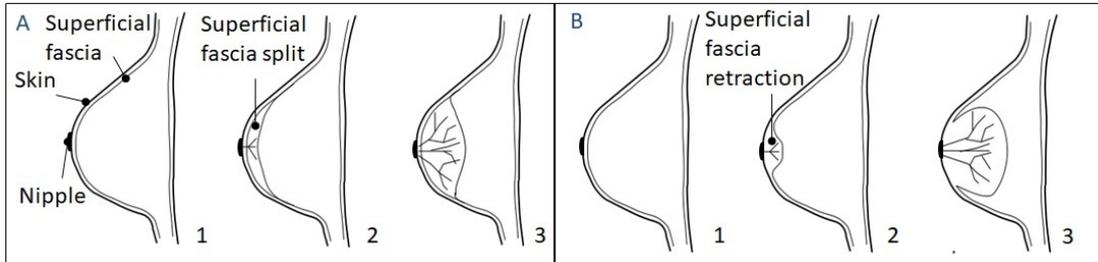


Figure 1.2: Breast development sequence in the subcutaneous tissues. A) Mammary bud development by splitting the superficial fascia in 2 layers. B) Mammary bud development by fascia retraction, reproduced from [83].

1.1.2 Breast external appearance

In order to describe the breast appearance, several notions for localization into the breast volume and its vicinity are defined. Usually, the breast volume is divided into four quadrants: upper outer quadrant (UOQ), upper inner quadrant (UIQ), lower outer quadrant (LOQ), lower inner quadrant (LIQ)(see Figure 1.3). On the other hand, the anatomical structures surrounding the breast are localized using the anatomical landmarks such as the inframammary fold, the clavicle, the sternal angle, the sternal line, the costal margin and the axilla.

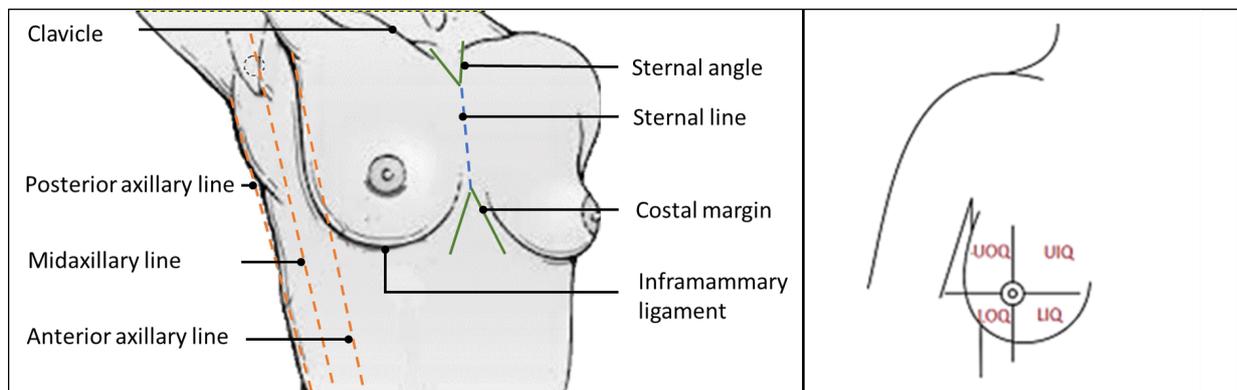


Figure 1.3: Left: thorax landmarks; Right: four breast quadrans [140]

Anatomically, the adult breast is localized on top of the ribcage, between the clavicle superiorly and costal margin inferiorly. Its transverse boundaries are defined from the sternal line medially to the midaxillary line laterally (Figure1.3). The intra-individual asymmetry (between left and right breasts) is considered as a normality for the young and the adult breast. The breast shape and contour are influenced by [96]:

- The volume of mammary gland in each breast quadrant.
- The amount of the subcutaneous and intra-lobular fat.
- The body contour of the chest wall.
- The muscular covering and thickness.
- The thickness and elasticity of the skin.

Anthropomorphic characteristics of women breast were studied almost for the aim of cosmetic and reconstructive surgery. Vandeput J. and Nelissen M [140] measured distances between anatomical landmarks of the thorax of 973 women with aesthetically near-perfect breasts. The authors proposed different relations as guidelines to compute the recommended breast size parameters (nipple-mid clavicle distance, nipple inframammary fold distance) as a relation of body parameters (body height, torso width). In their study, a poor correlation was found between body height or weight and breast volume. Contrariwise a high correlation was found between the nipple to inframammary fold distance or the nipple to mid clavicle distance and the thorax width. Catanuto et al. [20] mentioned that the breast shape after surgery cannot be predicted by volumetric measurements only; they have proposed additional measures (areas, distances or angles) allowing unambiguous characterization of the breast shape. According to the authors, the curvature of the thoracic surface is the most relevant parameter to evaluate the outcome of a reconstructive breast surgery.

Starting with the Warner Brother Corset Company in 1935, the underwear industry introduced a new unit to measure the breast volume, the cup. The cup size is computed using a relation between the circumference of the chest at the level of the nipples and the torso width [109].

1.1.3 Internal structures

Breast heterogeneous structure includes a mixture of parenchyma and adipose tissue (Figure 1.4). The breast parenchyma consists of glandular components, lymphatic network and blood vessels [28]. Skin, Cooper's ligaments and fascias are the supporting system of the breast; their interconnection and intersections with the pectoral muscle fix and support the breast soft tissue [96].

The **adipose tissue** is the predominant tissue of the breast that fills up depressions between the deep and superficial fascia. In the intra-fascial space, adipose tissue surrounds and is dispersed among the glandular structures. Fat properties and its spatial distribution give the breast a soft consistency. The main aim of this tissue is to protect the lobes and lactiferous ducts.

The **glandular tissue** is represented by breast lobes. A healthy female breast is made up of 12-20 lobes. They are distributed centrally and laterally within the breast. The total amount of glandular tissue depends on the hormonal fluctuation, age and physical state.

Mammary ducts arise from the lobes as branches and connect them to the nipple. There are about ten duct systems with a tree-like structure in each breast that carry the milk from the lobes to the nipple. The dark area of skin surrounding the nipple is called the areola.

Huang S. and team [73] have studied the breast shape and fibro-glandular distribution using dedicated breast CT images. This study shows that the glandular tissues is situated in the central portion of the breast. In prone position about 60 % of glandular tissues is located near to the nipple. A mean percentage of glandular tissue was computed by Yaffe and colleagues [147], the values varied from 13.7% to 25.6 % within different groups. They also mentioned a drop in glandular fraction with advancing age.

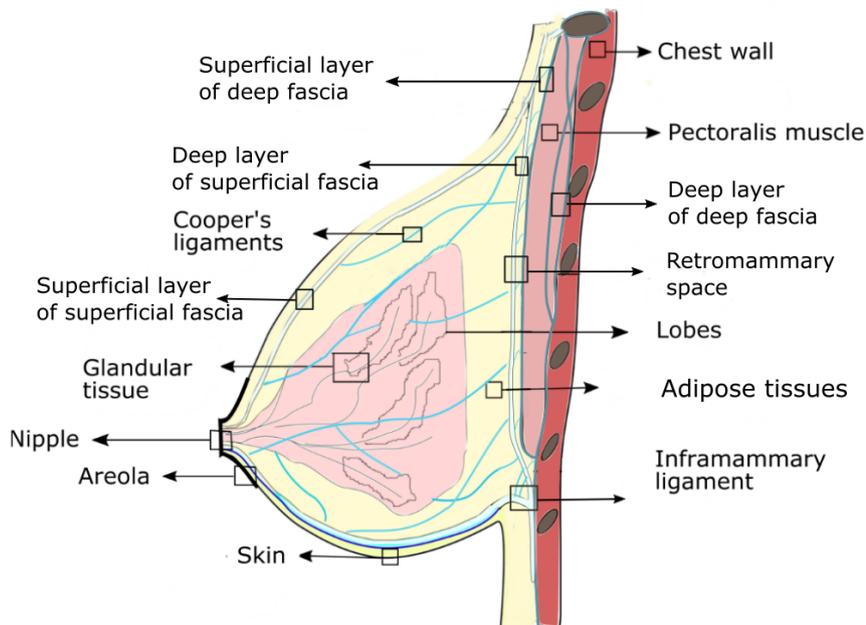


Figure 1.4: Breast anatomy [28].

A layer of adipose tissue and connective fascia separates the breast from the pectoral muscle forming a retro-mammary fat space.

The **skin** is the covering breast layer which provides protection and receives sensory stimuli from the external environment. It is a heterogeneous organ composed of three layers (see Figure 1.5, [77]): epidermis (dead cells) mainly composed of keratin, dermis composed of collagen and elastin fibers in a viscous matrix made of water and glycoproteins and hypodermis, mainly composed of adipocytes cells.

The breast skin thickness varies from the breast base to the nipple between $\sim 2 \text{ mm}$ and $\sim 0.5 \text{ mm}$. At the nipple areola region, the skin is 4-5 mm thick. [4]. Sutradhar A. and Miller M.J. [134] studied the breast skin thickness of 16 different sectors radially

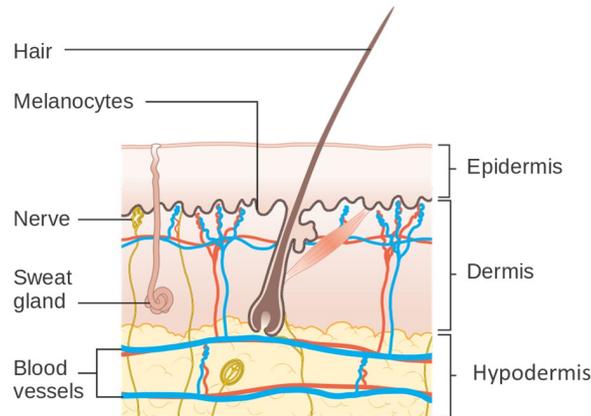


Figure 1.5: Skin anatomy, *Cancer Research UK*

oriented around the nipple. The thickness range proposed by the authors varies between 0.83mm and 2.35mm with a mean of $1.55 \pm 0.25\text{mm}$. According to this study, the skin thickness varies as follows: the lateral region thickness is the thinnest among all the breast regions followed by superior/inferior and medial region; there is no significant difference between the inferior and superior breast regions; in the radially exterior region, the skin is thicker than in the radially interior region (close to the nipple). During the breast puberty, the breast volume increases and the skin thickness decreases in all regions [138].

The **connective tissue** is represented by Cooper's ligaments and fascial system. The breast fascial system is composed of deep fascia and superficial fascia. During puberty, breast is growing and the superficial fascia divides in two layers: the deep layer of the superficial fascia and the superficial layer of the superficial fascia [83]. Cooper's ligaments run throughout the breast tissue parenchyma from the deep layer of the superficial fascia beneath the breast to the superficial layer of superficial fascia where they are fixed (Figure 1.4). Because they are not taut, these ligaments allow the natural motion of the breast [28]. Between the deep layer of the superficial fascia and the superficial layer of the deep fascia, a layer of loose connective loose tissue form the retro-mammary space, allowing the breast tissue to slide over the chest [96]. In regions where the superficial fascia meets the deep fascia, suspension ligaments are created. One of these ligaments is situated at the level of the sixth and seventh ribs and is called the **inframammary ligament** [11]. It evolves into the **deep lateral ligament** and the **deep cranial ligament** that are respectively attached to the axillary fascia and to the clavicle. The second meeting point of the two fascias is situated on the sternal line and is called the **deep medial ligament** (Figure 1.6). On the upper part of the breast, near the second rib space, the deep fascia tightly connects with the two layers of the superficial fascia, and create a the third meeting point. The three ligaments are 3D structures, evolving from the pectoral muscle toward the nipple, underlying the skin surface.

The existence, the topography, and the thickness of the membranous layers of the superficial fascia have been studied in various regions of the body [2]. According to the

authors, the thickness of these superficial layers in both superior and inferior breast regions is equal to $88.12 \pm 7.70\mu m$ and $140.27 \pm 11.03\mu m$ respectively.

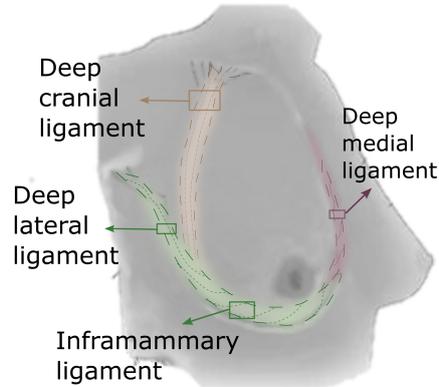


Figure 1.6: Suspensory ligaments. The suspensory ligaments together with the fascias constitute the breast support matrix and ensure the tissues inter-connection [96].

The lymphatic system is a vessel network which insures the transportation of white blood cells from tissues into the bloodstream. All intramammary lymph nodes are located in the lateral half of the breast along the margin of the breast parenchyma [83]. The lymphatic drainage of the breast extends from the subareolar plexus deep to and around the nipple (Figure 1.7).

The blood supply to the breast comes primarily from the internal mammary arteries named respectively subclavian, axillary, and brachial arteries (Figure 1.7). From them, the lateral and internal thoracic arteries run underneath the main breast tissue.

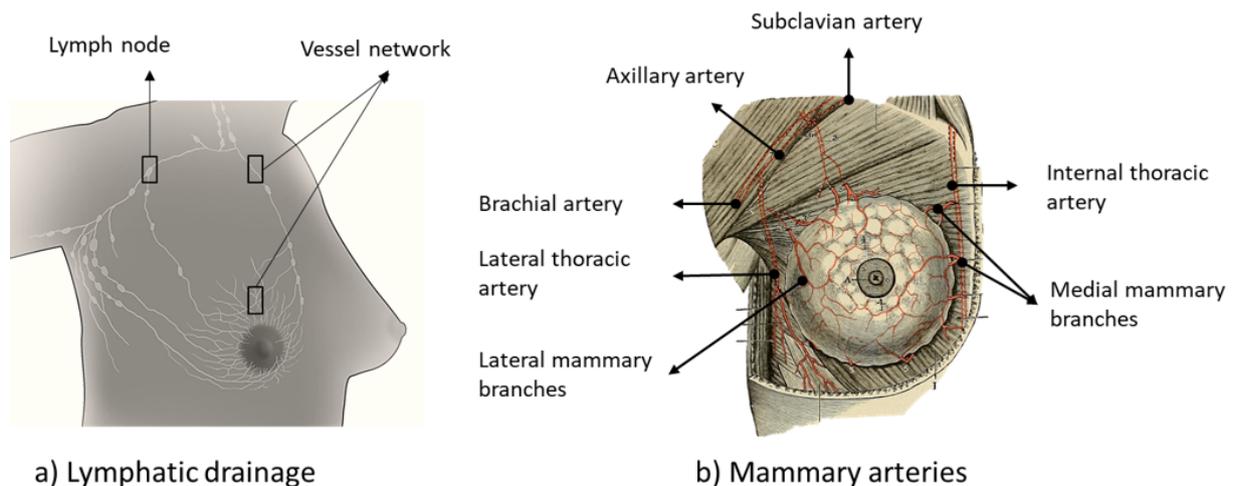


Figure 1.7: Lymphatic system and Mammary Arteries for adult female breast. Images reproduced from National Cancer Institute [97] and Pilcher et al. [115]

1.1.4 Adult breast texture changes

The female breast undergoes substantial changes during the woman's lifetime. Most changes are caused by hormones and by the woman's physiological condition. Important changes in female breast stiffness and composition occur during the menstrual cycle, pregnancy and menopause.

There are three important phases during the menstrual cycle caused by hormonal fluctuation [4]. During the first phase, the estrogen (hormones) diffusion stimulates the epithelial cell multiplication and the enlargement of ductal structures. Next, during ovulation, epithelial cells begin to grow in the lobule due to progesterone hormone; an increase in blood flow is also noticed. In the last phase, the ductal structures and the lobes support an involution and a regression process. It must be mentioned that not all lobules regress, therefore during the menstrual cycle new lobules can be created. The work by Lorenzen et al. [89] showed that, during the premenstrual phase the stiffness of fibro-glandular tissue and glandular tissue can change by 30% and 14 % respectively. They also have shown that in the middle of the menstrual cycle, the parenchyma volume increases by up to 38% and the water content by 24.5%.

During pregnancy, under the influence of estrogen and progesterone, the breast enlarges in volume and density, the veins dilate and the proportion of parenchyma tissues increases. When lactation is weaned the breast returns to the pre-pregnancy state, and the atrophy of glandular, ductal, and stromal elements is observed [106].

The menopausal breast contains a larger fraction of fatty tissues and reduces the number of ductal and lobular elements. During the first four years after menopause, the breast is the subject of an atrophy process. The atrophy begins medially and posteriorly, then laterally, working its way to the nipple [4]. In this period the breast loses progressively fat and stroma tissue, resulting in breast shrinkage and loss of contours.

The breast support matrix can be stretched and attenuated by weight changes occurring during pregnancy and can relax with aging. These various changes can result in an excess of breast mobility over the chest and ptosis.

1.2 Breast Cancer

The first written description of breast cancer was on ancient Egyptian papyrus. At that time the treatment was considered futile and the woman was left without any medical assistance. Ancient Greeks, thought that breast cancer was caused by an excess of black bile. It was thought that the monthly menstrual flow naturally relieved women of this excess, which explained why breast cancer was more common after menopause [4].

Nowadays, several researchers [114, 90] have shown that cancer is always caused by damages of a cell's DNA. The initiation of the mutagenic process that may result in various genetic errors requires cell division. A factor that increases cell proliferation will increase also the risk of cancer. The woman hormones, estrogen and progesterone, appear to impact the breast cell division rate [27, 44], which explains the high rates of breast cancer in women

(99% of breast cancer occurs in women). The risks of developing a cancer is increased by various factors like age, genetics, family history or life style. According to Martin et al. [90] the breast cancer risk factors can be explained by the exposure of women to the ovarian hormones during their lifetime.

The breast cancer is the second most frequent type of cancer and is the leading cause of death within women with cancer diagnosis [132]. The Foundation for Medical Research [48] estimates the risk of developing breast cancer for french women as 1 in 8 with more than 47% of cases diagnosed on women under 65 years old. According to the French Public Health Agency [132] the incidence of breast cancer has increased by 138% between 1980 and 2005. In United Kingdom and United States by year 2000 the death rate from breast cancer was reduced by almost 20% and in 2005 was down by 25% [113]. This significant improvement was attributable to the rise in the life expectancy and the upgrowth of screening technologies.

1.2.1 Cancer classification

The breast cancer type is determined by the specific cells that are affected. When a woman is developing a breast cancer in the epithelial cells, this type of tumor is called carcinoma. The primary tumor can also start in cells from other tissues such as muscle, fat or connective tissues. These types of tumors are called sarcomas, phyllodes, Paget disease and angiosarcomas but they are less frequent [3].

The carcinomas are then classified based on their location and how far the cancerous cell have spread. When the cancerous cells remain within the milk ducts or lobules, the cancer is classified as a non-invasive cancer. Otherwise, the malignant cancerous cells break through normal breast tissue barriers and spread out through other body organs, and they are classified as invasive cancer [4]. The most common types of carcinomas characterized by their location are: ductal carcinoma and lobular carcinoma.

The invasive ductal carcinoma starts in the epithelial cells that line the milk ducts, whereas the invasive lobular carcinoma starts in the lobules. Both evolve through the surrounding tissues and may spread to the other organs through bloodstream and lymph nodes (metastasize).

Although the non-invasive carcinomas are not malignant, they have a 40% chance become invasive carcinomas over a 30-year period. The non-invasive ductal carcinomas start and stay inside the milk duct. The non-invasive lobular carcinomas overgrowth the normal breast cells and stay inside the lobule.

Invasive lobular carcinoma (ILC) may be harder to detect on physical exam as well as imaging, like mammograms, than invasive ductal carcinoma. Moreover, compared to other kinds of invasive carcinomas, about 1 in 5 women with ILC might have cancer in both breasts. Non-invasive ductal carcinoma is the more commonly detected form, making up 4% of symptomatic cancers and 20% of the cancer detected during a screening program. Its presence may be indicated on X-ray mammograms by microcalcifications ($\mu calc$) [3].

1.2.2 Breast cancer screening

Early detection remains the primary defense available to prevent the development of breast cancer. Early detection of breast cancer is made possible by regular screening tests aimed to find suspicious lesions before any symptom can develop. The principal benefit of the regular screening is the potential to prevent the premature and often prolonged, painful death of the individual. Studies have shown that regular mammographic screening resulted in a 63% reduction in breast carcinoma death among women who actually underwent screening [135]. In 2012, the review of the UK screening program [98] showed that, it prevented 1300 deaths from breast cancer every year.

Secondary benefits include a reduction in the trauma by treating earlier-stage lesions. Indeed, the earlier the invasive carcinoma detection, the better the response to treatment, which means that the patient may avoid having mastectomy or a chemotherapy.

Various countries have adopted organized breast cancer screening programs. Depending on the regional statistics and the estimated risk factors (age group, breast density, family history etc) the population is invited to participate to a free screening examination. In 1994, the French National Authority for Health approved a national screening program [47]. Since then, every woman between the ages of 50 and 74 years old, is invited every two years for a clinical exam and mammography.

The individuals who are suspected of having breast cancer, will have additional diagnostic tests as: diagnostic mammography, ultrasound (US), Magnetic Resonance Imaging (MRI), biopsy, blood test etc. The diagnostic test not only helps to confirm or to reject the screening suspicion, but also, in case of a positive test, to determine the stage and the type of the breast cancer.

1.3 Medical imaging

Medical imaging is a technology domain used in medicine to capture information on human body internal structures or internal tissues properties. This information is then processed and analyzed in order to diagnose, monitor, or treat medical conditions. This technology encompasses different imaging modalities and processes, each with their own advantages and disadvantages. Next, the most relevant modalities for breast imaging are presented .

1.3.1 X-ray mammography

X-ray mammography is a type of medical imaging that uses X-rays to capture images of the internal structures of the breast (FDA definition). In digital mammography (also known as Full Field Digital Mammography or FFDM) X-rays are beamed through the breast to an image receptor (Figure 1.8). A detector converts X-rays to digital information.

Mammography is used to detect parenchymal distortions, asymmetries, masses and clusters of microcalcifications within the breast. These findings are not pathogenic and require a tissue diagnosis to confirm the presence of an invasive cancer, a cancer in-situ,

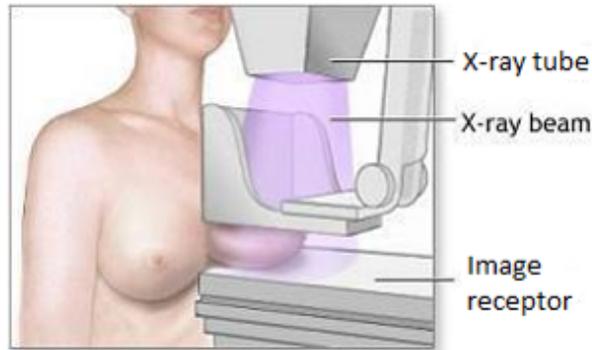


Figure 1.8: Mammography exam

or a non-malignant lesion. Microcalcifications are small calcium deposits embedded in a protein matrix. They present X-ray attenuation coefficients substantially higher than breast tissue and therefore appear as bright spots in the X-ray images. The diameter of a microcalcification is typically below 1 *mm* [69]. Breast microcalcifications present many shapes and sizes. They can be round, linear, coarse or granular. A mass is a radiological finding demonstrating an increased density versus the surrounding tissue. There is a large variation on mass size and shape. Usually a suspicious mass is larger than 8 *mm* and has irregular or spiculated margins [92]. Asymmetries and parenchymal distortions are visualised as tethering or indentation of breast tissue. They are the third most common mammographic appearance of nonpalpable breast cancer, representing nearly 6% of abnormalities detected in screening mammography [53].

A standard mammographic protocol always includes breast compression prior to image acquisition. The woman's breast is compressed between two plates until a nearly uniform breast thickness is obtained. Nowadays, the European Commission recommends a standardized breast compression force, i.e. the compression should stop at a level of force just below the subject's pain threshold or to the maximum setting of the machine (not to exceed 200 N). Analog mammography used screen/film detector technology in order to display breast internal structures, thus a uniform breast compression was needed in order to ensure a uniform exposure over the breast volume. With digital mammography, the exposure variation could be corrected with post-processing, while the breast compression is still indispensable to hold the breast away from the chest wall, to reduce the blur due to physical motion, to reduce the absorbed dose of ionizing photons, to separate overlapping structures or to reduce image degrading scatter [83].

Studies in different countries have assessed mammography sensitivity and specificity. The obtained sensitivity ranges between 81 and 88 %, and the specificity between 83 and 98 % [80, 71]. The mammography sensitivity is mostly affected in dense breasts. A dense breast is a breast for which the proportion of the fibroglandular tissues greatly exceed the proportion of fatty tissues. Fatty tissues are radiographically translucent, and lead to high intensity signal appearing on the mammographic images as dark areas. Meanwhile, the fibroglandular tissues and breast cancers tend to absorb more X-rays photons, therefore

they will appear as white areas. The lack of contrast between the cancer and dense regions of the background makes the detection more difficult.

1.3.2 Ultrasound

Breast ultrasound uses high-frequency sound waves to image breast tissues. The ultrasound technician puts gel on the skin above the area of interest and moves the sound-emitting probe over the skin. The emitted waves are reflected by the breast tissue interfaces. The probe picks up the reflected waves and transforms them into an image.

For asymptomatic women, a careful investigation of lateral and profound breast tissues is needed to identify the suspicious lesions. The limited field of view of the ultrasound image prevents from seeing abnormalities that lie deeper in the breast. Consequently, ultrasound imaging is not sufficient for regular screening but is used to complement other screening tests. However, it is widely used to investigate suspicious lesions found within mammography, clinical or self-examinations. Breast ultrasound is particularly effective in differentiating cysts from solid lesions. It has a low sensitivity for detecting microcalcifications which is the most common feature in addition to masses associated with breast cancer. Breast ultrasound can also be used for differential diagnosis, local staging and intervention guidance.

Ultrasound elastography is a sonographic imaging technique combining the ultrasound technology with the basic physical principles of elastography. Elastography assesses tissue deformability by providing information on the tissue elasticity. It consists of either an image of strain in response to force or an image of estimated elastic moduli.

Shear-wave elastography (SWE) uses focused pulses of ultrasound generated by the probe to induce soft tissues deformation. The tissue elasticity is assessed either by directly measuring soft tissue deformation or by measuring the speed of shear wave propagation. The combination of SWE with conventional ultrasound increases the diagnostic performance for breast lesions, compared with conventional ultrasound alone [149]. Elastography serves as a complementary tool to differentiate benign from malignant lesions by providing information about the lesion stiffness [75, 103].

1.3.3 Magnetic resonance imaging

Magnetic resonance imaging (MRI) is a noninvasive procedure used in breast imaging for studying internal structure of the breast that cannot be properly visualized using standard mammography (dense breasts). It employs radio-frequency waves and intense magnetic fields to excite hydrogen atoms. Body parts that contain hydrogen atoms (i.e. in water) are then imaged with contrasts depending on relaxation parameters characteristic of the tissues in the body. The quality of the image produced by MRI techniques depends, in part, on the strength of the received signal. For higher image quality, it is optimal to use an independent RF receiving coil placed in close proximity to the region of interest. For breast imaging, dedicated breast MRI coils can be used. The patient is usually placed in prone position with the breast inside the coil and both arms by the sides of the body.

When the cancerous tumor develops, new vascularization is created on the direct surrounding to supply the tumor with oxygen and nutrient. Thus, for breast cancer imaging, a contrast agent may be used to enhance highly vascularized regions. These regions, most of the time associated to lesions, are visualized due to their uptake of contrast agent. Contrast enhanced MRI is used as a screening modality for women with high risk of breast cancer.

Low specificity and high cost of MRI restricts its use in a routine screening [112]. However, it is increasingly used for high-risk groups and for lesions that are difficult to detect with mammography or ultrasounds tests.

1.4 Conclusion

Today, mammography is the primary imaging modality used in breast cancer screening and plays an important role in cancer diagnosis. Ultrasound and Magnetic Resonance Imaging are complementary imaging techniques mostly used for dense breasts and high-risk women.

In order to obtain an accurate reading, the mammography machine needs to compress the breasts. The discomfort and pain produced by breast compression might deter women from attending breast screening by mammography [8, 46]. Postponing a mammography exam can lead to delayed breast cancer diagnosis and worse prognosis (expected outcomes) for some women.

The main direct cause of pain in mammography is the flattening of the breast, which is directly linked to the applied compression force. Recent research indicates that with a reduced level of compression (10N vs 30N), 24% of women did not experience a difference in breast thickness. If breast thickness is not reduced when compression force is further applied, then discomfort increases with no benefit in image quality or average glandular dose. Therefore, a detailed study on alternative breast compression techniques considering the patient comfort in addition to the image quality and ionizing radiation dose is needed.

The aim of this work is to provide a simulation framework capable to assess the patient physical comfort, as well as the corresponding image quality and average glandular dose for breast compression with different paddle designs. The developed numerical methods would serve to build an improved compression paddle in terms of latter listed parameters, and therefore increase the adherence to breast cancer screening.

In this scope, a subject-specific biomechanical Finite Element (FE) model is developed and evaluated on real deformations measured on MR images. The proposed model is then used to compute the tissues deformation associated with breast compression during mammography. The resulting internal stress/strain intensities are then used as a first estimate of the patient comfort. The deformed breast geometry is the subject of an image simulation allowing to assess the image quality (IQ) and the average glandular dose (AGD), in order to validate the image quality for the different strategies of compression we are considering.

BIOMECHANICAL BREAST MODELING

State of the art

Finite elements models are widely used to estimate soft tissue deformations under pre-defined boundary conditions. Several biomechanical models of the breast were recently developed providing physics-based predictions of tissue motion and internal stress and strain intensity. A biomechanical model obtained from patient's MRI volumes can be subsequently used to mimic breast compression during mammography acquisitions.

This chapter provides theoretical background on continuum mechanics theory applied to soft tissue modeling. The principles of finite element theory are described including solid bodies and contact mechanics. A review of the existing biomechanical breast models is given, presenting the main challenges in the field and the proposed solutions. These developments provide the core foundation of our proposed patient specific breast model.

2.1 Continuum mechanics

Continuum mechanics is a branch of mechanics that deals with the analysis of the kinematics and the mechanical behavior of materials modeled as a continuous mass. Continuum mechanics is based on the following hypothesis: the matter is continuously distributed throughout the space occupied by the matter. Its formulation relies on how physical quantities, as for example pressure, temperature, and velocity, are measured macroscopically.

In this section the continuum mechanics theory applied to solid bodies is described using the books by Belytschko et al. [12] and Abeyaratne R. [1].

2.1.1 Deformation and strain

Continuum mechanics is the mathematical description of how physical objects respond to the application of forces.

A **body** is the mathematical abstraction of an **object** and is defined by its geometric and constitutive properties. At a macroscopic level, a solid object is described as a homogeneous and continuous body. Then, the substance of the object has a unique composition and completely fills the space it occupies, ignoring the granular (atomic) nature of matter. In continuum mechanics, a body \mathcal{B} is composed of **particles** p (or material points). Each particle is located at some defined **point** x in three dimensional space. All the points corresponding to the locations of all the particles, constitute the **domain** Ω occupied by the body in a given configuration, also named *geometry*. A particular body can change its configuration and therefore the occupied region in the space when exposed to some external stimulus, such as force, pressure or heat.

The **configuration** of a body is defined as a one-to-one mapping between the particle p and position x , $\Omega_0 = \chi_0(\mathcal{B})$ (see figure 2.1). To describe the solid's response to external stimuli, one needs to know the changes in geometrical characteristics between at least two configurations: the configuration Ω_1 that one wishes to analyze, and the **reference configuration** Ω_0 relative to which the changes are to be measured. Here, (Figure 2.1), the mappings χ_0 and χ_1 take $p \rightarrow X$ and $p \rightarrow x$, where X and x are the positions of particle p in the two configurations under consideration.

Frequently, the reference configuration is fixed for a given study and is arbitrarily chosen in a the most convenient way among all the configurations that the body can sustain.

The **deformation** of the body from the reference configuration Ω_0 is characterized by the next defined mapping Φ :

$$x = \Phi(X) = \chi_1(\chi_0^{-1}(X)), \quad \text{where } X \in \Omega_0 \text{ and } x \in \Omega_1. \quad (2.1)$$

The **displacement** u of a particle is the difference between its position in the analyzed configuration (or current configuration) and its position in the reference configuration

$$u(X) = \Phi(X) - X. \quad (2.2)$$

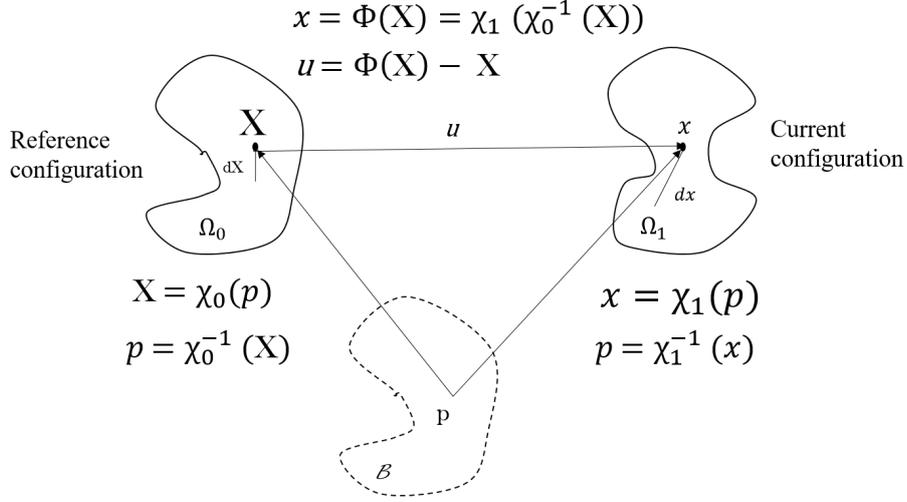


Figure 2.1: The position of a particle in the reference and current body configurations.

Suppose that $G(\Omega_1)$ is the value of some extensive physical property associated with the body \mathcal{B} in the current configuration (such as the body mass m). There exists a density $g(x)$ such that:

$$G(\Omega_1) = \int_{\Omega_1} g(x) dv \quad (2.3)$$

where dv is the volume of the material element. Thus, the property $G(\Omega_1)$ is related to the body, while the density $g(x)$ is related to the position of the body particle.

Eulerian and Lagrangian formulations

There are two classical techniques used to describe the body physical characteristics depending on the choice of independent variables. Some physical characteristics, such as the mass density, can be defined for each individual particle. In such a case, the body characteristics are defined by:

$$\forall p \in \mathcal{B}, m = \mathcal{M}(p). \quad (2.4)$$

Here the coordinate system remains consistent and moves with the particle. Therefore, the coordinates of both the particle and the attached variable do not change along the deformation. A particle is an abstract entity and cannot be used in numerical calculations. Therefore, it is described by its location in the reference configuration $p = \chi_0^{-1}(X)$

$$m = \mathcal{M}(p) = \mathcal{M}(\chi_0^{-1}(X)). \quad (2.5)$$

We call X Lagrangian or material coordinates, and its application is called Lagrangian or material description.

Instead of defining body characteristics as a function of body particles, one can define directly a body as a function of particle locations in current configuration by using the relation $x = \chi_1(p)$, and therefore

$$m = \tilde{\mathcal{M}}(x) = \mathcal{M}(\chi_1^{-1}(x)). \quad (2.6)$$

Here the coordinate system is fixed and the particle coordinates are changing. Therefore, the position of particles, and any related quantity, change during the deformation. We call x Eulerian or spatial coordinates, and its application is called Eulerian or spatial description.

These approaches are distinguished by three important aspects: the mesh description, the stress tensor and momentum equilibrium, and the strain measure. The advantages and drawbacks of these two formulations will be discussed later in this chapter. Further, only Lagrangian formulation is used to describe the continuous deformation of soft tissue.

Deformation gradient

In mathematical formulation the deformation gradient tensor F is the Jacobian matrix of the deformation $\Phi(X)$:

$$F = \frac{\partial \Phi(X)}{\partial X} = \frac{\partial x}{\partial X}. \quad (2.7)$$

Considering infinitesimal quantities, the deformation gradient relates the segment dX in the reference configuration to the corresponding deformed segment dx in the current configuration (Figure 2.1)

$$dx = F \cdot dX. \quad (2.8)$$

In addition to the mapping of such vectors, the deformation gradient tensor allows also the mapping of differential volumes as:

$$dv = \det(F)dV = JdV. \quad (2.9)$$

The Jacobian determinant J of the deformation gradient tensor F is a measure of the volume variation during the deformation. It can be used to relate extensive physical properties in the current and reference configurations:

$$\int_{\Omega_1} g(x)dv = \int_{\Omega_0} g(\Phi(X))JdV. \quad (2.10)$$

Local decomposition of the deformation gradient tensor into rotation and stretch

The deformation gradient tensor F completely characterizes the body deformation in the vicinity of a particle p . This deformation consists, locally, of a rigid body rotation and a body *stretch* (see Figure 2.2). As dX and dx are differential segments, the map F is not affected by rigid-body translations.

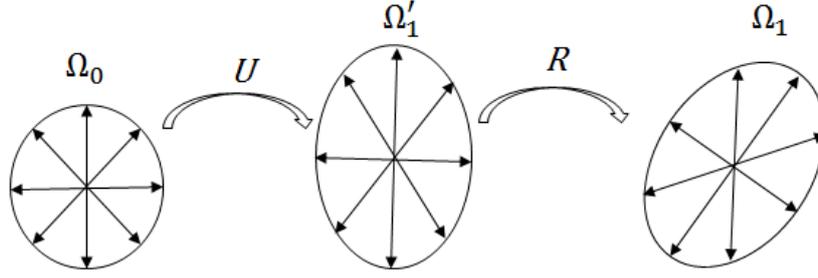


Figure 2.2: Local decomposition of the deformation tensor into stretch and rotation.

Generally, the body stretch is defined as the ratio of the deformed line elements to the length of the corresponding undeformed line element

$$l = \frac{|dx|}{|dX|}, \quad (2.11)$$

and consists locally on three mutually orthogonal stretches named **the principal stretches**.

According to the polar decomposition theorem, the deformation tensor can be written as the product of a proper orthogonal tensor R representing the rotational part, and a symmetric positive defined tensor U representing the body distortions

$$F = R \cdot U. \quad (2.12)$$

where U and R are given by the relations $U = (F^T \cdot F)^{\frac{1}{2}}$ and $R = F \cdot U^{-1}$. The essential property of tensor U is that it is symmetric and positive, therefore it has three real positive eigenvalues $\lambda_1, \lambda_2, \lambda_3$ and a corresponding triplet of orthonormal eigenvectors r_1, r_2, r_3 . Thus, when an infinitesimal segment dx is stretched by the tensor U , the segment is distorted in the principal directions of U by amounts of corresponding eigenvalues of U . The tensor U is also called the **right stretch tensor**. Since there is a one-to-one relation between U and U^2 , for the simplification of numerical calculus, the stretch tensor can be replaced by the **Green deformation tensor** $C = F^T \cdot F$.

There are three particular functions of C called the principal invariants

$$I_1(C) = trC, \quad I_2(C) = \frac{1}{2} [trC^2 - (trC)^2], \quad I_3(C) = det(C). \quad (2.13)$$

These functions are related to the three principal stretches by the following relations:

$$I_1(C) = \lambda_1^2 + \lambda_2^2 + \lambda_3^2, \quad I_2(C) = \lambda_1^2\lambda_2^2 + \lambda_2^2\lambda_3^2 + \lambda_3^2\lambda_1^2, \quad I_3(C) = \lambda_1^2\lambda_2^2\lambda_3^2. \quad (2.14)$$

The essential property of the principal invariants is that they do not change under coordinate transformations for a given body configuration. Their use to compute the body stretch is an essential part of constitutive modeling, because the behavior of a material should not depend on the coordinate system.

It also can be shown that:

$$det(C - \mu I) = -\mu^3 + I_1(C)\mu^2 - I_2(C)\mu + I_3(C). \quad (2.15)$$

Strain measures

Referring to small deformations, the engineering nominal strain is defined as the ratio of the change in length of the deformed line element to the length of the corresponding undeformed line element:

$$\epsilon = \frac{dx - dX}{dX}. \quad (2.16)$$

When the body is not deformed, the deformation gradient F and therefore the right stretch tensor U is equal to identity tensor I . The strain in such a case is equal to zero.

For most biological soft tissues, large deformation has to be considered. In that case, the previously defined strain is no more applicable. For large deformations, a measure of strain can be any monotonically increasing function related to stretch in a one-to-one manner, this function has to vanish in the reference configuration [93]. In an orthogonal coordinate system, considering that m is an integer, an admissible function is

$$f(x) = \frac{1}{m}(x^m - 1) \text{ for } (m \neq 0) \text{ and } \ln(x) \text{ for } (m = 0). \quad (2.17)$$

For $m = 0$, this function represents the Hencky strain tensor,

$$E = \ln(U), \quad (2.18)$$

for $m = 1$, this function represents the Biot strain tensor

$$E = U - I, \quad (2.19)$$

and for $m = 2$, this function represents the Green-Lagrangian strain tensor:

$$E = \frac{1}{2}(U^2 - I) = \frac{1}{2}(C - I). \quad (2.20)$$

The Green-Lagrangian tensor is commonly used in practice as, by using the relation 2.15, it can be computed without prior knowledge of the eigenvectors of the Green deformation tensor C .

2.1.2 Stress measures

Generally, forces are categorized as internal and external forces. An **external force** is a force caused by an external agent outside of the system. Contrariwise an **internal force** is a force exchanged by the particle in the system. The external forces are categorized in **body forces** (acting at the distance) and **contact forces** (acting on the body surface). The relation between body forces per unit undeformed volume $\tilde{b}(X)$ (Lagrangian coordinates) and body forces per unit deformed volume $b(x)$ is given by the following relation:

$$\tilde{b} = \frac{dv}{dV}b = Jb. \quad (2.21)$$

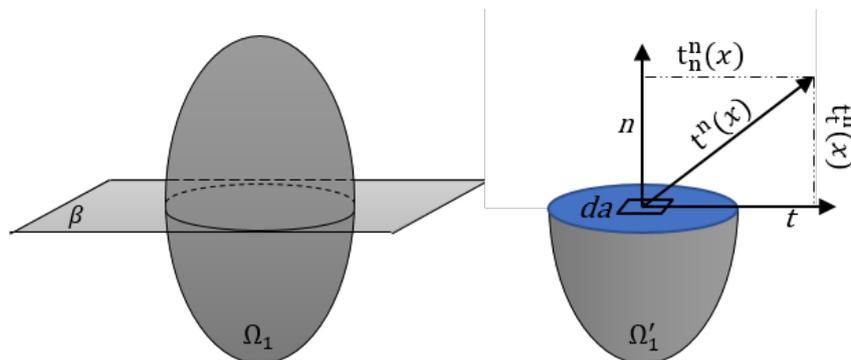


Figure 2.3: True stress vector $t^n(x)$ at point x on the fictitious surface created by the cutting plane β of normal \vec{n} passing through the point x .

The contact forces can act on the external surface of the body or on an imaginary internal surface enclosing a volume element (Figure 2.3). In general terms, the stress (or the **traction vector**) $t^n(x)$ is defined as contact force per unit area da in the limit as $da \rightarrow 0$. Therefore $t^n(x)$ varies from point to point in intensity and orientation depending on the $da(n)$ orientation. The stress vector projection on normal axis n defines the **normal stress vector** and its projection on the tangential axis defines the **shear stress vector**.

The stress on the boundary $\partial\Omega_1$ of the region occupied by the body is applied by external forces through physical contacts along the boundary. When formulating and solving a boundary-value problem, this stress defines the boundary conditions.

Cauchy's lemma

Cauchy's lemma states that traction vectors acting on opposite sides of a surface are equal and opposite

$$t^{-n}(x) = -t^n(x). \quad (2.22)$$

Cauchy's Law

Cauchy's law states that there exists a Cauchy stress tensor σ which maps linearly the normal to a surface to the stress vector acting on that surface, according to the next relation

$$t^n = \sigma \cdot n \quad \text{where} \quad t_i^n = \sigma_{ij}n_j. \quad (2.23)$$

When large deformations are considered, the reference and current configurations of the body are significantly different and a clear distinction has to be made between them. The traction vector t^n is defined in Eulerian coordinates (body current configuration) and is also called the **true stress**. Accordingly, the Cauchy stress tensor σ is called the true stress tensor.

The definition of any measure with respect to the deformed configuration is less practical as it is usually unknown a priori. For the simplification of mathematical formulation, a

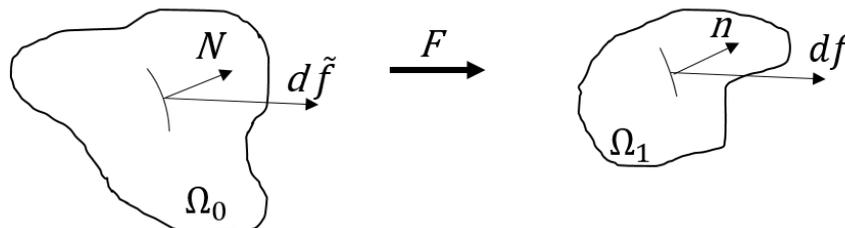


Figure 2.4: Deformation of area dA into area da . The force df acting on deformed area da and the pseudoforce $d\tilde{f}$ acting on undeformed area dA

new pseudostress is defined in the Lagrangian coordinate space named the **engineering stress**. The engineering stress has no physical meaning and has to be converted into true stress for any interpretation.

Below, two pseudostress vectors are defined (Figure 2.4):

- T^N defined as the contact force df per unit area dA in reference configuration.
- \tilde{T}^N defined as the contact pseudoforce $d\tilde{f}$ per unit area dA in reference configuration.

Accordingly, two pseudostress tensors are defined based on pseudostress vectors:

- $T^N = P \cdot N$, P is called **first Piola-Kirchhoff stress tensor**,
- $\tilde{T}^N = S \cdot N$, S is called **second Piola-Kirchhoff stress tensor**.

where N is the normal vector of unit area dA in the reference configuration.

The three stress tensors are linked by the next relation

$$\sigma = J^{-1}F \cdot P = J^{-1}F \cdot S \cdot F^T. \quad (2.24)$$

2.1.3 Conservation equations

Three conservation laws must be satisfied by physical system subject to any applied boundary conditions: **conservation of mass**, **conservation of linear momentum** and **conservation of angular momentum**. The resulting equations describe partially the mechanical behavior of a continuous body.

Conservation of mass

The mass m of a body with the density ρ , that infills the space region Ω_1 is given by :

$$m(\Omega) = \int_{\Omega} \rho(X) dV. \quad (2.25)$$

The mass conservation law requires that the body mass remains constant throughout all possible body configurations. In a Lagrangian formulation, this results in a relation between

the body density in the reference configuration ρ_1 and the body density in the current configuration ρ

$$\int_{\Omega_1} \rho_1 dv = \int_{\Omega_0} \rho_0 dV = \text{const.} \quad (2.26)$$

Using the relation 2.9 one can deduce that:

$$\int_{\Omega_0} (\rho_1 J - \rho_0) dV = 0 \quad \text{and} \quad \rho_1 J = \rho_0. \quad (2.27)$$

Conservation of the linear momentum

Let assume that the body \mathcal{B} is defined on a arbitrary region Ω_0 with a boundary Γ_0 , and is subject to a body-force $\rho_0 b$ and the surface traction T^N . And let X be the particle location in the undeformed solid. The total force acting on the body \mathcal{B} is then defined as:

$$f = \int_{\Omega_1} \rho_0 b(X) dV + \int_{\Gamma_0} T^N(X) dA. \quad (2.28)$$

The conservation of the linear momentum requires the total force acting on the body to be equal to the time rate change of the linear momentum. In a static problem, the time rate change of the linear momentum is neglected and thus an equilibrium equation is obtained by applying the divergence theorem to the surface integral.

$$\rho_0 b + \nabla_0 \cdot P = 0. \quad (2.29)$$

where the P is the first Piola-Kirchhoff stress tensor. The equilibrium equation can be formulated in terms of the second Piola-Kirchhoff stress tensor by using relations 2.24 .

Conservation of angular momentum

The conservation of the angular momentum requires that the resultant momentum on any part of the body about a fixed point \mathcal{O} equals the rate of increase in angular momentum (about \mathcal{O}). For a static problem, the integral form of the conservation of the angular momentum is defined as:

$$\int_{\Omega_0} X \times \rho_0 b(X) dV + \int_{\partial\Omega_0} X \times T^N(X) dA = 0. \quad (2.30)$$

The relation 2.30 requires that the second Piola-Kirchhoff stress tensor is a symmetric tensor:

$$S = S^T. \quad (2.31)$$

In summary, the conservation equations are fulfilled if and only if the following local conditions are fulfilled at each point in the body:

$$\rho_1 J = \rho_0, \quad \nabla_0 \cdot (S \cdot F^T) + \rho_0 b = 0, \quad S = S^T. \quad (2.32)$$

with the traction on the surface related to the stress through $\tilde{T}^n = S \cdot N$. For the simplification of mathematical calculus, the constitutive equations are formulated in terms of the second Piola-Kirchhoff stress tensor using the relations 2.24.

2.1.4 Constitutive models

The constitutive models, called also material models, define the relation between stress and strain of a physical system under the action of external stimuli. It is almost impossible to define a universal material behavior capable to model the material response to all possible conditions. Thus, for a given material, several constitutive models can be defined depending on the studied characteristics.

Biological materials are classified into:

- *Isotropic or anisotropic materials:* in a isotropic (anisotropic) material the values of a property are constant (vary) with respect to the direction.
- *Compressible or incompressible materials:* in a compressible (incompressible) material the volume changes (remains constant) during the deformation and the density remains constant. For an incompressible material the Jacobian determinant of the deformation tensor J is equal to 1.
- *Homogeneous or heterogeneous materials:* in a homogeneous (heterogeneous) material the values of a property are constant (vary) with respect to the position within the body.

Biological soft tissues are modeled using elastic materials model. The elasticity is the property of a solid material to return to its original size and shape when the influence of an external force is removed. In this case the strains are said to be reversible.

Considering small deformations, the stress-strain law of a linear material is given by the **Hooke's law**

$$\sigma = \lambda \epsilon, \quad (2.33)$$

where the coefficient of proportionality λ is named **Young's modulus**.

Elastic materials may be defined also with a non-linear stress-strain relationship. In such cases the elastic modulus (λ) is defined in function of strain ϵ

$$\lambda = \frac{\partial \sigma}{\partial \epsilon} = f(\epsilon). \quad (2.34)$$

For example, for an elastic exponential material [10] the elastic modulus is computed using the function

$$f(\epsilon) = b e^{m\epsilon}, \quad (2.35)$$

where b and m are material parameters.

For large deformations the stress-strain relationship is deduced from a potential function. A **hyperelastic** material is an elastic material for which the work is independent of the deformation path. The material reversibility and path-independent behavior implies the absence of energy dissipation during the deformation. Thus, it exists a **potential** function $W(E)$ such that

$$S = \frac{\partial W(E)}{\partial E} = 2 \frac{\partial \psi(C)}{\partial C}. \quad (2.36)$$

Moreover, if the material is isotropic, the stored strain energy W of a hyperelastic material can be written as a function of principal invariants (I_1, I_2, I_3) of the Green deformation tensor C previously defined in equation 2.13.

We introduce below the most used potential functions for the characterization of biological soft tissues.

For the simplification of potential expressions, we define the first and the second deviatoric strain (strain related to the deformation at constant volume) invariants:

$$\bar{I}_1 = \frac{I_1}{I_3^{2/3}}; \bar{I}_2 = \frac{I_2}{I_3^{4/3}}. \quad (2.37)$$

We also define the **Bulk modulus** K as measure of a material's resistance to compression, the **shear modulus** μ as the ratio of shear stress to the shear strain, and the **Poisson ratio** as the ratio between longitudinal strain to the transverse strain describing the body shape change. For small deformations the Bulk modulus and the shear modulus are linked to the Young's modulus and the Poisson ratio by the following relations:

$$K = \frac{\lambda}{3(1-2\nu)} \quad \text{and} \quad \mu = \frac{\lambda}{2(1+\nu)}. \quad (2.38)$$

Neo-Hookean potential function

The Neo-Hookean [137] law is an extension of the Hooke's law to large deformations. The potential function is based only on the first invariant and is given by

$$W = \frac{\mu}{2}(\bar{I}_1 - 3) + \frac{K}{2}(J - 1)^2, \quad (2.39)$$

where μ and K are the initial shear modulus and the initial Bulk modulus respectively.

Mooney-Rivlin potential function

The potential function of a Mooney-Rivlin [122] material can be defined as:

$$W = \frac{\mu_1}{2}(\bar{I}_1 - 3) + \frac{\mu_2}{2}(\bar{I}_2 - 3) + \frac{K}{2}(J - 2)^2, \quad (2.40)$$

where the constants μ_1 and μ_2 describe the material properties are linked to the initial shear modulus $\mu = (\mu_1 + \mu_2)$, and the constant K is the initial Bulk modulus.

Gent potential function

The potential function of a Gent [58] material model is defined as:

$$W = -\frac{\mu J_m}{2} \ln \left(1 - \frac{\bar{I}_1 - 3}{J_m} \right) + \frac{K}{2} \left(\frac{J^2 - 1}{2} - \ln J \right), \quad (2.41)$$

where the constants μ and K constants are the initial shear modulus and the initial Bulk modulus respectively. And J_m is a parameter limiting the value of $(\bar{I}_1 - 3)$.

Ogden model

The Ogden [101] material model is based on the three principal stretches $(\lambda_1, \lambda_2, \lambda_3)$ and $2N$ material constants, where N is the number of polynomials that constitute the potential function:

$$W = \sum_{i=1}^N \frac{\mu_i}{\alpha_i} (\lambda_1^{\alpha_i} + \lambda_2^{\alpha_i} + \lambda_3^{\alpha_i} - 3) + \sum_{k=1}^N \frac{K}{2} (J - 1)^{2k}, \quad (2.42)$$

where μ_i and α_i are material constants, and K is the Bulk modulus.

Yeoh model

The potential function of Yeoh [148] model is based on the first invariant:

$$W = \sum_{i=1}^N \mu_i (\bar{I}_1 - 3)^i + \sum_{k=1}^N \frac{K}{2} (J - 1)^{2k}, \quad (2.43)$$

where the μ_i are material constants and K is the Bulk modulus.

Governing equations of Lagrangian formulation

We consider a body \mathcal{B} which occupies in the reference configuration the domain Ω_0 with a boundary Γ_0 . The governing equations for the mechanical behavior of a continuous body are:

1. Conservation of mass $\rho_1 J = \rho_0$
2. Conservation of linear momentum $\nabla \cdot P + \rho b = 0$
3. Conservation of angular momentum $F \cdot P = P^T \cdot F^T$
4. Constitutive equations
5. Measure of strain $E = \frac{1}{2}(C - I)$
6. Boundary conditions: $e_i \cdot N \cdot P = e_i \cdot \bar{t}$ on $\Gamma_0^{t_i}$
7. Internal continuity condition: $\llbracket e_i \cdot N \cdot P \rrbracket = 0$ on Γ_0^{int}

where we note $\Gamma_0^{t_i}$ the set of prescribed tractions \bar{t} on the body boundary Γ_0 ; and Γ_0^{int} is the union of all surfaces where the stresses are discontinuous in the body (material interfaces).

The momentum equation together with the traction boundary conditions and the interior traction continuity condition are called the generalized momentum balance (GMB).

2.2 Finite Element Discretization

In continuum mechanics the body deformation is expressed in terms of partial differential equations (PDE). For the majority of problems, the PDE cannot be solved analytically, therefore approximation methods are developed. To this end, the finite element (FE) method has become the standard numerical calculation to compute such approximations. The computational domain, the unknown solution, and its partial derivatives are discretized, so as to obtain a set of algebraic equations for the function values at a finite number of discrete locations. The unknowns of the discrete problem are associated with a computational mesh which represents a subdivision of the domain Ω_0 into many small control volumes Ω_k

2.2.1 Eulerian and Lagrangian mesh description

The mesh description depends on the chosen independent variables (Eulerian or Lagrangian formulation). An Eulerian mesh formulation is usually used to solve problems linked to fluid like materials, and a Lagrangian mesh for solid like materials. In an Eulerian mesh, the Eulerian coordinates of nodes are fixed (coincident with spatial points) and the material points change in time (see Figure 2.5.b). In this case the mesh has to be large enough to contain the body in its current configuration. Throughout the deformation, the material points will belong to different elements. On the contrary, in a Lagrangian mesh, the Lagrangian coordinates of nodes are time invariant, nodal trajectory corresponds with material points trajectory and no material passes between elements (see Figure 2.5.a).

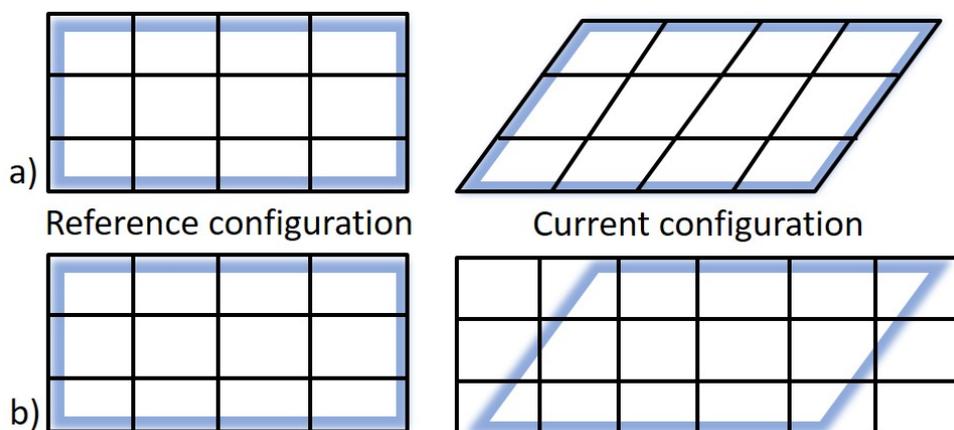


Figure 2.5: a) Lagrangian mesh formulation. b) Euler mesh formulation

In a Lagrangian mesh, the boundary and interface nodes remain coincident with body boundaries and material interfaces throughout the entire deformation. Thus, the boundary conditions are defined directly on the respective nodes. On the other hand, in an Eulerian mesh, the boundary and interface conditions have to be defined on points which are not nodes. This implies important complications in multi-dimensional problems.

An important drawback of a Lagrangian mesh affects mainly the large deformation domain. As the nodes are coincident with the material points, the elements deform with materials. Therefore, the magnitude of deformation is limited because of the element distortion. The limited distortion that most elements can sustain without performance degradation or failure is an important factor in nonlinear analysis with Lagrangian formulation.

2.2.2 Lagrangian mesh

The general approach of the FE method in Lagrangian formulation is illustrated in Figure 2.6. First, the momentum equations with given boundary conditions are multiplied by a set of appropriate test functions. The test functions have to satisfy all displacement boundary conditions and to be smooth enough so that all derivatives in momentum equations are well defined. Then, performing an integration by parts, the weak formulation of GMB is obtained, also called the principle of virtual work [12].

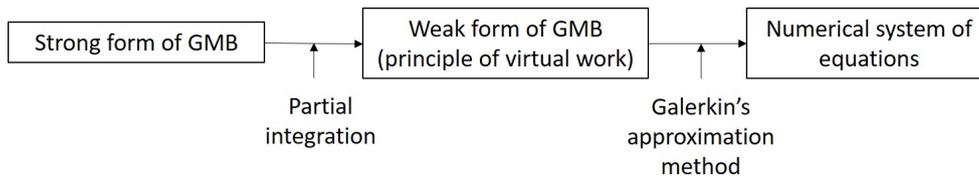


Figure 2.6: From strong formulation of the generalized momentum balance (GMB) to numerical equations.

The momentum equations and the traction boundary conditions, usually called the strong form, cannot be directly discretized by an FE method. The strong formulation of the GMB equations imposes the C_1 continuity conditions on the field variables. Therefore, the solution of this problem does not always exist. This is true especially in the case of complex domains with different material interfaces. In order to overcome these difficulties, weak formulations are preferred. The weak formulation of the GMB reduces the continuity requirements thereby allowing the use of easy-to-construct and implement polynomials. Due to reduced requirements in function smoothness, the weak forms never give an exact solution, but one can obtain a relatively accurate solution with the discretization refinement.

From the weak form of the GMB equations, the numerical system of equations is formulated by using finite element interpolants for the mechanical displacement and the test functions. The whole domain is discretized into a number of smaller areas or volumes which are called **finite element** (or elements) and their assembly is called a **mesh**. Finite elements can be of various shapes (as shown in Figure 2.7.b), quadrilateral or triangular in two dimensions, and tetrahedral or hexahedron in three-dimensions.

The mechanical displacement is approximated at the discretization points called finite element **nodes**. The nodes are at the vertices of the finite elements for a linear type,

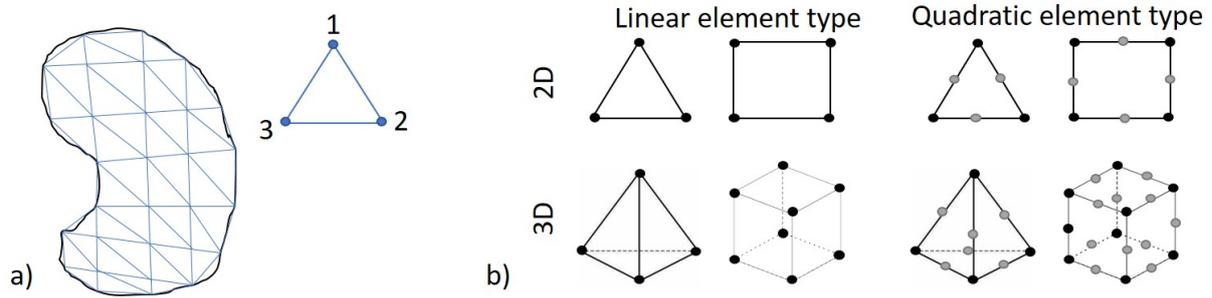


Figure 2.7: a) Discretization of a 2D domain with triangular finite element: Lagrangian mesh. b) Different types of finite elements

and at the vertices and mid-side of the finite element edges for a quadratic type (Figure 2.7.b). The displacement of each point within an element is interpolated from the values of the displacements of the nodes of the this element. In this way, the problem of finding the displacement of every point within the body is replaced by the problem of finding the displacements of a finite number of nodes.

As in a Lagrangian mesh the nodes are following the motions, for large deformations the finite elements can be highly distorted. A poor element's shape will often cause convergence problems in nonlinear analyses and can produce inaccurate results because of integration errors. Therefore, the shape regularity is generally checked all along the deformation process. Several shape parameters for each element type have been proposed, such as: aspect ratio, maximum corner angle, Jacobian ratio, skewness, parallel deviation, warping factor. The shape parameters measure the ability of an element to map data between element (numerical) space and real, physical space. The ideal element shape is one that has near 90 degree angles for quadrilaterals and hex elements, and near 60 degree corners for triangles and tetrahedral elements, while also having low elongation (aspect ratio). The element surfaces should also be relatively flat, as measured by the warping factor. In the following, only the shape parameters of the linear triangular elements are defined [6].

Triangle aspect ratio

The element's shape aspect ratio is computed using only the vertices, corner nodes, of the element (Figure 2.8). First, two lines are created: one through a node (K) and the midpoint of the opposite edge (K'), the second through the midpoint of the others two edges (J' and I'). Then two rectangles are created, with each rectangle having a pair of edges parallel to one of the previously defined lines. The rectangle edges have to pass through the nodes and the triangle's edge midpoints. This construction is repeated for each triangle's node resulting in 6 rectangles. The aspect ratio of a rectangle is defined as the ratio between the longer and shorter sides. Thus, the triangle's aspect ratio is defined as the maximal aspect ratio over the 6 rectangles multiplied by the squared root of 3. The scaling factor ensures that for an equilateral triangle the aspect ratio is equal to 1. Lets

consider an equilateral triangle with the edges length equal to a . The six corresponding rectangles are then equivalent with the longer side $L = a \sin(60)$ and the shorter side $l = a/2$. Therefore, the aspect ratio of an equilateral triangle is equal to

$$\text{aspect ratio} = \sqrt{3} \frac{L}{l} = \sqrt{3} \frac{a \sqrt{3} 2}{2 a} = 1 \quad (2.44)$$

The equilateral triangle has the best possible aspect ratio. An element with an aspect ratio larger than 20 is considered as a bad aspect element.

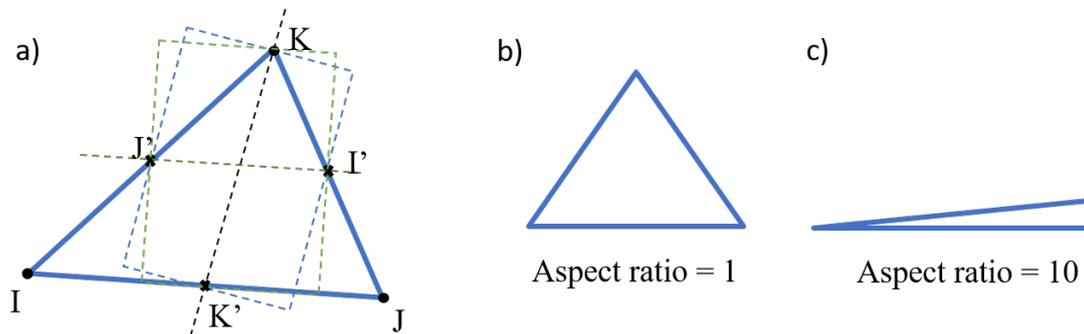


Figure 2.8: Computation of the aspect ratio for a triangle

Triangle maximum corner angle

The maximum corner angle is computed using nodes position in 3D space. The best possible maximum corner angle is 60° . An element having a maximal corner angle larger than 165° is considered as a bad shape element. Figure 2.9 shows a triangle with a good (60°) and bad (165°) quality.

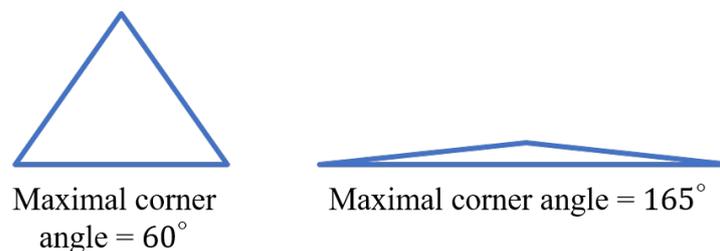


Figure 2.9: Example of triangles with different maximal corner angles.

The aspect ratio and the maximal corner deviation of a tetrahedra is computed using the definition of the same measure on a triangle. The element shape parameter is assigned as the worst value over the triangles defined by the tetrahedra's faces and cross-sections.

Skewness

The skewness of a triangular element is computed using the equivalent volume deviation method. It is defined as

$$skewness = \frac{\text{optimal volume} - \text{real volume}}{\text{optimal volume}}. \quad (2.45)$$

Where the real volume is the actual cell volume and the optimal volume is the volume of an equilateral cell with the same circum radius as the actual cell. According to its definition, the value of 0 indicates an ideal cell, from 0 to 0.75 the cell is considered to have a good quality, from 0.75 to 1 the cell is considered to have a bad quality and a value of 1 indicates a completely degenerated cell (Figure 2.10).

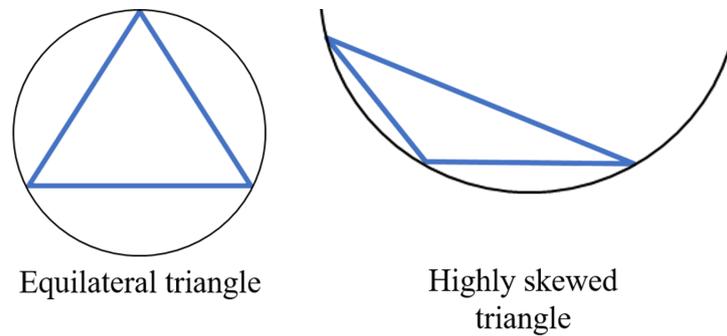


Figure 2.10: Example of triangles with different skewness with the corresponding circum radius.

To control the mesh quality, some FE softwares propose automatic element shape checking. The tool is aimed to warn the user if the mesh quality is too low. In such cases a detailed analysis of finite element solution is required. If the results are not accurate the mesh quality have to be improved. The mesh quality can be increased by reducing the mesh resolutions or using the adaptive mesh method. For large deformations, even a fine mesh with extremely good quality may be highly distorted during solution computation. To ensure the convergence an automatic re-meshing scheme may be used.

2.3 Contact mechanics

In order to transfer the loads between elements, the nodes have to be connected together. If two bodies are separated with no common nodes, no interaction will occur during the deformation and the bodies will pass through each other.

Let's consider two different bodies \mathcal{A} and \mathcal{B} and their occupied domains Ω_A and Ω_B with boundaries Γ_A and Γ_B respectively (see Figure 2.11). Also, we note Ω the domain of intersection of two bodies. The contact interface is the intersection of the surfaces of the two bodies:

$$\Gamma = \Gamma_A \cap \Gamma_B. \quad (2.46)$$

The intersection consists of two surfaces, usually distinguished as **target** and **contact** surfaces. For an asymmetric contact each surface has a single designation and the choice of the surface types is made following these next guidelines (the target surface properties are enumerated in their priority order):

- If the body \mathcal{A} is stiffer than the body \mathcal{B} , the surface Γ_A defines the target and Γ_B the contact surface.
- If Γ_A is a concave surface getting in contact with the convex surface Γ_B , the surface Γ_A defines the target and Γ_B the contact surface.
- If Γ_A is larger than Γ_B , the surface Γ_A denotes the target and the surface Γ_B the contact surface.

For the following, we identify Γ_A as the target surface and Γ_B as the contact surface (Figure 2.11).

Sometimes, the asymmetric contact does not provide satisfactory results and a symmetric contact is needed. When defining a symmetric contact, each surface coming in contact is designated to be both contact and target surface types. Therefore, two sets of contact pairs are defined. The symmetric contact may be used when the distinction between the contact and the target surfaces is not clear or to reduce the contact penetration. However, it usually results in a more time-consuming solution. In our model, an asymmetric surface-to-surface contact method is used to solve the multi-body interaction problems.

2.3.1 Contact interface equations

In the case of multi-body interaction, besides the standard mechanical governing equations, two additional contact conditions have to be fulfilled: the two bodies cannot interpenetrate, and the traction must satisfy momentum conservation on the contact interfaces.

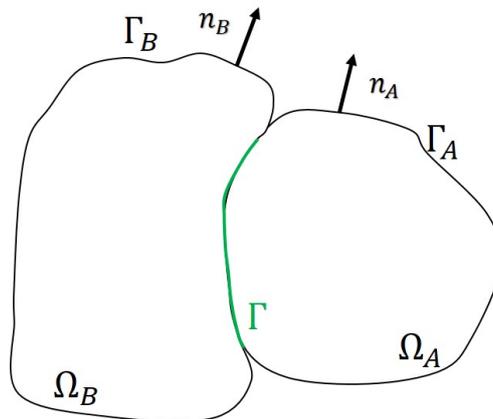


Figure 2.11: Multi-body contact problem.

Traction conditions

Traction conditions must follow the balance of momentum across the contact interface:

$$t_A + t_B = 0. \quad (2.47)$$

On the contact boundary surface Γ , the traction vector is decomposed into its normal and tangential components:

$$t_A^n = t_A \cdot n_A, \quad t_B^n = t_B \cdot n_B, \quad (2.48)$$

$$t_A^t = t_A - t_A^n n_A, \quad t_B^t = t_B - t_B^n n_B. \quad (2.49)$$

Therefore the momentum balance requires:

$$t_A^n + t_B^n = 0, \quad t_A^t + t_B^t = 0. \quad (2.50)$$

Inter-penetrability condition

The bodies implied in a multi-body problem must fulfill the inter-penetrability condition:

$$\Omega_A \cap \Omega_B = 0. \quad (2.51)$$

Decomposing the displacement u into its normal and tangential components, u^n and u^t respectively, the inter-penetrability condition can be written as:

$$t^n \leq 0, \quad u^n - gn_A \leq 0, \quad t^n(u^n - gn_A) = 0, \quad (2.52)$$

where g is the gap between the two bodies and n_A is the normal to the target surface.

2.3.2 Surface interaction models

When two solid bodies are placed together under a nonzero normal force and act one over the other with a tangential force, a **friction force** ($f_{friction}$) tangential to the interface and opposite to the applied force is created. Depending on whether the applied force can overcome or not the opposing friction force, the bodies may or may not move relative to each other. The body motion along the interface is called **sliding**. The **sliding force**, $f_{sliding}$ is the resulting tangential force which causes the sliding motion between the two bodies.

According to the allowed relative body motion in tangential or normal directions, five types of surface interaction models can be distinguished: bonded, rough, no-separation, frictional and frictionless. Table 2.1 resumes each corresponding mechanical behavior. If the body motion is not allowed in normal or tangential directions, once the bodies get in contact, the respective components of traction are equal ($t_A = t_B$). This means that, for a pure **bonded** contact, the two bodies are considered as a unique solid body.

Name	body motion in normal direction	body motion in tangential direction
Bonded	No	No
Rough	Yes	No, $f_{friction} \gg f_{sliding}$
No-separation	No	Yes, $f_{friction} = 0$
Frictionless	Yes	Yes, $f_{friction} = 0$
Frictional	Yes	Yes, if $f_{sliding} > f_{friction}$

Table 2.1: Surface interaction models and corresponding mechanical behaviors

The *frictional* contact behavior is defined using Coulomb friction law. For a continuous body, the Coulomb friction model is applied at each point of the contact interface. Considering that bodies \mathcal{A} and \mathcal{B} are in contact within the surface Γ , then for all $x \in \Gamma$:

$$\text{if } \|t^t(x)\| < -\mu_f t^n(x), \quad \Delta u^t = 0 \quad (2.53)$$

$$\text{if } \|t^t(x)\| = -\mu_f t^n(x), \quad \Delta u^t = -k(x)t^t(x), \quad k(x) > 0, \quad (2.54)$$

where μ_f is the material property named **friction coefficient**, Δu^t is the slip incremental in the tangential direction and $k(x)$ is a variable computed from the momentum equation. The equation (2.53) is known as the sticking condition: the tangential traction is lower than the critical value, thus no sliding occurs. Reciprocally, equation (2.54) is called the sliding condition.

When a frictionless contact model is used, $\mu_f = 0$, the tangential tractions vanish completely: $t_A^t = t_B^t = 0$. On the contrary, when a rough contact is modeled, the friction coefficient μ_f is equal to infinity, so that the sticking condition is always fulfilled.

In practice, several contact models can be combined to model a physical contact between two bodies.

2.3.3 Contact formulation algorithm: pure penalty model

Pinball region

Contact formulation presents two primary difficulties from a computational point of view. The first, is the unknown traction conditions for each considered frictional model. And second, the regions which will get in contact during the deformation process can not be predicted.

The region of contact depends on materials properties and imposed boundary conditions. Therefore, it is difficult to know a priori where the surfaces will be in contact. To formulate analytic equations, one has to know exactly the nodes involved in the contact process. Therefore, during body deformation, the program searches if the contact is *opened* or *closed*. The status is defined using a sliding pinball (Figure 2.12). The pinball slides over the contact surface nodes and searches for the target surface. If the node to surface distance is smaller than the pinball radius, the contact is considered to be closed (Figure

2.12, green nodes). Otherwise the contact is considered to be opened (Figure 2.12, gray nodes).
nodes).

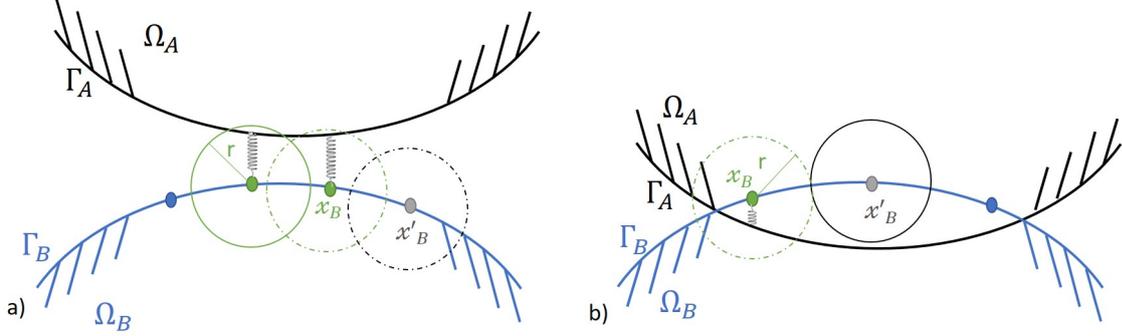


Figure 2.12: Contact status update using a pinball of radius r . Green nodes - updated nodes to closed contact status; gray nodes - updated nodes to open contact status; blue nodes - nodes which contact status need to be updated

Gap and penetration measures

Let's consider a point x_B belonging to the body surface Γ_B , and x_A the intersection point of the surface normal n_B with the surface Γ_A (Figure 2.13). The point to surface distance $d_1(x_B, \mathcal{A})$ is defined as:

$$d_1(x_B, \mathcal{A}) = \|x_B - x_A\| = \left[\sum_{i=1,2,3} (x_B^i - x_A^i)^2 \right]^{\frac{1}{2}}. \quad (2.55)$$

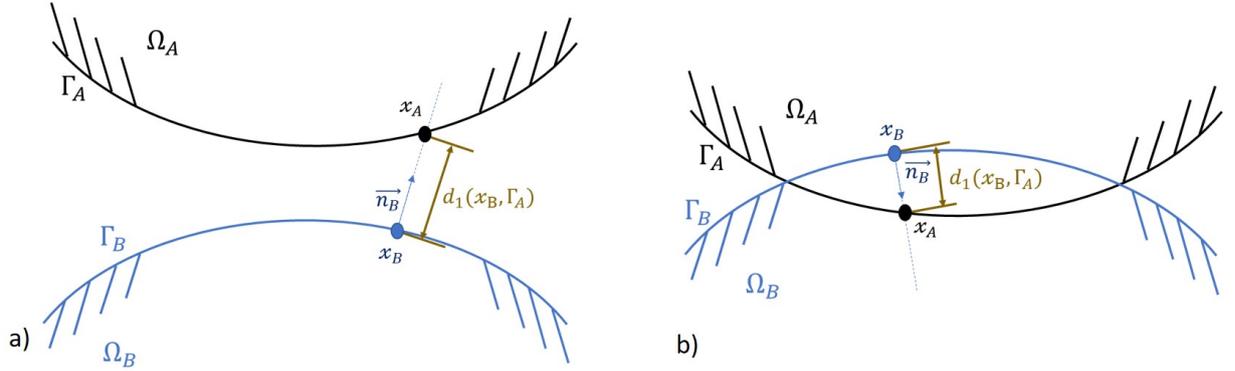


Figure 2.13: a) Body \mathcal{A} and body \mathcal{B} are close but not in contact. The $d_1(x_B, \mathcal{A})$ measure define the gap between the bodies at point x_B . b) Body \mathcal{B} have penetrated the body \mathcal{A} . The $d_1(x_B, \mathcal{A})$ measure gives the penetration at point x_B .

If the intersection point x_A is located inside the pinball area, the node to surface distance defines the amount of **gap** or **penetration** of the respective node (Figure 2.13).

Computing the gap or the penetration at single points increases numerical instabilities. Therefore, in this work, surface projection based contact method proposed by ANSYS was used. In Figure 2.14 the computation method of each projected area over the contact surface is explained. Figure 2.14.a represents the contact surface elements and Figure 2.14.b represents the target surface elements. If the two surfaces are overlapped, each unique area becomes a surface projected contact area (Figure 2.14.c). Therefore instead of calculating the penetration or the gap at each element node, the method computes an average value for each overlapping area.

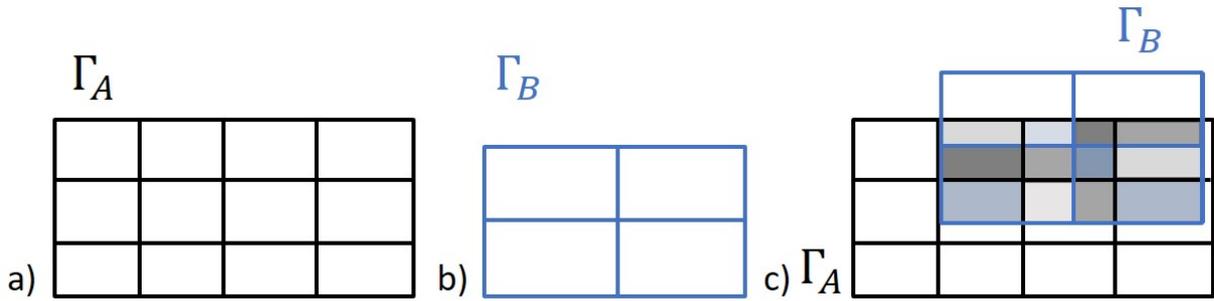


Figure 2.14: The contact surface projection over the target surface: a) Target surface elements; b) contact surface elements; c) surface projected contact areas.

This approach provides a more accurate calculation of contact traction and stresses for the underlying elements, however it is computationally more expensive. The interested reader is referred to ANSYS contact technology guide [5] for more details on the contact modeling.

Finite element mesh

For the finite element computation, contact and target surfaces have to be discretized with 2D linear or quadratic elements (Figure 2.7) consistent with the underlying 3D element mesh. The elements are named contact and target elements respectively. They have no material properties apart the friction coefficient μ_f . The stress-strain as well as the gap or penetration measures are computed for each mesh node of the discretized surface.

Pure Penalty method

In this manuscript, one of the most popular mathematical expression of contact compatibility conditions is used, namely the penalty method. With such a method, additional contact properties are defined to manage contact behavior: a normal stiffness factor, opening stiffness factor, and a tangential stiffness factor. Such factors play an important role in the numerical computation but have no physical meaning.

The penalty method uses a spring like relationship to introduce a force for all nodes pairs (contact-target) that are defined to be in closed contact (Figure 2.55). The contact

force is computed using the following expression:

$$f_c = k_c d, \quad (2.56)$$

where d represents the penetration or gap amount and k_c is the normal stiffness factor or the opening stiffness factor respectively. The tangential stiffness factor works in the same way enforcing the responding frictional force. Even if physical contacting bodies do not interpenetrate ($d = 0$), some finite amount of penetration, $d > 0$, is required mathematically to maintain equilibrium.

The magnitude of the stiffness contact factors is unknown beforehand which makes difficult a proper estimation of contact mechanics. The contact force at each node has to be large enough to push the contact surface back to the target surface and eliminate unwanted penetration or gap. At the same time, if the contact force is too large, it pushes the contact surface far away from the pinball region causing error and solution instabilities.

2.4 Breast biomechanical model: an overview

Biomechanical modeling of breast tissues has been widely investigated for various medical applications such as surgical procedure training, pre-operative planning, diagnosis and clinical biopsy, image guided surgery, image registration, and material parameter estimation (Table 2.3). For the last 20 years, several research groups have presented their breast models based on finite element theory. The complexity and relevance to breast anatomy of each model depend on the research purpose for which it was designed.

Several groups have proposed biomechanical breast models to register uncompressed volumetric breast data sets to compressed ones [26, 66, 117, 124, 133] or to compressed mammography projections [86, 79]. Within this framework, the authors modeled the breast deformation from prone to compressed prone position assuming linear elastic materials, zero residual stress and Dirichlet boundary conditions. However, compression-like breast deformation is too limited to characterize global breast mechanics.

Applications such as image guided surgery or preoperative planning imply a wider range of deformations. Therefore biomechanical breast models capable of estimating gravity induced deformation between different body position were proposed, for example from supine to prone positions (named also multi-loading gravity simulations) [51, 59, 43, 118, 119, 120]. Considering the involved large deformations, these models need to be accurate with respect to mechanical and anatomical breast properties. In this respect, a patient-specific model is needed considering more personalized boundary conditions, material models and a better representation of breast anatomy.

As described in Section 2.1, to build such a mechanical breast model, one needs to provide the breast geometry in a **reference configuration**, the **constitutive models** of tissues composing the breast volume and the **boundary conditions**. A proper definition of all these variables has a significant impact on model accuracy.

2.4.1 Breast reference configuration

A large number of existing patient specific models are using volumetric data from MR images [19, 79, 29, 41, 91] or CT images [105, 133] to design the breast geometry. During the acquisition of such images, the breast tissues are already under large deformations implying significant changes of breast geometries, for example if the patient is in a supine or in a prone position. Moreover, the deformed breast configurations include already the initial pre-stresses which are generally unknown and are extremely difficult to measure in clinical conditions.

To model the breast tissues deformation under gravity loading, the reference state is chosen to be the breast geometry in a stress-free configuration, i.e. without being deformed by any force, including gravity. The breast stress-free geometry is practically impossible to measure; therefore, several estimation methods have been proposed. The four most used methods are described below.

Inverse gravity

Palomar et al. [105] and Sturgeon et al. [133] used the inverse gravity method to estimate the stress-free geometry from the prone position measured using MRI modality. In their works, the authors just reversed the gravity effects without considering the initial stresses already included in the breast prone configuration. However, it has been proved that the inverse gravity method gives a poor approximation of the breast reference state and can be used only with small deformations or highly constrained models [42].

Breast neutral buoyancy configuration

Assuming that breast density is equal to water density, Rajagopal et al. [119] compute the breast stress-free configuration by imaging the breast immersed in water. Following the same physical assumptions, Kuhlmann et al. [85] proposed to estimate the stress-free configuration by applying a hydro-static distributed load on the breast surface collected in a prone configuration. Although the estimated geometries are relatively accurate, these methods are time-consuming and are difficult to transpose in a clinical framework.

Prediction-correction iterative algorithm

The prediction-correction iterative method was first proposed by Govindjee S. and Mihalic P.A. [60] and adapted later by Carter T. [19] and Eiben et al. [42]. The original method is based on the prediction-correction iterative scheme represented in Figure 2.15. The first approximation of the breast reference configuration is estimated by applying the inverse gravity method on the prone breast configuration (see above). Then, a numerical breast prone configuration is computed and compared to the corresponding measured one. The difference between the two prone geometries (the measured one and the simulated one) is used to update the reference breast configuration. The process is repeated until the convergence is achieved (i.e. when the difference is minimal). These methods were validated

using the breast shape in the neutral buoyancy configuration. The iterative algorithms have shown good accuracy, however they might fail to converge.

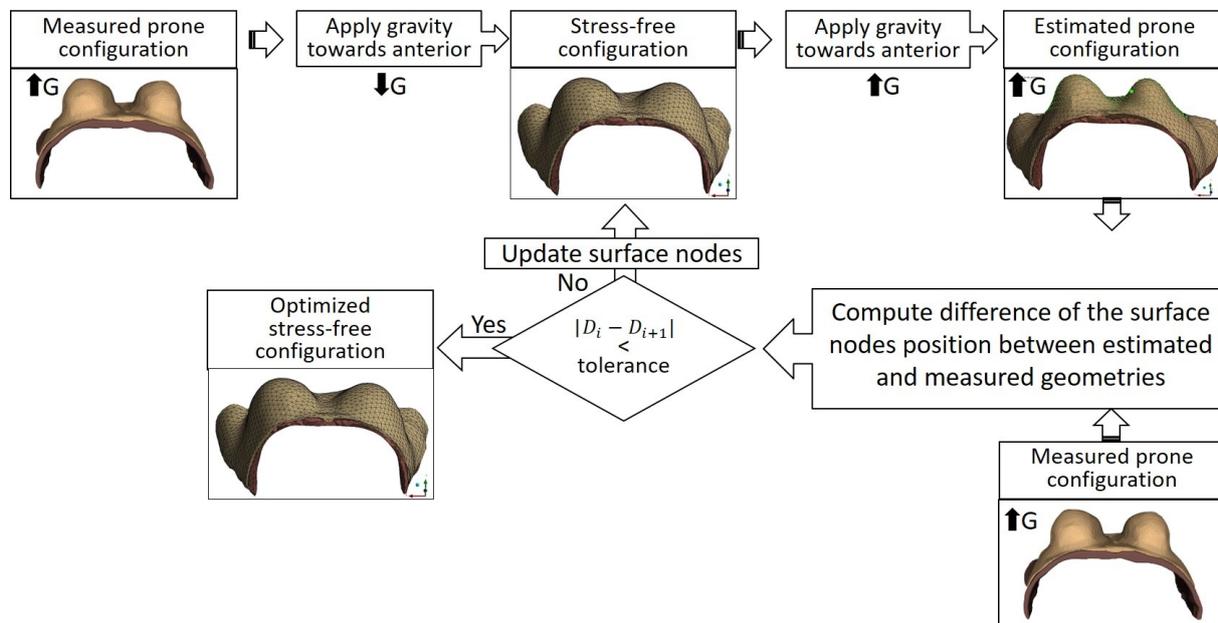


Figure 2.15: Prediction-correction algorithm

Inverse FE algorithm

Later an analytic computational method was developed to estimate the breast reference state by reparametrizing the equilibrium equation and by solving a finite element formulation of the inverse motion [108, 118, 141]. The method provides good estimates of breast reference configurations but needs important numerical resources.

The estimate of the breast reference configuration depends on the chosen material constitutive relations and the corresponding parameters. The prediction-correction iterative algorithm and the inverse FE algorithm are both assuming that the strain-stress relations are well known. However, mechanical properties of soft tissues are usually inaccurately estimated. The error associated with the solution sensitivity to the material stiffness may have a significant impact on estimated reference state[42]. In such cases, both algorithms are equally accurate, however the iterative scheme is computationally slower than the direct one[42].

2.4.2 Constitutive models

Global breast mechanics is governed by breast internal consistency and tissues' individual mechanical properties. The breast soft tissue is known to be incompressible, nonlinear,

anisotropic, and viscous materials. However, when simulating the breast deformation under gravity loading the breast tissues viscosity can be neglected [142].

Under large compressions, the breast volume can vary due to fluids (blood and lymph) flows. Thus, soft tissues are not considered as totally compressible materials, and are frequently modeled as quasi-incompressible with a value of the Poisson ratio ν ranging between 0.45 and 0.5. The influence of the Poisson ratio within linear constitutive models was studied by Tanner and colleagues [136]; according to the authors, the best breast geometry estimates are obtained with high Poisson ratio ($\nu = 0.495 - 0.499$). The breast tissues being predominately composed of water, the density is considered to be equal to 981 kg/m^3 .

For the last decades, several constitutive models were used to model the breast tissues response to an external force: exponential elastic [10], Neo-Hookean hyper-elastic [19, 120, 133, 40, 65, 52] and Mooney-Rivlin models [127, 136, 18, 91]. The most used models are analyzed in the following section.

Glandular and adipose tissues biomechanical properties

Multiple studies have shown that breast composition, and therefore its mechanical behavior, undergo substantial changes during woman lifetime (section 1.1.4). The first studies on mechanical properties estimation of breast tissues were done for diagnosis purposes. When the breast is developing benign or malignant disorders, its mechanical properties differ from the ones of the normal breast tissues [84].

Several research groups (Table 2.2) have studied the elastic modulus of adipose and glandular tissues. The breast tissue Young's modulus ranges between 0.1 kPa and 271.8 kPa . Such huge variation may be explained by the differences in the experimental setups used to estimate tissues stiffness, but also by the participant's physical condition, age or period in the menstrual cycle. For example, Han et al. [66], though using the same FE method, found significantly inter-individual variability, with the shear modulus ranging between 0.22 kPa and 43.64 kPa . Lorenzen J. and team [89], showed that during the menstrual cycle, due to the hormonal changes, the elastic properties of the glandular tissues can change by about 30%.

An important difference in estimated values of breast elastic modulus is observed between the linear elastic and hyperelastic models. Considering only in-vivo studies with Neo-Hookean material models, the adipose and glandular shear modulus values are lower than 50 kPa .

Carter T. [19] compared a one parameter Neo-Hookean potential function with a five-parameter Mooney-Rivlin potential function for various constitutive parameters. The multi-loading gravity simulations were thus performed on 3 subjects. According to the authors, even with parameters 10 times softer than described in the literature [125], the Mooney-Rivlin model underestimates the tissues deformation by at least 75% (prone to supine loading simulation). The best estimates were given by the Neo-Hookean model with the initial shear modulus equal to 0.2 kPa .

Similarly, differences between estimated mechanical properties using FE method are

Ex-vivo estimation				
Author	Method	Material model	material properties	
			Adipose <i>kPa</i>	Glandular <i>kPa</i>
Krouskop et al. [84]	Indentation-5% .	Linear elastic	$\lambda = 19 \pm 7 \text{ kPa}$	$\lambda = 33 \pm 11 \text{ kPa}$
Krouskop et al. [84]	Indentation-20%	Linear elastic	$\lambda = 20 \pm 6 \text{ kPa}$	$\lambda = 57 \pm 19 \text{ kPa}$
Wellman et al. [142]	Indentation - 5%	Linear elastic	$\lambda = 6.6 \text{ kPa}$	$\lambda = 33 \text{ kPa}$
Wellman et al. [142]	Indentation - 15%	Linear elastic	$\lambda = 17.4 \text{ kPa}$	$\lambda = 271.8 \text{ kPa}$
Azar et al. [10]	Indentation	Exp. elastic	$b = 4.46 \text{ kPa};$ $m = 7.4$	$b = 15.1 \text{ kPa};$ $m = 10$
Samani et al. [126]	Indentation	Linear elastic	$\lambda = 3.25 \pm 0.91 \text{ kPa}$	$\lambda = 3.24 \pm 0.61 \text{ kPa}$
In-vivo estimation				
Van Houten et al. [139]	MRE	Linear elastic	$\lambda = 17 - 26 \text{ kPa}$	$\lambda = 26 - 30 \text{ kPa}$
Sinkus et al. [130]	MRE	Visco-elastic	$\mu = 2.9 \pm 0.3 \text{ kPa}$	
Rajagopal et al. [119]	MRI-FEM	Neo-Hookean	$\mu = 0.16 \text{ kPa}$	$\mu = 0.26 \text{ kPa}$
Carter [17]	MRI-FEM	Neo-Hookean	$\mu = 0.25 \text{ kPa}$	$\mu = 0.4 \text{ kPa}$
Han et al. [66]	MRI-FEM	Neo-Hookean	$\lambda = 1 \text{ kPa}$	$\lambda = 0.22 - 43.64 \text{ kPa}$
Gamage et al.[51]	MRI-FEM	Neo-Hookean	$\mu = 0.1 \text{ kPa}$	
Griesenauer et al [61]	MRI-FEM	Hooks law	$\lambda = 0.25 \text{ kPa}$	$\lambda = 2 \text{ kPa}$

Table 2.2: Material properties for adipose and glandular tissues.

due to the variability of modeling techniques. Inappropriate or incomplete assumptions on breast mechanics can substantially affect the estimated parameters. Overconstrained kinematic boundary conditions may involve very soft material properties. On the other hand, allowing too much sliding of the breast over the chest wall can lead to extremely stiff material properties.

Previously listed researches clearly showed the variability of elastic modulus of the same tissue between and within individuals. Eder M. [39] made a larger analysis including all material models proposed in the literature. According to authors, many of them are too stiff, permitting not enough deformation within the gravity loading. This study has shown

that the most reliable values of the elastic modulus are the ones given by Rajagopal and colleagues [119] (Table 2.2).

Muscle biomechanical properties.

Muscle is a kinematically, geometrically, and materially complex tissue. The muscle mechanical behavior depends on its contractile active and passive elastic properties [99]. In biomechanics the muscle is modeled using complex models such as Hill-type models [151] or Feldman's lambda model [45] which are considering the variation of muscle elasticity as function of the muscle state. For breast biomechanical modeling, the muscle is combined with the thoracic cage and is frequently considered as a rigid breast support. In most of cases, the pectoral muscle is modeled by imposing zero-displacement conditions on nodes closer to the chest wall or by allowing them to slide along the chest wall line (see Section 2.4.3).

The muscle is a nonlinear, anisotropic, incompressible material. The bibliographic data on static mechanical properties of the muscle-tendon unit assessed by supersonic shear wave imaging elastography states a Young's modulus ranging between $20kPa$ and $300kPa$ depending on the muscle location and subject's physical condition [88]. The muscle shear modulus on the upper trapezius was studied by Leong et al [87]. According to the authors, the muscle shear elasticity at rest was $17.11 \pm 5.82kPa$, and it increased to $26.56 \pm 12.32kPa$ during active arm holding at 30° abduction.

Skin biomechanical properties

Several studies have shown the importance of considering the skin in biomechanical breast modeling. According to Carter T. [19], a model which includes the skin better estimates the tissues deformations under gravity loading.

Sutradhar A. and Miller M.J. [134] published a complete study about breast skin, estimating its elasticity for 16 different breast regions. The study was done on 23 female volunteers aged from 29 to 75 years old. The authors found that the skin elastic modulus ranges between 15 and $480kPa$ with an average of $334 \pm 88kPa$. The elastic modulus in the lateral region has the highest value (mean $370kPa$), followed by the superior region (mean $355kPa$). The inferior region (mean $331kPa$) follows next, with the medial region having the lowest value (mean $316kPa$). Significant variation of the elastic modulus in radial direction was found.

The skin was proved to have a highly nonlinear and anisotropic behavior due to collagen fibers (see Section 1.1.3). Therefore, linear material models are not appropriate for skin mechanics modeling. Other researches on skin elasticity are available, but they are not specific to the breast skin. Hendriks and colleagues [68] estimated in-vivo skin properties by suction testing. The skin was considered as a homogeneous, isotropic, incompressible, hyperelastic material. The study was performed on 14 subjects, and the average value of the elastic modulus for skin was $58.4kPa$.

The estimation of the breast skin elasticity by the means of finite elements using Neo-Hookean potential function has resulted in softer materials model. Carter T.[17] found an initial shear modulus equal to $16kPa$, whereas Han et al [65] found that for the five studied subjects, the skin shear modulus ranged between $2.47kPa$ and $5.78kPa$.

Fascias and ligaments biomechanical properties

The surrounding breast fascias and the suspensory ligament form the breast support matrix. These structures are well described for surgical purposes (thickness, location etc), however little is known about their mechanical properties. The first biomechanical breast model taking into account the effect of Cooper's ligaments was proposed by Azar and colleagues [10] and took up later by Pathmanathan et al [108] and Han et al [66]. The authors designed a new material model for fatty tissues including the anisotropic behavior of breast ligaments. Later, Georgii and colleagues [59] came up with a spring-mass generic model for the breast support matrix. According to the authors, including the ligaments into the finite elements breast model improved the solution stability of the prone-supine simulation with respect to the input parameters.

To our knowledge, there is no experimental data, available in the literature, describing the mechanical properties of breast superficial fascia. An approximation of the elastic modulus of Cooper's ligaments is provided by Gefen A. [56] by extrapolating known ligamentous structure in the human body. The authors estimated the elastic modulus of suspensory ligaments ranging between 80 and $400MPa$.

Fibrous tissues get their elasticity from elastin fibers and their structural support from collagen fibers. As reported by Riggio et al [121], the superficial fascia is made up of both collagen and elastin fibers. In contrast, the Cooper's ligaments appeared to be composed almost of collagen fibers. The mechanical properties of a single collagen fiber from a rat tail were studied by Wenger et al. [143]; according to the authors the corresponding elastic modulus ranges between $5 GPa$ and $11 GPa$. Other studies on biomechanical characterization of human body superficial fascia from various regions are available in the literature. The most frequently studied structures are the plantar fascia and foot ligaments, with a Young's modulus ranging between $0.1kPa$ [55] and $700MPa$ [24].

2.4.3 Boundary conditions

Breast deformations can be modeled by solving the motion equations using two different types of boundary conditions, regarding either displacements (Dirichlet conditions) or forces (Neumann conditions).

Dirichlet conditions are usually used to constrain the sternum/axilla ends and the posterior surface of the breast or the thoracic cage if the muscular tissues are considered [61, 119, 108, 51, 61]. As reported by Carter T. [19] the zero-displacement boundary conditions in a multi-gravity loading framework result in an over-constrained model. In that case, sliding conditions over the chest wall have to be considered.

Later, several teams using biomechanical breast models for multi-modality image registration or surgical planing showed that including the sliding boundary conditions [59, 65, 86] improves the registration accuracy. However, for most studies in which a biomechanical model is designed for breast compression, tissues sliding over the chest wall is neglected and fixed boundary conditions are usually assumed [133, 91].

2.4.4 Summary

During the last decades, several breast biomechanical models were proposed (see Table 2.3). However, only a small number of them [118, 19, 51, 65] were evaluated with respect to real tissue deformations. As we intend to build-up a subject-specific breast biomechanical model capable of estimating multi-loading gravity deformations, we will only consider as relevant the biomechanical models that were evaluated and compared with real data. In this chapter, three main challenges were identified: the estimation of the breast reference geometry, the estimation of subject-specific material properties and the definition of the boundary conditions at the breast-muscle interface. State of the art of breast biomechanical models were published by: Eiben et al [43], Han et al. [65], Gamage et al. [51].

Gamage and colleagues [51] proposed a finite element model capable to estimate the supine breast configuration from the prone one. The breast stress-free configuration was estimated using an inverse FE algorithm. The optimization process was performed by using as ground-truth the skin surfaces on prone configuration. Contrariwise, the material constitutive parameters were identified using the skin surface on supine breast configuration. Breast tissues sliding over the chest wall were considered partially by modeling the pectoral muscle as a soft structure and including it into the optimization process. The model accuracy was assessed for the supine breast configuration only. The root-mean-squared error (RMSE) was computed from the point to surface distances between the estimated and measured data. According to the authors, the breast supine geometry was estimated within an RMSE of 5mm (maximal distance of 9.3 mm).

Later on, Han et al. [65] developed a breast biomechanical model for image registration. The estimates of supine breast configuration were computed for five subjects, and the accuracy was assessed by computing the Euclidian distance between anatomical landmarks. The mean Euclidian distance ranged between 11.5 mm and 39.2 mm (maximal Euclidian distance ranged between 20.3 mm and 61.7 mm). The authors modeled the elongation of the pectoral muscle using a contact sliding model. The material constitutive parameters were adapted to the patient's breast mechanics, the stress-free breast geometry was estimated by inverse gravity.

Finally, Eiben et al [43] proposed a new model to estimate the up-standing breast configuration from the prone one. The model was evaluated on 3 subjects. The patient specific stress-free geometry was computed using an inverse finite elements u-p formulation. The material parameters were optimized such that the best fit in supine configuration was obtained. The model accuracy was measured in terms of the mean Eulerian Distance between manually selected internal landmarks. The supine breast configuration was estimated with the mean error ranging between 12.2mm and 19.8mm. The model evaluation for the up-

standing configuration was not presented.

In the next chapter, a new biomechanical model of the breast will be described. The proposed model considers the subject-specific breast geometry and elastic properties as proposed in previous models. However, breast tissues sliding over the chest wall is modeled by including new anatomical structures such as superficial fascia and suspensory ligaments. Finally, the model was evaluated by comparison with real data collected from MR images.

Authors	Application	FE mesh	Material models	Boundary conditions	Stress-free config.
Azar et al. [10]	Computer assisted breast surgery	8-Node hexahedrons (trilinear isotropic elements)	Skin-elastic adipose, glandular-hyperelastic polynomial	Sliding between breast - thorax and breast-paddle	Prone breast geometry
Rajagopal et al. [118]	Breast compression	8-Node hexahedrons (tricubic Hermite elements)	Homogeneous, Neo-Hookean model	Zero-displacement BC	Buoyant breast in water
Pathmanathan et al. [108]	Image registration	8-Node hexahedrons (trilinear elements)	Homogeneous breast-polynomial hyperelastic; Skin exponential hyperelastic	Zero-displacement on muscle; Compression with imposed displacement	Inverse FE algorithm
Han et al. [65]	Image registration	4-Node tetrahedrons	Muscle, glandular, fatty, skin - Neo-Hookean model	Sliding on pectoral muscle	Inverse gravity
Gamage et al. [51]	Computer assisted breast surgery	8-Node hexahedrons (tricubic Hermite elements)	Homogeneous + muscle-Neo-Hookean incompressible model	Zero-displacement BC on rib cage surface, Sternum, axilla ends, shoulder	PC iterative algorithm
Patete et al. [107]	Computer assisted breast surgery	4-Node tetrahedrons (trilinear isotropic elements)	Adipose, glandular, skin	Zero-displacement BC on the chest wall	PC iterative algorithm
Kuhlmann et al. [85]	image registration	4-Node tetrahedrons	Adipose, glandular-linear gel-like (Eulerian formulation); Skin - hyperelastic material (Lagrangian formulation)	Zero-displacement chest wall	PC iterative algorithm
Georgii et al. [59]	Surgery simulation	8-Node hexahedrons, 2-node 3D spars	homogeneous elastic material, Cooper's ligaments-generic mass-spring model	sliding BC (breast on the pectoral muscle)	NA
Eiben et al. [43]	Surgery outcome prediction	4-Node tetrahedrons	Fatty, glandular-Neo-Hookean model; skin-exponential hyperelastic	Zero-displacement BC	Inverse FE algorithm
Garcia et al. [52]	3D breast lesion localization	4-Node tetrahedrons	adipose, glandular - Neo-Hookean models	zero-displacement BC	Prone breast configuration

Table 2.3: Breast biomechanical models

A NEW BIOMECHANICAL BREAST MODEL EVALUATED ON REAL DATA

The state of the art in breast finite element modeling was presented in the previous chapter. Three models were identified representing the cutting-edge technologies in the field. The authors used prone MRI to estimate the breast reference geometry. The subject-specific constitutive parameters were chosen such as the best fit between the supine configuration estimate and the corresponding measured breast geometry was obtained. The models were evaluated using the measured and the estimated positions of superficial fiducial landmarks or internal anatomical landmarks in the supine breast configuration. As the optimization and evaluation processes were based on the same data, the model limitations must have been underestimated. For a better assessment of the accuracy of a breast biomechanical model, we think that the evaluation on a third breast configuration is required.

This chapter introduces a new biomechanical model developed by combining the best practices and concepts proved by previous works. To be as realistic as possible, our model considers breast heterogeneity, sliding boundary conditions, initial pre-stresses and personalized hyper-elastic properties of breast tissue. In addition, new types of soft tissue are included representing the breast support matrix. Moreover, our model was built using prone and supine breast configurations and was evaluated in supine tilted configuration ($\sim 45^\circ$) of the same volunteer.

In the first part of this chapter, the acquisition protocol of our data is described. Details on numerical methods and software used to extract the subject-specific breast geometry are provided. Next, the different components of the finite element mesh are presented and the mesh quality is assessed using shape parameters. Then, the assumptions on boundary conditions and materials models are explained. Finally, the model optimization process is detailed and results on subject-specific parameters and breast reference configuration are presented.

3.1 Geometry extraction

Geometry extraction is the first step in FE analysis, and it consists of obtaining the 3D surfaces of the breast. We use MR images to obtain the subject-specific breast volumes and the surrounding soft tissues distribution. Prior to surface extraction, the MRI volume is segmented and mapped to a single reference coordinate system. The next section describes the image acquisition protocol and the numerical method used to generate the 3D subject-specific breast geometry.

3.1.1 Data acquisition

The images were acquired using a Siemens 3T scanner with T2 weighted image sequences. The in-plane image resolution was 0.9×0.9 mm, and the slice thickness was 0.96 mm. During the acquisition, the contact between the breasts and the relatively narrow MRI scanner tunnel, or with the patient body (arms or thorax), was minimized. Three different positioning configurations were considered: prone, supine and supine titled ($\sim 45^\circ$). These positions were chosen to assess the largest possible deformations

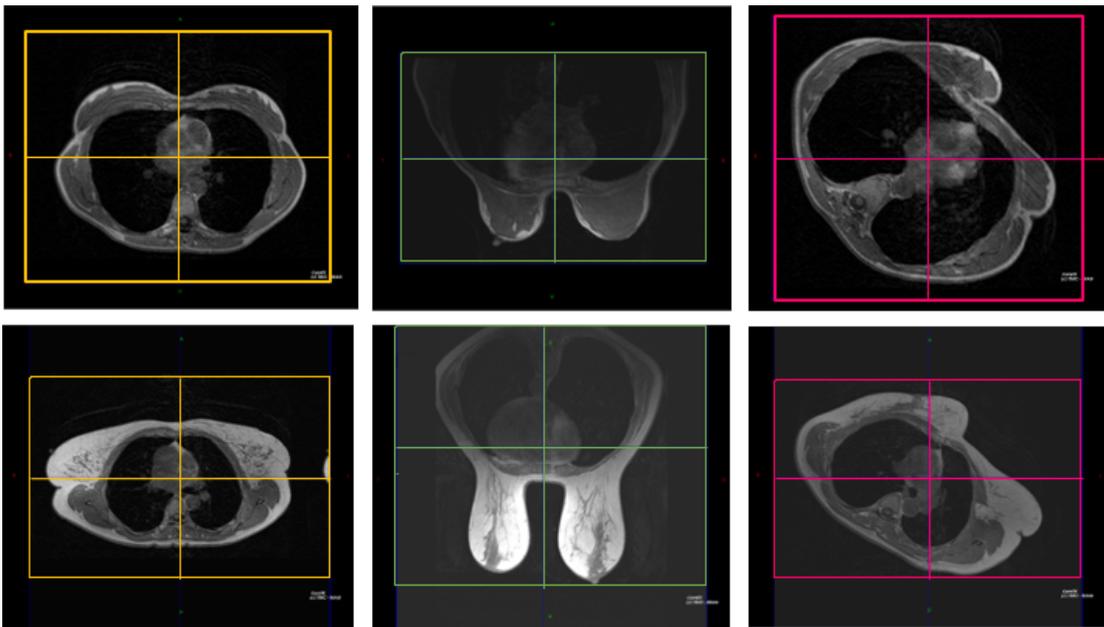


Figure 3.1: MR images in three breast configurations: first line - volunteer 1, second line - volunteer 2; first column - supine configuration, second column - prone configuration, third column - supine tilted configuration.

Two volunteers agreed to participate in a pilot study approved by an ethical committee (MammoBio MAP-VS pilot study). The volunteers are 59 and 58 years old and have A-cup (volunteer 1) and F-cup (volunteer 2) breast size respectively.

Both volunteers were also asked to provide the compression force and breast thickness as measured during their most recent mammography. Such data are summarized in Table 3.1.

	Subject 1		Subject 2	
	Right breast	Left breast	Right breast	Left breast
Force (N)	21.9	40.9	94.8	56.6
Breast thickness (mm)	47	42	50	49

Table 3.1: Compression force and breast thickness in both subjects for a cranio-caudal mammogram

The biomechanical breast model that we propose was developed and evaluated using the MRI volumes of the first volunteer only. However, simulations of the breast deformation under compression, detailed later in this manuscript, were performed for the both breast volumes.

3.1.2 Image segmentation

A semi-automated active contour method proposed in ITK-Snap software was used to segment the pectoral muscle and the breast tissues from MR images [150]. To segment a specific type of tissue, the image is divided in several regions of interest (ROI, see Figure 3.2.a). For each ROI the segmentation of one type of tissue takes place in 3 steps (Figure 3.2):

1. First, the random forest algorithm [70] is used to compute the probability of each pixel to belong or not to the segmented tissue. Figure 3.2.c shows the synthetic volume corresponding to the previously selected ROI (Figure 3.2.b). In the new defined volume, the pixels are classified into background (blue) and breast tissue (gray) with a given probability (color intensity). The training data set for the random forest algorithm is manually selected by the user. It includes state and space characteristics such as voxel grey intensity, voxel's neighbors gray intensity (with variable radius of neighboring) and voxel position (x, y, z) .
2. Then, spherical regions with variable radius (seeds), are placed manually into the new synthetic volume. The seeds mark all the connected components belonging to the segmented tissue (Figure 3.2.d.1).
3. Finally, the seed contours evolve in the 3D space with a speed and direction derived from the pixel values in the synthetic volume (Figure 3.2.d.2-4). In Figure 3.2.c, the value of a pixel p_{val} belonging to the background ranges between -1 and 0: $p_{val} \in [-1, 0]$. Contrariwise, the value of a pixel p_{val} belonging to the breast tissues ranges between 0 and 1: $p_{val} \in [0, 1]$. Thus the seeds contours expand over the positive regions and shrink over the negative ones. The propagation speed is proportional to

the pixel intensity $|p_{val}|$. The process is stopped by the user when the growing region covers up the entire relevant volume.

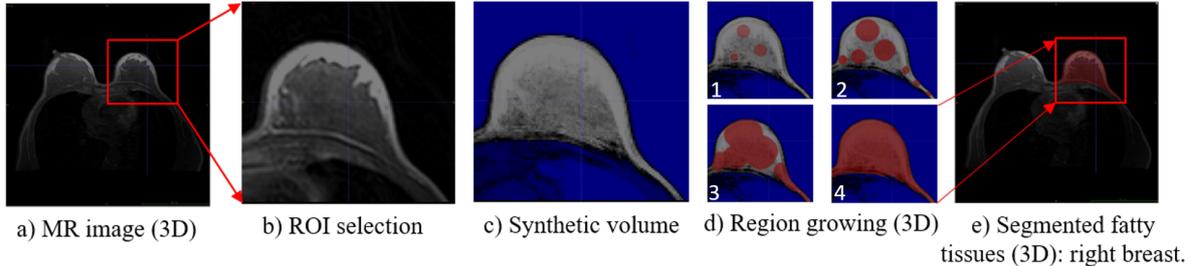


Figure 3.2: Breast tissues segmentation on the breast MRI of the second volunteer. Prone breast configuration.

The breast and pectoral muscle components are computed by merging the set of segmented ROIs. After segmentation, an additional manual correction was performed to refine the boundaries of each component. Simple erosion and dilatation operations were applied on segmented volumes in order to obtain smoother surfaces. Then, to avoid tissues overlapping at juncture border between the pectoral muscle and the breast, binary operations were used. First the two segmented volumes were merged together to create a single volume. Then, from the full component, the pectoral muscle volume was subtracted to redefine the breast volume without overlapping.

The process was repeated for both volunteers and for each breast configuration: supine, prone and supine tilted. The extracted surfaces in supine and prone configurations are used for model definition and optimization the latest surface, in supine tilted configuration, is used for the evaluation of the model.

3.1.3 Image registration

During the imaging acquisition process, the subject was moved in and out of the MRI scanner tunnel. Therefore, the breast does not only undergo an elastic deformation, but also a rigid transformation. Prior to image acquisition, four landmarks were fixed on the chest wall in order to make image registration possible. The landmarks were placed on sternum and inframammary fold lines; these regions are indeed known to be rich in fibrous ligaments limiting the soft tissue elastic deformation. To assess the body position changes, a rigid transform was computed by minimizing the Euclidian distances between the two configurations of the four points defined by the four landmarks. The transformation was estimated using the iterative closest point (ICP) algorithm proposed by ITK library.

However, due to small local deformations of the skin, the computed rigid transformation was not accurate enough. Therefore, a second registration step was performed by aligning the bone structures of the thoracic cage from prone and supine tilted positions to the supine one. The muscular tissues mask previously segmented was used in order to remove

non-breast soft tissue. The image registration was implemented using a gradient descent based algorithm minimizing the image cross correlation (ITK library).

Figure 3.3 shows overlapping prone-supine and supine tilted-supine breast images of the first volunteer in the transversal plane after registration. The registration error was assessed by computing the distance from the muscle's anterior surface in prone and supine tilted configurations to the muscle's anterior surface in supine configuration (Figure 3.4). The chest wall lines of both volumes were well aligned within an error of 5 mm. Higher differences may be observed because of elastic thoracic cage deformations due to hand repositioning or body-mass force repartition. A maximal error of 16.25 mm and 14.9 mm is observed over the region of the right arm in prone configuration and supine tilted configuration respectively, however these regions are out of the scope of interest.

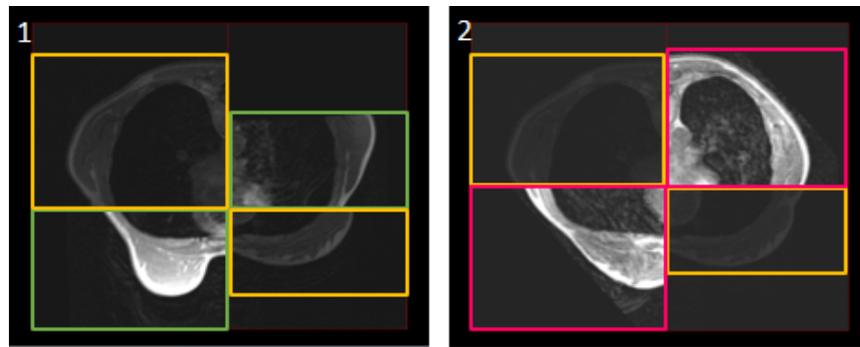


Figure 3.3: Registered MRI images for the first subject, 1) prone configuration versus supine; 2) supine tilted versus supine. Yellow frame - supine configuration; Green frame - prone configuration; Red frame - supine tilted configuration.

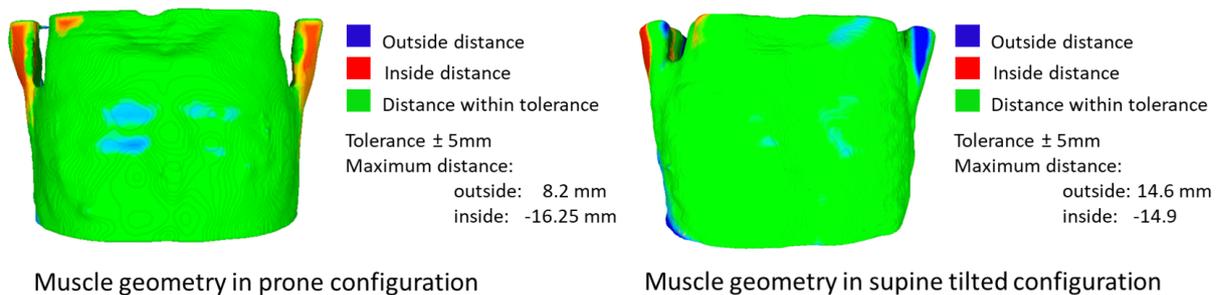


Figure 3.4: Registration accuracy measured over the anterior muscle surface.

As described in the next sections, the breast model calibration and evaluation is a time consuming procedure. As a consequence, we only performed the model calibration and evaluation based on the geometry and mechanical properties of the first subject only.

In a multi-loading gravity finite element simulation, the gravity force is applied to the whole model as a body force. The gravity force orientation can be broken down into three components of the Cartesian coordinate system labeled as X, Y, and Z directions (Figure

3.5). The supine configuration was chosen as a reference state, therefore the gravity loading direction was set in that configuration to be oriented on the inverse direction of the Y axis (posterior-anterior direction, Figure 3.5): $\gamma_s = (0, -1, 0)$. The gravity loading direction for the two other positions are given by the rigid transformation computed by image registration: $\gamma_p = (0.037, 0.985, -0.165)$ direction vector for gravity in prone position and $\gamma_{st} = (-0.744, -0.667, 0.023)$ direction vector for supine tilted position. These direction vectors characterize the breast configurations of the first volunteer only.

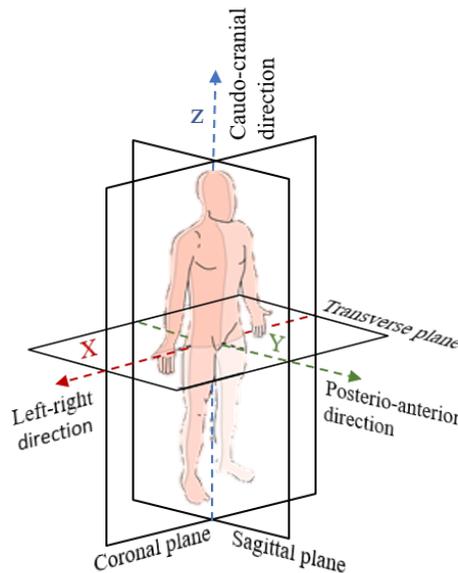


Figure 3.5: Anatomical planes and nominal Cartesian axis directions.

3.1.4 Subject-specific 3D geometry

The breast subject-specific geometry was created based on the MR images in supine configuration. Following image segmentation (Figure 3.6.b), the outer shape of labeled regions was subsequently discretized by triangular elements. A semi-automatic Skin Surface module proposed by SpaceClaim Direct Modeler was used to convert the mesh surfaces to non-uniform rational basis spline (NURBS) surfaces (Figure 3.6.c).

The NURBS are averaging curves between points, therefore they are smoother and easier to use in mechanical applications. Figure 3.7 shows the distance from the mesh surface to the NURBS surface for the breast and muscle geometries of the first volunteer in supine position. The NURBS surface fits nearly all over the initial geometry within a tolerance of 0.5 mm . In areas with small curvature angles, the distance between the two surfaces increases up to 1.6 mm and 3.06 mm for breast and muscle geometries respectively.

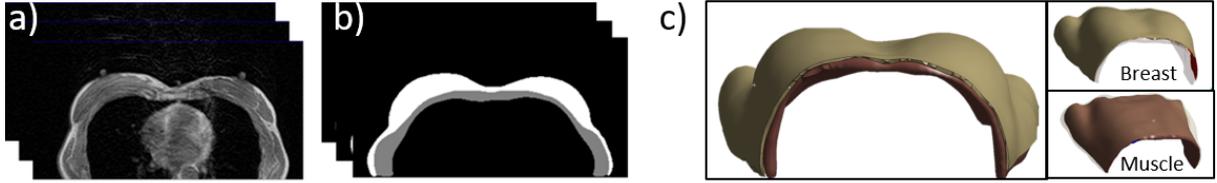


Figure 3.6: 3D geometry generation. a) MR images; b) segmented images; c) corresponding 3D geometries (NURBS surfaces).

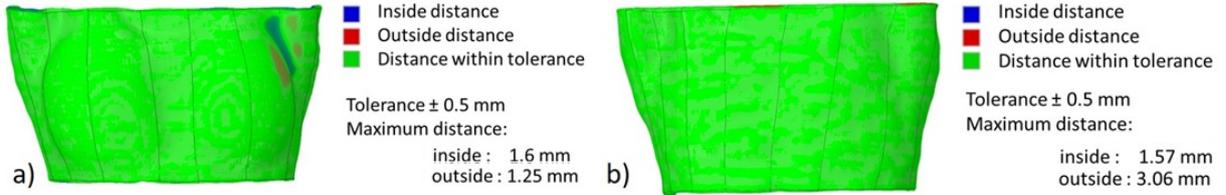


Figure 3.7: The distance between the mesh surface and the corresponding estimated NURBS surface. a) breast volume; b) muscle volume.

3.2 Finite Elements Mesh

After computing the NURBS surfaces, the internal spatial information needs to be encoded using a volumetric mesh. The optimal elements type or mesh density for such a simulation is still an open question and topic of debate. The use of hexahedral elements is usually assumed to result in a more accurate solution, especially when expecting high strain/stress gradients. However, in the literature, because of the large computational time, such meshes are mostly used with a reduced number of elements [124, 51]. Tetrahedral elements are widely used due to their geometrical flexibility and because they provide a good trade-off between computation time and estimated displacement accuracy [65, 105, 61].

In our case, an iterative optimization process is being considered to estimate the tissue's constitutive parameters. Therefore, to reduce the computation time, only linear tetrahedral elements were used. The first order elements are known to bear volumetric locking problems when used to model large strains for quasi-incompressible materials [50]. When volumetric locking occurs, the displacements calculated by the finite element method are orders of magnitude smaller than they should be. It has been shown that a linear element with a mixed U-P formulation can avoid these problems [123]. Therefore, in our work, the geometries are meshed using the tetrahedral element solid285 (ANSYS Mechanical) which provides a mixed U-P formulation option.

On the other hand, the mesh density has also an impact on model accuracy. A finer mesh results in a more accurate and stable solution, but also increases the computational time. To our knowledge, no studies have determined the optimal resolution of the volumetric mesh for simulating breast tissues deformations. To determinate the appropriate mesh size, a mesh convergence study was performed. The details can be found in Appendix B.

According to these results the optimal element's size ranges between 7 and 10mm. Thus, the mesh that was chosen for the first volunteer consists in 18453 tetrahedral elements with 9625 elements assigned to the pectoral muscle and the thoracic cage and 8828 elements assigned to breast tissues (Figure 3.8).

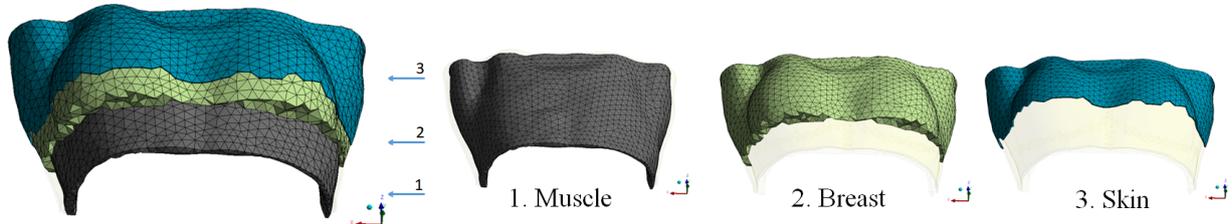


Figure 3.8: Finite element mesh components. The tissues components are cropped for visualization purposes.

The mesh quality was measured using three criteria: element skewness, aspect ratio and maximal corner angle. The Figure 3.9 shows the values distribution for these shape parameters. The element's aspect ratio and maximal corner angle range between the nominal limits defining a good mesh quality (Section 2.2). There is a small number of elements with a skewness larger than the maximal theoretical quality limit (0.75), however there are no degenerated elements (skewness = 1).

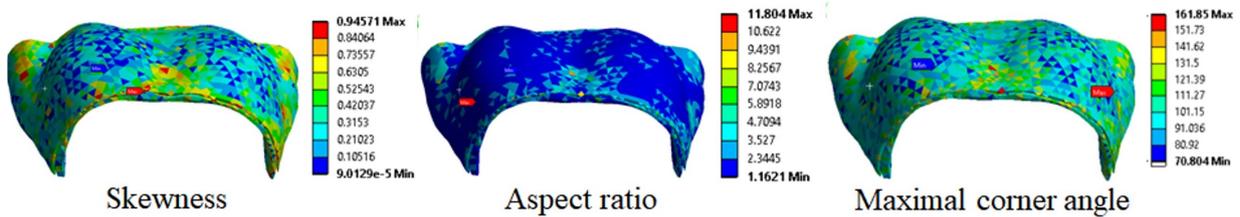


Figure 3.9: Finite elements mesh quality.

The breast skin layer is added a posteriori as a 2mm thick single layer of shell elements (1980 elements). Shell elements and the underlying solid elements are sharing the same nodes (Figure 3.9.a).

3.3 Breast reference configuration

To estimate the reference configuration of the breast (*stress-free* configuration), an adapted prediction-correction iterative approach was implemented [42] using prone and supine image data sets. In the following section, the mechanical behavior of breast tissues was assumed to be known. The detailed definition of the constitutive relations and the method used to estimate the associated parameters was described further in this manuscript (see Section 3.5). The overall iterative process is presented in Figure 3.10. The first estimate

of stress-free breast configuration is computed by applying an inverse gravity on the supine geometry. Then, at each iteration, the estimated stress-free configuration is used to simulate breast deformation due to gravity in a prone position. The differences between the result of this simulation and the real shape of the breast in prone position is quantified by computing the Euclidian distances d_j for each *active node* j defined at the breast external surface. These distances are then used in the next iteration of the process to simulate imposed displacements (Dirichlet condition) to the active nodes in the stress-free configuration. To reduce the mesh deformation, and thus to limit any element distortion, the displacements are only partially imposed using a multiplicative regularization factor ($\alpha < 1$). The process repeats as long as the new transformation improves the similarity between the two geometries in prone configuration by more than 1 mm on average, $|D_{i+1} - D_i| > 1 \text{ mm}$. The similarity between the estimated and measured configurations at iteration i is given by the mean Euclidean distance D_i over the active nodes.

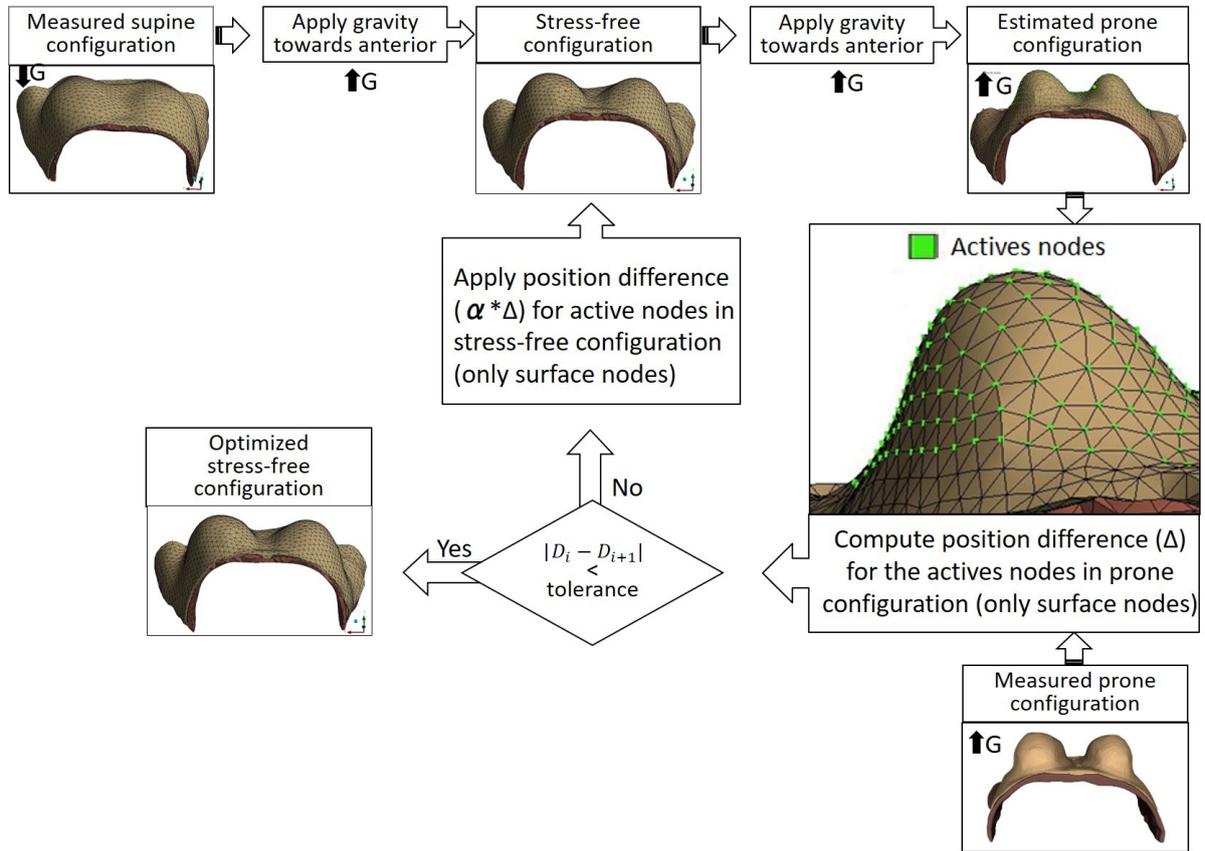


Figure 3.10: Fixed point type iterative algorithm for stress-free geometry approximation. D_i - mean node to node distance over the active nodes at iteration i , G - gravity force

During the fitting process, the active nodes are chosen to be the ones corresponding to the breast surface. The skin nodes belonging to the arms and the lateral thoracic areas are excluded in order to neglect as much as possible the error due to rigid body changes.

To compute the distance d_j between the node position in the estimated and the measured breast configurations, the positions of the active surface nodes on prone configuration have to be known. Thus, an additional mesh registration step was performed at each iteration: the active nodes were morphed into prone configuration using the elastic deformation method proposed by Bucki M. [15]. The method estimates a C^1 -diffeomorphic, non-folding and one-to-one transformation to register a source point cloud onto a target data set, which can either be a point cloud or a surface mesh. The set of input source points is initially embedded in a deformable virtual hexahedral elastic grid. Then, an iterative registration technique is performed. At each iteration the grid is deformed such that the distance between the target and the source nodes is minimized. The use of the grid allows to speed-up the registration process. The distances between the grid vertices and target nodes are computed only once, prior to registration. The location of the source points is then computed by interpolation between the closest grid vertices. To increase the registration accuracy, the regular grid is progressively refined by subdividing each cell into eight smaller ones. Seven refinement steps were performed resulting in a minimal cell size of about 2 mm.

3.4 Boundary conditions

To provide a rigid support for the muscle mesh component, zero displacement conditions are imposed to its posterior face, assumed to be attached to the rib cage (Figure 3.11). Then, the interface between the breast mesh and the muscle mesh is modeled using contact mechanics. The muscle is stiffer than the adipose tissues, thus according to ANSYS technical manual, its anterior face represents the target surface and the posterior breast face represents the contact surface (see Section 2.3 for a reminder of definition of target and source surfaces).

Previous works have shown that modeling breast deformations from prone to supine configurations requires taking into account breast tissues sliding over the chest wall [18, 65]. Therefore, the juncture surface is modeled as a no-separation contact with a frictional behavior proposed by the ANSYS Contact Technologies (see Section 2.3.2). The penalty algorithm is used with a meticulous control of contact normal and opening stiffness parameters. At this stage, stiffness parameters do not have a physical meaning and have to be identified by *trial and error* methods. Since these parameters are extremely sensitive to the stiffness of the underlying elements and to the direction of the local deformation, new values have to be identified for each new simulation case.

To study the impact of the friction coefficient (μ_f) on tissues sliding, several simulations have been performed at different values of μ_f . We found that, with the Coulomb friction law, even for a high value of μ_f , too much sliding is allowed when estimating the prone breast configuration. At the contact surface, because of excessive sliding, the tissue accumulation in the region of the sternum line results in a sinuous surface (Figure 3.12); thus, the finite element mesh undergoes important distortions and the solution is compromised. Therefore, different strategies based on anatomical breast structures were investigated to

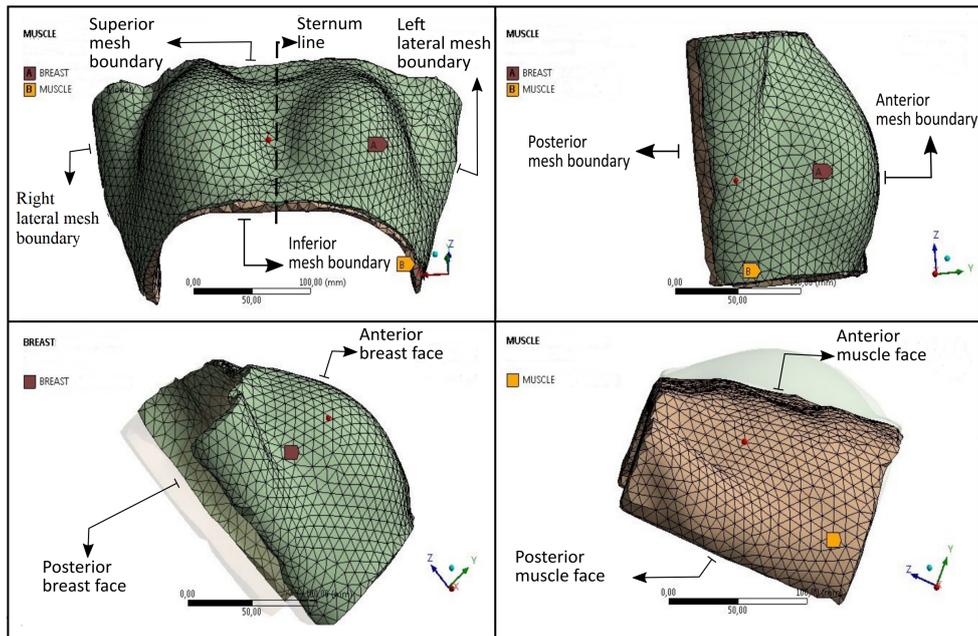


Figure 3.11: Finite elements mesh boundaries

limit the amount of sliding and to overcome solution instabilities (see Appendix C for more details on boundary conditions). We found that a small amount of friction improves the solution convergence capabilities [5]; therefore the friction coefficient was kept to $\mu_f = 0.1$.

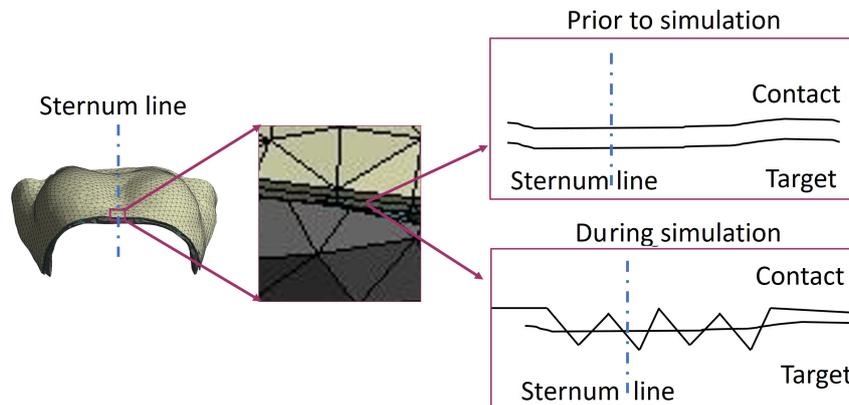


Figure 3.12: Tissues accumulation on the sternum line with excessive sliding

The breast soft tissue is firmly attached to the deep fascia via suspensory ligaments but can move freely over the pectoralis muscle [96, 28]. Therefore, the strategy chosen to control the sliding amount of the breast tissues relies on ligamentous breast structures described in Section 1.1.3. As far as breast support matrix is concerned, only the largest structures were modeled (i.e. fascias and suspensory ligaments). The superficial layer of the superficial

fascia was integrated in the skin layer, assuming a higher material stiffness. In addition, a new layer of 0.1 mm thick shell elements was added at the juncture surface between muscle and breast tissue to model the deep layer of the superficial fascia. The shell and the underlying breast elements share the same nodes. Since the deep fascia and muscle tissues are supposed to present similar elastic properties (see Section 2.4.2), the deep fascia was not explicitly modeled. In addition, two ligamentous structures (inframammary ligament and deep medial ligament) were modeled using ANSYS link type elements connecting the nodes of the breast posterior surface to the nodes of the anterior muscle surface (Figure 3.13).

Several additional Dirichlet conditions were set on the mesh boundaries: the superior and inferior ends of the deep fascia layer were constrained in Z direction; the superior and inferior ends of the skin layer were constrained in Y direction. For left and right lateral breast boundaries (Figure 3.11), Dirichlet conditions are too strong and preclude breast tissue to slide laterally. Therefore, in these regions, new ligamentous structures were included using link elements with a cable-like behavior (Figure 3.13).

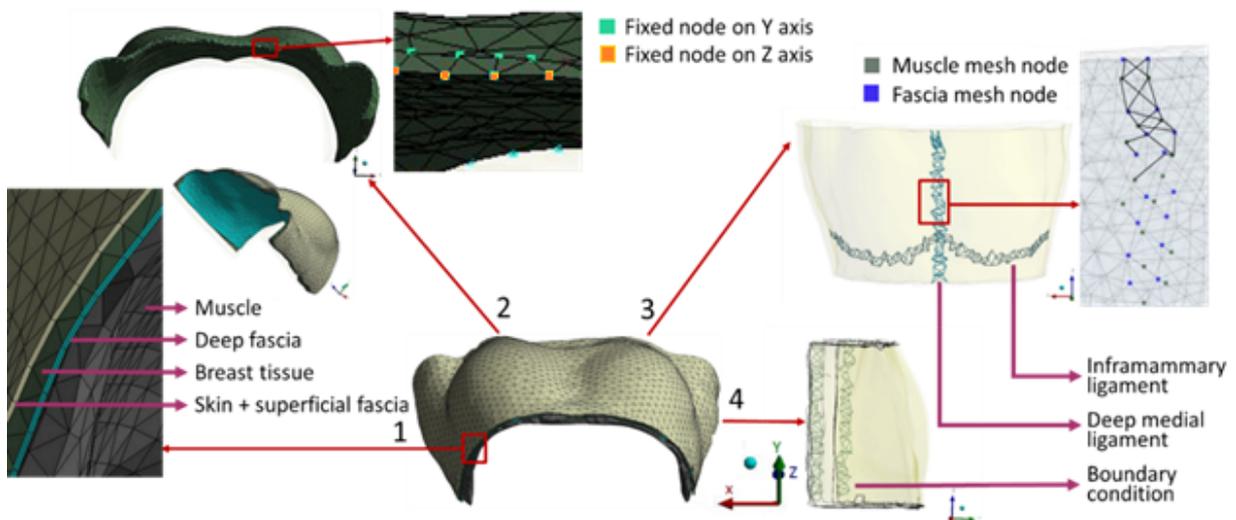


Figure 3.13: Components of the finite element mesh.

The deep layer of the superficial fascia is much stiffer than the underlying adipose tissues. Due to imposed boundary conditions, the amount of sliding depends on fascia's elasticity. The suspensory ligaments define regions where the breast sliding is minimal regardless of the applied deformations. These additional stiff structures reduce the tissues sliding and improve the solution convergence capability.

3.5 Material constitutive models

Our final model consists of 6 types of tissues, wherein 4 tissues (glandular, fatty, muscle and skin) are well described and regularly used in biomechanical modeling, and 2 of them (fascia

and suspension ligaments) are with limited use and poorly described in the literature. A large range of values of the constitutive parameters are available for each tissue. Because of this large interindividual variability, subject-specific parameters had to be identified.

Here, all tissues excluding the suspensory ligaments were modeled using the Neo-Hookean strain energy functions. Breast suspensory ligaments were assumed to undergo only small deformations, thus they were considered as linear materials. Subject-specific mechanical tissue properties were computed using an optimization process based on a multi-loading gravity simulation procedure (Figure 3.14).

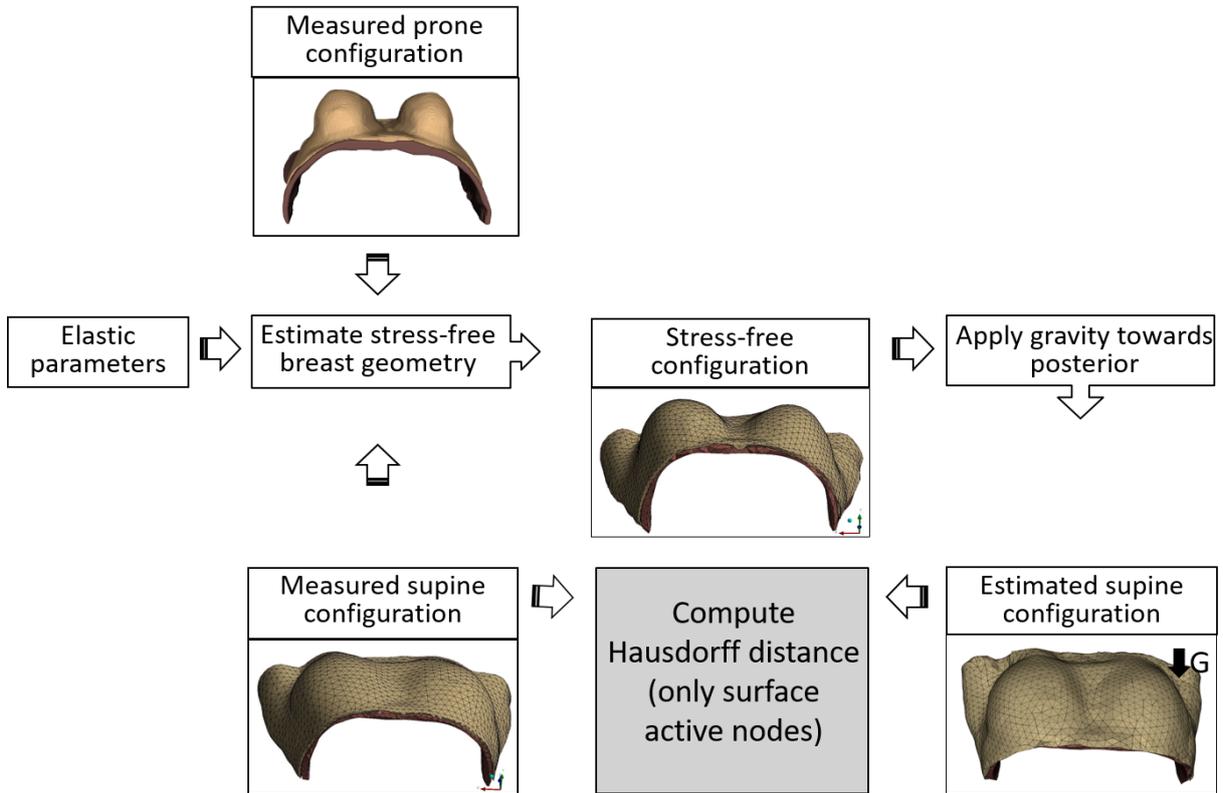


Figure 3.14: Process to estimate optimal material parameters

First, for a given set of parameters ($\lambda_{glandular}, \lambda_{adipose}, \lambda_{muscle}, \lambda_{skin}, \lambda_{fascia}, \lambda_{ligam}, \nu$), the stress-free configuration was estimated by minimizing the difference between the simulated and the measured breast geometry in prone configuration. Then, from the new estimated stress-free geometry, the supine breast configuration was derived. The estimated supine geometry was compared to the measured one using modified Hausdorff distance (see Appendix A for distance definition), representing the estimation error. To avoid including the geometry dissimilarities due to arm position, the modified Hausdorff distance was computed only on breast skin surface.

The algorithm estimating the breast reference configuration requires multiple simulations based on imposed node displacements; therefore the FE mesh can be significantly altered (with convergence issues) before reaching an optimal stress-free geometry. Mainly

for that reason, we chose to perform an exhaustive manual research (rather than an automatic one) of the optimal set of constitutive parameters.

An optimization process including finite element simulations with 6 parameters results in a complex and time-consuming problem. The model simplification was then performed in two steps. First, the parameters which variations have limited effects on simulation results were identified and set to a fixed value. Next, for parameters which variations have a high impact on simulation results, a sensitivity study was performed to redefine the search intervals and interval's discretization step.

3.5.1 Model simplification

The breast tissues are mainly composed of water; a usual assumption is to consider them as nearly incompressible materials [49]. However, previous works proposed a Poisson's ratio value ranging between $\nu = 0.3$ [72] and $\nu = 0.5$ [51]. In a multi-loading gravity simulation, the breast volume is nearly constant, thus, the influence of Poisson's ratio on node displacements was studied only for values ranging between $\nu = 0.45$ and $\nu = 0.495$] (Figure 3.15).

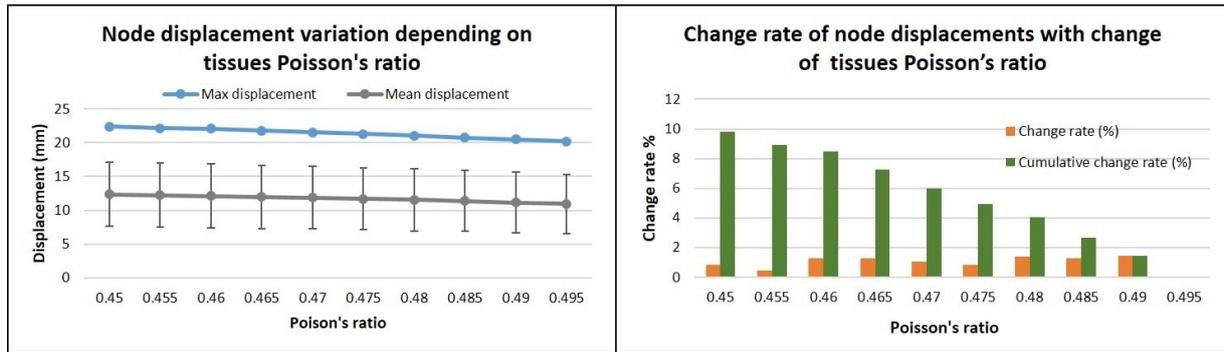


Figure 3.15: Estimation of the optimal material parameters

The simulations were performed by applying the gravity force in postero-anterior direction on breast geometry in supine configuration. We present on Figure 3.15, the node displacement variation and the change rate of node displacement as function of the tissue Poisson ratio. On the left-hand side, the mean and the maximal displacements of the skin nodes are given for each value of ν . On the right-hand side, the maximal difference of nodal displacements between two consecutive simulations (change rate) and the maximal difference of node displacements between the actual and the less deformed geometry (cumulative change rate) are plotted. The change rate is computed within the assumption that the maximal displacement over the simulations set represents 100 % change rate. Non-significant variations are observed on the mean and maximal displacements of skin nodes, thus a constant value of $\nu = 0.49$ was chosen.

The pectoral muscle together with the thoracic cage support the breast tissues. The deformation of the muscle under gravity loading was neglected. Therefore, its Young's

modulus was not included on the parametric study and was chosen so that only minimal deformations occur ($\lambda_{muscle} = 10kPa$).

The ligamentous breast structures were added with a cable-like behavior to reduce tissues sliding. Their Young's moduli are also not included in the optimization process and is set sufficiently high ($\lambda_{ligam} = 500kPa$) to preclude their elastic deformation (see Section ??).

The adipose and glandular tissues are known to be extremely soft and to undergo large deformations under gravity loading. Calvo-Gallego J.L. [16] proposed a uniform polynomial material model for the mixture of adipose and glandular tissues. The authors have also shown that the breast outer shape deformation does not depend on glandular distribution but is highly dependent on its volumetric ratio. In this work, it was chosen to model the glandular and fatty tissues as a single homogeneous material with an equivalent Young's modulus λ_{breast} . The mechanical properties of the equivalent breast tissue are in direct relation with glandular and adipose volumes ratios. Because the left and right breasts may have different glandularities, two different parameters were considered (λ_{breast}^l , λ_{breast}^r), one for each laterality.

Breast skin and superficial fascia are an essential part of the breast support matrix. The two layers are much stiffer than breast tissues and are the structures governing the amount of deformations. Their elastic behavior was included on the optimization process.

Based on existing publications, an interval of possible values are given in Table 3.2 for each parameter included in the optimization process (λ_{breast}^l , λ_{breast}^r , λ_{skin} , λ_{fascia}). To characterize model sensitivity to parameters' variations, a set of simulations was performed. The defined intervals for each type of tissues were discretized by steps of 10% and at each step the skin nodes displacement were computed. Results of the corresponding simulations are shown on Figure 3.16. As previously, the first column represents the variation of mean and maximal displacements of skin nodes in function of the elastic parameter of each material; the second column represents the change rate and the cumulative change rate of skin nodes displacements.

	Search intervals from bibliographic data			Search intervals after model simplification		
	Breast	Skin	Fascia	Breast	Skin	Fascia
Min (kPa)	0.3	7.4	100	0.3	2	50
Max (kPa)	6	58.4	5000	4	20	250

Table 3.2: Minimal and maximal value (in kPa) for Young's moduli.

The figure shows that the model is very sensitive to the variation of Young's modulus of breast tissue, skin and fascia (Figure 3.16). However, beyond some values, the materials become too stiff and do not change significantly the breast deformations under gravity loadings. Therefore, the search intervals for breast tissue and skin Young's moduli were reduced so that a larger value impacts the cumulative change rate less than 20% (max displacement less than $\sim 5mm$). As the fascia stiffness governs the lateral displacement

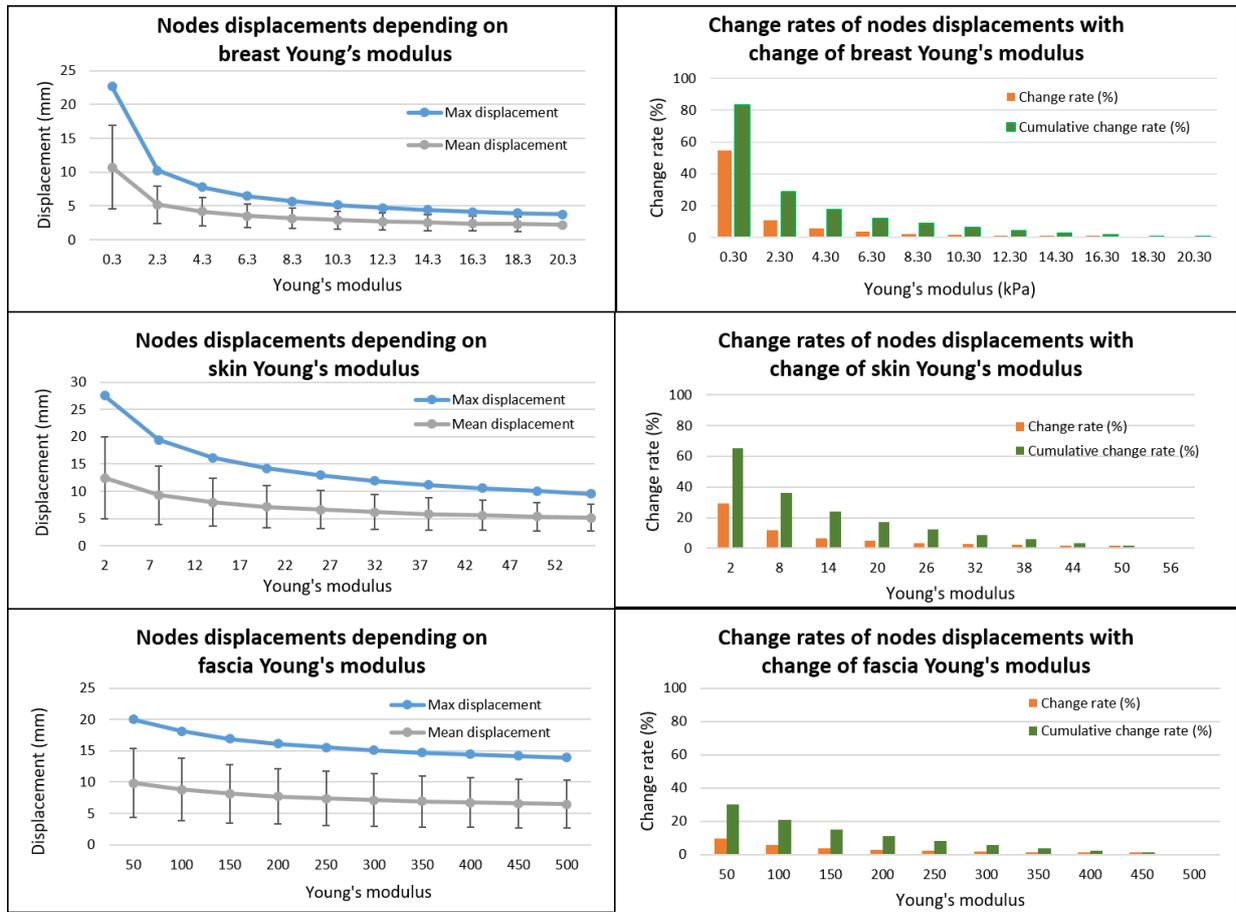


Figure 3.16: First column: relation between maximal and mean nodes displacement and the equivalent Young's moduli variation for different tissues. Second column: rate and cumulative change rate of skin node displacement as function of equivalent Young's modulus

and shows a smaller variation over the search interval, a threshold of 10 % ($\sim 2.5mm$) was chosen. The obtained search intervals are summarized in Table 3.2

3.5.2 Estimation of the optimal constitutive parameters

The model optimization is a tough and time consuming process. It was extremely difficult to obtain the solution convergence when combining the tissues large deformations with the sliding contact conditions. Because of the large computation time, the reference breast configuration and the optimal constitutive parameters were computed only for the first volunteer. The model optimization of the second volunteer is considered for future work.

To estimate the constitutive parameters describing the breast mechanics of the first volunteer, the new intervals defined by the above sensitivity analysis were discretized by steps of $0.1kPa$, $1kPa$ and $40kPa$ for breast, skin and fascia tissues respectively. The discretization step was chosen such that the change rate between two consecutive simulations

is less than 10%. The previously described multi-loading gravity process was performed for each set of parameters and the corresponding model error distribution is shown in Figure 3.17. The contour lines are estimated by linear interpolation between two consecutive simulations.

We found values of the Young's modulus for the breast tissues lower than the ones reported in the bibliography. Therefore more simulations were done outside the defined intervals. However, for very low values, below 0.2 kPa , 2 kPa and 80 kPa for breast, skin and fascia's Young's modulus respectively, the tissues deformation is too large and the finite element mesh becomes degenerated at the first step of the multi-loading simulation. For values above 1 kPa , 5 kPa and 160 kPa , tissues deformation is too small compared to the ones observed from the MR images and the simulations using such values were excluded. All other missing values correspond to failed simulations due to a non-converging force, specifically in the region of the contact surface between the breast and the muscle.

For soft fascia ($\lambda_{fascia} = 80 \text{ kPa}$), the lateral displacement of breast tissues is more important than the one measured on MR images. Contrariwise, for stiff fascia material ($\lambda_{fascia} = 160 \text{ kPa}$) the amount of sliding is too small. To match the breast geometry in supine configuration, very low values of breast Young's modulus are required ($\lambda_{breast} < 0.2 \text{ kPa}$). For such low values, the breast tissues are highly deformed, thus the finite elements undergo large distortions. Due to such errors in element formulation, the simulations giving the minimal Hausdorff distance did not succeed.

The set of parameters providing the best match between simulated and measured supine breast configurations is ($\lambda_{breast}^r = 0.3 \text{ kPa}$, $\lambda_{breast}^l = 0.2 \text{ kPa}$, $\lambda_{skin} = 4 \text{ kPa}$, $\lambda_{fascia} = 120 \text{ kPa}$).

CHAPTER 3. A NEW BIOMECHANICAL BREAST MODEL EVALUATED ON REAL DATA

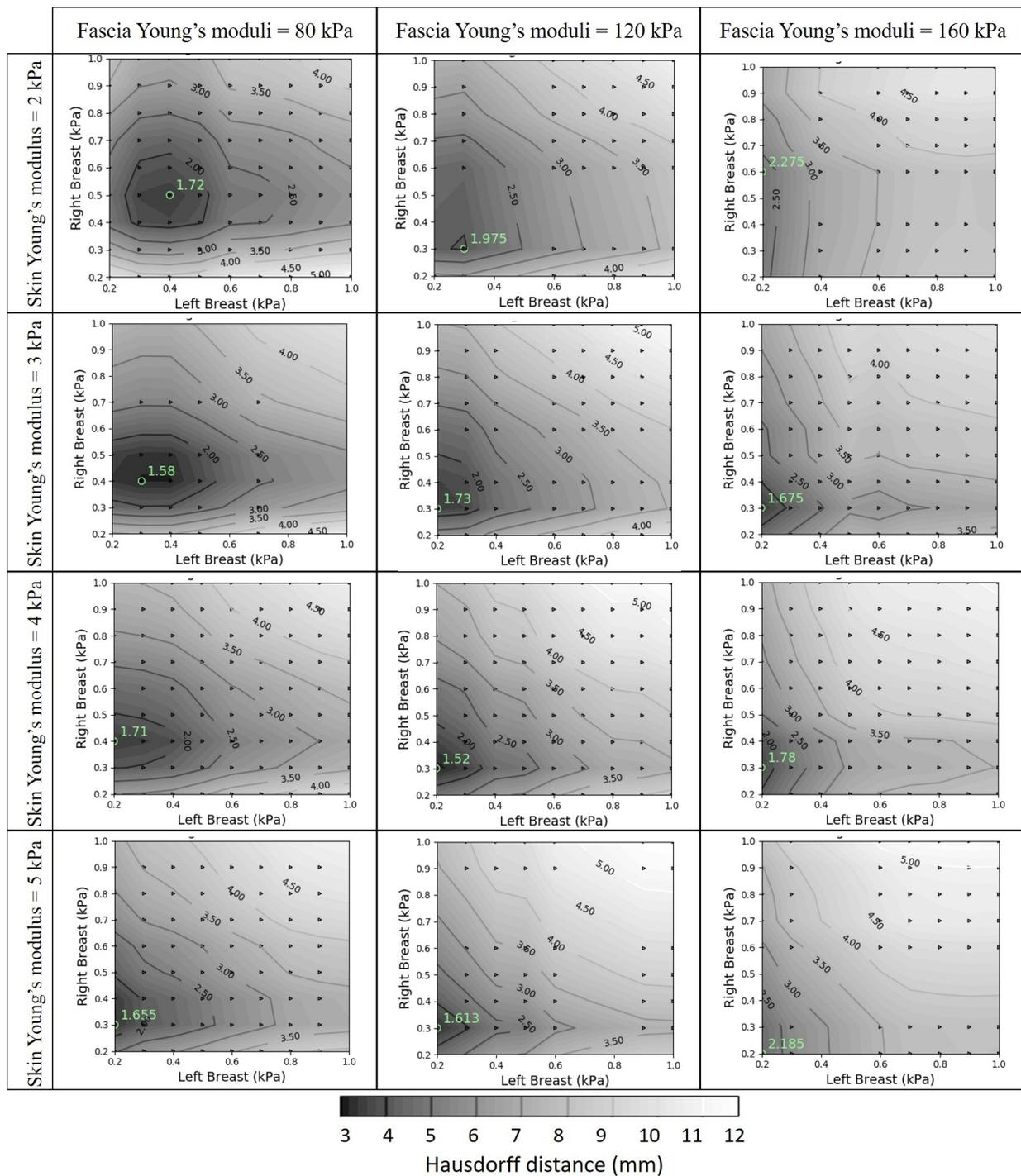


Figure 3.17: Hausdorff distance on the skin surface over the constitutive parameters space. X-axis represents the equivalent Young's modulus of the left breast, Y-axis represents the equivalent Young's modulus of the right breast. The minimal Hausdorff distance for a fixed value of the skin and fascia Young's modulus are highlighted in green.

Figure 3.18 shows the differences between the measured and estimated breast geometry in prone (left) and supine (right) configurations. Each distance was computed over the skin active nodes used also for the model optimization.

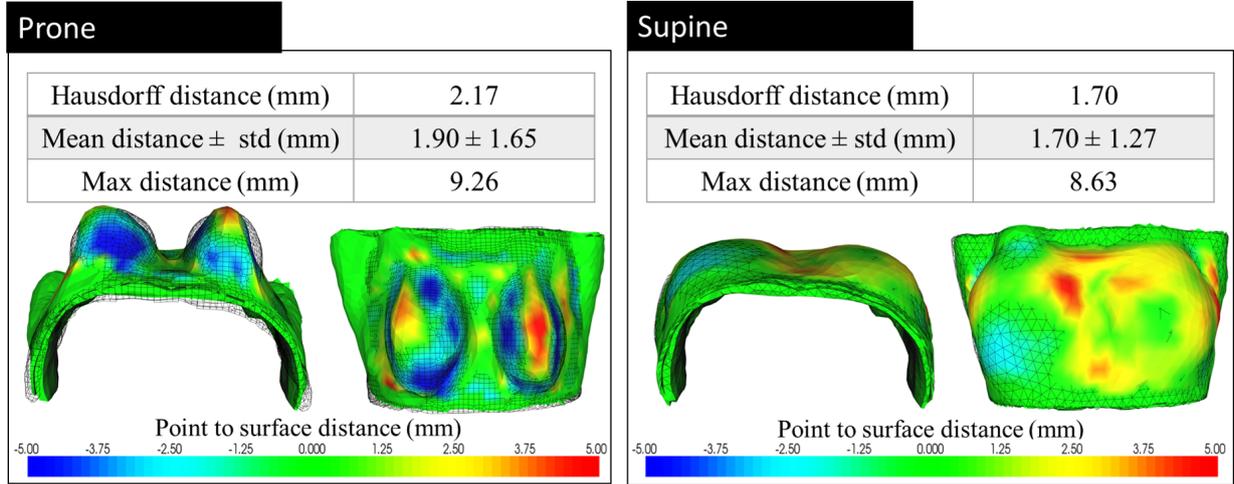


Figure 3.18: Difference between estimated and measured data, in prone and supine configurations, obtained with optimal Young’s moduli and stress-free geometry.

The breast geometry is better estimated in supine configuration, with an Hausdorff distance equal to 1.72 mm. This is probably due to a better representation of the boundary conditions in supine configuration, as this configuration was used to create the initial finite element mesh. The breast geometry in prone configuration is also well estimated, with a modified Hausdorff distance equal to 2.17 mm. The maximal node to surface distance is obtained on the breast lateral parts. Considering non uniform skin thickness or elastic properties over the breast surface, as described by Sutradhar and Miller [134], should improve the obtained results in prone configuration.

3.6 Model evaluation

MRI-based biomechanical models already published in the literature have used the same breast configurations for the optimization and the evaluation process. The model accuracy was then assessed for a single deformation configuration, namely the one used during the optimization process. Therefore small estimation errors are expected. However, there is a high probability that the same model will fail in computing the global breast deformations within different conditions, for example a different gravity orientation or in presence of breast compression.

To verify the estimation fidelity to real breast deformation, the model error must be assessed in a more general framework. The supine tilted breast configuration was not used during the optimization process. Then, the difference between the estimated and measured data in this position was computed to evaluate the capabilities of our model.

To compute the breast deformation under gravity loading on supine tilted configuration, the reference geometry together with previously defined material models were used. The body force direction was defined according to the vector obtained by image registration (section 3.1.3). The model accuracy, in reference with the real deformations, was assessed using 4 measures of distance based on the spatial location of the skin nodes (Appendix A). As previously described only the subset of active nodes was considered for distance computation. Figure 3.19 shows the magnitude of the node to surface distance, mean and maximal node to surface distance, and modified Hausdorff distance.

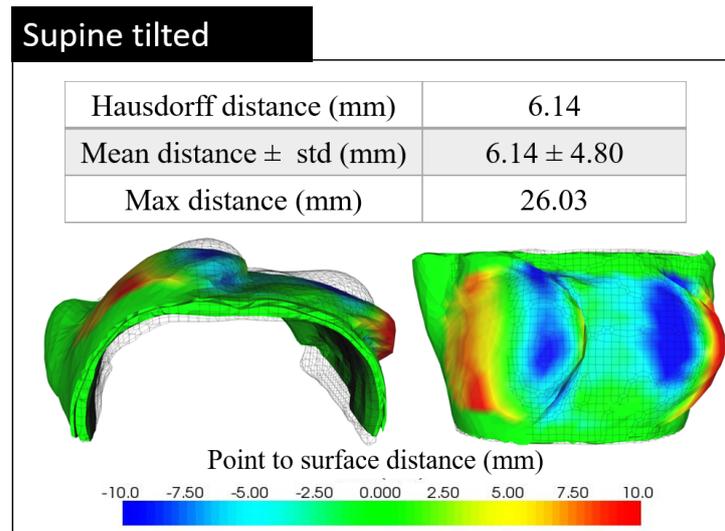


Figure 3.19: Difference between estimated and measured breast geometries in supine tilted configuration.

One may see that the supine tilted breast configuration is unwell described by the breast biomechanical model (Hausdorff distance equal to 6.14 mm). Large difference between simulated and measured breast surfaces is caused by the excessive sliding of breast tissues over the chest wall. Numerical or structural modeling choices could explain such a behavior.

Firstly, such discrepancies between the measured breast geometry in supine tilted configuration and its estimate could be caused by an inaccurate registration between the supine and supine tilted configurations. Moreover, one may observe on MRI images that, during the volunteer's position change, the pectoral muscles undergo deformation. Therefore it also involves changes of model boundary conditions that were not considered during simulations.

Secondly, the fascial and ligamentous tissues are usually characterized by a cable-like behavior. The strain-energy density function must behave asymptotically in order to limit the fascia stretch and thus reduce non-linearly the breast sliding over the chest wall. Limitations of the neo-Hookean model to capture the mechanical response of some nonlinear materials is well known [76]. For large strain, the Neo-Hookean material may undergo a strain-softening and therefore becomes easier to deform. Our numerical results have shown

that the maximal strain at the fascia level is significantly higher in supine tilted position (about 140%) than in supine or prone positions (about 50%). Therefore, an asymptotic behavior of fascia mechanical response must be considered. The Gent form of the strain-energy function characterizes better such mechanical response [57] and was considered later in our work as an alternative choice .

Finally, the breast support matrix is composed of 4 suspensory ligaments. However only two of them were partially modeled, namely the inframammary and deep medial ligaments. The 3D structures connecting the skin to some muscular areas, namely the cranial ligament, were neglected. The particularity of the cranial ligament consists in its position. Indeed, almost its entire structure is attached to the skin and the only attachments to the thorax are situated at the clavicle and at the seventh rib levels (inframammary ligament). However, including such structures at the skin surface may result in local high strain gradient causing solution instability and aesthetic surface deformations.

3.7 Discussions and conclusion

In this chapter, a new finite element breast model was proposed and evaluated with real tissues deformations measured on MR images. To this end, MR images of two volunteers were acquired in three different configurations: supine, prone and supine tilted. The supine and prone MRI volumes were used to adapt the biomechanical model to the volunteer individual breast geometry and its respective tissues mechanical properties. The optimal mechanical properties were determined by exhaustive search over predefined parameter intervals. For each combination of tissues elastic properties, the breast reference configuration was computed using an adapted prediction-correction iterative scheme. The set of parameters giving the best fit between estimated and measured breast configurations was selected. Using these optimal estimates, the supine, prone and supine tilted breast configurations were computed and compared to the MRI volumes.

It was found that, extremely soft materials laws ($0.2-0.3kPa$ for breast tissues and $4kPa$ for skin) must be used in order to obtain the same tissues displacement observed on MR images. Moreover, the breast tissues sliding must be considered when computing such large deformations. However, because of tissues hyper-elasticity, the model boundary conditions have to be revisited in order to ensure the convergence capability of the solution. With such soft tissue, the finite element mesh may become highly distorted. Therefore to limit element distortion, a stiffer layer was added between the breast tissues and the pectoral muscle, representing the deep layer of the superficial fascia. Excessive sliding was prevented by using ligamentous structures fixing the soft tissue to the pectoral muscle.

Contrary to the previous published works, our model was evaluated in 3 breast configurations. Among the 3 geometries, two of them were used for the model calibration and evaluation, and the last one was used for the evaluation only. The choice of geometries directly affects the obtained results. The supine and prone body positions are used for clinical procedures therefore, the corresponding breast configurations are frequently used to build the biomechanical models. To be able to compare the actual results to other studies,

supine and prone configuration were chosen to calibrate the proposed model. Therefore, good estimates were obtained in these configurations with Hausdorff distances equal to $2.17mm$ and $1.72mm$ respectively. In supine tilted breast configuration (used for model evaluation only), the breast tissues displace too far laterally. The main factors that could contribute to such differences between the measured and estimated breast geometries are errors in alignment between the supine and supine tilted breast configurations, inaccurate boundary conditions or inappropriate constitutive material models.

Choosing different combinations of breast configurations for the optimization process may also affect the model accuracy. Using the breast geometry in supine-tilted body position to calibrate the constitutive models may improve the obtained results.

Assuming that our model describes well enough the mechanical behavior of the breast, we may use it to compute breast tissues deformation when breast is under compression. In that case, we hypothesized that internal tissues strains and pressure distribution over the skin surface can be used to quantify the patient comfort during a mammography exam.

BREAST COMPRESSION

State of the art

Mammography is the sole breast cancer screening method recognized by the European Commission for women aged 50-69 years. This method enables examination of the breast in its entirety and offers a high sensitivity for early-stage tumors. However, the mammographic exam is known to be unpleasant for the patient, the main source of discomfort being related to breast compression. For such a standardized and wide-used procedure, good exam conditions and patient comfort should be ensured. Therefore, a study on the relevance of breast compression in mammography is of a potential interest.

This chapter describes the standard mammographic procedure, including the breast positioning methods and the design of the most used paddles. The need of compression is explained in terms of image quality and average glandular dose. Patient comfort and the respective current gold standards are introduced. Finally, the interest of developing a simulation environment to assess the quality of breast compression is explained.

4.1 Mammography positioning

During the mammography exam, a qualified radiology technologist positions the breast of the patient between the stationary image receptor and a movable paddle. A routine screening mammography exam consists of two views per breast: cranio-caudal (CC) and mediolateral oblique (MLO) projections.

In a regular workflow, the breast compression is performed in the upright body position. In the CC view (Figure 4.1) the breast is placed on the image receptor, that is initially positioned at the inframammary fold level. Then, the technologist lowers the compression paddle using a foot switch while gently pulling and positioning the breast onto the image receptor to maximize the amount of projected tissues in the image. In the MLO view (Figure 4.1), the image receptor is rotated to an angle between 30 °to 60 °. The lateral oblique side of the breast is positioned against the image receptor. In this view, the pectoral muscle is located between the detector and the compression paddle; as the muscle is stiffer than the breast tissue, the woman has to stay relaxed in order to get a better breast flattening. When lowering the compression paddle, the technologist has to pull the breast upward and forward to prevent breast drooping, and to smooth out any skin folds.

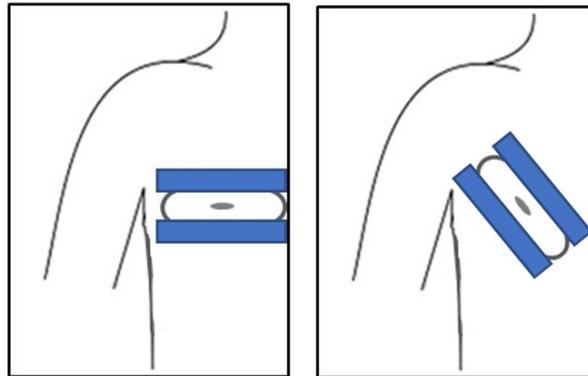


Figure 4.1: left: cranio-caudal breast compression; right: mediolateral oblique breast compression.

The two views are complementary. The MLO view covers a large amount of tissue and provides a better visualization of the upper juxtathoracic part of the breast, while the CC view suffers less from overlapping dense tissue and provides a better visualization on the central part of the breast [22, 81]. Further incidences or magnification views may be needed for diagnostic mammography [62].

The mammography devices are equipped with paddle position and force sensors to measure and display the compressed breast thickness and the amount of force applied to the breast.

4.2 Paddle designs

Nowadays, a wide range of compression paddles are available for breast clinical examination. Their shape and dimensions vary in function of the purpose for which they were designed but also from manufacturer to manufacturer. According to their specific indications of use, three categories can be distinguished: **standard paddle** used for regular screening, **spot paddles** used for diagnosis purposes, and **biopsy paddles** used for breast compression during breast biopsy (Figure 4.2).



Figure 4.2: Different breast compression paddles for GE Healthcare mammography units .

The standard compression paddles have usually a rectangular shape with a flat compression plate. Depending on the industrial manufacturer, they can have different sizes for both the lateral and longitudinal edges and for the paddle front edge height. Paddles with smaller compression area are used to compress small breasts or breasts with implants (Figure 4.2). Standard paddles are classified into rigid and flexible paddles. The standard rigid paddle (SRP) is fixed to its frame and is constrained to move in the up-down direction only. This paddle has some flexibility because of its material mechanical properties and can slightly bend when compressing the breast, while remaining globally parallel to the image receptor (Figure 4.3.b). On the other hand, the standard flex paddle (SFP) is attached to its frame by flexible joints and therefore, presents an additional degree of freedom enabling the paddle to tilt with respect to the image receptor plane (Figure 4.3). During compression the paddle remains parallel to the detector at first, tilts towards nipple side and then ends with the highest point at the thorax level. Depending on the breast position, the paddle may also slightly tilt in the medio-lateral direction.

Spot paddles apply the compression to a smaller area of tissue using a small compression plate or a cone. By applying compression to only a specific area of the breast, the effective pressure is increased on that spot. This results in a better tissue separation and allows for a better visualization of the small area in question. It is used to distinguish between the

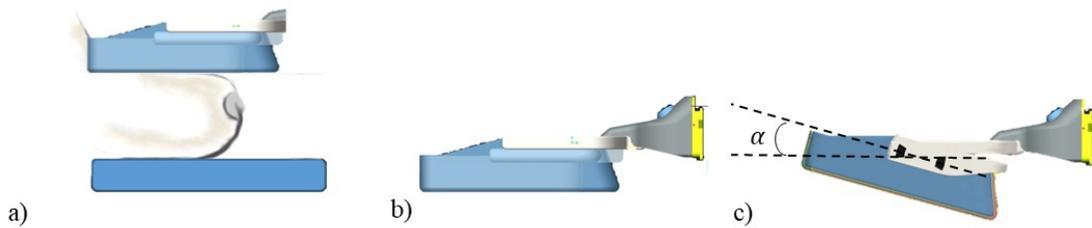


Figure 4.3: a) Breast compression between the paddle (up) and the image receptor (down): b) Rigid paddle; c) Flex paddle with a flexion angle α

presence of a true lesion and an overlap of tissues, as well as to better show the borders of an abnormality or questionable area or a little cluster of faint microcalcifications.

Biopsy exams require that the patient's breast remains immobile and compressed during the entire procedure. The biopsy paddles have basically the same shape as the standard rigid paddles. However, to allow the needle insertion and the accessibility to the biopsied area, the paddle plate contains multiple holes with various diameters or a single aperture.

In this chapter, only breast compression with the rigid paddle in the two main views (MLO and CC) is considered.

4.3 Compression mechanics

Nowadays, the European Commission recommends a force standardized breast compression, i.e. a compression that stops at a level of force just below the subject's pain threshold or at the maximum force setting of the machine. The compression guidelines state that force should be firm but tolerable with a maximum applied compression of 130-200 N [111]. As there is no exact specification for the application of breast compression, the applied force may vary between technologists and radiologists. Mercer and colleagues [94] have analyzed the variation of the applied force within 14 trained practitioners. Both views, CC and MLO, were included. The authors found a significant difference between the average applied forces and have highlighted three groups of radiologists depending on the mean force intensity. Between the consecutive groups, a mean difference of 16 N was found.

The global breast compression cycle is characterized by two phases: flattening and clamping [32]. During the flattening phase, the breast is gradually deformed by increasing the compression force; this step lasts about 7.5 ± 2.6 s. By contrast, during the clamping phase, which lasts approximately 12.8 ± 3.6 s, the compression paddle is immobilized holding the breast in a stationary position.

Figure 4.4 shows a typical compression cycle for a CC breast compression from experimental data on real patients described by Groot et al. [32]. One can see that, during compression phase, breast thickness and contact area evolve non-linearly; meanwhile, compression force and pressure increase quasi-linearly. During the clamping phase, the breast thickness remains constant; however, the skin pressure and the compression force slightly

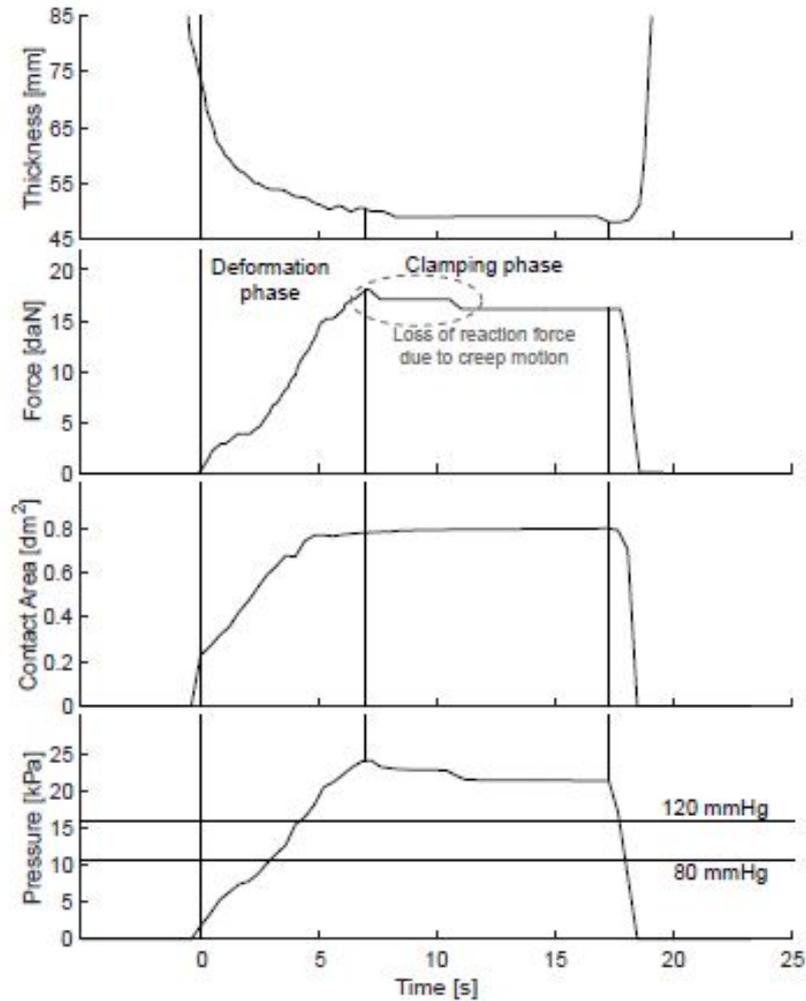


Figure 4.4: A typical breast compression cycle. Reproduced from Groot et al. [62]

decrease in the first 10s. This phenomenon may be explained by breast volume changes because of the viscous effusion of blood and lymph into the central systems.

In the same work, the authors present several in-vivo measured patterns describing the relation between breast thickness and compression force depending on breast size and its firmness (Figure 4.5). One can see that, for a larger breast, higher compression force is needed but the overall behavior remains the same as for smaller breasts. For similar breast sizes, the final compression forces range within the same values, however a firmer breast will reach faster the limiting value of breast thickness resulting in an asymptotic increase of the compression force.

Dustler and colleagues [37] have studied the pressure distribution patterns for MLO breast compression (55 °tilt). The authors showed that the pressure distribution varies widely within the breast. The obtained patterns from 131 subjects were classified into four main groups: a) skin pressure widespread over the breast (29%); b) skin pressure

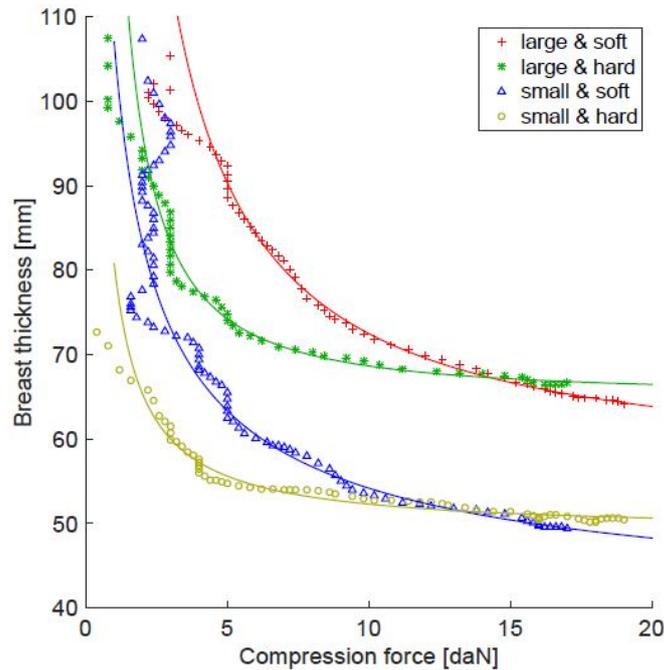


Figure 4.5: In-vivo measured breast flattening curves as function of the applied force. Reproduced from Groot et al. [62]

concentrated on the central part of the breast (8%); c) skin pressure concentrated on the juxtathoracic region (16%); d) skin pressure concentrated along a narrow zone at the juxtathoracic region (26%). According to their results, the pressure distribution depends on two factors: the variation of breast thickness, and the surrounding tissues stiffness. For example, for the groups c and d the compression of the breast anterior tissues is limited by the pectoral muscle which is much stiffer than the breast tissues. These results may explain the fact that, in MLO view, the breast thickness exceeds the one of the CC view, despite the larger force used in MLO compared to CC breast compression [94, 67].

4.4 Compression quality metrics

A standard mammography protocol always includes breast compression prior to image acquisition. Breast flattening improves the diagnostic image quality and reduces the absorbed dose of ionizing photons. However, discomfort and pain produced by this procedure sometimes might deter women from attending breast screening by mammography.

An important improvement concerning the patient comfort could be achieved with the emergence of digital mammography. Indeed, several studies have shown that digital mammography is better in terms of image quality [100] and radiation dose [23] than film-screen mammography.

Most digital mammography systems have an automatic beam quality selection mode (automatic optimization of parameters, AOP) with an automatic exposure control (AEC). The AOP mode automatically selects the X-ray tube voltage, the anode target material and the filter material defining the X-ray spectrum, in order to optimize the *contrast to dose ratio*, i.e. the appropriate amount of radiation for an acceptable low dose and an increased contrast, according to breast thickness and composition [145]. Then, the required exposure time for the actual image is calculated by the AEC. The AOP control allows to determine, for each patient and compression level, the X-ray spectrum that optimizes the ratio of benefits (higher image contrast) and drawbacks (higher dose). In this section, the compression quality will be measured in terms of three metrics: image quality, average glandular dose and patient comfort. A detailed description of each metric is given below with their impact for digital mammography.

4.4.1 Image quality

Many factors may influence the quality of the mammography image such as the knowledge and the skill of the person who performs the mammography examination, the equipment, the positioning technique, the compressed breast thickness, the type of breast cancer, and the radiographic appearance of the breast tissue [32, 4]. In our study, only the impact of the compressed breast thickness on image quality is analyzed.

Firstly, the breast compression facilitates the image interpretation. Higher compression leads to better tissues spread and consequently to less overlapping of clinical important structures. A thinner layer of breast tissues allows a more subtle differentiation between normal and suspicious findings. Secondly, breast compression affects the image sharpness. Since the X-ray exposure time lasts several seconds, a proper breast immobilization reduces the image blurring, preserving the conspicuity of abnormal lesions. Moreover, with a reduced breast thickness, the primary contrast is raised due to a reduced radiation scatter to primary ratio at detector level. Finally, the breast compression leads to a better use of the detector dynamic range. With a non-uniform breast thickness, the different levels of brightness are used to describe the thickness variation, thus the detector dynamic is not used optimally for the contrast representation due to different internal structures. This is particularly true for screen-film technology. With digital detectors, this constraint can be challenged.

It has been proved that image quality decreases with increasing breast thickness [82, 67, 128, 116]. Helvie and colleagues [67] analyzed the image quality for the observed breast thickness of 250 subjects using film-screen mammography. The difference in breast thickness and image quality between the MLO and CC paired images were computed. According to the authors, image sharpness decreased by 19% for 1 *cm* of increased breast thickness. In addition, contrast loss was observed due to scatter augmentation and beam hardening.

Later, Saunders et al. [128] have studied the effect of breast compression on mass conspicuity in digital mammography using Monte Carlo based simulation framework. The simulation was done for two breast thicknesses (4 *cm* and 6 *cm*) with two compression levels

(standard and reduced compression by 12%) and three photon flux conditions (constant flux, constant detector signal, and constant glandular dose). The results suggest that if a particular imaging system can handle an approximately 10% increase in total tube output and 10% decrease in detector signal, breast compression can be reduced by about 12% in terms of breast thickness with little impact on image quality or dose.

O’Leary et al. [102] performed a clinical study to assess the image quality in function of the applied compression force for digital mammography. The CC and MLO views of 4790 subjects were analyzed and image quality was categorized as perfect, good, moderate or inadequate. The results have shown that the image quality is highly correlated with the applied force. The mean compression force required to produce a perfect image was found to be equal to 121.34 N for a CC view and 134.23 N for a MLO view.

4.4.2 Average glandular dose

A mammography unit uses X-rays to obtain 2D-projection images from the breast tissues. As for any X-ray exposure, the irradiation of a targeted population is accepted if the benefits are significantly higher than the risks. Therefore, mammography exposures must provide a good image quality while preserving the radiation dose *as low as reasonably achievable*.

To assess the quality of breast compression, the risks from the X-ray exposure have to be considered. The absorbed energy from digital mammography depends on many factors such as the breast density, the breast thickness, the volumetric distribution of glandular tissues as well as the acquisition parameters.

It has been proved that glandular tissues of the breast are more vulnerable to radiation carcinogenesis than skin, adipose tissue, or areola [64]. Based on these findings, the average glandular dose (AGD) was defined to quantify the risk from breast irradiation and is widely accepted for regulations. The most often used method calculates the AGD as the product of the incident air kerma¹ at the upper surface of the breast with conversion factors called *normalized dose*. The normalized dose (DgN) is computed as a function of spectrum, breast thickness and breast density. Its computation is based on Monte Carlo simulations [30, 13].

Historically, only rigid paddles were used for breast cancer screening. Therefore, in numerical simulations, the breast is usually modeled as a flat semicircular object with a homogeneous content and surrounded by a layer of skin. The attenuation coefficient of the content corresponds to the breast density, the ratio of the amount of gland to total breast [30].

When a flex paddle is used, the breast thickness decreases towards the nipple side, resulting in a wedge-shaped breast. Since the AGD model assumes a flat shape, apart from inherent uncertainties due to general assumptions concerning breast geometry and composition, additional uncertainties due to the paddle tilt are included. In a clinical framework, no difference is made between the flex and the rigid paddles for the AGD computation [14]. To our knowledge, the associated errors are not quantitatively described

¹radiation dose measurement at a point on a patient’s skin

in the literature.

Recent reports have updated dose estimates from screen-film mammography (SFM) and full field digital mammography (FFDM), indicating that two-view screening with FFDM delivers a slightly lower dose than SFM. The mean average dose was estimated for different populations. A geographical classification shows that the AGD delivered by digital mammography for a European woman ($1.48mGy$) is higher on average than the one for North American ($1.42mGy$) or Asian woman ($1.42mGy$) [54]. Osteras and colleagues [104] have classified the CC and MLO view of 3819 women in two classes by breast density. The authors reported a mean AGD of $1.73mGy$ for the dense breasts and an AGD of $1.74mGy$ for the fatty breasts. The AGD was estimated using the model proposed by Dance et al. [30].

4.4.3 Pain and discomfort

Many women have reported discomfort or pain during mammography exams. A literature review over the last decades shows that the prevalence of pain varies widely, the percentage of women experiencing pain or discomfort is ranging between 16% and 72% [78, 110, 36, 144]. This difference could be due to the interpretation of pain intensity (i.e. distinction between *pain* and *considerable pain*), but also could be attributed to differences in the instruments used to measure pain.

Pain intensity is influenced by the meaning of the pain to the patient and its expected duration. The environment also has an impact on the experience of pain, as do expectations, attitudes and beliefs. Pain is rarely caused by psychological factors, but is associated with psychological and emotional effects such as fear, anxiety and depression [146].

The three most-used pain metrics in clinical studies are the visual analog scales, the numeric rating scales and the verbal rating scale [146]. The **visual analog scale** (VAS) is presented as a $10cm$ continuous line together with a verbal descriptors at the line's ends (no pain and worst imaginable pain). The patient is asked to mark the pain intensity on the line. The score is measured from the zero to the patient's mark using a millimeter scale which provide 101 levels of pain intensity. The **numerical rating scale** (NRS) is a discrete point scale where the end points are the extremes of the pain range. In mammography, a 6 or 11 point scale is generally used. The patient will mark the point corresponding to the perceived pain intensity. The **verbal rating scale** (VRS) comprises a list of adjectives used to denote increasing pain intensities, such as no pain, mild pain, moderate pain and severe pain. The patient will choose the adjective corresponding to the perceived pain intensity. According to Williams et al. [146] the numerical rating scale provides the best trade-off between metric sensitivity and the metric repeatability.

In mammography, the pain experienced by women during the exam depends on psychological (technician behavior, patient anxiety) [7], sociological (ethnicity, education level) [36] and physiological factors (compression level, breast size)[116]. It was found that, the main factors associated with the patient discomfort are the satisfaction with care and the perception of the technologist's *roughness* [36]. Besides these findings, several studies have also suggested the pain expectation and the anxiety level as among the main risk factors

associated with the pain [7, 146, 78, 9].

The physiological factors such as breast thickness, breast size or periods are also positively correlated with the patient comfort [78, 63]. The relationship between applied compression force, breast thickness, reported discomfort and image quality has been studied by Poulos et al [116]. According to the authors, the patient comfort decreases with the compressed breast thickness. The authors reported a significant relationship between patient discomfort and breast thickness. However, no significant relationship between the reported discomfort of the procedure and the applied compression force was found. According to the authors, force does not correlate well with subject discomfort since it does not account for differences in breast thickness.

A painful mammography contributes to non-re-attendance. Twenty five percents of US women rated their experience of screening 30 months after their latest mammogram as at least moderately painful [110]. It is thus plausible that remembered pain can possibly dissuade women from attending later screening exams.

4.5 Recent advances in breast compression

Breast compression is an important part of mammography exams. A good breast compression improves image quality, better separates breast tissues structures and reduces the absorbed dose. At the same time, breast positioning and compression are the main sources of discomfort experienced by patients. Because anxiety is documented to be the most important contributor to procedural pain, interventions designed to reduce both physical and psychologic discomfort are needed.

Considering the previous listed risk factors, various pain reducing techniques concerning the usual care were proposed during the last years [95]. To decrease the patient anxiousness and pain expectations, verbal and written information was proposed prior to mammogram acquisition. Informing the patients and accompanying them during the exam have shown to decrease the population mean pain score from 25 to 17 in a 100-mm VAS [129]. At the same time, the effect of some relaxation techniques has been studied. Domar et al. [34] compared the perceived pain from a usual mammogram to the one accompanied by music or a relaxation audiotape. The music subjects had a choice of classical music, jazz, or soft rock. The relaxation audiotape contained information that led the subject through breath focus, body scan, and meditation. According to the authors, there was no significant difference in perceived pain between the various groups.

Later, with the emergence of digital mammography, pain reducing compression techniques were proposed. Several studies [25, 128] suggest that the compression force may be reduced by at least 10% without a significant impact on image quality or average glandular dose. However, according to Poulos et al. [116], patient comfort is not related to the applied force intensity but to the compressed breast thickness, which in its turn is associated with the breast size and firmness. To achieve the optimal compression considering the patient breast specific morphology, a pressure controlled compression is recommended instead of a force controlled compression [32]. The recommended target pressure is equal to

10 *kPa*. For clinical integration, the SigmaScreening company has proposed a new standard rigid paddle with integrated pressure control while the Volpara Solutions company has proposed a software computing the contact area between the breast and the compression paddle in order to extrapolate the mean applied pressure. At the same time, Dustler et al [38] analyzed alternative breast positioning strategies according to previously found pressure distribution patterns. Because of stiff juxtathoracic structures, the authors proposed to increase the distance between the compression paddle and the chest wall by 1 *cm*. The results have shown that within the new breast positioning, the pressure is reduced on the juxtathoracic area. The breast thickness was decreased by 4.4 ± 2.3 *mm* with no significant effect on force intensity. However, the six participants have identified the repositioned compression as the most painful, which, according to the authors, may be explained by the higher pressure intensities on the overall breast surface itself. The main drawback of this technique is the exclusion of juxtathoracic tissues which may obscure small posterior suspicious lesions.

According to latter studies, several constructors started to propose various solutions to reduce the physical discomfort during mammography. Hologic company proposed the MammoPad cushion which is claimed to reduce the discomfort by 50%. In the review proposed by [95], such radiolucent breast cushions are supposed to reduce the pain score (100mm VAS) from 35 to 20 in CC view and from 43 to 26 in MLO. GE Healthcare company proposed a patient-controlled breast compression with the new Senographe Pristina system. This technique lets women control themselves how much the device compresses their breasts. The breast is firstly positioned by the technologist between the compression plates; then, the patient terminates her compression up to a level she can withstand. It has been shown that the patient-controlled compression is less painful than the technologist-controlled compression with no significant impact on image quality [95].

The breast positioning is a fastidious task for the technologist. For example, a larger amount of posterior tissue included in breast compression may result in a larger breast thickness breast at the anterior area, which in turn may reduce the image quality and hide important clinical information. The technologist has the critical job of applying positioning methods using common sense. If the breast area is not well covered by the first two projections, an additional third projection may be necessary. The use of flex paddles proposed by some constructors, such as American Mammographics S.O.F.T. Paddle, GE Healthcare Flex Paddle or Hologic FAST Paddle aims at increasing the area of compressed tissues and thus avoiding an additional projection.

To our knowledge, there is only one study assessing the difference in image quality, average glandular dose and patient comfort between flex and rigid paddles [14]. According to the authors the flex paddle affects the technical image quality without improving the patient experience. Because the flex paddle pulls the soft tissues towards the pectoral wall, they are less visible in the image. It must be highlighted that the study of Broeders and colleagues included CC and MLO projections with force-controlled compressions (target force between 12-20 daN). Based on the same principle as the study presented by Dustler et al [38], one may guess that breast compression with a flex paddle will result in a higher pressure over the breast surface itself (less pressure on the juxtathoracic area which may

be the origin of the pain over the breast surface). It may be interesting to assess the patient discomfort and the image quality with a pressure-controlled compression. Moreover, the average glandular dose is computed by neglecting the wedge form of the flex paddle, therefore it is difficult to compare the flex and the rigid paddles.

To better quantify the difference between flex and rigid paddles, further investigations are needed. In this scope, we have developed a simulation framework allowing to assess breast compression quality as function of breast patient specific morphology and compression paddle design.

This framework is presented in the next chapter, where the breast compression modeling by finite element as well as the numerical methods to assess the corresponding image quality and the average glandular dose are described. In a numerical environment, it is almost impossible to model the psychological patient discomfort, thus this work is focused on analyzing the patient physical discomfort which here is assumed to be associated with tissues internal strain/stress due to breast compression. Ultimately, the breast compression quality for CC view is evaluated for flex and rigid paddles and for various paddle positions.

BREAST COMPRESSION & COMFORT

A comparative study

In this chapter, a numerical simulation able to replicate the most common breast compression techniques was developed. This tool is used to compare different breast compression paddles considering the patient experience as well as the image quality and average glandular dose. The breast biomechanical model described in Chapter 3 was used to create two different breast models corresponding to the two involved volunteers. To simulate breast compression, finite element models of standard paddles were developed and put in contact with the two breast models.

First, a comparative study was performed between various paddle designs. The compression of the right breast of both volumes was simulated with flex and rigid paddles. We proposed to quantify the perceived pain for a given paddle design through three entities, namely contact pressure, internal stress and strain distributions. After compression, a set of virtual macrocalcifications were inserted into the breast volumes. A Monte-Carlo based simulation mimicking the acquisition of images with a mammography system was applied to the breast volumes. Then, the imaging performance was assessed by measuring the signal-difference-to-noise-ratio (SDNR), the signal-to-noise-ratio (SNR) and the average glandular dose (AGD).

Finally, the compression mechanics was analyzed as a function of breast positioning. To this end, the breast geometry of the second volunteer was compressed with different paddle positions with respect to the chest wall. The patient comfort was assessed for three paddle positions.

5.1 Breast compression modeling

In Chapter 3 a new biomechanical breast model was proposed. An optimization process was developed allowing to determine subject-specific breast stress-free geometry and the corresponding mechanical properties. At this stage, the exhaustive semi-automatic search of the constitutive parameters is computationally expensive to perform. Therefore, because of lack of time, the model calibration was carried out for the first volunteer only. However, to perform a qualitative study comparing different paddle models, data of more than one subject is needed. To provide our study with a larger data set, the biomechanical breast model of the second volunteer was created without performing the model calibration to the subject specific mechanical properties. This model represents a new realistic breast geometry with a larger volume and different tissues mechanical behavior which will not characterize the actual breast mechanics of the second volunteer.

To simulate breast compression, finite element models of compression paddles were developed. The realism of these simulations was evaluated by comparing the resulting breast thickness and the applied force to the corresponding data measured during the most recent mammograms of both volunteers. The resulting mechanical response revealed the limitations of a Neo-Hookean strain energy function and the necessity of updating the tissues constitutive models.

In the following section, first the designed compression paddles were introduced. Then, the compression mechanics as simulated using the biomechanical breast model are described. Accordingly, the constitutive models of breast tissues were reviewed and a new form of the strain energy density function was proposed.

5.1.1 FE modeling of compression paddles

In this study, standard paddles (standard rigid and flex paddles) generally used for regular screening were considered. Only one paddle geometry was modeled based on the technical specifications from a Senographe Pristina mammography unit. Three different paddle models were created.

First, the paddle flexibility due to its material properties was neglected. The rigid paddle model (RPM) was therefore defined as a fully rigid body with only one translational degree of freedom in the downward direction.

Then, for the flex paddle model (FPM), a rotation around the longitudinal axis was added. The additional degree of freedom was modeled using a rotational-only joint type of element. The joint stiffness was computed by fitting the force-deflection curve of a standard flex paddle measured on a Senographe Pristina unit. For this, a rigid plate was fixed perpendicularly to the image receptor at its external edge, in order to block the SFP translation degree of freedom (Figure 5.1.a). To ensure the paddle rotation around the Oy axis only, the rigid plate was chosen to have the same length (in Oy direction) as the compression paddle. The deflection angle was measured using a digital inclinometer ($\pm 0.1^\circ$ accuracy). The paddle was lowered progressively, such as the deflection angle

was incremented by steps of 0.5° , until the maximal recommended compression force was reached ($F = 200N$). At each step, the compression force was read from the calibrated mammography unit. The experiment was repeated 3 times. The relation between the mean compression force and the deflection angle is shown in Figure 5.1.b. An estimated second-degree polynomial was used to define the joint stiffness for the FE analysis.

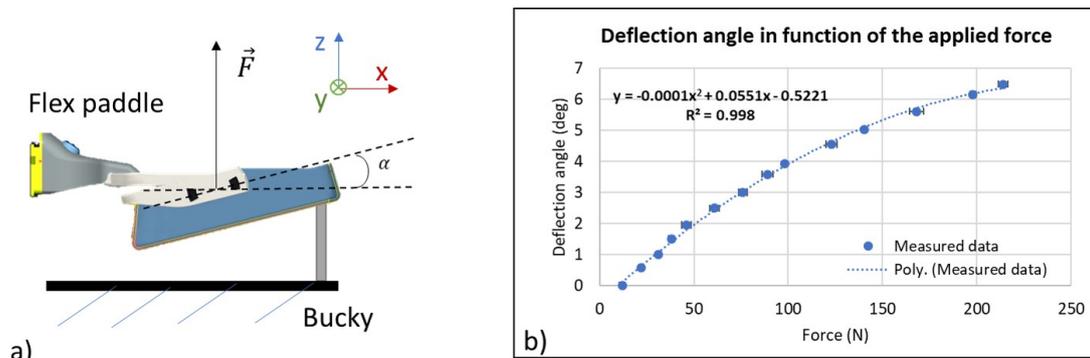


Figure 5.1: a) Experiment set-up, b) Deflection angle as function of the applied force

As concerns the third paddle model, namely the elastic paddle model (EPM), the deflection due to the material properties was included. The paddle thickness was set to $4mm$ and it assumed to be made of Lexan material ($\lambda_{lexan} = 2250 MPa$ and $\nu_{lexan} = 0.4$). Only one translational degree of freedom in the downward direction was considered. The paddle was modeled using shell elements.

For the three paddle models, the interaction between the compression paddles and the breast was modeled using a frictionless contact. The penalty algorithm was used with a penetration factor equal to 0.1 and a contact stiffness equal to 1.

5.1.2 Breast compression mechanics

The realism of breast compression simulations was verified by comparison with real data. The positioning and compression of a small breast, like the one we have for the first volunteer, may be complex. Sometimes the technologist has to hold the breast between the image receptor and the paddle until the compression force is high enough to preclude the breast from sliding outside of the image receptor field of view. This difficulty is also present in a simulation framework, especially since we do not simulate the breast positioning gesture by the radiologist. To facilitate the compression process during the evaluation step, it was therefore decided to use only the larger breast geometry provided by the second volunteer.

In a clinical framework, a woman's breasts are compressed in an up-right or prone body positions. Under compression, the gravity induced tissues pre-stresses can be neglected when compared to the compression-induced stresses [66, 124, 133]. Therefore, the prone breast configuration was used as the reference configuration, neglecting the tissues internal pre-stresses due to gravity loading. The breast compression was simulated using the rigid and flex paddle models.

Prior to breast compression simulations, the breast biomechanical model corresponding to the geometry of the second volunteer in the prone configuration was developed. The optimization problem estimating the set of constitutive parameters is expensive in terms of the computation time. Therefore, for this chapter, we decided to replace the tissues constitutive parameters of the second volunteer, with the ones found in the literature [65, 118, 56]. The corresponding equivalent modulus for each involved tissue was chosen to be the following: $\lambda_{breast} = 0.5kPa$, $\lambda_{muscle} = 10kPa$, $\lambda_{skin} = 10kPa$, $\lambda_{fascia} = 160kPa$. Of course, with this assumption, this new biomechanical model does not properly represent the breast mechanics of the second volunteer. However, it provides a realistic model with a larger breast volume and with stiffer breast tissue which may be used in a comparative study between various compression strategies.

The cranio-caudal incidence was modeled by positioning the image receptor at the inframammary ligament level while the paddle compresses the breast by a downward movement. The compression was stopped when the target breast thickness was reached. Such target thickness was given by the data recorded during the most recent mammogram of the second volunteer (Table 3.1). Figure 5.2 shows the breast thickness as a function of the applied force for the flex and the rigid paddles. The breast thickness for the flex and the rigid paddles was considered constant along Oy axis. For a rigid paddle, the distance between the paddle and the image receptor was used to assess the breast thickness, and was named h_r (Figure 5.2). Concerning the flex paddle, the distance between the image receptor and the paddle was measured at two distinct points, first at the nipple level (named h_1 in Figure 5.2) and the second at the breast base (named h_2 in Figure 5.2). Therefore, the breast thickness for the flex paddle (named h_f on Figure 5.2) is given by the mean value of h_1 and h_2 .

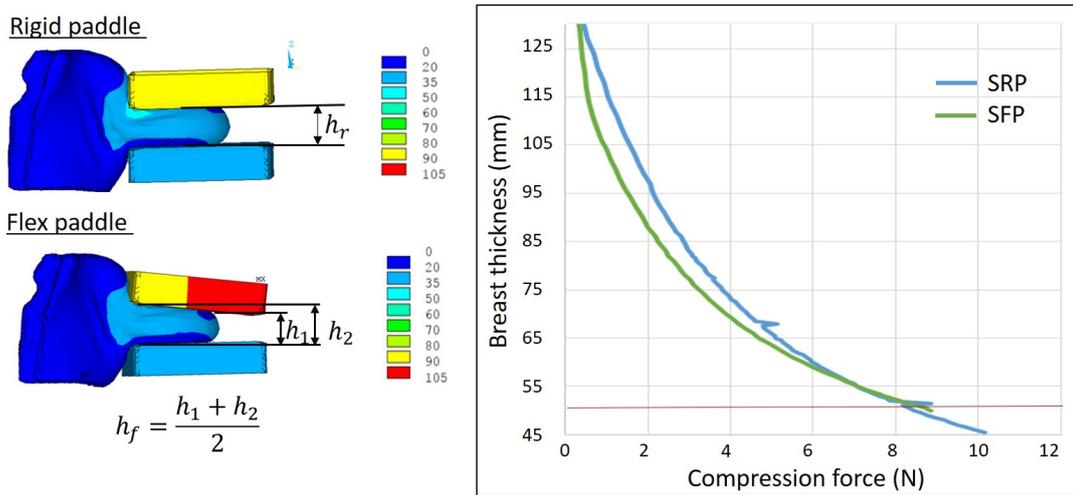


Figure 5.2: Breast flattening curve as function of the applied force for a Neo-Hookean strain energy function. SRP - standard rigid paddle, SFP -standard flex paddle

Several irregularities can be observed over the curve describing the force-thickness rela-

tion when the breast is compressed with a rigid paddle. These numerical artifacts are due to inherent finite elements discretization errors. One can see that, the total compression force at the target breast thickness ($50mm$) is about 12 times lower than the force measured during the volunteer's last mammography ($8N$ versus $94.8N$). Even if the chosen constitutive models were not accurately adapted to the patient mechanical properties, a force of $6N$ remains too low when compared to the standard compression force of $120N$ [25]. Usually, a larger force is applied when compressing such large breast volumes as the one of the second volunteer. Several compressions were tested (e.g. paddle closer to the juxtathoracic area, frictional contact with different friction coefficient) without observing any significant increase of the compression force.

An analysis of the literature revealed that the constitutive parameters used to model breast compression are usually higher than the ones used to model the breast deformation under gravity loading. For example, Sturgeon and colleagues [133] have estimated the tissues deformation under compression considering the initial shear modulus for a Neo-Hookean strain energy function equal to $\mu_{skin} = 88kPa$, $\mu_{adipose} = 1kPa$ and $\mu_{glandular} = 10kPa$. Moreover, our simulations did not demonstrate the asymptotic behavior of the compression force versus breast thickness, as described by Groot et al. [32]. One can conclude that, for high strains, the soft tissues undergo a stiffening process more rapidly than the stiffening as described by a Neo-Hookean law.

The limitation of the Neo-Hookean model to capture the mechanical response of some nonlinear materials is well known [76]. For large strain, the Neo-Hookean material may undergo a relaxation and thus become easier to deform. Therefore, another strain energy model has to be considered for the modeling of breast compression.

5.1.3 Gent strain energy function

Given that the Neo-Hookean strain energy function provides a poor estimation for large strains, the Gent strain energy function (see Section 2.1.4.a) could be used as an alternative model. The Gent function is characterized by three parameters (μ , K , and J_m). For small strains, it approximates the Neo-Hookean model [21]. For large strains, the J_m parameter acts as a stiffening parameter and defines the upper limit of the first invariant of the left Cauchy-Green deformation tensor (Figure 5.3.a). When $J_m \rightarrow \infty$, the Gent model is reduced to the Neo-Hookean model even for large strains (Figure 5.3.a).

These properties are particularly interesting for our simulation framework. In Chapter 3, the material properties have been estimated and validated for multi-loading gravity simulations. Therefore, the tissues mechanical behavior is well estimated for relatively small strains. The strain due to breast compression is significantly larger than the one due to gravity loading. In this respect, the J_m parameter may be estimated such that, for relative small strains, the Gent model remains equivalent to the Neo-Hookean model. However for larger strains, the energy function will behave asymptotically to approach a compression force equivalent to the standard compression force (Figure 5.3.b). Then, only the third parameter of the energy function has to be estimated (J_m), the initial shear modulus (μ) and the Bulk modulus (K) being already known from the multi-loading gravity

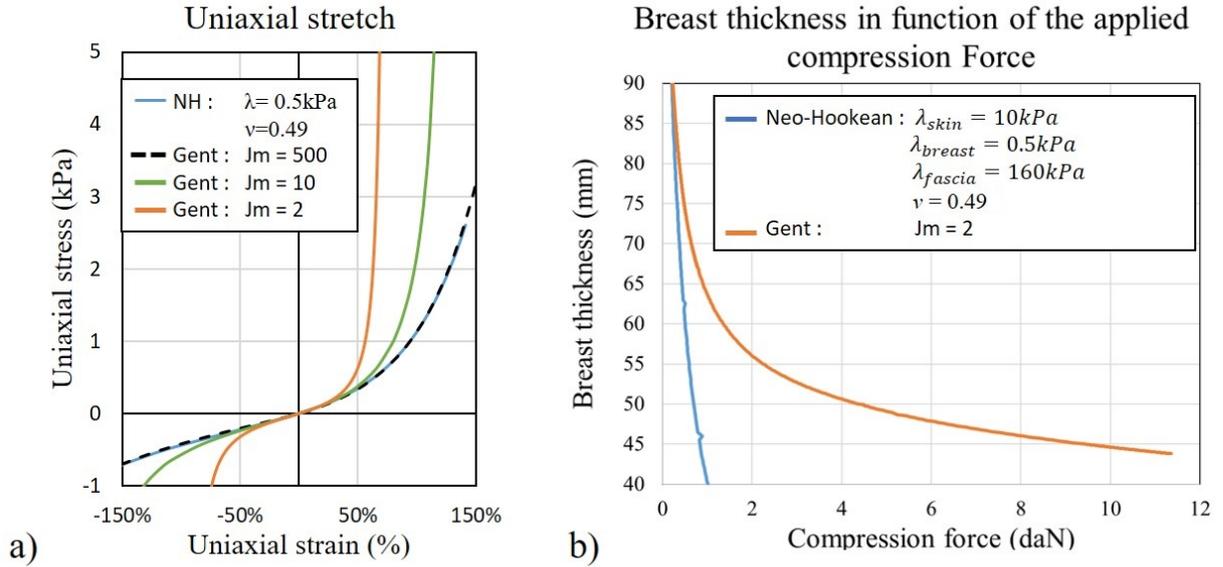


Figure 5.3: a) Stress-strain relation for Neo-Hookean and Gent energy functions; b) Breast flattening curve as function of the applied force for a Gent energy function.

optimization process.

Figure 5.3.b shows the breast flattening curve as function of the applied force when using Neo-Hookean and Gent material models. One can see that, when using the Gent model the curve shape is closer to the results described by Groot and colleagues [32] from experimental data on real patients. Moreover, for a breast thickness of 45 mm, the compression force obtained with the Gent material model is 10 times higher than the one obtained with the Neo-Hookean material model, i.e. 10 N versus 100 N (Figure 5.3). The Gent model definitively provides more realistic simulation results. Therefore, in the next section, the constitutive parameters of the Gent function will be estimated in order to improve breast compression mechanical behavior for both breast models.

5.1.4 Updated material constitutive models

We have seen that a Neo-Hookean model can not describe correctly the breast mechanics under compression. The force needed to flatten the breast during simulation was too small when compared to the mean compression force measured in mammography. The Gent model performed better, giving a more realistic breast flattening curve as function of the applied force (Figure 5.3). Therefore, to compute tissue deformations under compression, the Gent energy function was used.

For the following, the compression simulations were performed on the right breast only. The constitutive parameters for the Gent energy strain function were chosen as follows. For the first volunteer the tissues mechanical properties have already been estimated. Therefore the equivalent Young's modulus of each tissue was kept as defined by the multi-

loading gravity simulations ($\lambda_{breast}^r = 0.3kPa$, $\lambda_{muscle} = 10kPa$, $\lambda_{skin} = 4kPa$, $\lambda_{fascia} = 120kPa$). For the second volunteer, the constitutive parameters are unknown. However, in order to build up a new mechanical behavior, different from the first volunteer, the equivalent Young's modulus as described in the literature can be used. The appropriate values were selected among studies which have provided an in-vivo parameters estimation within similar frameworks ($\lambda_{breast}^r = 0.5kPa$, $\lambda_{muscle} = 10kPa$, $\lambda_{skin} = 10kPa$, $\lambda_{fascia} = 160kPa$) [65, 118, 56]. While the first model represents a small breast volume with soft tissues, the second model represents a large breast volume with stiff tissues.

To estimate the J_m parameter, additional information was needed. To this end, the subjects were asked to provide the data from their most recent mammogram. Several compression simulations were performed to estimate the J_m value that gives the compression force and the breast thickness as measured during the mammography exam (Table 3.1). The Poisson ratio for these simulations was changed to 0.499 (nearly incompressible material allowing a better convergence of the simulations). According to the sensitivity analysis performed in Chapter 3, this change does not significantly impact the mechanics of the small breast volume in the multi-loading gravity framework. For the first volunteer, a breast thickness of $46mm$ with a compression force of $22N$ is obtained with $J_m = 1$. For the second volunteer, a breast thickness of $48mm$ with a compression force of $95N$ is obtained with $J_m = 2$.

Figure 5.4 shows the breast flattening curve as function of the applied force obtained with rigid and flex paddle models. All simulations were performed with the Gent strain energy function.

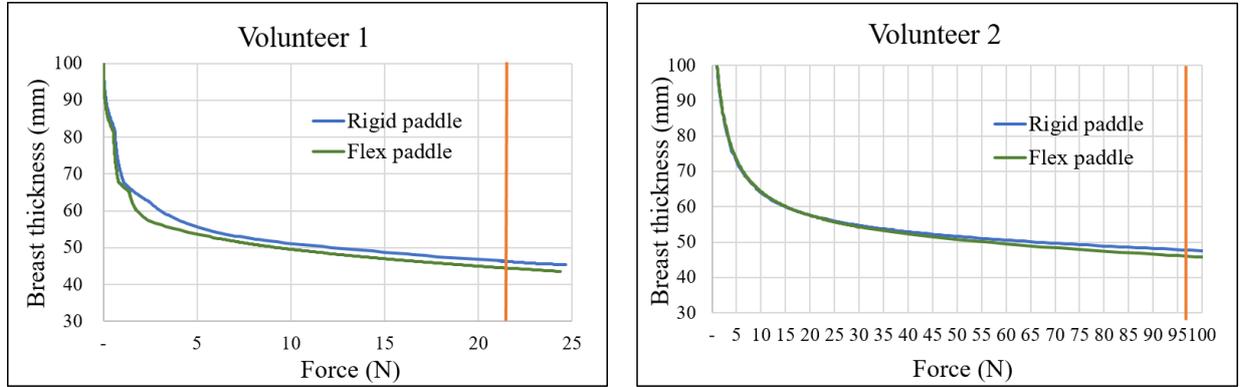


Figure 5.4: Resulting breast flattening curve as function of the compression force with Gent constitutive model. The orange line shows the breast thickness corresponding to the target compression force measured during mammography.

One can see that the compression force range is comparable with the one measured during mammography. Moreover, the curve behavior is similar with the one given by Groot et al [32], with an asymptotic behavior at the end of breast compression.

In this section, it was assumed that introducing a Gent strain energy function will have a non-significant impact on breast mechanics under gravity loading since the Neo-Hookean

and the Gent models have similar behaviors for small deformations. Therefore we can consider that the previous optimization process performed on the breast volume of the first volunteer remains valid.

5.1.5 Gent model and breast mechanics under gravity loading

When looking back to the Gent function properties, an appropriate J_m parameter was defined as following. The J_m value has to be small enough in order to obtain an appropriate compression force. In the same time, it has to be high enough in order to preserve the fidelity of the model to the gravity loading deformations computed with a Neo-Hookean material.

In Chapter 3, the biomechanical breast model corresponding to the first volunteer was evaluated for Neo-Hookean material models. The worst estimate was found in supine tilted configuration due to the tissues oversliding on the lateral direction (maximal distance of 26.03 mm). Introducing Gent tissues model should not impact the breast deformation under gravity loading. However, when looking at the supine tilted configuration simulated with Neo-Hookean material, large deformations were observed at the fascia and skin surfaces. Figure 5.5 shows the strain distributions in supine, prone and supine tilted configurations obtained with Neo-Hookean material models. The strain for the skin and fascia surfaces in supine tilted configuration were twice as large as those observed in the supine and prone configurations. Therefore, considering the Gent model in the multi-loading gravity simulations may improve the supine tilted estimate by reducing the fascia and skin deformations under large strains.

Several simulations were performed considering $J_m = 1$, as identified during the compression simulations. However this value seems to constrain too much the tissues deformation in prone and supine configurations. It will be shown that the compression force is highly dependent on the paddle positioning with respect to the chest wall (Section 5.4.2). For an accurate estimation of the parameter J_m , more data is needed concerning the paddle position during compression. In our study, the paddle position with respect to the chest wall was not available. Therefore, the estimated J_m value is only an approximation and does not characterize completely the subject breast mechanics.

When the multi-loading gravity simulations were performed using a Gent model with $J_m = 2$, better estimates were obtained. In this respect, to show the impact of using a Gent model within multi-loading gravity simulations, the parameter J_m of all involved tissues was set to 2. Figure 5.6 shows the corresponding strain distributions over the skin and fascia surfaces. The maximal strain does not differ significantly in supine and prone configurations (less than 10% of difference). On the other hand, important differences were observed over the left breast in supine tilted configuration. The maximal strain decreased by about 30% over the fascia surface and by about 26% over the skin surface. As previously described, these tissues provide the breast support, accordingly, the lateral displacement of the left breast was reduced.

The estimates of breast external geometry in the three configurations computed using the Gent material models are presented in Figure 5.7. One may see that the breast

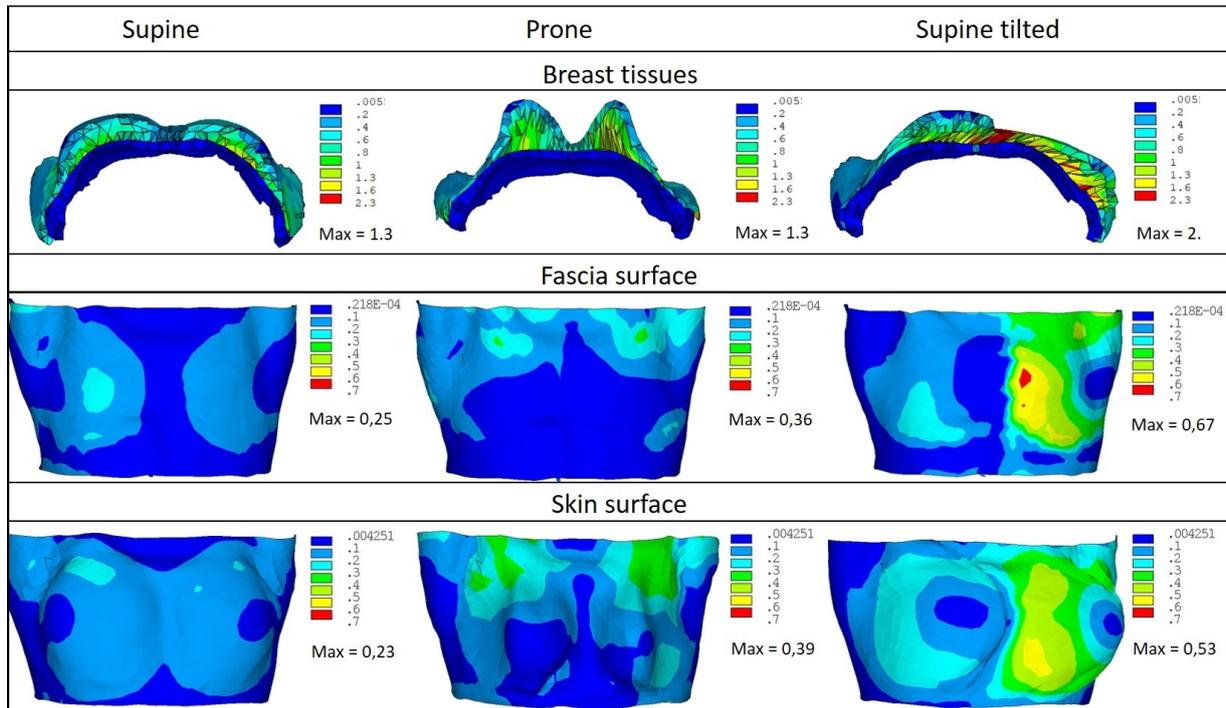


Figure 5.5: Strain distribution when using a Neo-Hookean material model.

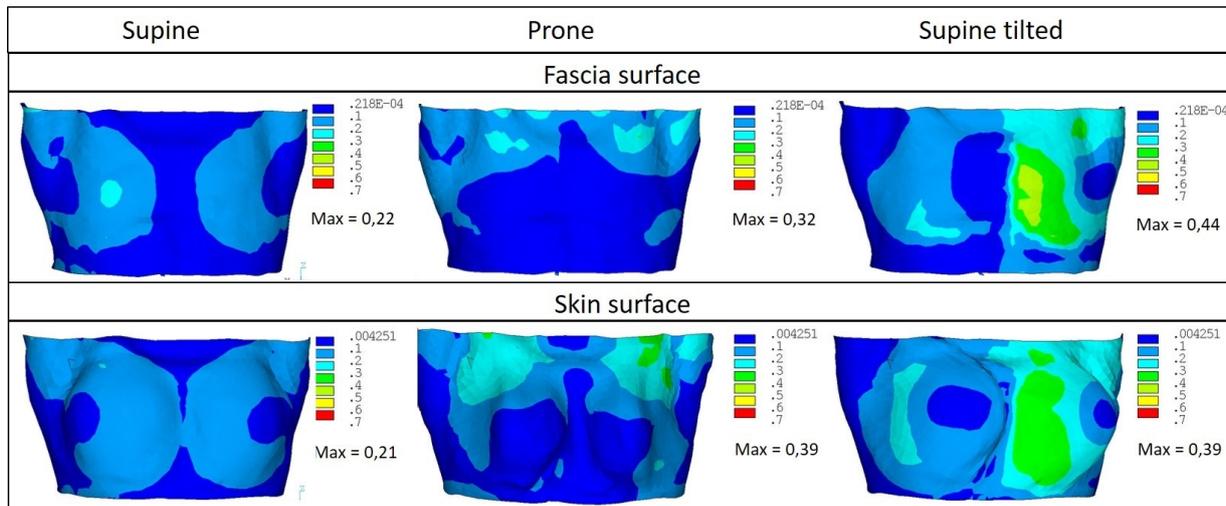


Figure 5.6: Strain distribution when using a Gent material model.

deformations in supine and prone configurations remain on the same range of precision. The Hausdorff distance being increased by only 0.46 mm and 0.6 mm respectively (maximal distance by 0.17 mm and 0.93 mm respectively). Contrariwise, the sliding of the left breast was significantly reduced. Even if the Hausdorff distance was reduced by only 1 mm (5.15 mm with Gent models versus 6.14 with Neo-Hookean models), a significant decrease

of 10 mm in maximal distance was observed. Moreover, smaller deformations imply also better solution convergence.

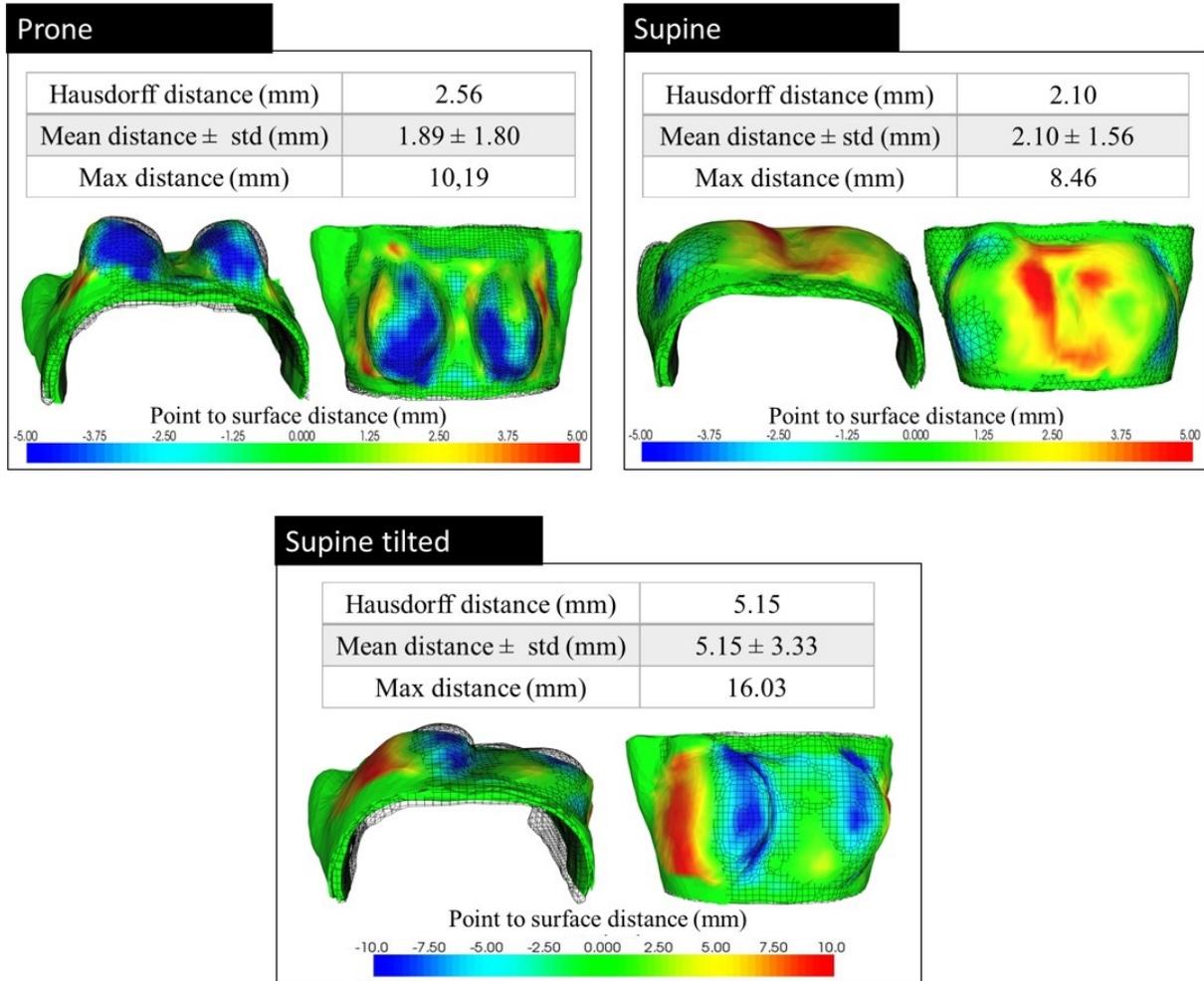


Figure 5.7: Difference between estimated and measured breast surfaces, in supine, prone and supine tilted configurations obtained with a Gent material model.

Using the Gent model improved the overall performance of the breast biomechanical model. However, different values of parameter J_m were used to simulate breast deformations under compression and under gravity loading. A more detailed study is needed to find appropriate constitutive parameters characterizing a wider panel of breast deformations.

In this chapter we assumed a constant value of J_m for all involved hyperelastic material models, while their mechanical response under large stresses are different. A variable J_m parameter within tissues types may improve model accuracy. On the other hand, it also implies an optimization process with more constitutive parameters. An optimization process with a higher number of variables is also more expensive in terms of data and time resources.

For the breast compression simulations presented below the parameter J_m for the first volunteer was set to 1. This assumption satisfies the thickness-force relation obtained during the mammography exam.

5.2 Simulation of digital images

Once the compression simulations were performed, the compressed breast geometry was extracted and used to create numerical object defined by the means of a surface meshes, also named numerical phantoms. These objects were used as input for the CatSim environment able to simulate a digital mammography acquisition [31, 33]. The simulated images were used to assess the image quality as function of the compression paddle design.

5.2.1 Physical characteristics

The X-ray projections of phantom objects were simulated using a GE Senographe Pristina system topology (Figure 5.8). The focal spot was modeled as a point source. A 24 keV mono-energetic X-ray beam was considered. This beam quality is similar to the effective X-ray energy of a 34 kVp Rh/Ag target/filter spectrum filtered by a 46 mm compressed breast. Spreading of the light photons in the CsI scintillator of the detector was modeled by filtering the detected X-ray beam by an empirically assessed modulation transfer function of the cesium iodide (CsI) scintillator. X-ray scatter from the test object and other system components were not included in the simulation. Quantum noise, modeled by a Poisson random distribution, was considered as the only noise source. The simulated X-ray flux was tuned to match the average signal intensity ($\langle SI \rangle$) and signal-to-noise ratio (SNR) measured in real images of a 46 mm thick, 20% fibroglandular equivalent phantom acquired with the automatic exposure control. To do so, a calibration was performed on a real Senographe Pristina mammography unit.

5.2.2 Breast phantom objects

The phantoms were created by first extracting the compressed breast external shape. Then, a set of virtual microcalcifications ($\mu calc$) was inserted into each compressed breast volume. The smallest breast volume contains 21 microcalcifications arranged in a matrix of 7 rows and 3 columns (Figure 5.9.a). The largest breast volume contains 56 microcalcifications arranged in a matrix of 7 rows and 8 columns. The matrix of $\mu calc$ was parallel with the entrance surface of the image receptor and was positioned at the breast mid thickness (Figure 5.9.b). The distance between two consecutive columns or rows was equal to 10 mm. The anatomical background was assumed to be a uniform breast-equivalent material composed of glandular/adipose tissue with a 20/80 ratio. Two simulations were performed for each compression considering microcalcifications of 0.2 mm and 0.3 mm in diameter.

Microcalcifications were simulated as round-shaped surface mesh. To add irregularities, initially spherical objects were randomly deformed. Their X-ray attenuation properties

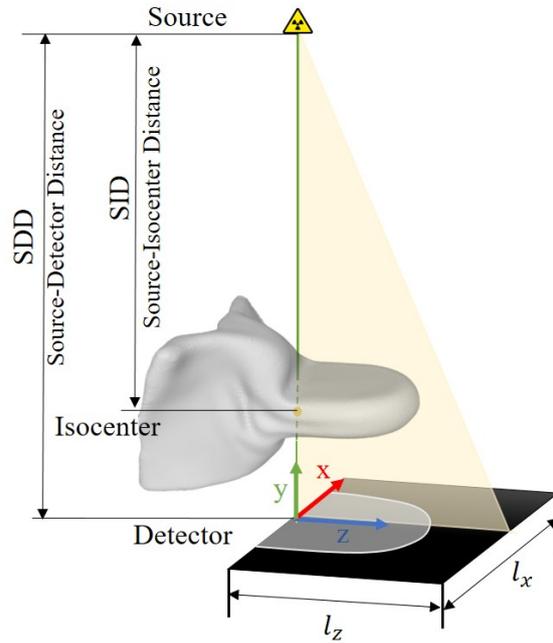


Figure 5.8: A schematic illustration of the simulated GE Senographe PristinaTM mammography unit.

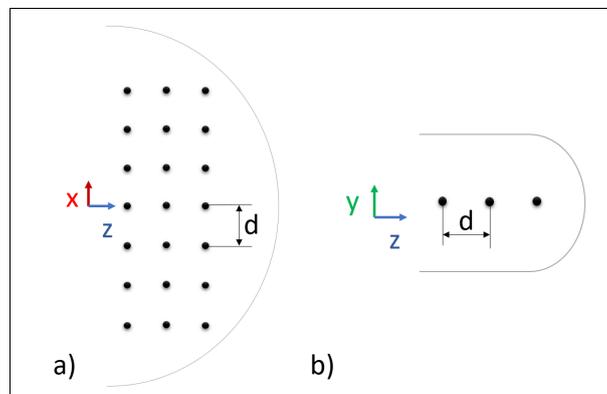


Figure 5.9: Microcalcification distribution over the smallest breast volume ($d = 10mm$): a) axial view, b) sagittal view.

were chosen to correspond with the attenuation of aluminium (Al) at $24 keV$, their volumetric mass density correspond to 60% of the Al density (i.e. $1.63 \frac{kg}{m^3}$). The choice of $24 keV$ corresponds to the photon energy of the X-ray source used in our study.

5.3 Compression quality metrics

The measures used to quantify the three criteria characterizing the quality of breast compression (patient comfort, image quality and average glandular dose) are described in the following section.

5.3.1 Patient comfort

Today, pain estimation and quantification still remain an open question. The perceived pain during mammography, or its interpretation, may depend on the social status, pain history or psychological condition of the patient. But it also depends on physical parameters such as compression force, amount of strain or pressure at skin surface. In clinical studies, the patient comfort is assessed using pain scales. The repeatability of such methods is questionable, because they are based on the patient own interpretation and expertise. More quantitative measures such as pupil dilatation or heart beat rate are interesting in assessing the patient comfort; however they may indicate not only the pain but also the fear of pain.

In this work, only physical pain associated with tissues deformations was considered. In this scope, the maximal strain and stress intensities as well as the maximal pressure intensity at the contact surface were chosen as pain quantifiers. Their distribution over the breast volume were obtained from FE simulations of breast compression performed with Ansys software and were analysed in order to compare the patient experience between two distinct compression systems.

In Ansys software, the theory of large strain computations is addressed by using the Hencky strain tensor (see section 2.1.1). The strain intensity is defined as a function of the three principal strains $\varepsilon_1, \varepsilon_2, \varepsilon_3$

$$\varepsilon_{Int} = MAX(|\varepsilon_1 - \varepsilon_2|, |\varepsilon_2 - \varepsilon_3|, |\varepsilon_3 - \varepsilon_1|). \quad (5.1)$$

The principal strains are computed from the Hencky strain tensor components ε_{ij} using the cubic equation:

$$\begin{vmatrix} \varepsilon_x - \varepsilon_0 & \frac{1}{2}\varepsilon_{xy} & \frac{1}{2}\varepsilon_{xz} \\ \frac{1}{2}\varepsilon_{xy} & \varepsilon_y - \varepsilon_0 & \frac{1}{2}\varepsilon_{yz} \\ \frac{1}{2}\varepsilon_{xz} & \frac{1}{2}\varepsilon_{yz} & \varepsilon_z - \varepsilon_0 \end{vmatrix} = 0. \quad (5.2)$$

The principal strains are the three roots of the equation and are ordered so that ε_1 is the most positive and ε_3 is the most negative.

Similarly, the stress intensity σ_{Int} is computed from the Cauchy stress tensor (see Section 2.1.2) using the three principal stresses

$$\sigma_{Int} = MAX(|\sigma_1 - \sigma_2|, |\sigma_2 - \sigma_3|, |\sigma_3 - \sigma_1|) \quad (5.3)$$

where $\sigma_1, \sigma_2, \sigma_3$ are the roots of the equation

$$\begin{vmatrix} \sigma_x - \sigma_0 & \frac{1}{2}\sigma_{xy} & \frac{1}{2}\sigma_{xz} \\ \frac{1}{2}\sigma_{xy} & \sigma_y - \frac{1}{2}\sigma_{xz} & \frac{1}{2}\sigma_{yz} \\ \frac{1}{2}\sigma_{xz} & \frac{1}{2}\sigma_{yz} & \sigma_z - \sigma_0 \end{vmatrix} = 0. \quad (5.4)$$

5.3.2 Image quality

To assess image quality, the signal-difference-to-noise ratio (SDNR) and the signal-to-noise ratio (SNR) were measured in the raw simulated images. To this end, squared ROIs of $1\text{cm} \times 1\text{cm}$ were defined centered on the μcalc s position. The pixels inside of each ROI were divided into two sets. Pixels located at the ROI's center within a radius equal to the radius of the μcalc s represent the μcalc s attenuated signal intensity ($SI_{\mu\text{calc}}$). Pixels located within the ROI but outside the μcalc radius represent the background signal intensity (SI_{back}). The two sets were used to compute the average detected signal per μcalc s pixel ($\langle SI_{\mu\text{calc}} \rangle$), the average detected signal per background pixel ($\langle SI_{\text{back}} \rangle$) and the standard deviation in the background signal intensity σ_{back} :

$$\langle SI_{\mu\text{calc}} \rangle = \frac{1}{|SI_{\mu\text{calc}}|} \sum_{p_i \in SI_{\mu\text{calc}}} p_i \quad (5.5)$$

$$\langle SI_{\text{back}} \rangle = \frac{1}{|SI_{\text{back}}|} \sum_{p_i \in SI_{\text{back}}} p_i \quad (5.6)$$

$$\sigma_{\text{back}} = \sqrt{\frac{1}{|SI_{\text{back}}|} \sum_{p_i \in SI_{\text{back}}} (p_i - \langle SI_{\text{back}} \rangle)^2} \quad (5.7)$$

where $|\cdot|$ is the number of pixels in the respective set.

The SDNR per pixel of the inserted microcalcifications is defined as follows

$$SDNR = \frac{\langle SI_{\text{back}} \rangle - \langle SI_{\mu\text{calc}} \rangle}{\sigma_{\text{back}}}, \quad (5.8)$$

The SNR per background pixel was defined as follows

$$SNR = \frac{\langle SI_{\text{back}} \rangle}{\sigma_{\text{back}}}. \quad (5.9)$$

5.3.3 Average glandular dose

The estimation of the dose delivered to the glandular tissue remains an essential component of quality control in X-ray mammography. We derived the average glandular dose (AGD) using the approach proposed by Dance D. [30] regardless the paddle type. The method uses conversion factors to relate measurements of the incident air kerma K at the upper surface of the breast to the AGD.

$$AGD = K gcs \quad (5.10)$$

where g is the factor allowing to convert air kerma to AGD considering a breast with 50% glandularity, c addresses any difference in breast composition from this 50% glandularity and s accounts for the X-ray spectrum under consideration. Dance et al. used Monte-Carlo simulation to estimate these factors by modeling the compressed breast as a semi-circular cross section cylinder. The s -factor for the recently introduced Rh/Ag target/filter spectrum was provided to us by D. Dance and has not been published yet.

The considered cross section cylinder has a uniform thickness, meanwhile the compressed breast thickness varies due to paddle elasticity (SRP) and paddle flexibility (SFP). Therefore, in a clinical framework, the breast thickness is adjusted by applying an offset characterizing the paddle deflection during compression.

For the rigid paddle model, as paddle elasticity was neglected, the AGD was computed assuming the breast thickness is equal to the distance between the image receptor and the paddle itself. Regarding the flex paddle, the breast thickness decreases quasi-linearly from the chest wall to the nipple. Thus, breast thickness was computed as the mean of the maximal and minimal distance over the breast contact area.

5.4 Results

Two studies were performed using the previously defined components for modeling the breast compression and simulating digital mammography. First, the results of a comparative study between flex and rigid paddles is presented with the effects on image quality, AGD and patient comfort. Then, the impact of paddle positioning on breast mechanics is analysed.

5.4.1 Compression quality for rigid and flex paddles

To compare the breast compression quality when using a standard rigid paddle against a standard flex paddle, the rigid and flex paddle models were used. The right breasts of the two volunteers were first compressed until the target compression force measured during mammography was obtained (Table 3.1). Then, the breast phantoms with $\mu calc$ were imported into CatSim environment and mammography images were simulated. The compression quality was measured in terms of image quality, AGD and patient comfort.

The resulting average breast thickness after compression varies by less than $2mm$ between rigid and flex paddles for both volunteers (Table 5.10). Accordingly, small AGD differences were found and namely dose reductions of 2.6% for the smaller breast and 4.2% for the larger breast were observed in favor of the flex paddle.

The SNR and SDNR have been estimated and compared between flex and rigid paddles. When using a flex paddle instead of a rigid paddle on the largest breast (volunteer 2), we observed a statistically significant higher SNR. We did not observe statistically significant differences on SDNR for both $200\mu m$ and $300\mu m$ microcalcifications, when using rigid or flex paddle. Therefore, despite a breast thickness varying linearly from chest wall to

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	Rigid Paddle		Flex Paddle		p-Values	Rigid Paddle		Flex Paddle		p-Values
	Mean SNR	StdDev SNR	Mean SNR	StdDev SNR		BNT (mm)	AGD (mGy)	BNT (mm)	AGD (mGy)	
Volunteer 1	82.90	43.09	83.70	37.72	0.706	46	1.15	44	1.12	
Volunteer 2	126.89	8.75	137.21	10.73	0.000	48	1.20	46	1.15	

	$\mu\text{calc diameter} = 200 \mu\text{m}$					$\mu\text{calc diameter} = 300 \mu\text{m}$				
	Rigid Paddle		Flex Paddle		p-Values	Rigid Paddle		Flex Paddle		p-Values
	Mean SDNR	StdDev SDNR	Mean SDNR	StdDev SDNR		Mean SDNR	StdDev SDNR	Mean SDNR	StdDev SDNR	
Volunteer 1	0.74	0.68	0.79	0.54	0.689	2.01	1.28	1.85	1.02	0.224
Volunteer 2	1.14	0.57	1.13	0.53	0.885	2.96	0.76	3.15	0.92	0.093

Figure 5.10: Breast nominal thickness (BNT), average glandular dose (AGD), signal-to-noise-ratio (SNR) and signal-difference-to-noise (SDNR) for both volunteers and both compression paddle types

nipple when the flex compression paddle is used, the image quality is preserved or improved compared to the image quality obtained with the rigid compression paddle.

In a clinical study, Broeders et al. [14] have also compared the image quality and patient comfort between the standard rigid and flex paddles. According to the authors, the standard flex paddle performed slightly better image quality in the projected breast area, however it moved breast tissue from the image area at chest wall side. According to our compression simulation, for the small breast volume, no difference in tissues lateral displacement was observed. On the other hand, for the larger breast, using the flex paddle indeed increased the tissues displacement toward the chest wall side, but not by more than 4 mm (Figure 5.11).

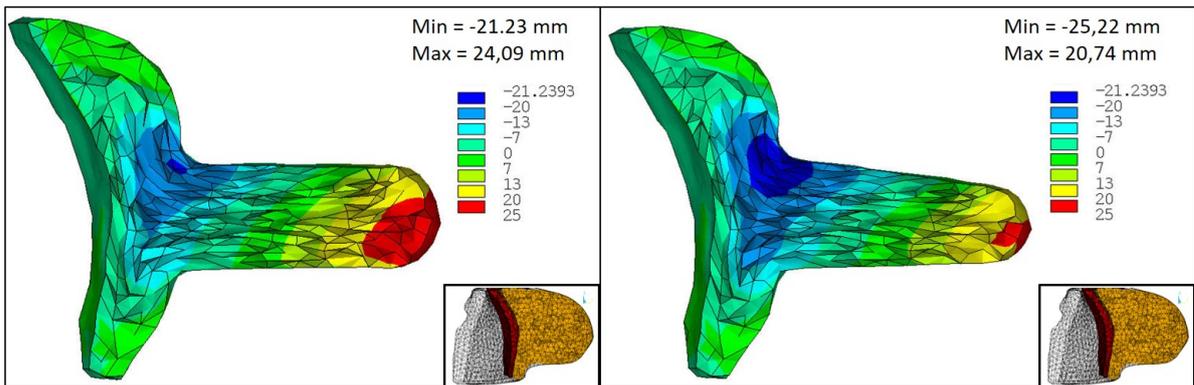


Figure 5.11: Node displacements on the direction parallel to the paddle (O_y axis). Left hand side - rigid paddle, right hand side flex paddle.

To assess the patient comfort during compression, the resulting internal stress and strain distributions, as well as the contact pressure maps were derived. These data were collected at the target compressive forces as measured during mammography: 22 N for the

first volunteer (Figure 5.12) and 95 N for the second one (Figure 5.13).

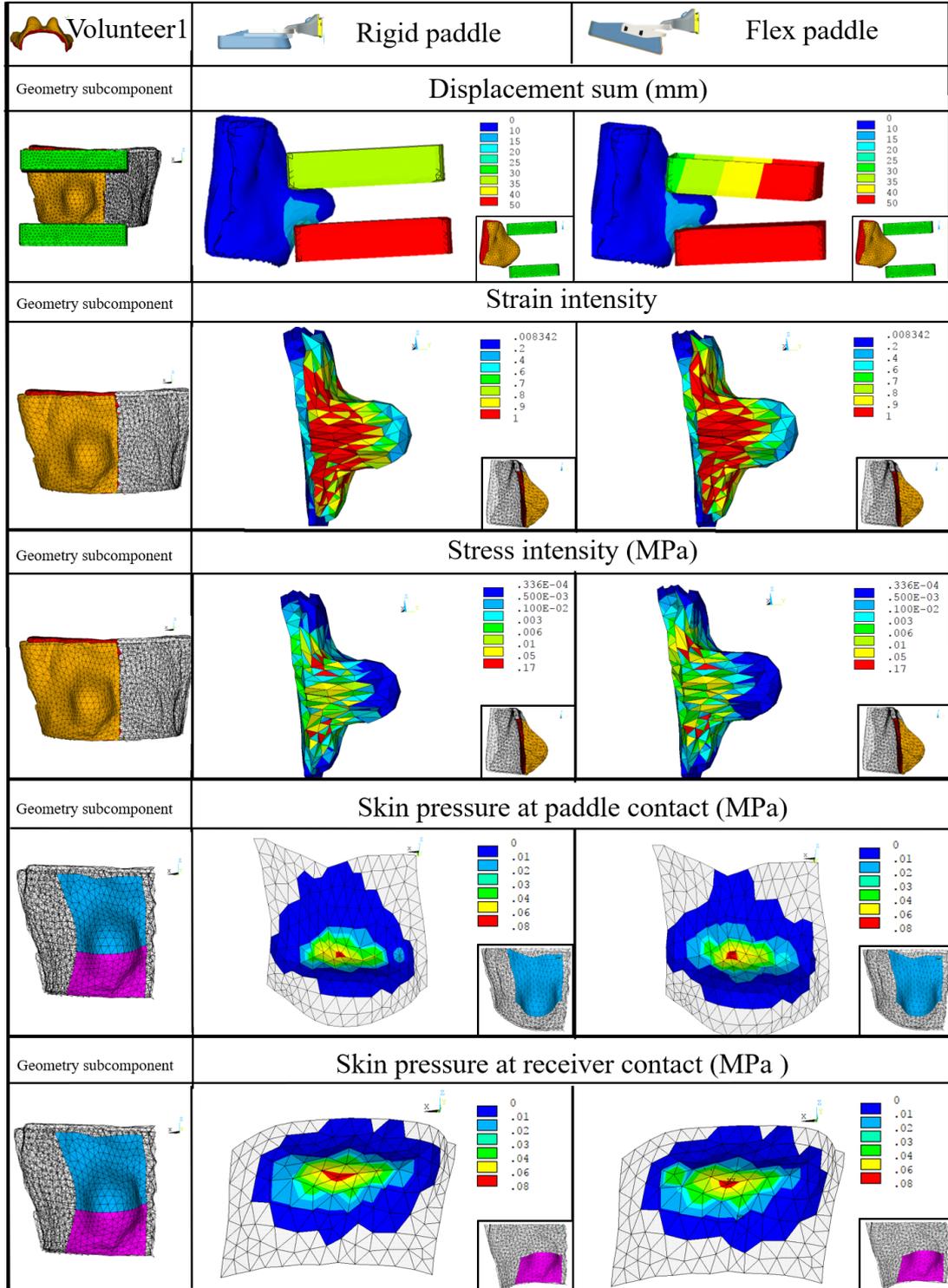


Figure 5.12: Stress, strain and contact pressure distributions for the first volunteer

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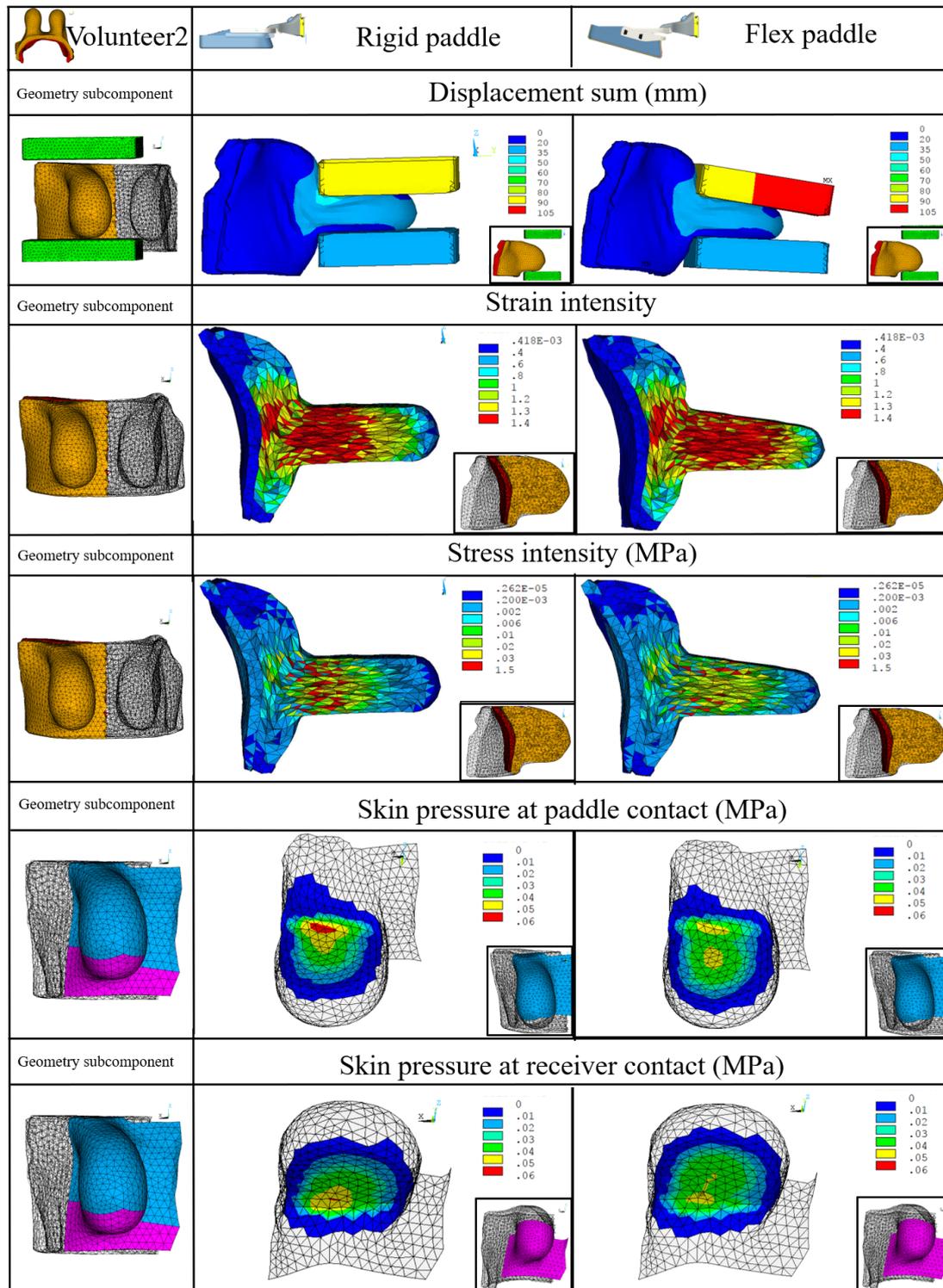


Figure 5.13: Stress, strain and contact pressure distributions for the second volunteer

Regarding the smallest breast volume (Figure 5.12), there is no significant difference

between FPM and RPM in pressure distribution over the skin surface or in internal stress/strain intensity distributions. For both compression paddles, high pressure at the skin surface is concentrated in the juxtathoracic region with a maximum pressure of 77.7 *kPa*. In addition, the FE simulations confirm that in small breasts the paddle tilt is too small to impact the tissues compression in the middle part of the breast. FPM applied on larger breast volumes (Figure 5.13) results in significantly lower intensities of pressure at the skin surface in contact with the compression paddle, with a maximal pressure of 37 *kPa*, compared to 56 *kPa* when using RPM. No significant differences in the measured maximal intensities of strain and stress were observed, however strain and stress distributions were different. When the breast was compressed with a rigid paddle, maximal strain and stress were concentrated in the retromammary space and decrease considerably toward the nipple. When a flex paddle was used, stress and strain were more uniformly distributed over the breast volume with the highest values in the middle third of the breast.

The area pressure distribution patterns have already been demonstrated in the work by Dustler et al. [37]. The authors have studied the pressure distribution patterns of 103 women undergoing breast compression with a rigid paddle at different compression levels. Four groups were differentiated: a) skin pressure widespread over the breast (29%); b) skin pressure concentrated on the central part of the breast (8%); c) skin pressure concentrated on the juxtathoracic region (16%); d) skin pressure concentrated along a narrow zone at the juxtathoracic region (26%). The pressure distribution patterns observed for our first and second volunteers correspond to the group d).

5.4.2 Paddle positioning impact on compression mechanics

A second study was performed in order to assess the paddle positioning impact on the compression force. The simulations were performed only on the right breast of the second volunteer. Indeed, the geometry of the first volunteer is too small to allow simulation with various paddle positions with respect to the chest wall.

Using the rigid paddle model to perform compressions with different paddle position with respect to the thoracic cage (thoracic cage to paddle distance TPD, Figure 5.15) generated large convergence problems. For example, when the paddle was positioned closer to the chest wall, the finite elements were distorted because of high contact pressure at the juxtathoracic are. Therefore, for further investigations, the elastic paddle model was used. This model is closer to the mechanical properties of the standard rigid paddle from a mammography unit. In addition, material elasticity allows a slight paddle bending which seems to reduce elements' distortions.

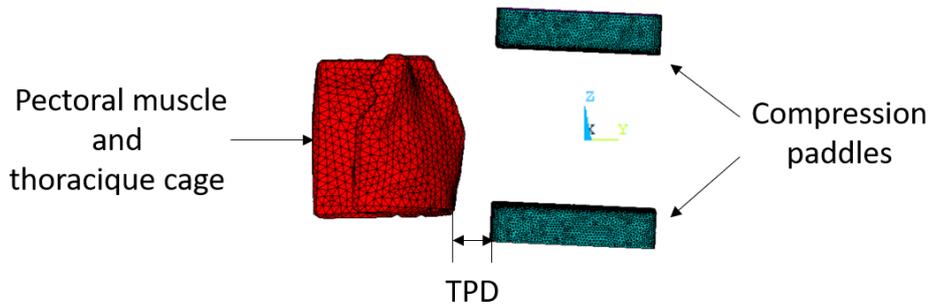


Figure 5.14: Thoracic cage to paddle distance (TPD).

The breast was compressed until a minimal thickness of 50mm was reached. Then, the compression force as well as surface pressure at the contact with the compression paddle were compared. The compression force was computed as the product between the mean surface pressure and the contact area $\langle P_{contact} \rangle * A_{contact}$.

Figure 5.15 shows the strain/stress as well as the pressure distributions over the contact area for three distinct distances between the thoracic cage and the paddle (TPD). The compression force varies considerably within paddle positions. A compression force of 59 N , 94 N and 158 N was obtained when the paddle was positioned at a distance from the chest wall of 48 mm , 40 mm and 33 mm respectively. Positioning the paddle 15 mm closer to the chest wall tripled the force intensity.

Due to the paddle elasticity, the breast thickness slightly varies, with a maximal deflection equal to 3.5 mm (Figure 5.15 first line). A very small difference between the maximal paddle deflection ($\sim 1\text{ mm}$) was observed between the previous three compressions. Thus, image quality or AGD were not significantly impacted by the breast thickness variation. However, the wider the space between the chest wall and the compression paddle, the fewer breast tissues in the projected mammography image. In a standard framework, the

Subject 2 : Elastic paddle 

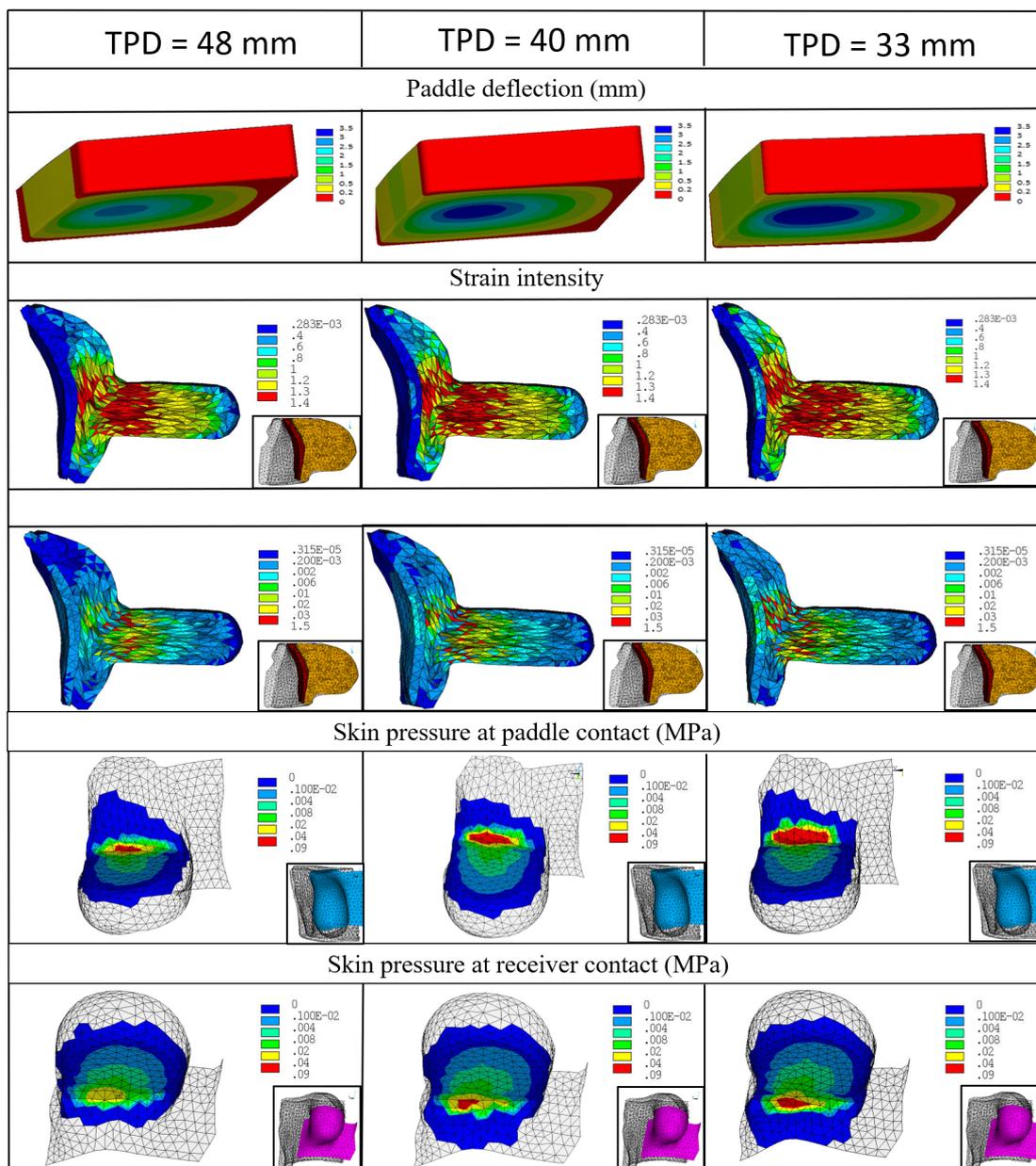


Figure 5.15: Stress, strain and contact pressure distributions for a variable thoracic cage to paddle distance (TPD).

technologist will include as much breast tissues as possible in order to reduce the risk of missing a suspicious lesion.

When looking at the strain distribution, one can see that, when the compression paddle is positioned closer to the chest wall, the juxtathoracic soft tissue undergoes higher deformation resulting also in a higher stress intensity. Concerning the skin surface pressure dis-

tribution, the highest intensities ($\sim 90 \text{ kPa}$) are always concentrated in the juxtathoracic area. However, for a thorax to paddle distance equal to 33 mm , the area corresponding to the high pressure is considerably larger. This means that a significant part of the total force was used to compress the tissues in the juxtathoracic area only, which may increase the patient discomfort.

5.5 Discussion and conclusion

In this chapter, the breast compression was simulated using models of three paddles, the rigid, flex and elastic models. In order to comply with the compression mechanics as described in literature, an update of the tissues constitutive models was needed. Applying the Gent form of strain-energy potential, instead of the Neo-Hookean form, allowed to obtain compression force magnitudes comparable with the real subject data. However, when the same law is used to perform the multi-loading gravity simulations, the breast deformations in supine and prone configurations are over-constrained. We found that, with a larger value of J_m parameter, the Gent model may improve the breast geometry estimates obtained with a Neo-Hookean model. In conclusion, the estimated value of J_m does not characterize the subject-specific mechanical properties and gives only an estimation of a standard behaviour. Our second study shows that, to obtain a proper estimation of parameter J_m , more information like the paddle position with respect to the breast volume is needed.

The patient comfort (measured as strain and stress) as well as the image quality (measured as SNR, SDNR) and AGD were compared for breast compression with rigid and flex paddles. The results from the two volunteers were analysed. The compression simulations indicate that, for the smallest breast, there is no significant difference for the patient perceived pain when using the rigid or the flex paddles. We did not observe any statistically significant difference in SNR or SDNR for microcalcification of any size. Therefore, our results suggest that using a flex paddle should not significantly impact image quality and delivered dose in small breasts and should not reduce significantly the perceived pain. For the largest breast, our simulations indicate that using a flex paddle may reduce the maximal pressure intensity on the skin surface by about 30% compared to the rigid paddle. The tissues deformation is more uniformly distributed inside the breast volume, and the highest deformation occurs in the middle breast region corresponding to the supposed location of dense tissues. Moreover, the FE simulations suggest that using the flex paddle to compress the right breast of the second volunteer may have no significant impact on the average glandular dose, but it might improve the resulting image quality.

The impact of paddle positioning on patient comfort and image quality was also addressed. Three paddle positions with respect to the chest wall were studied using the elastic compression paddle. Even if a variable breast thickness is obtained due to the paddles deflection, the variations are too small ($\sim 1 \text{ mm}$) to impact the AGD or the resulting image quality in terms of the SNR or SDNR. However, some authors reported a risk of excluding some retromammary tissues from the imaged area, and consequently information on small

posterior cancerous lesions may be lost. In terms of patient comfort, the simulations have shown that the high pressure are always localized in the juxtathoracic areas. When the paddle is too close to the chest wall, the compression force is mostly dissipated on this narrow area resulting in very high pressures compared to the skin pressure over the breast ($90kPa$ vs $10kPa$).

CONCLUSION AND PERSPECTIVES

The main aim of this PhD work was to develop a simulation framework capable of assessing breast compression as a function of paddle design, compression force or breast positioning. Image quality, average glandular dose as well as patient comfort were considered when comparing different compression strategies.

A simulation software was used to compute the X-ray propagation through matter and to generate simulated mammography images. The image quality was dependent on the compressed breast thickness. The average glandular dose was computed using the method proposed by Dance et al. [30].

To assess the breast deformations depending on the paddle design or the applied compression force, a new biomechanical breast model was developed. After being evaluated by comparison with real data collected through MR images, this model was used to predict the outer shape of the breast under compression as well as the patient comfort assumed to be associated to internal strain and stress intensities and distributions.

In this chapter, the main results and conclusions on the implemented application are recalled. The possible improvements for a large prospect of applications are discussed.

6.1 Biomechanical breast model

Before modeling the mammography breast compression, the model fidelity to real tissues deformations had to be assessed. In this scope, data sets describing in-vivo breast mechanics were collected. MRI is an interesting imaging modality allowing the extraction of the whole 3D breast geometry with the distribution of each internal structure. MR images of two volunteers in three body positions (prone, supine and supine tilted) were acquired and used in this study. The two volunteers were chosen such that two different breast sizes were represented: small volume (breast cup A) and large volume (breast cup F). The boundary conditions describing breast deformation under gravity loading are easy to reproduce in a simulation framework. Thus, the acquired data made possible the calibration and the evaluation of our biomechanical model.

The development of the biomechanical breast model was performed using the small breast volume (first volunteer). A small breast volume undergoes smaller deformations under gravity loading, thus the corresponding breast model was suspected to lead to less convergence difficulties. To this end, the MRI breast volume of the first volunteer in supine position was used to build the finite element mesh. Then, combined with the MRI breast volume in prone body position, it was used to estimate the subject-specific constitutive parameters and the corresponding stress-free geometry.

From the first performed simulations, the role of sliding boundary conditions at the juncture surface between the pectoral muscle and the breast was pointed out. Indeed, the displacements driven by only tissues' elasticity were not enough to reflect the geometrical changes between the supine and prone breast configurations. Therefore, breast tissues were allowed to slide over the pectoral muscle surface. Additional boundary conditions were considered by modeling the breast suspensory ligaments and fascial system. Including stiffer structures into the finite element model improved solution convergence capabilities. They also allowed to compute the breast deformations for a larger range of soft tissue constitutive parameters.

According to the literature, a well defined breast model has to consider in-vivo measured constitutive parameters. To this end, the tissues Young's moduli giving the best fit between the simulated and measured breast configurations of the first volunteer were computed. The optimal estimates, assuming Neo-Hookean material models, were found to be $\lambda_{breast}^r = 0.3 \text{ kPa}$, $\lambda_{breast}^l = 0.2 \text{ kPa}$, $\lambda_{skin} = 4 \text{ kPa}$ and $\lambda_{fascia} = 120 \text{ kPa}$. The obtained mechanical properties are comparable to the ones proposed in the literature when considering only the breast models with similar simulation frameworks [118, 51, 61]. This result allowed to compute the breast geometry in supine and prone configurations with an accuracy of 1.70 mm and 2.17 mm respectively. The model fidelity to the global breast deformation was evaluated using the breast geometry in supine tilted position. The Hausdorff distance between the breast skin surface extracted from the MRI volume and the simulated skin surface was equal to 6.14 mm . The larger error ($\sim 26.03 \text{ mm}$) was obtained on the left breast where the lateral displacements of the tissues were overestimated due to large strains observed over the fascia and skin surfaces.

These results may be improved by developing a more complex breast support matrix or considering region dependent stiffness for the skin or the fascia system. Adding stiffer materials in the strategically localized areas on the contact surface may limit the fascia' deformations under large strain range. Consequently, the breast tissues sliding in supine tilted configuration may be reduced.

When developing a subject-specific finite element model, the source of error may be both an inaccurate definition of model components or an imprecise model calibration. One may observe that, the objective function used during the model optimization does not properly consider the tissues lateral displacements. The supine and prone breast configurations are not sufficient to describe the soft tissue sliding over the pectoral muscle. Therefore, new information characterizing such breast deformations has to be added. We believe that, considering the supine tilted breast configuration, as a target volume, when performing the optimization of the constitutive parameters, may result in a more accurate estimation of tissues' material models. However, in such case, additional volumes with different breast configurations would be needed to perform the model evaluation. Furthermore, in this work, the similarity between the estimated and measured breast configurations was assessed by computing the minimal distance from the estimated position of each skin node to the measured breast shape. Using only surface measurements does not entirely describe how both the skin surface and the internal tissues deform. During the MRI acquisitions, both volunteers were asked to fix six fiducial landmarks over the breast surface, in order to enable volumes registration. Even if this is difficult, one could envisage to identify internal anatomical landmarks defined by singular structures within breast volume (i.e. clusters of microcalcifications), in order to extend the registration process to internal structures of the breast. Such additional landmarks may bring new information about the internal tissue deformations. In future work, considering this type of information as additional constraints in the calibration process may provide a more realistic estimation of breast mechanical properties. Moreover, including the distance between landmarks location in addition to the distance between breast skin surfaces should also provide a more accurate model evaluation.

After performing the calibration process using the data of the smaller breast volume (first volunteer), the breast biomechanical model was built up for the larger breast volume (second volunteer). However, because of a lack of time, the model calibration process was not performed for this volunteer. In future work, it would be interesting to perform such model optimization and evaluation on more subjects with different breast morphologies and mechanical properties. The model calibration on a larger population should improve its flexibility for further studies on breast compression techniques.

Despite providing good results in the multi-loading gravity framework, the developed breast model turned out to be less reliable in simulating breast compression. With this model, the maximal force needed to simulate breast flattening was estimated to be relatively low when compared to the mean recommended force of a typical mammography exam (10N vs 120N). These low values of the compression force were due to tissue's abnormal softening under large stress rates. Strain-softening from a given stress threshold is a well known phenomenon when using Neo-Hookean materials. We therefore suggested to overcome this

issue by replacing the Neo-Hookean model by a Gent model for all involved hyperelastic tissues.

The stress-strain relations of Gent and Neo-Hookean models are equivalent for low strains. For large strains the Gent material model is stiffening exponentially resulting in an asymptotic behavior, the asymptotic limit being defined by the J_m parameter. These properties allow to change the tissues mechanical response only for large strain, as during breast compression. On the other hand, they also allow to preserve the same mechanical response for relatively small strains as induced by gravity loading simulations.

The breast compression simulations were performed using both breast volumes. As the tissues constitutive parameters of the second volunteer were not optimized, the values proposed by others similar works were used. Therefore, the second breast model does not describe the subject-specific mechanical behavior. However, it provides a new geometrically realistic model that may be used to assess the compression quality of different compression types. The Gent material model improved the tissues mechanical response when the breast is compressed between the paddle and the image receiver. A compression force of 22 N for the first volunteer and 95 N for the second volunteer were obtained to reach the target breast thicknesses, which fits well the measured clinical data (21.9 N and 94.8 N respectively).

Based on the same constitutive parameters, as estimated during breast compression, the Gent tissues model was used to estimate breast deformation under gravity loading for the first volunteer. We found that, with such a model, tissues displacements were over-constrained in both supine and prone configurations. However, we demonstrated that the Gent model may also improve the biomechanical model fidelity to the real deformations under gravity loading. Therefore we suggested to use two different values of the parameter J_m in order to obtain the best estimates for multi-loading gravity and breast compression simulations. A more detailed study has then to be considered in order to estimate a unique tissues constitutive model. To this end, more data describing the breast compression process, such as breast position with respect to paddle, is needed. The impact of using different constitutive parameters within tissues types should also be studied. However, increasing the number of model parameters might increase the complexity of the optimization problem, as well as the computation time and the size of the data set describing the subject breast mechanics.

In this work, we have assumed that the breast mechanics does not depend on the glandular tissues distribution. This assumption is only valid if a global breast deformation is assessed, such as the breast surface deformation. However, when one wants to estimate the breast internal tissues displacements under compression or gravity loading, a more subtle definition of tissues materials is needed. In such a case, the differentiation of the glandular and adipose tissues should be more relevant.

During the modeling process, it has been observed that the breast tissues undergo extremely large deformations (up to 150%). This involves large convergence difficulties due to bad element formulation during simulations. To improve solution convergence capabilities, an hexahedral adaptive mesh might be considered.

In conclusion, the proposed biomechanical model was able to provide a good estimation

of breast deformation under different boundary conditions. The models based on breast geometries of two subjects were used to perform comparative studies between various compression methods.

6.2 Breast compression and patient comfort

The developed biomechanical breast model together with the image simulation framework were used to assess the clinical compression quality within different compression strategies.

A first study was performed to compare the breast compression quality when using standard rigid or flex paddles. To compute breast compressions, a biomechanical model was built for two breast volumes (small and large) with various mechanical properties (soft and firm). The results showed that, using the flex paddle may improve the patient comfort without affecting the image quality and the delivered average glandular dose. Moreover, despite a breast thickness varying linearly from chest wall to nipple, the image quality seems to be preserved or even improved compared to the image quality obtained with a rigid compression paddle. Such a better image quality obtained when using the flex paddle could be explained by a better overall breast compression. The paddle tilt allows a better compression of the tissues close to the nipple, relaxing the tissues located in the chest wall region. Our simulations tend to confirm that the paddle tilt may displace breast tissues towards the chest wall. The tissues accumulation on the retromammary space may hide clinical relevant information and thus may increase the risk of false negatives.

A second study was performed to assess the impact of breast positioning on breast compression mechanics. This time, the paddle deflection due to its material elastic properties was considered to enable solution convergence when the compression paddle is close to the chest wall. Three breast compression simulations were performed with various distances between the paddle and the chest wall. In this context, only the larger breast volume was used, the smaller volume being not adapted to such a simulation. The results showed that patient comfort can be improved by positioning the paddles further from the pectoral muscle. For an equivalent breast thickness under compression, the compression force decreased from 158 N to 59 N for a difference of 15 mm in the distance from chest wall to paddle. On the other hand, clinical guidelines request to place the paddle as close as possible to the chest wall.

These two preliminary studies have shown that the clinical compression quality can be assessed using such simulation frameworks. The tools designed during this PhD thesis may be used to perform wider studies on existing breast compression systems, but also to provide a first estimation of the performance of a new, not yet implemented, paddle design. Simulation based studies are less expensive in time and materials than the usual clinical studies, therefore they may be used to discharge the less relevant paddle models.

KEY CONTRIBUTIONS

The key contributions concerning the finite element breast modeling are the following:

- We introduced new boundary conditions which reflect the motion of the breast over the thoracic cage. They included sliding contact surface based on Coulombs friction law combined with stiff support structures. To our knowledge, the breast support matrix was considered for the first time into the finite element model. The generic model includes suspensory ligaments together with the fascial system, and was built based on their anatomical description.
- The iterative algorithms allowing to estimate the breast stress-free geometry are generally using only one breast configuration (supine or prone breast configuration). In this work we proposed an optimization algorithm which estimate the breast stress-free geometry starting from supine configuration and then iteratively correct it based on the prone configuration.
- We have a data set of breast MR images in three different body positions of the same volunteer. Therefore, our biomechanical breast model was first calibrated using prone and supine configurations. Then, its mechanical response was evaluated on a third breast configuration (supine tilted). Because of a lack of reliable data, none of previously published biomechanical breast models was evaluated in such wide range of deformations.
- We evaluated the capability of the proposed biomechanical breast model to reproduce the breast compression mechanics as described by several clinical studies. This analysis allowed us to point out the limitations of the Neo-Hookean strain energy function when modeling such large deformations. Accordingly, a new material constitutive model defined by the Gent strain energy function was proposed.
- We developed a simulation framework allowing to quantify breast compression in terms of image quality, average glandular dose and patient comfort. Due to its

modularity, this framework supports different paddle designs and different breast geometries and compositions.

Using previously described tools, two studies assessing the breast compression quality were performed, demonstrating:

- The difference of the compression quality in terms of patient comfort, image quality and average glandular dose between a standard rigid and flex paddles was quantified. We have shown that, for the first volunteer (small breast), there were no differences in maximal intensities of stress, strain or skin pressure between the two paddles. Similarly, for this volunteer, no significant difference was found between the computed signal to noise ration or signal difference to noise ratio. However, using the flex paddle to compress the right breast of the second volunteer (large breast) have decreased the skin pressure intensity without affecting the signal difference to noise ratio or the average glandular dose.
- The impact of breast positioning on the compression mechanics and patient comfort were analyzed. The obtained results demonstrated that breast positioning has a significant impact on patient comfort. The surface pressure in the juxtathoracic area increased when the paddle was positioned closer to the chest wall.

A list of publications summarizing the results of this work is provided below.

PUBLICATIONS

Mira, A., Payan, Y., Carton, A. K., de Carvalho, P. M., Li, Z., Devauges, V., & Muller, S. (2018, March). Simulation of breast compression using a new biomechanical model. *In Medical Imaging 2018: Physics of Medical Imaging* (Vol. 10573, p. 105735A). International Society for Optics and Photonics.

Mira A., Carton A.K., Muller S. & Payan Y. (2018). Breast biomechanical modeling for compression optimization in digital breast tomosynthesis. *Computer Methods in Biomechanics and Biomedical Engineering*, Lecture Notes in Bioengineering, A. Gefen and D. Weihs editors, pp. 29-35, DOI 10.1007/978 – 3 – 319 – 59764 – 5_4

Mira A., Carton A.K., Muller S. & Payan Y. (2016). Breast biomechanical modeling for compression optimization in digital breast tomosynthesis. *Proceedings of the 22nd Congress of the European Society of Biomechanics (ESB2016)*

Appendices

DISTANCE MEASURES

For the sake of simplicity, only the distance between discrete 3D-surfaces represented by triangular meshes will be defined. A discrete 3D-surface is usually represented by a set of points $S = \{p_1, p_2, \dots, p_n\}$ in \mathbb{R}^3 (vertices), and by a set \mathcal{T} of triangles describing how the vertices from S are linked together. Thus, the similarity between two surfaces is measured by computing distances between the respective point sets. Let define a point p belonging to the surface S , and a point q belonging to the surface S' .

Euclidean distance between two points

The Euclidian distance is defined as the shortest possible path through space between two points (also named the L^2 - norm) and is defined as:

$$D(p, q) = \|p - q\|_2 = (|p_x - q_x|^2 + |p_y - q_y|^2 + |p_z - q_z|^2)^{\frac{1}{2}} \quad (\text{A.1})$$

Node to surface distance

The distance $D'(p, S')$ from the point p to the surface S' is defined as

$$D'(p, S') = \min_{q \in S'} \|p - q\|_2 \quad (\text{A.2})$$

Minimal distance between two surfaces

The minimal distance between two surfaces S and S' is defined as

$$D'_{min}(S, S') = \min_{p \in S} \{D'(p, S')\} \quad (\text{A.3})$$

Maximal distance between two surfaces

The maximal distance between two surfaces S and S' is defined as

$$D'_{max}(S, S') = \max_{p \in S} \{D'(p, S')\} \quad (\text{A.4})$$

Mean distance between two surfaces

The mean distance between two surfaces S and S' is defined as

$$D'_{mean}(S, S') = \frac{1}{|S|} \sum_{p \in S} D'(p, S') \quad (\text{A.5})$$

where $|S|$ is the number of nodes belonging to the surface S .

Hausdorff distance between two surfaces

The Hausdorff distance [74] between two surfaces is defined as

$$H(S, S') = \max\{D'_{max}(S, S'), D'_{max}(S', S)\} \quad (\text{A.6})$$

Modified Hausdorff distance between two surfaces

The modified Hausdorff distance between two surfaces is defined as

$$H'(S, S') = \max\{D'_{mean}(S, S'), D'_{mean}(S', S)\} \quad (\text{A.7})$$

Dubuisson and Jain [35] have studied 24 measures to assess the similarities between two discrete surface meshes. According to the authors, the Hausdorff distance has the best performance for object matching.

MESH CONVERGENCE

In finite element modeling, a finer mesh usually results in a more accurate solution. However, as a mesh is made finer, the computation time increases. To get a mesh that satisfactorily balances accuracy and computing resources, a mesh convergence study has to be performed.

In this scope, the breast and muscle geometries were meshed with different mesh sizes; the minimal elements sizes was set to $7mm$ and the maximal element size was varied to $\{7mm, 10mm, 13mm, 15mm, 17mm, 20mm\}$. Simulation with a mesh size of $5mm$ was not supported as it become too expensive in computation time and memory therefore a computer with higher computational power was needed. The compression paddle geometries were meshed with a constant element size of $1mm$. The number of elements obtained for each mesh size is given in Table B.1. We can see that, in general, larger the mesh size, lower the number of elements. However, we observed that for a mesh size equal to $17mm$, a higher number of elements was obtained when compared to a mesh size of $15mm$. This is due to the fact that the mesh size being defined by the maximal and minimal elements size, a higher number of *small* elements is needed to cover the areas smaller than the *large* elements. With such meshes, the element density is usually concentrated on the corners or narrow spaces which, in our case, do not coincide with the region of interest.

Mesh size	20 mm	17 mm	15 mm	13 mm	10 mm	7 mm
Nb. of elements	8367	10897	8099	10751	18453	65785

Table B.1: Number of elements obtained for each mesh size.

Our model was developed to compute breast deformation under compression, an equivalent simulation was performed to estimate the optimal mesh size. Starting from the breast supine geometry, the gravity was applied in the postero-anterior direction. Then, the right breast was compressed between the breast support and the paddle (Figure B.1). In this work we are interested in tissue deformations, therefore the strain range for each mesh density was analysed. The strain intensity distribution over the breast volume for

APPENDIX B. MESH CONVERGENCE

each mesh size are given in Figure B.1.

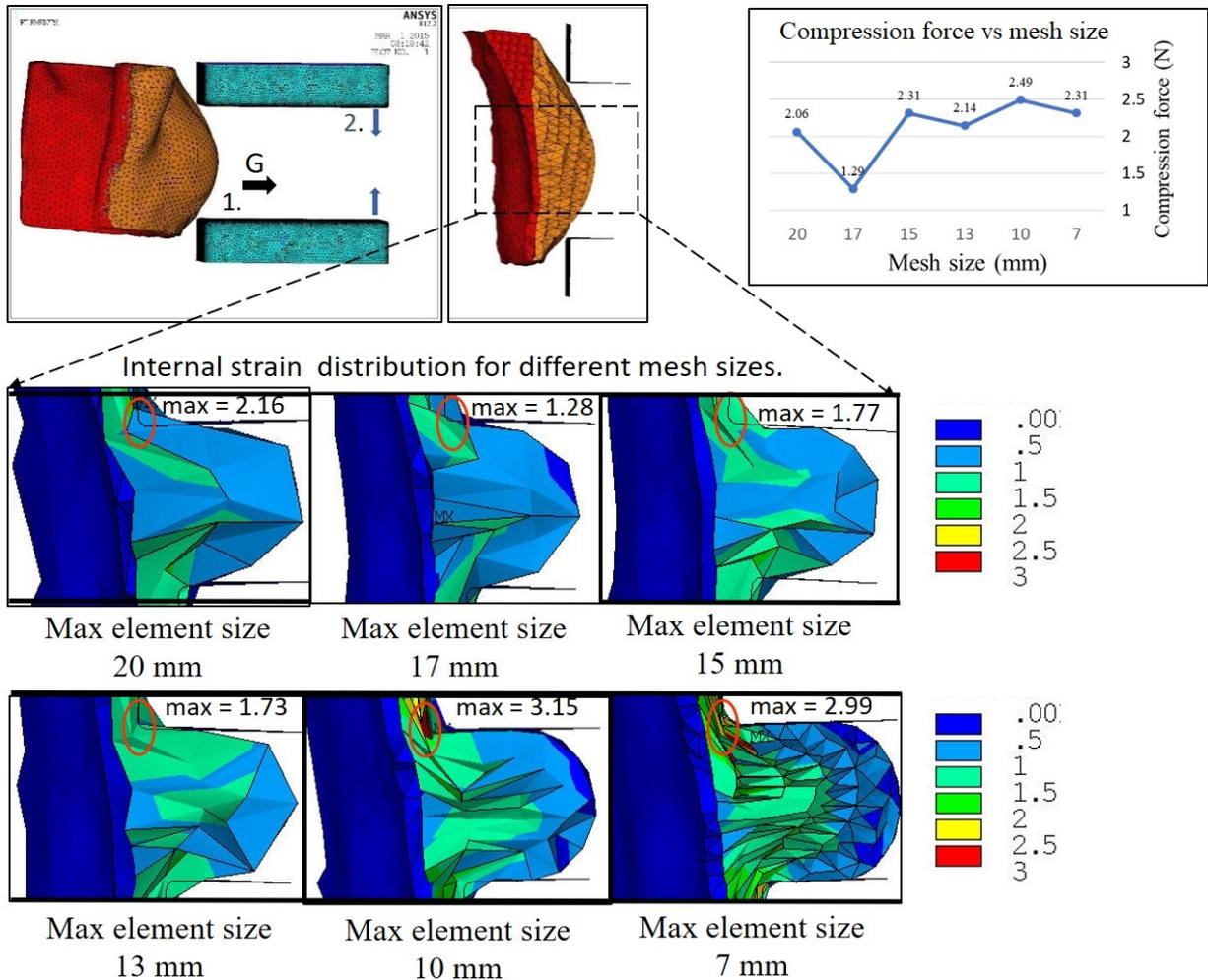


Figure B.1: Internal strain distribution as a function of the elements size.

Under compression, the maximal strain is expected to occur in the juxtathoracic area at the contact with the paddle corner (marked area with an orange ellipsoid in Figure B.1), therefore the maximal strain was measured in this region for each mesh density. However, the observed values did not show a converging behavior within different mesh sizes. To analyze the mesh convergence, the applied force for a target compressed breast thickness was plotted (Figure B.1). One can see that the force intensity converges starting with a mesh size equal to 15mm . However, a visual analysis of the strain distributions over the breast volume shows that using a mesh size equal to or lower than 10mm results in a better estimation of the internal strain distribution. Therefore, to optimize the computation time, a mesh size equal to 10mm is used.

BOUNDARY CONDITIONS *contact models*

The proposed biomechanical model consists of two bodies, one representing the pectoral cage with the pectoral muscle, and the second representing the breast soft tissue. Between the two bodies, a contact surface is defined in order to model tissues mechanics at the juncture interface.

The next section describes the implementation of different interaction models tested during the model development process. Since the breast tissues are always attached to the pectoral muscle (Figure C.1), the contact surface was modeled using *bonded* and *no-separation frictional* interaction model only.

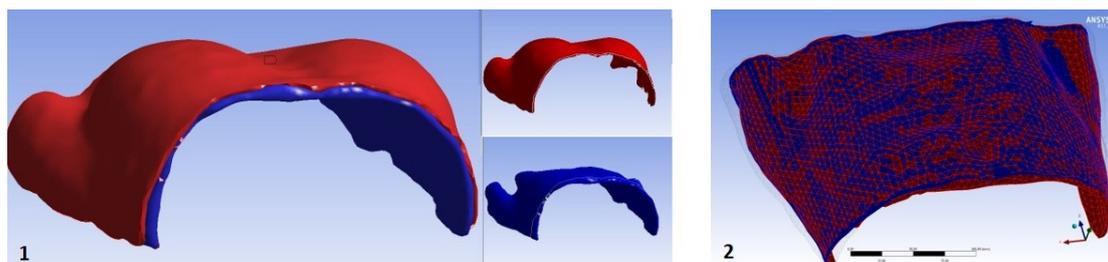


Figure C.1: The two bodies representing the thoracic cage and breast (1) with their the associated contact surface (2). Blue surface - muscle representing the target surface, red surface - breast representing contact surface

The results for pure bonded and pure no-separation sliding models, as well as one combined contact surface, are listed bellow. For some contact models, because of large instabilities or a poor fidelity to the real breast mechanics, only partial results are presented.

Bonded contact surface

First, a pure bounded contact was used to model the interaction between the breast and the pectoral muscle. To achieve large tissues displacements as measure on MR images, extremely low values of equivalent Young's modulus and Poisson ratio were needed ($\lambda_{breast} = 0.3kPa$ and $\nu_{breast} = 0.45$). An example of breast deformation in prone and supine configuration is illustrated in Figure C.2.

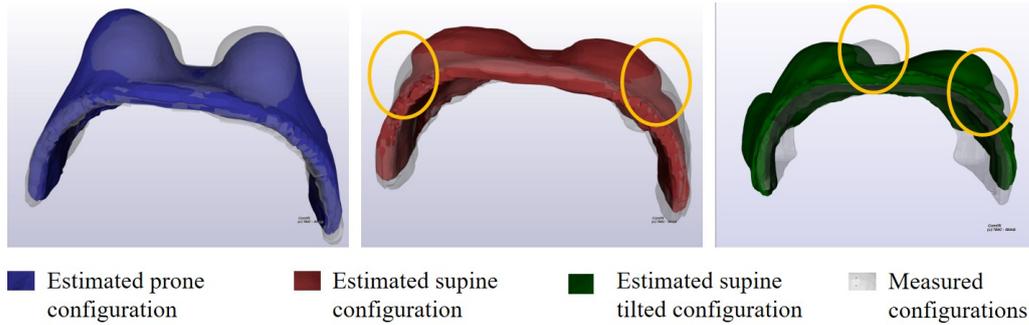


Figure C.2: Resulting breast deformation with a bonded contact model.

One can see that, even if the breast geometry in prone position is well estimated, the ones in supine and supine tilted configurations are constrained laterally. Moreover, an important volume variation was observed which is not a characteristic of breast changes under gravity loading. The volume variation is due to a too low value of the Poisson ratio.

Sliding contact surface

Pure sliding contact surface was considered in order to allow larger tissues displacements on lateral direction. The breast sliding over the muscle surface was modeled using the Coulomb friction low (Section 2.3.2). Additional boundary conditions were set by imposing zero-displacement on the right, left, superior and inferior mesh boundaries representing the breast volume (see Figure 3.11 for a recall on different mesh boundaries). This model caused large convergence problems because of breast tissues over-sliding. It was obvious that the model needs to be further constrained in order to achieve convergence. Moreover, a non-linear and a non-uniform sliding model was needed in order imitate the behavior of rich fibrous areas where the breast is attached to the chest wall (see Section 1.1.3 for a recall on breast anatomy).

Mixed contact surface

In order to limit breast tissues sliding, a mixed contact surface was defined. Herein, the contact surface consists of two complementary areas (Figure C.3), the first one modeled as bonded contact and the second one modeled as no-separation sliding contact. The regions corresponding to the bounded contact are defined following the anatomical structures where the concentration of fibrous tissues is significantly higher than overall breast volume. Such

regions are encountered along the muscle surface where the superficial muscle fascia meets the breast suspensory ligaments, as it is the case for the inframammary ligament, the deep medial ligament or the deep lateral ligament.

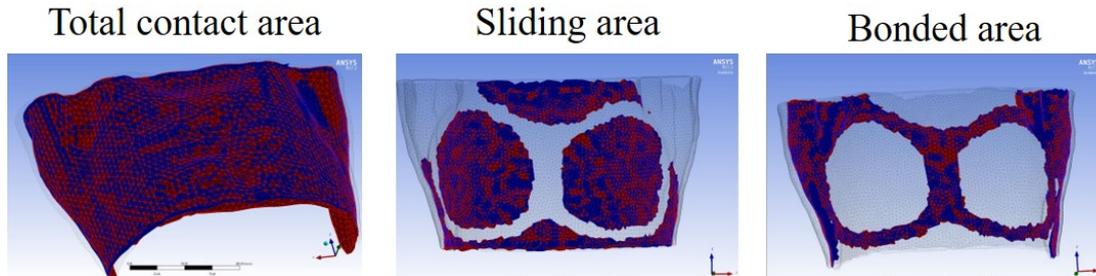


Figure C.3: The contact surface divided in two regions: sliding region and bonded region.

Using such a contact model improves substantially the estimate of the supine breast configuration. However, because of a high deformation gradient imposed at the juncture border between the two contact areas, convergence problems were observed. Moreover, when the supine configuration was estimated, several folds were created at the skin surface (Figure C.4). The same types of folds were obtained in supine tilted configuration creating large convergence problems because of tissues superposition.

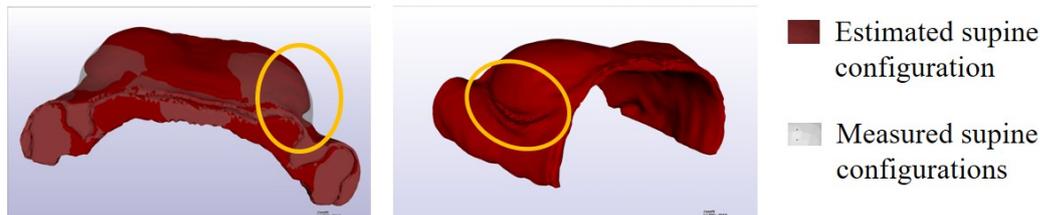


Figure C.4: The contact surface divided in two regions: sliding region and bonded region.

This last described model has provided satisfactory results, however it led to important solution convergence problems. Therefore, the model was improved by replacing the bonded contact regions with stiff ligaments connecting the breast tissues to the muscle. Contrary to the bonded contact, the ligaments preclude progressively the breast tissues from sliding and allow slight displacements avoiding the creation of folds. Moreover, an additional layer modeling the deep layer of breast superficial fascia was added at the juncture surface between the breast and muscle. Knowing that the fascia is stiffer than the breast soft tissues, it controls the amount of sliding and facilitates the solution convergence. For more information on ligaments and fascia mechanical properties, see Section 3.4.

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