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Guacira Costa de Oliveira

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Advances in Multi-Terminal HVDC Transmission Systems: Nonlinear controllers for Modular Multilevel Converters

**Thèse de doctorat de l'Université Paris-Saclay et
Université de São Paulo**

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Information and Communication (STIC)
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**Thèse présentée et soutenue à en visioconférence totale, le 21
décembre 2020, par**

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Titre: Avancées sur les Systèmes Multi-terminaux HVDC: Contrôleurs Non linéaires pour Convertisseurs Modulaires à Plusieurs Niveaux

Mots clés: Convertisseurs modulaires à plusieurs niveaux, contrôle non linéaire, théorie de Lyapunov, modèle MMC bilinéaire moyen

Résumé: Le convertisseur modulaire à plusieurs niveaux est un sujet d'intérêt important et actuel dans le contexte des applications de systèmes de transmission haute tension à courant continu. Cette topologie convient à plusieurs applications, en raison de pertes de commutation plus faibles dues à une fréquence de commutation plus petite, à une faible distorsion harmonique de courant alternatif, à une structure modulaire permettant une construction évolutive, et une maintenance plus simple. Cependant, une stratégie de contrôle plus complexe est nécessaire pour contrôler le courant circulant, pour compenser le déséquilibre de tension entre les circuits et l'équilibrage de tension de Submodules (SMs), de manière à maintenir constantes les tensions des condensateurs de SM. Cette thèse présente deux contrôleurs non linéaires pour un Modular Multilevel Converter (MMC), capables de contrôler les courants circulants et l'énergie dans le convertisseur. Le premier est conçu selon la théorie bilinéaire basée sur le contrôle de rétroaction quadratique. Le deuxième contrôleur proposé est développé en utilisant la théorie de Lyapunov, fortement basé sur des techniques de perturbation singulière et de linéarisation par bouclage. Pour les deux, une étude mathématique est réalisée sur la stabilité, basée sur la théorie de Lyapunov. Ce résultat assure une

stabilisation asymptotique pour les trois phases MMC. L'utilisation d'une fonction de Lyapunov implique une vérification formelle de la stabilité et une région explicite d'attraction pour le modèle considéré. Les deux techniques de contrôle sont développées à partir d'un modèle bilinéaire moyen, et la robustesse et les performances sont vérifiées au moyen d'un modèle de commutation MMC provenant des simulations électriques Matlab Simscape. L'évaluation comprend des variations de référence de puissance active et réactive, des conditions de déséquilibre du réseau, des incertitudes de paramètres et même une comparaison avec un contrôleur PI standard. Aussi, pour les contrôleurs non linéaires sont étudiés: l'effet des gains du contrôle sur la dynamique du système et les performances du contrôleur en cas de changement du point de fonctionnement. Les contributions principales de la thèse sont les deux algorithmes de contrôle non linéaires distincts, basés sur un modèle mathématique bilinéaire, conçus pour les convertisseurs MMC; Les deux algorithmes sont capables de contrôler l'équilibrage du courant et énergie du convertisseur au niveau du modèle détaillé du MMC par commutation; Il existe une analyse formelle de la stabilité par la théorie de Lyapunov pour ces systèmes; et une fois que le contrôle proposé n'est pas basé sur un modèle linéarisé, une vaste région d'opération est garantie.

Title: Advances in Multi-Terminal HVDC Transmission Systems: Nonlinear Controllers for Modular Multilevel Converters

Keywords: Modular Multilevel Converter, Nonlinear Control, Lyapunov Theory, MMC Average Bilinear Model

Abstract: MMC is a very important topic in the context of high voltage direct-current transmission systems applications. This topology is suitable for several applications, as a result of smaller switching losses due to lower switching frequency, low alternating-current harmonic distortion, modular structure enabling scalability construction and practical maintenance. However, a more complex control strategy is required to control circulating current, to compensate the voltage imbalance between legs and voltage balancing of SMs, such as to maintain SM's capacitors voltages constant. This thesis presents two nonlinear controllers for an MMC, able to control circulating currents, and the energy in the converter. First proposed controller is developed using Lyapunov theory, strongly based on singular perturbation and feedback linearization techniques. Second one is designed following bilinear theory based on quadratic feedback control. For both, a mathematical proof is given for its stability, which is based on Lyapunov's theory. This result provides asymptotic stab-

lization for the three-phases MMC. The use of a Lyapunov function implies a formal verification of stability and a broad region of attraction for the considered model. Both control techniques are developed by means of an average bilinear model and performances are verified by means of a detailed MMC switching model at Matlab Simscape Electrical environment. The evaluation includes active and reactive power reference variations, grid imbalance conditions, parameters uncertainties and even a comparison with a standard PI controller. Also, for the nonlinear controllers, it is studied the effect of control gains on the system's dynamics. The main thesis' contributions can then be stated as the two distinct nonlinear control algorithms, based on a bilinear mathematical model, designed for MMC converters; Both algorithms are able to control circulating currents and converter's energy at the switching MMC model; There are formal stability analysis by Lyapunov theory for these controllers; and once these proposed controllers are not based on a linearized model, a broad operation region is obtained.

Título: Avanços em Sistemas de Transmissão Multi-terminal HVDC: Controles Não-lineares para Conversores Modulares Multiníveis

Palavras-chave: Conversores Modulares Multiníveis, Controle Não-linear, Teoria de Lyapunov, Modelo Médio Bilinear de MMC

Abstract: O conversor multinível modular é o tópico de interesse amplo e atual no contexto de aplicações de sistemas de transmissão de corrente contínua de alta tensão. Essa topologia é adequada para várias aplicações, como resultado de menores perdas de chaveamento, devido à menor frequência de comutação dos IGBTs, baixa distorção harmônica na corrente alternada, estrutura modular que permite escalabilidade na construção e manutenção prática. No entanto, é necessária uma estratégia de controle mais complexa para controlar a corrente circulante, para compensar o desequilíbrio de tensão entre as pernas e o equilíbrio de tensão dos sub-módulos, de forma a manter constantes as tensões dos capacitores dos sub-módulos. Esta tese apresenta dois controles não-lineares para conversores MMC, capazes de controlar correntes circulantes e a energia no conversor. O primeiro é projetado seguindo a teoria bilinear baseada no controle de feedback quadrático. O segundo controlador proposto é desenvolvido usando a teoria de Lyapunov, fortemente baseada em técnicas singular perturbation e feedback linearization. Para ambos, é definida uma prova matemática de sua estabilidade, baseada na teoria de Lyapunov. Este resultado fornece estabi-

lização assintótica para as três fases MMC. O uso de uma função de Lyapunov implica uma verificação formal da estabilidade e uma região explícita de atração para o modelo considerado. Ambas as técnicas de controle são desenvolvidas por meio de um modelo médio bilinear e a robustez e o desempenho são verificados por meio de um modelo chaveado de conversores MMC nas simulações do Matlab Simscape Electrical. A avaliação inclui variações de referência de potência ativa e reativa, condições de desequilíbrio da rede, incertezas de parâmetros e até uma comparação com um controlador PI. Além disso, para os controladores não lineares, são estudados: o efeito do controle de ganho na dinâmica do sistema e no desempenho do controlador em caso de alteração no ponto de operação. As principais contribuições da tese são os dois algoritmos distintos de controle não-linear, baseados em um modelo matemático bilinear, projetados para conversores MMC; Ambos os algoritmos são capazes de controlar o equilíbrio de corrente circulante e a energia do conversor; Há uma análise formal de estabilidade pela teoria de Lyapunov para esse sistema; e uma vez que os controles propostos não se baseiam em um modelo linearizado, uma vasta região de operação é alcançável.

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Contents

1	Introduction	19
1.1	History and background	21
1.2	Equipment	23
1.2.1	HVDC topologies	23
1.2.2	Line-commuted converters	25
1.2.3	Voltage-source converters	25
1.2.4	Modular-multilevel converter	25
1.3	Controlling Modular Multilevel Converters	26
1.4	Main objective of the thesis	27
1.4.1	Specific objectives	27
1.5	Main contributions	27
1.6	Thesis's organization	27
2	Modular Multilevel Converters	31
2.1	MMC internal topology	31
2.2	Modeling	39
2.2.1	Full order models	40
2.2.2	Reduced order average model	42
2.2.3	Derivation of reduced order average model	42
2.3	Control designs for MMC systems	50
2.4	Chapter conclusion	57
3	MMC Linear Control and Test System	59
3.1	Equilibrium points for state variables and control inputs	59
3.2	PI controller	62
3.2.1	Tuning	66
3.3	Simulation test of MMC with the Proportional-integral (PI) controller at switching-model and average-model	67
3.4	Medium-voltage system test with PI controller	68
3.4.1	Control Effort	80
3.4.2	Robustness over parameters' uncertainties and voltage fluctuation on medium-voltage system with PI controller	84
3.5	High-voltage system test with PI controller	92
3.5.1	Robustness over parameters' uncertainties and voltage fluctuation on high-voltage system with PI controller	97
3.6	Chapter conclusion	108
4	Nonlinear control	109
4.1	Nonlinear controller in the context of MMC	109
4.2	Mathematical model - Recalling main definitions	110
4.3	Control Objective	110
4.3.1	The Actuated States	110
4.3.2	Free-dynamic States	113
4.4	Main result	115
4.5	Medium-voltage system test with the nonlinear controller	115
4.5.1	Robustness over parameters uncertainties and voltage fluctuation for medium-voltage system with nonlinear controller	120
4.6	High Voltage system test with nonlinear controller	128
4.6.1	Comparison of nonlinear and PI controllers	130
4.6.2	Robustness over parameters' uncertainties and voltage fluctuation for high-voltage system with nonlinear controller	139
4.7	Chapter conclusion	147

5 Bilinear Quadratic Feedback Control	149
5.1 Bilinear Control Theory	151
5.1.1 Bilinear System Stability - a general case	151
5.1.2 Bilinear System Stability: studied case	152
5.2 Robustness over parameters' uncertainties and voltage fluctuation for medium-voltage system with bilinear controller	163
5.3 Chapter conclusions	172
6 General Conclusion	173
6.1 Main Results	174
6.2 Perspectives for future research	175
6.3 Publication	175
A Introduction en Français	185
A.1 Contrôle des convertisseurs modulaires à plusieurs niveaux	185
A.2 Objectif principal de la thèse	186
A.3 Principales contributions	186
A.4 Conclusion générale	186
A.4.1 Résultats principaux	188
A.4.2 Perspectives pour les recherches futures	189

List of Tables

2.1 Modulation features.	37
3.1 Parameters of simulated medium-voltage system and PI control gains.	68
3.2 Parameters of simulated high-voltage system and PI controller gains.	92
4.1 Parameters of simulated medium-voltage system and nonlinear control gains.	117
4.2 Parameters of simulated high-voltage system and nonlinear control gains.	129
5.1 Parameters of simulated system and bilinear control's gains.	155

List of Figures

1.1	Share of energy from renewable sources in the Europe Member States in % of the gross final energy consumption.	20
1.2	Relation between HVDC and HVAC cost: the break-even distance to system which uses cables is near to 50 km, and using overhead transmission line is near to 600 km.	20
1.3	Sketch of electrical grid.	21
1.4	Direct transmission technology evolution over the years	22
1.5	HVDC transmission line topologies. (a) Symmetric monopole. (b) Asymmetric monopole with ground return. (c) Asymmetric monopole with metallic return. (d) Bipolar with ground return. (e) Bipolar with metallic return.	28
1.6	Multi-terminal test system proposed by CIGRÉ.	29
1.7	Line-commuted converter topology.	29
1.8	Voltage Source Converter topology.	29
1.9	Modular Multilevel Converter topology.	30
2.1	Modular Multilevel Converter (MMC) based in the symmetric monopole topology and half-bridge's SMs.	32
2.2	Full-bridge SM and the related output voltage.	33
2.3	Half-bridge SM and the related output voltage.	34
2.4	Possible SM operations. a) active SM with positive current; b) bypassed SM with positive current; c) active SM with negative current; d) bypassed SM with negative current and; (e) and (f) submodule equivalent blocked state.	35
2.5	Traditional sorting algorithm achievement during one Pulse Width Modulation (PWM) period.	38
2.6	Phase Locked Loop (PLL) internal diagram.	39
2.7	Summary of MMC models.	40
2.8	Lumped elements on the left side and equivalent elements on the right. (a) resistor, (b) inductor, (c) capacitor and (d) Insulated Gate Bipolar Transistor (IGBT).	41
2.9	Thevenin equivalent SM.	41
2.10	Average model of a three-phase MMC.	43
2.11	Kirchhoff's voltage law for upper arm (a) and lower arm (b) at phase j.	44
2.12	MMC-HVDC necessary controls.	51
3.1	Block diagram of control input v_{ud}	65
3.2	Block diagram of control input v_{uq}	65
3.3	Block diagram of control input v_{ld}	65
3.4	Block diagram of control input v_{lq}	66
3.5	Block diagram of control input v_{d0}	66
3.6	Block diagram of firing pulses to m arms.	66
3.7	Medium-voltage system test.	68
3.8	Four-quadrant operation of MMC average model with PI controller.	69
3.9	Detail of step on <u>active</u> power, from figure 3.8.	70
3.10	Detail of step on <u>reactive</u> power, from figure 3.8.	70
3.11	Detail of state i_{cir0} while a step on <u>active</u> power, from figure 3.8.	70
3.12	Four-quadrant operation of MMC switching-model with PI controller.	71
3.13	Detail of step on <u>active</u> power, from figure 3.12.	72
3.14	Detail of step on <u>reactive</u> power, from figure 3.12.	72
3.15	Detail of state i_{cir0} while a step on <u>active</u> power, from figure 3.12.	73
3.16	Detail of state W_v	73
3.17	Switching-model and average-model comparison.	74
3.18	Energy change at MMC average-model with PI controller.	75
3.19	Detail from figure 3.18 of increase in energy W_h	77
3.20	Detail from figure 3.18 of increase in energy balancing W_v	77

3.21	Energy change at MMC switching-model with PI controller.	78
3.22	Average-model and switching-model comparison.	79
3.23	Control inputs of average and switching model for the operating points presented in figure 3.17.	80
3.24	Control inputs of average and switching model for the operating points presented in figure 3.22.	81
3.25	Double-fundamental frequency component of circulating currents at medium-voltage switching model with PI controller.	82
3.26	Voltage of each SM per arm of medium-voltage system with PI controller.	83
3.27	The system state over variation of parameter R of medium-voltage system with PI controller.	85
3.28	The system state over variation of parameter R_c of medium-voltage system with PI controller.	86
3.29	The system state over variation of parameter L of medium-voltage system with PI controller.	87
3.30	The system state over variation of parameter L_c of medium-voltage system with PI controller.	88
3.31	The system state over variation of parameter C of medium-voltage system with PI controller.	89
3.32	The system state over variation in the voltage at the PCC of medium-voltage system with PI controller.	90
3.33	The system state over variation in DC voltage of medium-voltage system with PI controller.	91
3.34	System diagram of 400 kV system.	92
3.35	Four-quadrants operation of high-voltage system with proposed PI controller.	94
3.36	Energy steps for high-voltage system with proposed PI controller.	95
3.37	Control effort of four-quadrant operation of PI controller.	96
3.38	Control effort of changes in energy of PI controller.	97
3.39	Share of energy among arms with PI controller.	97
3.40	Total energy in the three upper arms (W_u) and the three lower arms (W_l) with PI controller.	98
3.41	Double-fundamental frequency component of circulating currents at high-voltage switching model with PI controller.	98
3.42	SMs capacitor voltage per arm and equivalent detail from PI controller.	99
3.43	The system state over variation of parameter R of high-voltage system with PI controller.	101
3.44	The system state over variation of parameter R_c of high-voltage system with PI controller.	102
3.45	The system state over variation of parameter L of high-voltage system with PI controller.	103
3.46	The system state over variation of parameter L_c of high-voltage system with PI controller.	104
3.47	The system state over variation of parameter C of high-voltage system with PI controller.	105
3.48	The system state over variation in the voltage at the PCC of high-voltage system with PI controller.	106
3.49	The system state over variation in DC voltage of high-voltage system with PI controller.	107
4.1	Diagram of nonlinear control.	116
4.2	Response of state i_{vd} and i_{vq} over tuning of αs	117
4.3	Four-quadrant operation of the medium-voltage system with the nonlinear controller.	118
4.4	Energy changes of the medium-voltage system with the nonlinear controller.	119
4.5	The system state over variation of parameter R with nonlinear controller.	121
4.6	States over variation of parameter R_c with nonlinear controller.	122
4.7	States over variation of parameter L with nonlinear controller.	123
4.8	States over variation of parameter L_c with nonlinear controller.	124
4.9	States over variation of parameter C with nonlinear controller.	125
4.10	Fluctuation of Alternating Current (AC) voltage at the Point of Common Coupling (PCC) with nonlinear controller.	126
4.11	Direct Current (DC) voltage fluctuation with nonlinear controller.	127
4.12	Response of state i_{vd} and i_{vq} over tuning of αs	128
4.13	Four-quadrant operation of the high voltage system with the nonlinear and PI controller.	132
4.14	State variables response over changes on energy.	133
4.15	Control efforts over power changes.	134

4.16	Control efforts over energy changes.	135
4.17	Share of energy in each arm with the nonlinear controller.	136
4.18	Total energy in the three upper arms (W_u) and at the three lower arms (W_l).	137
4.19	Double-fundamental frequency component of circulating currents at high voltage switching model with the nonlinear controller.	137
4.20	SMS' capacitor voltage per arm and equivalent detail in time, accomplished by nonlinear controller.	138
4.21	The system state over variation of parameter R	140
4.22	States over variation of parameter R_c	141
4.23	States over variation of parameter L	142
4.24	States over variation of parameter L_c	143
4.25	States over variation of parameter C	144
4.26	Voltage in the PCC changes $\pm 10\%$ and $\pm 5\%$ from the nominal value.	145
4.27	DC voltage changes $\pm 10\%$ and $\pm 5\%$ from the nominal value.	146
5.1	Diagram of bilinear controller.	154
5.2	Four-quadrant operation for medium-voltage system with bilinear controller.	156
5.3	Energy change for medium-voltage system with bilinear controller.	157
5.4	SMS voltage balancing per arm with the bilinear control.	158
5.5	Energy per arm of MMC with the bilinear.	159
5.6	Total energy in upper (lower) arms using bilinear controller.	159
5.7	Double-fundamental frequency of circulating current with bilinear controller.	160
5.8	A performance comparison between PI and bilinear controller through four-quadrants operation.	161
5.9	A performance comparison between PI and bilinear controller through energy change.	162
5.10	The system state over variation of parameter R with bilinear controller.	164
5.11	States over variation of parameter R_c with bilinear controller.	165
5.12	States over variation of parameter L with bilinear controller.	166
5.13	States over variation of parameter L_c with bilinear controller.	167
5.14	Bilinear robustness over uncertainties in L with a larger gain.	168
5.15	Bilinear robustness over uncertainties in L_c with a larger gain.	168
5.16	States over variation of parameter C with bilinear controller.	169
5.17	Fluctuation of AC voltage with bilinear controller.	170
5.18	Fluctuation of DC voltage with bilinear controller.	171

Acronyms

AC Alternating Current

AVM Average-model

CAPES Coordination for the Improvement of Higher Education Personnel

CCC Capacitor-Commutated Converters

DC Direct Current

EPS Electric Power System

ECB Equivalent Circuit Based

HVDC High Voltage Direct Current

IGBT Insulated Gate Bipolar Transistor

LCC Line Commutated Converter

LS Least Squares

MMC Modular Multilevel Converter

MTDC Multi-terminal HVDC

NL Nearest-Level

NPC Neutral-Point Clamped

PLL Phase Locked Loop

PWM Pulse Width Modulation

PCC Point of Common Coupling

PLQR Periodic Linear Quadratic Regulator

PR Proportional-resonant

PI Proportional-integral

SM Submodule

SHE Selective Harmonic Elimination

SVM Space Vector Modulation

SPWM Sinusoidal Pulse Width Modulation

TE Thevenin's Equivalent

VSC Voltage Source Converter

Nomenclature

\bar{V}_C^{SM}	SM's nominal capacitor voltage
i_{cirj}	MMC circulating current per phase
$i_{cirj}^{2\omega}$	Double fundamental frequency circulating current per phase j
i_{dc}	DC current
i_{mj}	MMC arm current per phase
i_{vdq}	dq components of AC side currents
i_{vd}	Direct d component of AC side currents
i_{vj}	AC side currents per phase in ABC
i_{vq}	Quadrature q component of AC side currents
k_i^x	Integral gain of state x
k_p^x	Proportional gain of state x
L_c	AC phase inductance
P_e	Active power
P_{ej}^{AC}	AC active power on phase j
P_{ej}^{DC}	DC active power on phase j
Q_e	Reactive power
R_c	AC phase impedance
V_{arm}^j	Output voltage on the arm linked with phase j
V_o^n	SM n , output voltage
v_{Cn}^{SM}	Capacitor's voltage
v_{Ctotj}	Sum of all capacitors voltage on the leg linked with phase j
v_{Ctotmj}	Sum of all capacitors voltage on arm m of phase j
v_{d0}	DC voltage component
V_{DC}	DC output voltage
v_{fd}	Direct d component of AC voltage per phase at the PCC
v_{fq}	Quadrature q component of AC voltage per phase at the PCC
v_j	AC voltage per phase at the PCC
v_{mj}	Equivalent arm voltage produced by SMs per phase
W_C^{SM}	stored energy per SM
W_h	Total converter energy
W_v	Energy difference between MMC upper and lower part
W_l	Total energy in lower converter arms

W_u	Total energy in upper converter arms
avm	MMC average-model
j	AC phases
L	MMC arm inductance
l	MMC lower arm
m	MMC upper or lower arm
N	Number of series SMs per arm
R	SM switching power losses
swit	MMC switching-model
u	MMC upper arm

Chapter 1

Introduction

Green energy systems have been expanding considerably worldwide in the last decades. In 2017, for the first time, 30 % of the electricity generated in Europe was produced by renewable sources. This amount was the combination of solar, biomass, and, meaningfully, the wind, which has grown to 20.9 % of the production [1]. Figure 1.1 shows that in 2018 thirteen of twenty-seven European countries had already reached the targeted 20% of renewable share [2]. However, the target has been updated to at least a 32% share of renewable energy in 2030 [3]. Therefore, European renewable energy ambitions are close to those targeted, and the electrical grid infrastructure is changing to support the power consumption.

The new grid layout consists of both Alternating Current (AC) transmission and Direct Current (DC) systems. DC technology performs suitable solutions, such as high voltage transmission of large-scale power either for long distances or for offshore energy sources and underground lines. Moreover, the electricity market stimulates the European *SuperGrid* construction, allowing it to conduct electricity inside its borders and neighboring countries. The European *SuperGrid* aims to integrate 10 % of the European electrical production by 2020 [4], and to rise to 15% by 2030 to ensure stability and a more sustainable energy supply [5].

A 1000 MW \pm 320 kV part of the European *SuperGrid* that connects France and Spain is already operating with the MMC technology [6]. Nowadays there is a project to link offshore wind reserves in the North Sea to high population zones in the south region of Germany; and there is a link connecting France and Italy that is under development to date [4]. The European *SuperGrid* is a concrete plan along with distinct technical requirements related to control automation, DC protection, and grid stability.

An electrical grid with a variety of power sources creates new challenges for the system operation. Long electrical transmission lines may present power limiting to transmit high power levels and face oscillatory stability problems. Currently, High Voltage Direct Current (HVDC) is currently applied to interconnect asynchronous systems, large-scale power transfer in long-distance projects, and subsea and underground transmission, which is also a less expensive solution after a break-even distance. The cost of the DC stations is higher than AC stations, while DC lines are more affordable. Besides, losses in DC lines are smaller than in AC lines since there are no capacitive and inductive effects. Figure 1.2 presents break-even distance, which represents the length of the transmission line where the cost of DC station plus DC lines becomes equal to the price of AC station plus AC lines [7, 8].

Figure 1.3 shows an electrical grid from the AC generation to the final consumer. The most important equipment of a AC-DC station is the converter. It transforms the AC produced power into DC, which will flow through DC lines and

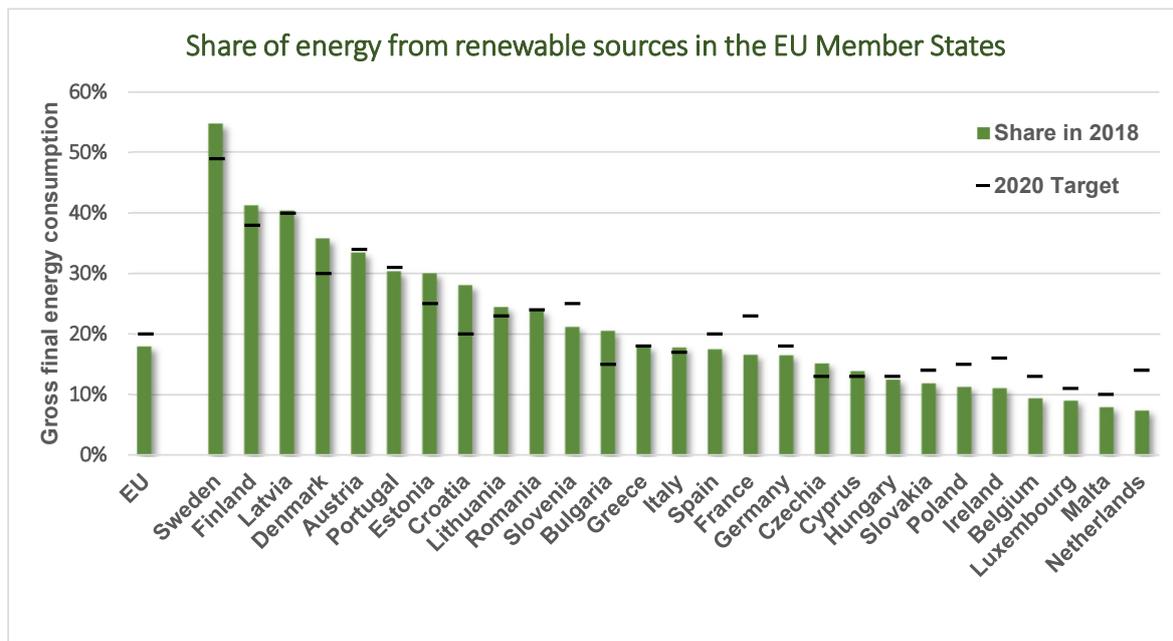


Figure 1.1: Share of energy from renewable sources in the Europe Member States in % of the gross final energy consumption.

Source: [2]

supply consumers.

The Modular Multilevel Converter (MMC) is the most recent converter topology used at HVDC stations. This converter topology outperforms the previous technology, especially concerning smaller switching losses due to the low switching frequency, lower AC harmonic distortion, modular structure enabling a scalable construction, and practical maintenance. On the other hand, the MMC presents a complex control and higher building cost than the previous topology. On the other hand, circulating current management and the voltage balancing of SMs are some challenges related to the use of this technology. Therefore, this thesis aims to develop a nonlinear control strategy for HVDC stations, particularly, an adequate solution for circulating currents and converter energy. Furthermore,

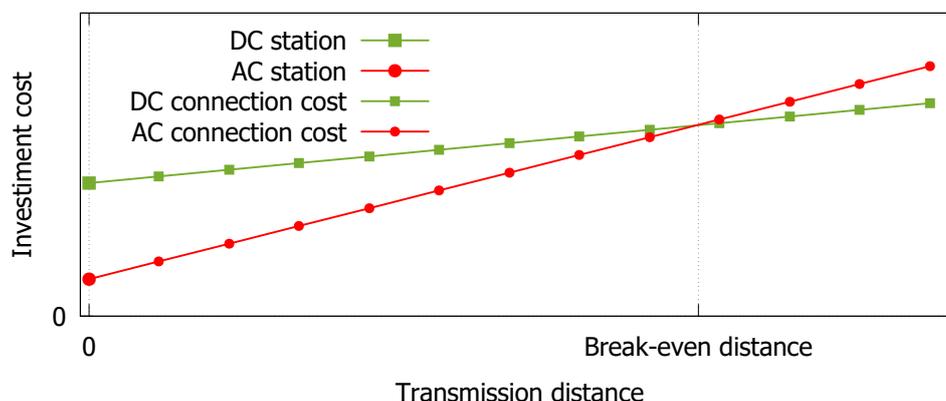
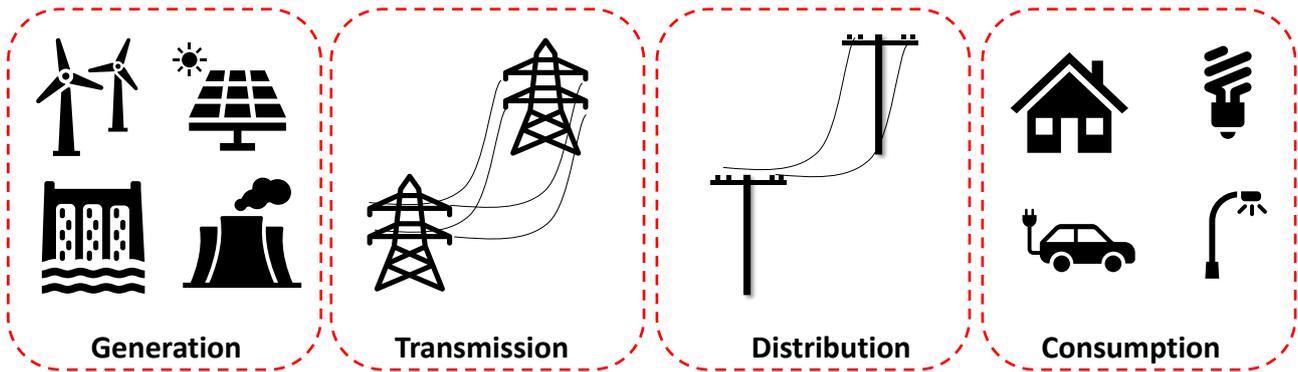


Figure 1.2: Relation between HVDC and HVAC cost: the break-even distance to system which uses cables is near to 50 km, and using overhead transmission line is near to 600 km.

Source: [7]

Figure 1.3: Sketch of electrical grid.



Source: Author

the controller will be designed to assure system stabilization.

1.1 History and background

The first use of direct current was in 1882, in a long-distance electrical energy transmission line, to connect two German cities: Miesbach and Munich [9]. At the same time, New York was lighted by DC circuits. However, technical constraints limited the DC application on power systems. Since the relationship between power losses and voltage transmission level is inversely proportional, the drawback was how to change the DC voltage between the transmission and the consumption level. On the other hand, it is not difficult to convert the voltage level in AC systems using transformers. Also, AC generators are more efficient and have a more straightforward structure and maintenance compared to the DC ones. Therefore, AC power generation, transmission, and distribution is the most dominant process in Electric Power System (EPS).

Meaningful development of power electronic devices has been noticed in the past few decades. In addition to that, many technical limitations on EPS have been overcome by DC applications, such as:

- Offshore applications;
- Connection between unsynchronized AC networks;
- Power transmission capacity of underground and undersea cables and overhead transmission lines, since there was a reduction in the capacitive and inductive effects;
- Large renewable energy generation connected to the main grid since renewable energies have a seasonal power production, DC converters maintain the voltage at the PCC, so the power variations will not affect the PCC voltage.

The progress in the field of power electronics is the result of many people's efforts and research. Figure 1.4 presents some important events in the power electronics development. At the beginning of the EPS's research, around 1882, DC projects were limited by lighting and simple line transmission applications. DC systems advanced in the creation of mercury-vapor valves (1901), and its first applications were the German project Elbe-Berlin (although it did not work

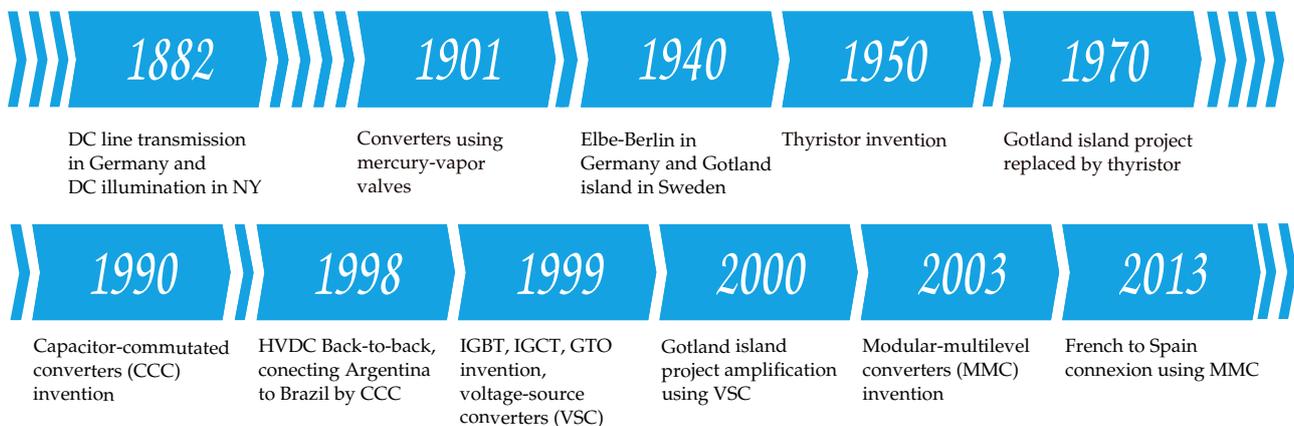
due to the second world war) and the Gotland island commercial project, in Sweden. However, mercury-vapor valves had some limitations, including electrical arcs inside the mercury tube, limited useful voltage, mercury heating time; the flexibility of small voltage levels; and the environmental issues related to exposure to mercury. As a result of these limitations, mercury-vapor valves were replaced by valves with thyristors (1970). They brought together the device's conversion and control, providing less space and weight, but their losses were higher compared to the valves.

Funding and research to develop thyristor valves in the 1960s ensured a technical improvement. For this reason, the Gotland island project was rebuilt using thyristors in the 1970s. This state-of-the-art thyristor technology is still used nowadays and has been called Line Commutated Converter (LCC).

In the late 1990s, the Capacitor-Commutated Converters (CCCs) were created using a combination of thyristors and capacitors, and they were able to provide reactive power control. Also, a back-to-back application of an asynchronous electrical system connection 2200 MW between Argentina and Brazil. In 2013, a 2385 km of HVDC system was built to interconnect south hydro power plants to the major load centers of southeastern Brazil.

Nowadays, there is almost no use of CCC in projects, as the advancement of the next technologies followed their development. High rated semiconductor devices (IGBTs, IGCTs, and GCOs) define the new concept of HVDC systems. The self-commutated devices principle allowed the construction of Voltage Source Converters (VSCs). The VSC first application was executed, once again, in Sweden, on the Gotland island.

Figure 1.4: Direct transmission technology evolution over the years



Source: [10]

The MMC concept is the latest advancement in HVDC technology, published in 2003 by professor Rainer Marquardt [11]. MMC has several advantages, such as lower switching losses, voltage level scalability, since they have a modular structure, more straightforward maintenance, and low AC current distortion, along with other benefits. The Siemens Trans Bay Cable Project in San Francisco, USA, employs the MMC [12].

Nowadays, the LCC, VSC and MMC projects coexist. Furthermore, the first connection of more than two DC stations is operated by China Southern Power Grid since 2013, using VSC ¹.

¹The history described in this section was based on [13, 10, 9, 14]

1.2 Equipment

HVDC systems are mainly composed of converters that connect the AC to DC electrical bar. Between them, transformers and phase reactors complete the interface. Transformers adjust the AC voltage level to converter operational voltage. Phase reactors are composed of a large inductor connected in series at each phase to smooth the AC current and promote the power flow control. Essential components of HVDC transmission are converters that are capable of converting AC to DC, and also the opposite, DC to AC.

These converters are composed of semiconductors connected in series, and they generate the desired voltage level. There are different types of converters, depending on the semiconductors technology used. The LCCs uses thyristors, while the VSCs employs transistors. LCCs features lower switching losses, and they are suitable for high power applications. On the other hand, VSCs transistors allow the switching control in both on and off positions, implying control of the power flow direction.

1.2.1 HVDC topologies

In the literature, there are many HVDC topologies. These variabilities allow flexibility concerning power demand, stability, operations, and implementing costs.

Distinct topologies, also based on LCC and VSC, are named as back-to-back, monopolar and bipolar, regarding DC transmission line as arrangement. Other features are obtained by combining these three topologies. HVDC systems based on back-to-back topology are about two directly linked converters, without transmission line. This topology is usually applied to connect unsynchronized systems in which each system has a distinguished frequency or different control method.

Figure (1.5) shows the most common HVDC topologies. Each subfigure is described as:

- Monopoles has a single converter per terminal connected by one or two transmission line and a current return path. Two types of the return path for current are possible: by ground or sea and metallic conductor. The ground/sea return is often favorite due to the cost reduction.
 - (a) Symmetric monopole topology is widely employed on VSC system projects. This topology links two converters by two transmission lines. Each one will assume a positive or negative polarity, and the ground reference is the capacitors grounding filters. Despite the fact there are two transmission lines, in case of a line-ground fault, the other line will not be able to maintain the operation by ground return;
 - (b) Asymmetric monopole topology with ground return comprehends two converters linked by a single transmission line. The pole is usually negative due to the reduced corona effect [15]. This configuration uses the ground as the return. About this configuration, just the transmission line works to keep the system voltage levels. In case of a fault, stop operation cannot be avoided. This topology has a cost advantage due to the use of just one line. However, there isn't much projects in which use it, because the environmental aspects linked with the ground current return;
 - (c) Asymmetric Monopole with the metallic return is similar to ground return. However, it uses a metallic conductor as a return. This topology can be easily upgraded to bipolar.

- Bipolar topology combines two asymmetric monopoles. They operate with opposite polarity. In this topology, each line can work independently, by ground return or metallic, in the other line's unavailability. Bipolar topologies, compared to monopolar topologies, duplicate the power rating operation and create a redundancy, in case of one converter to be out of service. On the other hand, it is a more costly option since it uses the double converter number, in comparison with other topologies. Furthermore, the ac side's connection is more tricky: it is necessary to provide two different transformers or a transformer with two secondary windings. The connection design need to manage the aspect as ac-side harmonic distortion and high direct voltage stresses — besides, bipolar installation demands attention concerning insulation;
- (d) Bipole with ground return presents a higher cost than the respective monopolar topology. Also, accomplish environmental concerns resulting from ground currents if there is an unbalanced between poles, such as pole outages and maintenance periods. In case of no grounding on bipolar configuration, the advantage of redundancy is loose because the return path for the current is necessary for the half system be available during faults;
- (e) Bipole with a metallic return is even costly once it needs an extra low-voltage insulated neutral conductor. However, this topology reduces environmental concerns.

Grids with more than two stations are called multi-terminal. They may combine two or more topologies. Figure 1.6 presents a multi-terminal test system proposed by *Conseil International des Grands Réseaux Électriques* (CIGRÉ). There is a diversity of connections in this CIGRÉ's system test, including the connection between AC and DC grid, symmetric monopole lines, and bipolar links. Also, includes the underground, oversea, and overhead lines.

1.2.2 Line-commuted converters

LCCs use thyristor valves to convert between AC and DC currents. Each phase connects two thyristor valves (one to the top and another to the bottom of the converter), so a three-phase converter consists of a six-pulse thyristor bridge, as show in figure (1.7). This topology produces an AC current and a DC voltage with high harmonic distortion, once each phase changes every 60° . Another challenge in the six-bridge LCC is to reach the operational voltage level. Usually, thyristors are connected in series to increase the operational performance. For modern LCC applications, the twelve-pulse thyristor bridge is dominant [9].

In LCC systems, the power flow inversion is obtained by the output voltage polarity inversion. Voltage polarity inversion is not allowed in weak bars, so the LCC application needs to consider this restriction [18].

1.2.3 Voltage-source converters

VSCs uses transistors, usually IGBTs. Transistors have two degrees of freedom, therefore, on and off switching control (see figure 1.8). A PWM, which produces a high-frequency signal, provides this switching control. As a result, VSC with PWM modulation has a wide range of voltage amplitude and the desired phase angle.

Due to the high-frequency modulation produced by PWM to switch IGBTs, there are fewer harmonic components in the current and voltage produced by VSC compared to LCC. Additionally, the on and off switching control allows VSC to control the active and reactive power by inverting the current direction and maintaining the output voltage polarity.

LCCs needs to absorb reactive power to maintain the output voltage at the desired value, so the PCC short circuit capacity must be high. On the other hand, there is no reactive power request for VSCs, so their connection can be made in both weak or strong AC grids.

1.2.4 Modular-multilevel converter

In 2003, the conception of modular converters was developed to reduce harmonic distortions in the output AC voltage, requiring little or no filters and increasing the operative voltage range. MMCs can produce an output voltage smooth and nearly an ideal sinusoidal because of the number of Submodules (SMs) used to construct the converter, see figure 1.9. N SMs imply in a output voltage with $N + 1$ levels (considering that each sub-module is a two level converter). By increasing the converter levels, there is switching loss reduction since the IGBT switching frequency is smaller. Converters that have scalability assets and produce output voltage with many levels are denoted as Modular Multilevel Converters (MMCs).

For instance, some completed projects using this technology (e.g., Siemens TransBay Cable project in San Francisco), and several other projects are still in

progress (e.g., Siemens project to France-Spain connection). As aforementioned, the power production from renewable energy generations is increasing across the world. However, green sources have inherent seasonal power production. Especially wind power plants since they have a dependence on wind speed and solar power plants, due to shadowing condition dependence. These inherent characteristics may affect EPS performance regarding protection, stability, and power dispatch [19, 20]. Integrating large renewable production to the main electrical grid is currently a challenge, and much research focuses on this issue [21, 22, 23]. Multi-terminal HVDC (MTDC) based on MMC is a suitable solution to solve these challenges. A MTDC is an arrange of more than two DC stations with a few more DC or AC stations.

MTDC is an outstanding solution to offshore wind plants, due to the higher oversea cable's capacitance, and also to the power generation variability in Europe and the *Supergrid* project [24].

1.3 Controlling Modular Multilevel Converters

The control of MMC has additional challenges in comparison to other converters' topology. The control method may have to deal with:

- Externally, manage active and reactive power flow, and AC and DC voltage;
- Internally, deal with converter's dynamics as circulating currents, SM capacitor's voltage, arm balancing, phase balancing, and converter's energy control.

MMCs also have a complex modeling technique because of the high number of Submodule (SM), which requires simultaneous control to attain capacitor voltage balancing. There are many MMC modeling approaches, and models directly affect the control design. In this thesis, a mathematical model based on the average arm is used to develop the controllers, and a switching model is used to verify controls' performances. Concerning the average model, there are many approaches in the literature. In [25], the average model considers a switching function model that accurately includes each SM's capacitors' dynamic.

Additionally, in [26], there is a continuous model where arms are represented by variable voltage sources function. However, a more complex average model will increase the system order, so the complexity of the proposed solution. In this way, the average model used in this research is based on [27], which uses an equivalent SM voltage, per arm.

A switching model is simulated using the proposed controller to verify the control performance. The switching model has a low-level controller, which properly attain SMs voltage balancing. The sorting algorithm implemented in the low-level control is based on the standard technique proposed by [24].

Concerning control, most of the existing results on the control strategy for MMCs consist of linear controllers, as vector control. Where only one point of operation is considered in its design and because the system's nonlinearities are disregarded [28, 29, 30].

In this point of view, one may cite works as [31], where the nonlinear MMC model is first linearized, and then linear controllers are designed for it. In a different way, [27] proposes a discrete-time bilinear model of an MMC, controlled by a sum-of-squares decomposition method, following a nonlinear analysis.

These studies are motivated by the relevance of designing nonlinear controllers that can assure stability throughout large electrical grid operation regions, including rigorous stability analysis [32, 33]. The next chapter will discuss with more detail about modeling and control of MMC.

1.4 Main objective of the thesis

This thesis's main goal is to develop an MMC's control method suitable to ensure the system state's stability, in particular circulating currents and converter stored energy.

1.4.1 Specific objectives

The following specific objectives must be accomplished:

- To develop a control method able to minimize the circulating currents and converter stored energy for an MMC converter;
- To prove the system's stabilization;
- To evaluate the control robustness for the converter's parameter variation;
- To evaluate the control gains' impacts on converter dynamics.

1.5 Main contributions

The main contributions of this thesis are to present two new nonlinear controllers applied to the MMC. The proposed techniques allow the control of the AC and DC voltages, circulating currents, and the total and balancing converter energy. Mathematical proofs are presented for its stability, which is based on Lyapunov's theory. These controllers provides asymptotically stabilization for the three-phases MMC.

1.6 Thesis's organization

This chapter presents a general discussion on this research's motivation and the state-of-the-art concerning HVDC transmission systems. Chapter 2 presents an overview regarding equipment and topologies that describe an HVDC system, and MMC modeling aspects are discussed. Additionally, the chapter presents dynamic equations of the MMC average model, represented in a bilinear form, followed by MMC switching model considerations and an overview of control design to MMC. Chapter 3 is dedicated to present the two used system tests and to a PI controller design. In chapter 4, a nonlinear controller is proposed for an MMC. In chapter 5, a bilinear control is designed. Finally, the conclusions, further research, and publications are presented in Chapter 6.

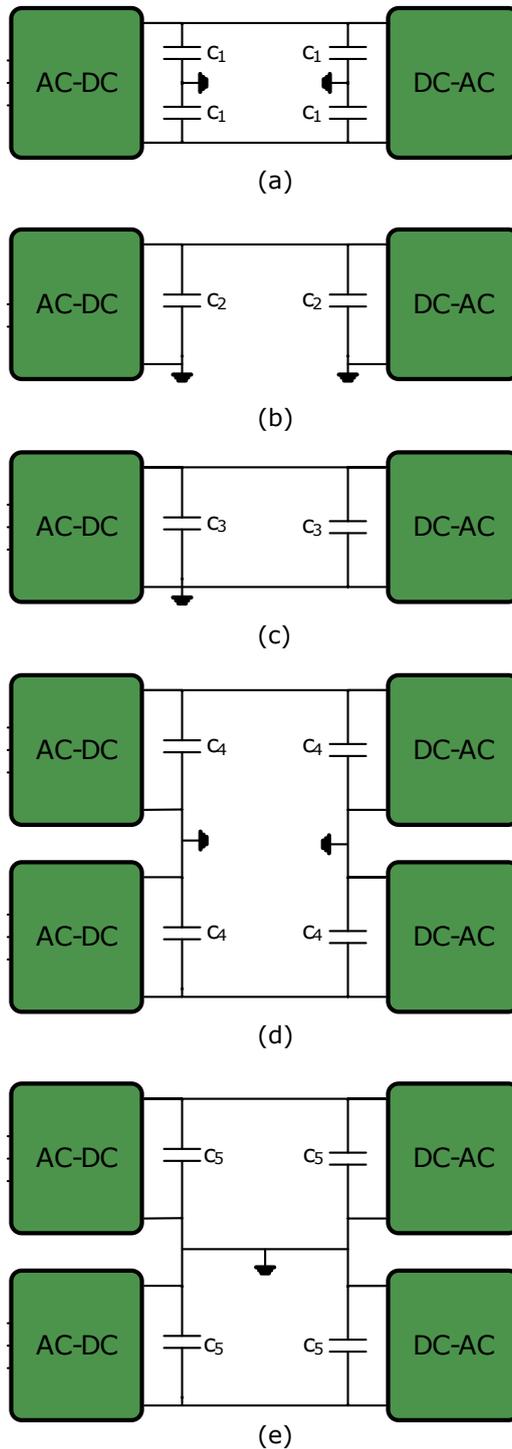


Figure 1.5: HVDC transmission line topologies. (a) Symmetric monopole. (b) Asymmetric monopole with ground return. (c) Asymmetric monopole with metallic return. (d) Bipolar with ground return. (e) Bipolar with metallic return.

Source: [16]

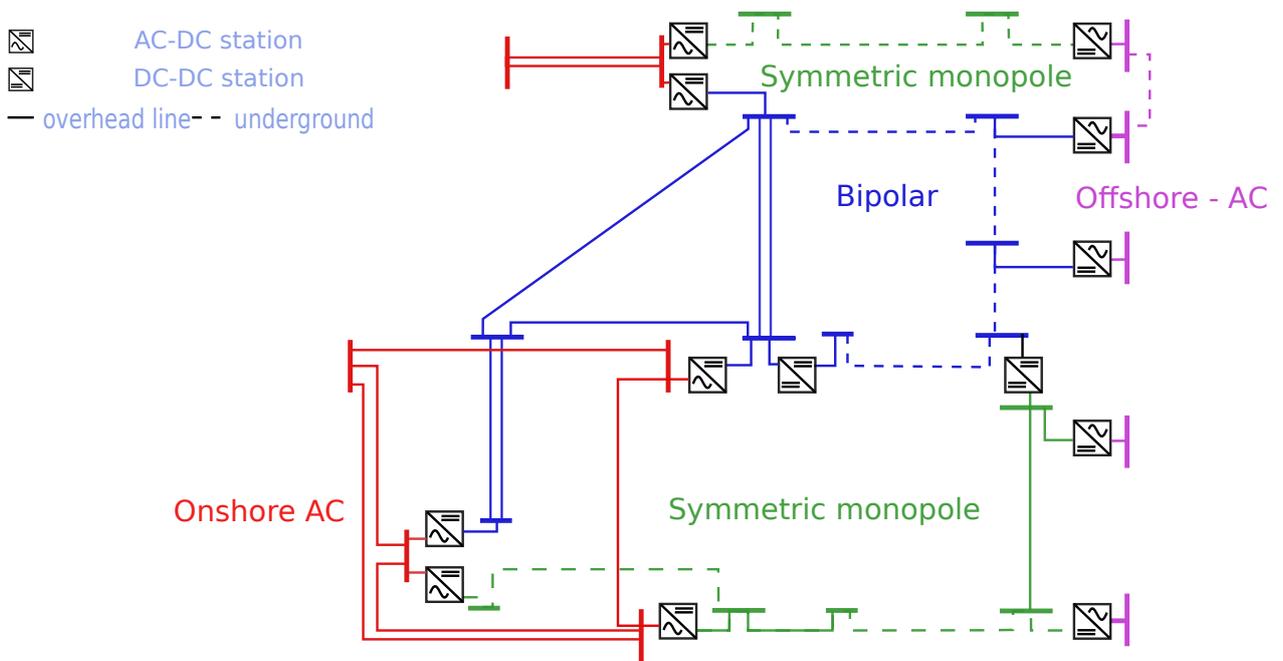


Figure 1.6: Multi-terminal test system proposed by CIGRÉ.

Source: [17]

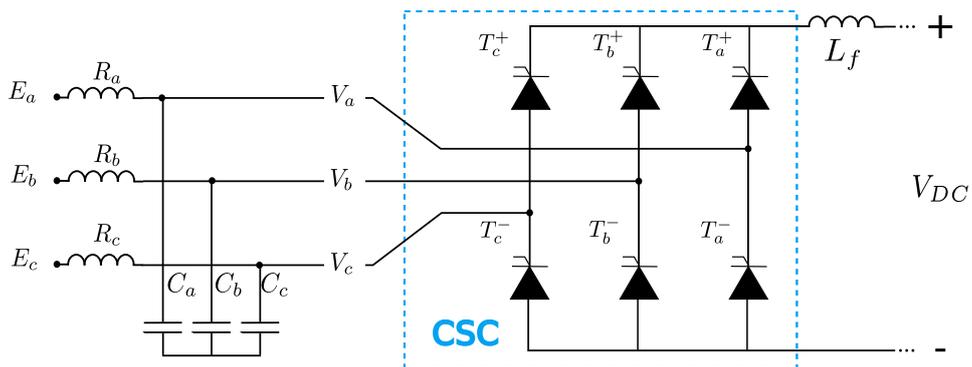


Figure 1.7: Line-commuted converter topology.

Source: [10]

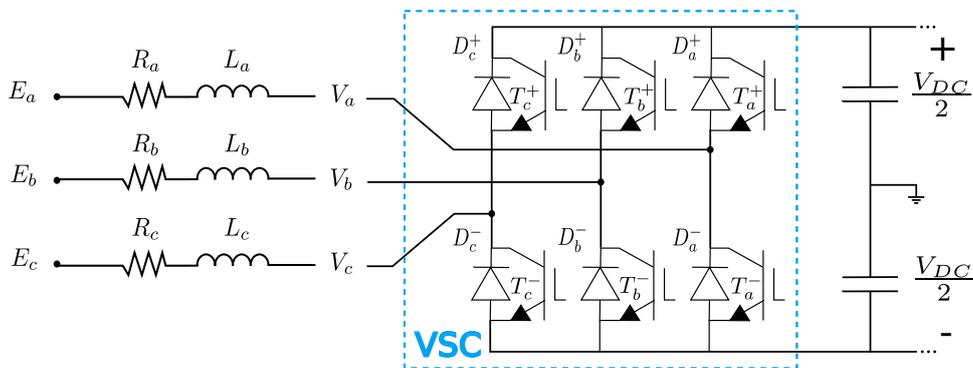


Figure 1.8: Voltage Source Converter topology.

Source: [10]

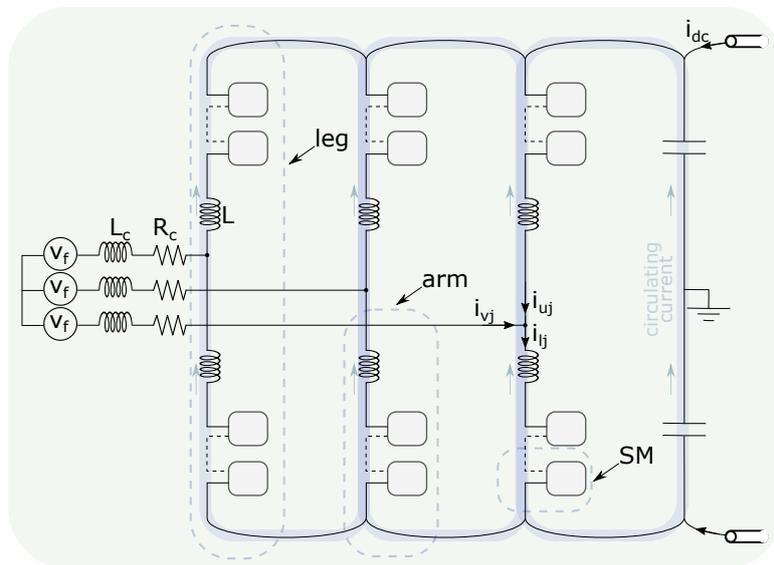


Figure 1.9: Modular Multilevel Converter topology.

Source: Author

Chapter 2

Modular Multilevel Converters

Modular Multilevel Converter (MMC) is a type of VSC for large scale power transmission. This technology has been considered the most viable solution for integrating renewable energy on the main grid, either AC or DC. Electrical grids composed of more than two nodes, connecting renewable generations, have been called Multi-terminal HVDC (MTDC), in which MMC is a suitable solution. MMC has high scalability and easy maintenance since the power level is directly related to the number of modules (SM) used.

The number of SM used on a MMC also implies the shape of the sinusoidal output voltage. A high number of SM units smooths the output voltage, reducing the need for filters. Each converter's leg produces a DC output voltage. However, the unbalance between voltage legs generates the circulating currents, for which the control is one of the challenges of this new technology.

Circulating currents are composed mainly of second and third harmonics and a DC component. The DC component is responsible for the converter's active power transfer, and the harmonics are mitigated. Other operational aspects related to MMC operation as SMs topology, modulation, and sorting algorithm of MMC are also introduced in this chapter. Furthermore, the feature related to modeling aspects and the detailed average model descriptions are presented. At last, MMC's control design is discussed.

2.1 MMC internal topology

In [11] it is first presented the MMC technology. These converters are suited to a high power scale, with even less distortion at the output voltage than the standard VSC. Although less distortion may not require filters, there is always a compromise with the cost when the converter uses many switches.

This thesis considers the symmetric monopole topology using half-bridge SM, as shown in Figure 2.1. So, a three-phase MMC with symmetric monopole topology comprehends three legs, one per phase of AC side [16]. On the other side, there is the DC terminal with two poles, positive and negative. At each leg, there are two branches, which are called arms. One of them is connected to the positive pole and the other connected to the negative pole of the DC side terminal. The subscript m denotes the physical location of the arm concerning the DC side terminal to which it is connected. Therefore, m can assume the value u or l : referring to the upper arms, for the ones in which link the AC side and the positive pole of DC side, while the l denotes the lower arms ones, that in turn is the link between the ac side and the negative pole of DC side terminal.

Converter's arm comprise N SMs connected in series and followed by an inductance L . The design of this inductor takes into account the external fault criterion.

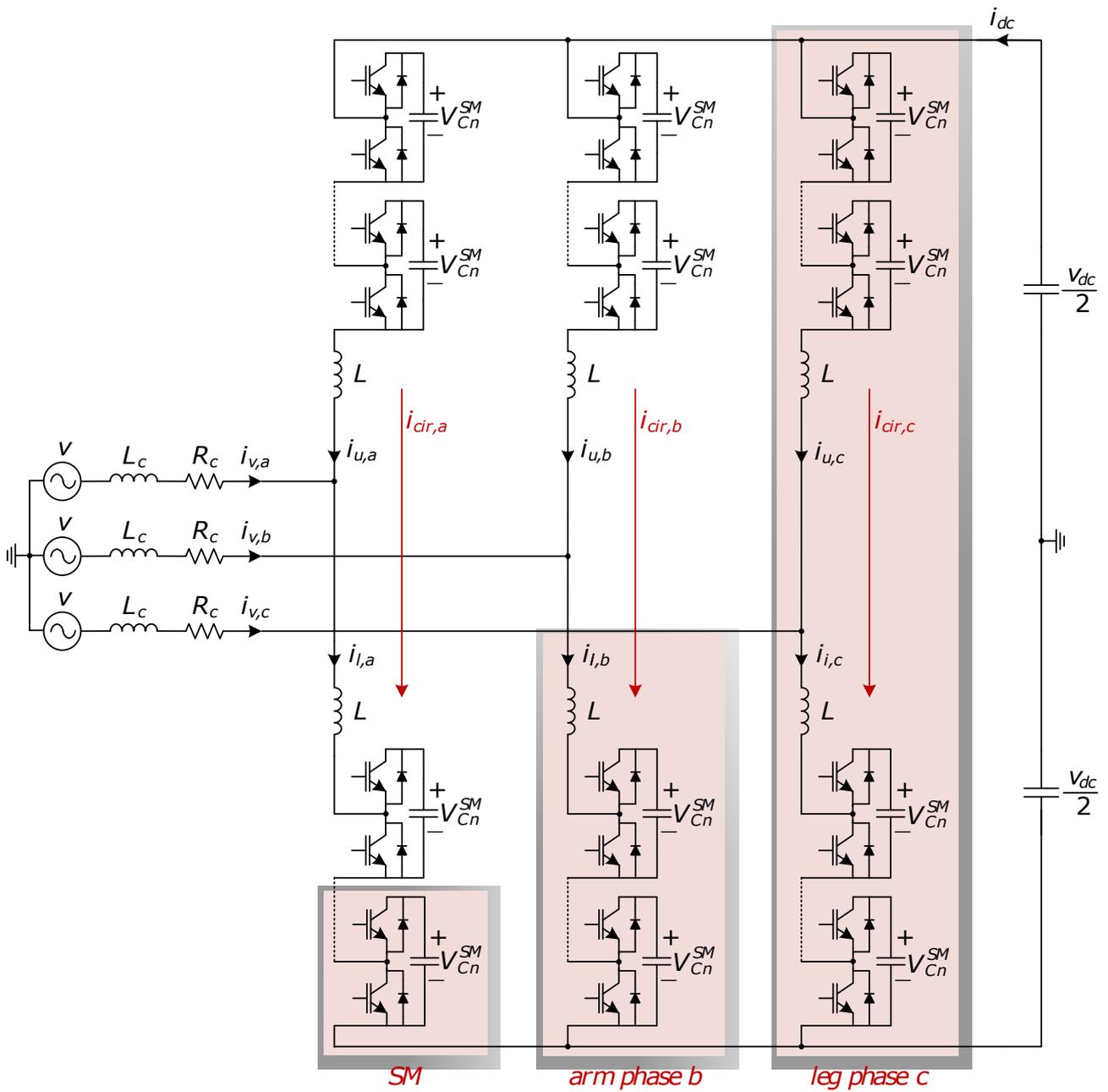


Figure 2.1: Modular Multilevel Converter (MMC) based in the symmetric monopole topology and half-bridge's SMs.

Source: Author

However, a large L , imply a slower system dynamic [34].

Regarding the modeling, it is reasonable to consider a resistance R , in series with L , which summarises the resistive behavior of the MMC. R must be the equivalent of the resistive voltage drop across conducting switches, cables, connections, and the inductor resistances. However, these effects should be minimized as much as possible since they are directly related to losses [34].

Converter dimensioning is mainly defined by the application goals. It essentially consists of the chosen number of SM per arm, which is directly related to the output voltage level. However it is necessary to consider a compromise between the number of SM and the associated cost, and even the nominal voltage of each capacitor at SM.

Converter's Submodule (SM)s are composed of IGBTs, freewheeling diode, and capacitors. These devices can be arranged in different ways: half-bridge, full-bridge, or hybrid configuration. Therefore, it allows for distinct project features.

- **Full-bridge:** A MMC based on full-bridge SM has more switching devices than the half-bridge based. Consequently, this configuration presents higher losses once two devices are in conduction per active SM. Meanwhile, DC cable fault can be handled by full-bridge SM. This topology allows the SM to generate a negative voltage, which opposes to AC voltage and restrain the short-circuit current from the DC side. This ability suits full-bridge converters to applications in overhead transmission lines, since these are more susceptible to faults [35].

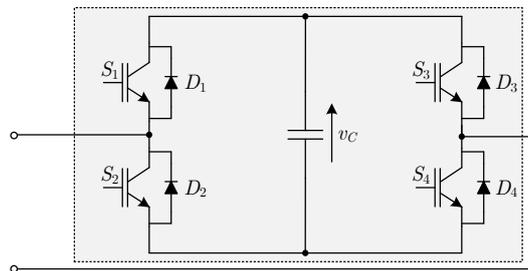


Figure 2.2: Full-bridge SM and the related output voltage.

Source: Author

- **Half-bridge:** HVDC projects usually employ half-bridge based converters; mainly in underground and submarine HVDC transmission systems. The reduced numbers of semiconductor devices reduce losses and cost compared to the full-bridge topology. However, half-bridge SMs do not have DC fault suppression ability since this configuration cannot produce a negative voltage. Therefore, it is necessary to include breakers at the terminals [36].

Due to its vast applicability, the half-bridge topology was chosen for the following analyses in this thesis.

SM's operation In general, MMC based on half-bridge SM synthesizes the output voltage defined by the PWM strategy, which manages the insertion of SMs. Each SM can produce an output voltage of two levels, $0 V$ and the capacitor voltage ($V_{C_n}^{SM}$), as shown in figure 2.3. The inserted modules are called active SM and, simultaneously, some SMs that are not active are called bypassed SM. It is possible to summarise four operation modes of half-bridge SM by figure 2.4. Active SMs

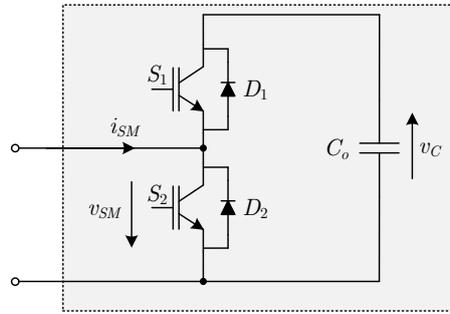


Figure 2.3: Half-bridge SM and the related output voltage.

Source: Author

are represented by a short-circuit. As noticed in this figure, the arrangement between current polarization and capacitor generates that diversity of modes [37]. The descriptions of each mode are:

- (a) S_1 is on and S_2 is off. The current has positive polarity, and the diode charges the capacitor. In this mode the SM is active;
- (b) S_1 is off and S_2 is on. The current has a positive polarity, and the capacitor is not connected. In this mode, the SM is bypassed;
- (c) S_1 is on and S_2 is off. The current has a negative polarity, and the capacitor is discharged through IGBT S_1 . In this mode the SM is active;
- (d) S_1 is off and S_2 is on. The current has a negative polarity, and the capacitor is not connected. In this mode, the SM is bypassed.
- (e) This state is out of work condition. In this case, both IGBTs, S_1 and S_2 are off, and just the freewheel diodes are used to submodule operation.
- (f) This state is out of work condition. In this case, both IGBTs, S_1 and S_2 are off, and just the freewheel diodes are used to submodule operation.

The direction that currents are flowing in Figure 2.4 are linked with the active power flow between the AC and DC side.

Modulations A MMC's leg consist of N SM connected in series. SMs are activated to ensure the desired output voltage. Modulation defines the exact time instants to change the status of each SM between active or bypassed. By modulating the commands of the SM, it is possible to generate a signal as the desired output voltage. To attain the desired reference voltage, the converter's controller generates the modulation, defining the exact moment to activate each SM. Modulation is the synthesis of a reference signal using pulse trains with the same average voltage at any instant [24].

There are several types of modulation strategies. They affect the total converter losses, the energy balance on the converter's arms, and voltage balancing across SMs capacitors. A proper modulation method choice implies significant dynamic effects, as mentioned above, with no further controllers [36, 38, 39, 40, 41].

In [24], modulation techniques are classified according to the switching frequency imposed on the converters, as high-switching PWM and fundamental-frequency modulation (also known as Staircase modulation).

The high switching PWM comprehends Space Vector Modulation (SVM) and Sinusoidal Pulse Width Modulation (SPWM), and also of their variations. They

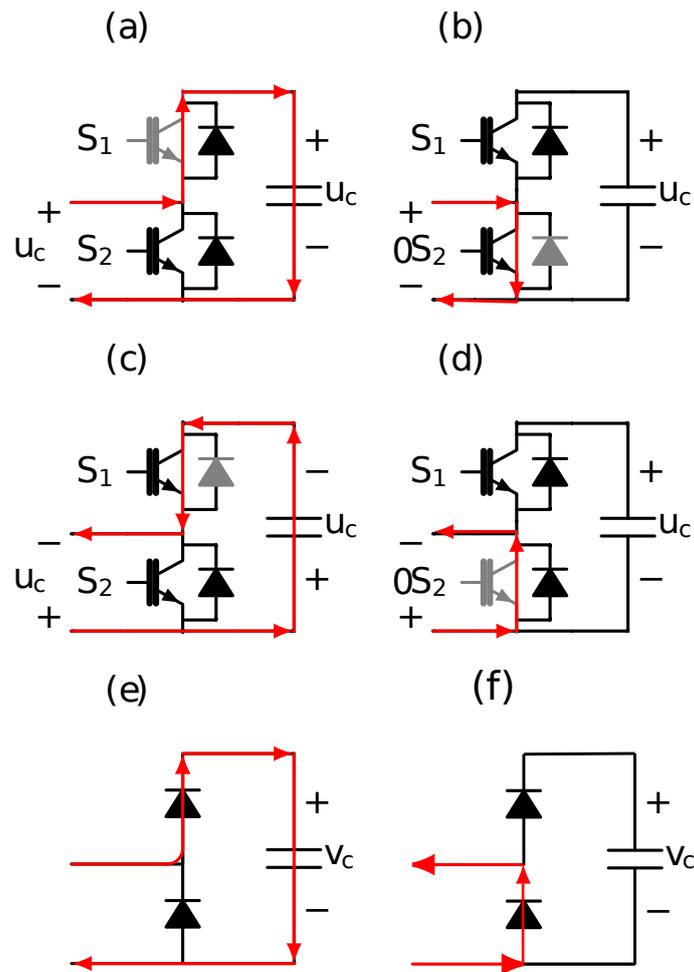


Figure 2.4: Possible SM operations. a) active SM with positive current; b) bypassed SM with positive current; c) active SM with negative current; d) bypassed SM with negative current and; (e) and (f) submodule equivalent blocked state.

Source: Author

are popular thanks to their simple implementation obtained from the two-level conventional PWM.

In [42], SPWM techniques are classified as follow:

- PWM carrier:
 - carrier-disposition:
 - * phase disposition;
 - * phase opposition disposition;
 - * alternate phase opposition disposition.
 - subharmonic techniques:
 - * saw-tooth;
 - * phase-shifted carrier-based.
- Reference signal:
 - one reference;
 - two references;
 - multiple references.

At fundamental-frequency modulation, the submodule switches once per cycle, and this became attractive thanks to the reduction of switching losses. This class of modulation comprehends Selective Harmonic Elimination (SHE) and Nearest-Level (NL) [43]. These techniques are often designed for practical applications on MMC [44].

This research will not attain to describe further details concerning each modulation; however, table 2.1 summarises the most traditional modulation techniques and their features.

While performing MMC simulation, the modulation must be considered. For an average model approach, it is necessary to have a well-performed modulation to produce a smooth and nearly to ideal sinusoidal output voltage per arm. Therefore, when using average model this research considers that the modulation is already well designed and able to balance SM capacitors' voltage. These previous conditions are necessary to the mathematical propositions on controllers on chapter 4 and chapter 5, where an MMC average model is considered. On the other hand, a phase-shift PWM is considered for the switching model performed on SIMULINK.

SM capacitor voltage balancing and sorting algorithm Modulation techniques can be combined with sorting algorithms to regulate SM capacitor voltages. A sorting algorithm is a low-level control strategy that can be used as an interface between modulation and SM's activation. It is in charge of the capacitor voltage balancing. The use of these algorithms can help to reduce switching losses and circulate currents. Therefore a sorting algorithm can adequately choose the SM activation sequence in a way to balance the SM's capacitor charge.

An active SM contributes to the output voltage in the arm in which it is placed. Regarding the SM capacitor voltage, it is expected to maintain an average value in all SMs to produce the same output voltage level per phase and smaller circulating currents, which reduces converter losses. For this purpose, the sorting algorithm is used to sort the SM arms to be active, considering their voltage. As a result, the desired output voltage is produced, and SM capacitor's loads are balanced.

Switching frequency	Modulation method	Feature
fundamental frequency modulation	SHE	This modulation define switching patterns which can eliminates the low-order harmonics of the output voltage waveform. The method calculates switching patterns and saves in tables for various modulation indices and the output-voltage phase angle [45, 46].
Fundamental frequency modulation	NL	This method is suitable for high-level MMC. Consists of choosing the output voltage level nearest to the reference. The harmonic content of the output voltage is inversely related to the converter level: as bigger the number of submodules, the harmonic content on the output is smaller. Compared to SHE, the implementation of this technique is less complex and requires less computational effort [42].
high switching PWM	SVM	This method consists of determining the switching sequences and the duty cycle of switching. An algorithm determines the vectors adjacent to the reference signal. A diagram composed of state vectors is used. Thus, the algorithm decides the vectors and vector zero-order, finally defining each switching device's states. [47] propose a general scheme for performing the SVM for multilevel inverters, in addition to a method for calculating the duty cycle and determining the switching sequence.
high switching PWM	SPWM	The SPWM consists of comparing a sinusoidal reference signal (modulation) with a triangular high-frequency waveform (carrier), thus generating a sequence of pulses. For multilevel converters, PWM can be performed through one or more modulating waveform, comparing them to multiple carriers. Thus, [42] summarize some SPWM modulation techniques according to the carriers' provisions and the number of modulators as presented above [48, 38].

Table 2.1: Modulation features.

There are many sorting algorithm techniques [42, 44, 49], and the traditional one is described in the flowchart in figure 2.5.

By using the traditional sorting algorithm presented on figure 2.5, the SMs capacitors voltage share of each converter arms at each period of PWM is accomplished. Modulation defines the number of submodules N to be activated in the arm m . SM capacitor voltages are measured and classified per arm. If the current arm m is positive, the algorithm identifies and activates the N submodules with the lowest voltages. Consequently, the current charges the corresponding inserted SM capacitors, and their voltages increase.

On the other hand, if the current is negative, the algorithm identifies and activates the SMs with the highest voltages. So, the current discharges the corresponding inserted SM capacitors, and their voltages decrease. Capacitors of bypassed submodules remain unchanged.

Despite the advantages mentioned above, there are disadvantages to the use of the traditional sorting algorithm. Although it achieves the capacitors' voltage

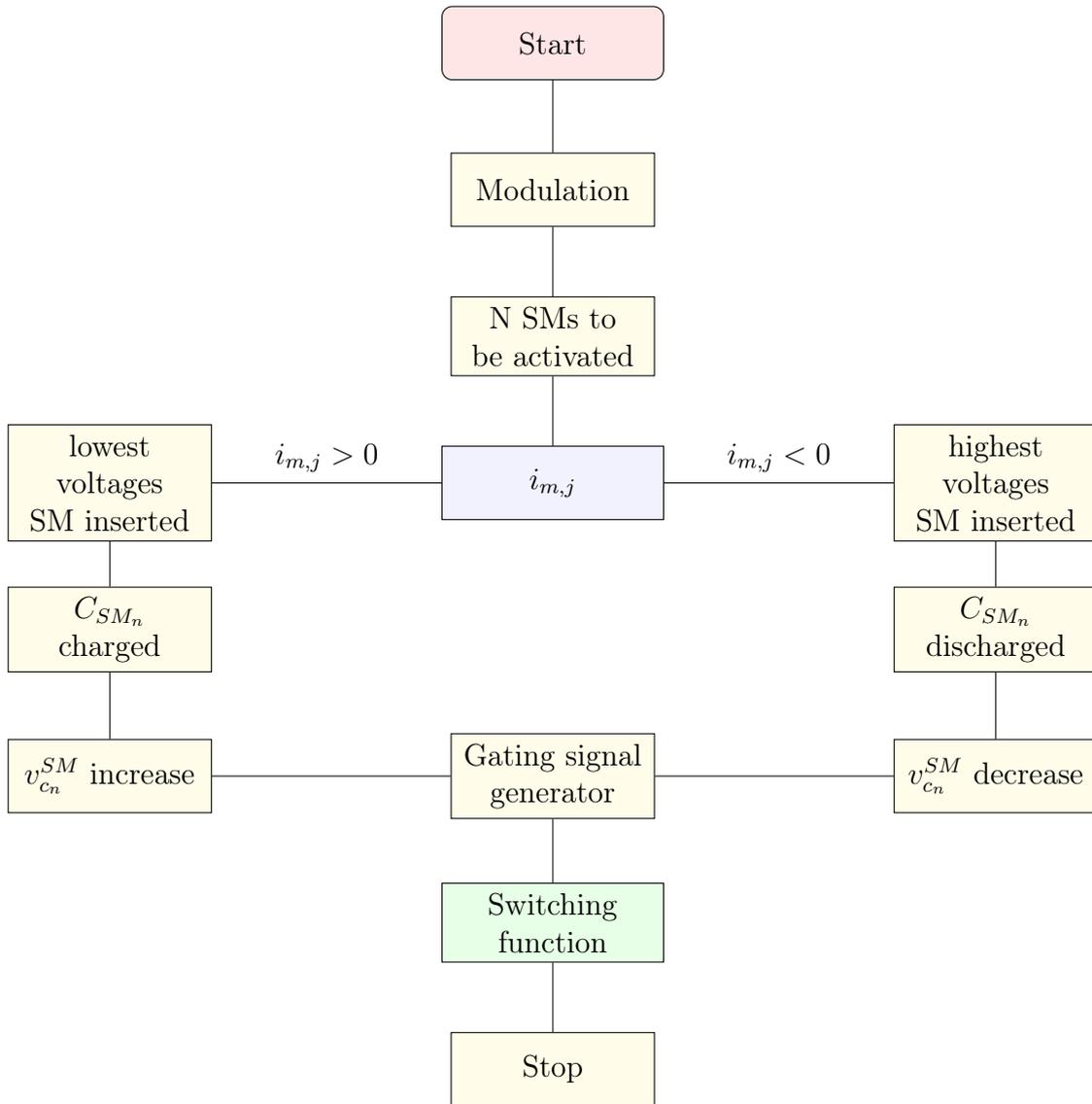


Figure 2.5: Traditional sorting algorithm achievement during one PWM period.

Source: Author

share for the MMC operating points, it increases the number of switching transitions among the SMs. Because of the sorting algorithm may change the submodule status (inserted/bypassed) through two consecutive PWM periods in which there is no change of inserted number N . The higher switching frequency also raises the power losses, which are undesirable in high-power systems projects.

This thesis use a sorting algorithm presented by [24]. The author considers that the phase-shift modulation technique combined with the sorting algorithm provides sufficient capacitor voltage share and contributes with a discussion concerning the attained results.

Circulating Current DC voltage generated by each leg is not necessarily balanced. Because of this unbalance, currents circulate in the three phases of the converter, and they are called circulating currents. They do not affect AC side currents, but produce the equivalent DC current (i_{dc}) [50].

Circulating currents ($i_{cir,abc}$ presented in figure (2.1)) are composed of a DC component and AC component, with the double of the grid nominal frequency. While the DC component is essential for the transmission of real power, the AC component needs to be mitigated. This comprehends one of the technical challenges of MMC technology, once these circulating currents can increase con-

verter's losses.

Phase Locked Loop It is fundamental to consider proper synchronization with the AC grid voltages and the MMC control. The synchronization process detects the positive-sequence voltage component at the fundamental frequency, so the magnitude and angle are used to convert voltage and control variables into rotating reference frames [51].

In this thesis, Phase Locked Loop (PLL) technique is used to detect positive-sequence voltages for the MMC switched model. In order to do that, the rotating reference frame ($dq0$) will follow the vectors of the alternating system (abc), with the same frequency and angle.

In Figure 2.6, the PLL schematic is presented. This circuit generates, using Park transformation, the signal $v_{f,d}$ which is synchronized with the fundamental component of v_a (see Figure 2.1). Also, frequency and phase angle θ are estimated either in steady state or during electromagnetic transients.

The quadrature axis produced ($v_{f,q}$) is the phase difference between the abc signal and the direct rotating frame. $v_{f,q}$ is controlled by PI to be equal to zero, and the angular velocity ω_0 is obtained. Integrating angular velocity, the phase angle θ is achieved. Additionally, homopolar component zero is null for balanced AC systems.

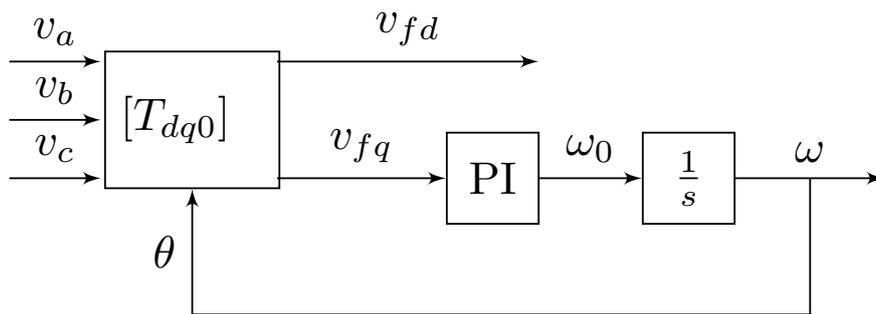


Figure 2.6: PLL internal diagram.

Source: [51]

2.2 Modeling

In order to develop an accurate MMC model, it should consider a high number of electrical nodes, a strong coupling effect among states, and an extensive set of operating points [52].

A MMC converter comprehends hundreds of SM independently controlled. Each arm of a MMC behaves as a variable voltage source, which allows controlling the output voltages (AC and DC) independently. Meanwhile, it results in an increase of the modeling complexity, in comparison with standard VSCs. A MMC model, which comprehends all intrinsic switching dynamics, is a computational challenge, once a high number of switching devices [36]. However, there are many simplified and computationally realizable models proposed by the literature.

Figure 2.7, adapted from [52], summarises different model types, often discussed in literature. In this figure, the computational effort increases from left to

right. There are two main divisions: full order models and reduced-order average models. Full order models describe each element and reduced-order models combine elements and describe it by a combined behavior.

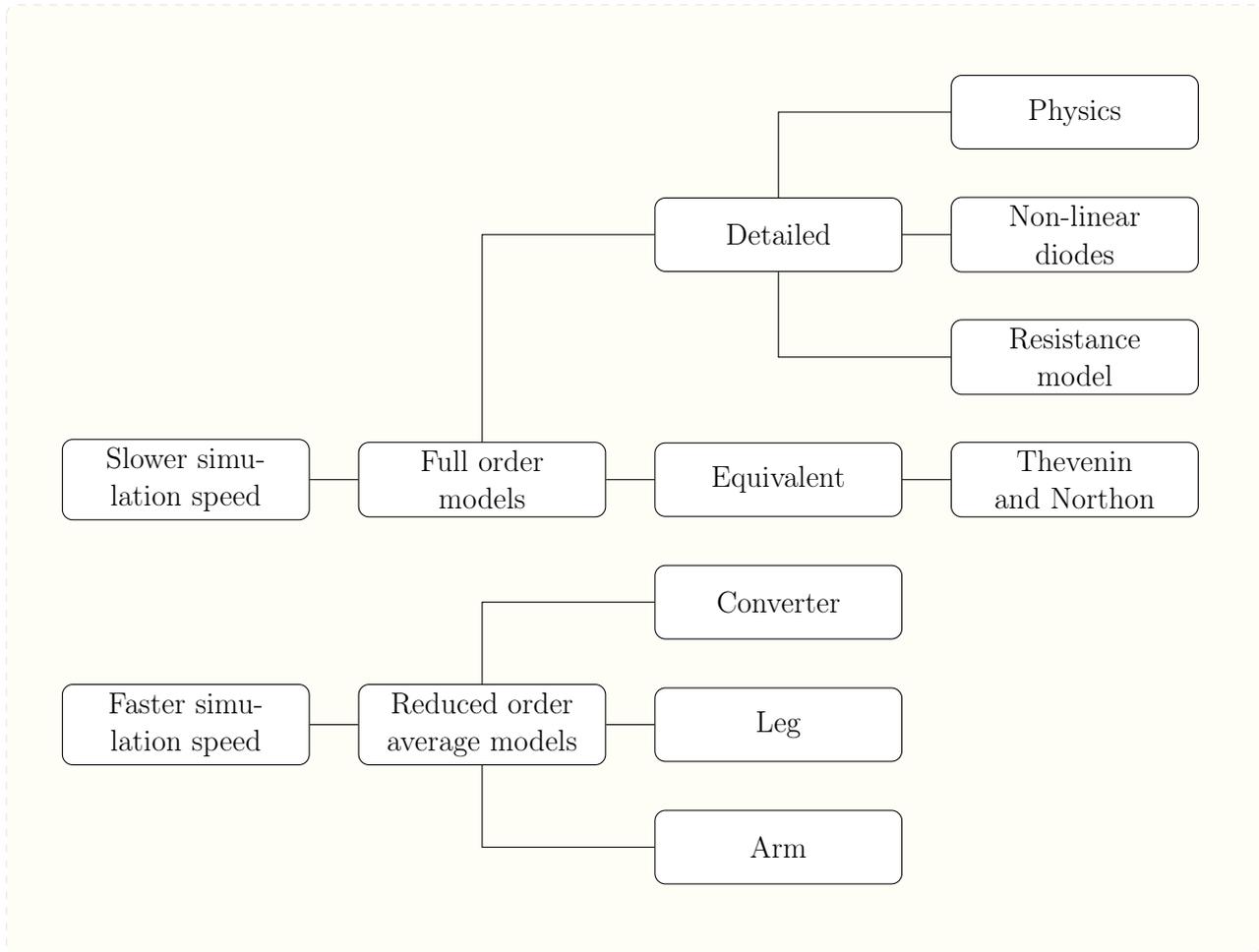


Figure 2.7: Summary of MMC models.

Source: Author

2.2.1 Full order models

Concerning more complex model representations, they use the classical nodal admittance method to describe the system. Usually, lumped elements are integrated by trapezoidal rule, as shown in figure 2.8 and the distributed elements are modeled by Bergeron's method. Also, subsequent time-dependent topology represents non-linear elements, like semiconductors, which results in a simulation computationally intensive [36]. In figure 2.8 lumped elements on the left side and equivalent elements on the right, as: (a) resistor, (b) inductor and equivalent Bergeron, (c) capacitor and equivalent Bergeron (d) a IGBT and the representation using two resistors which represent the active and the bypassed state of the switching element. This model simplify the complexity imposed by IGBTs. With this goal, IGBTs are replaced by a large resistor (R_{off}), for the no conduction state, and a small resistor (R_{on}), for the conduction state. The resistance is defined by the signal and current direction on a node that represents the gate of the IGBT.

This group of methods can reproduce the internal converter's dynamics, including all capacitor voltages and the circulating current. Therefore, the model describes with high accuracy all system phenomena. This modeling usually is used to validate another MMC simplified model.

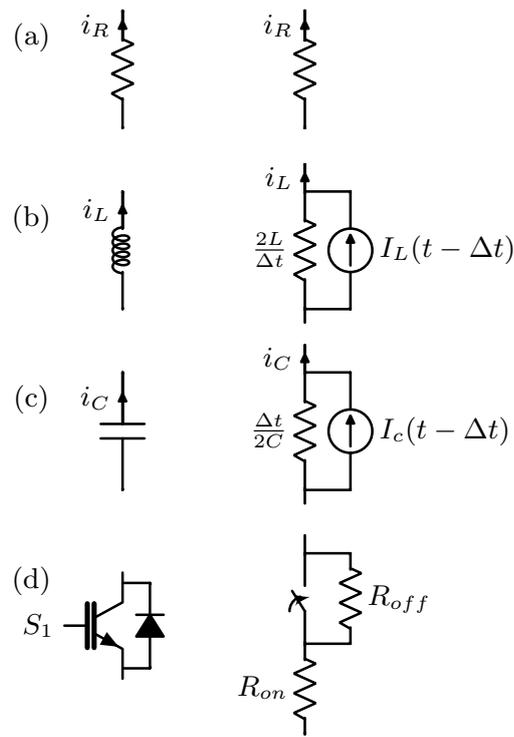


Figure 2.8: Lumped elements on the left side and equivalent elements on the right. (a) resistor, (b) inductor, (c) capacitor and (d) IGBT.

Source: [10]

Regarding detailed models, these can also use different representations of semiconductors since the full physics model is one of the closest representations of a MMC. Detailed models use the exactly equivalent circuit or their differential equation for the IGBTs. Also, use nonlinear functions or other representations [36, 53]. However, full order models have a hundred nodes to be simulated, which result in a large admittance matrix that is inverted for each converter switch. This process requires an excessive computational load resulting in a slow simulation [52].

In the literature, there are many MMC models that have moderate processing time and present an adequate performance in transient and steady-state as the real system behaviors. One of these modeling methods is the Equivalent Circuit Based (ECB) Model as Thevenin's Equivalent (TE) in which SMs are replaced by the Thevenin or Norton equivalent circuit [25, 53, 54], as shown figure 2.9.

This method drastically reduces the number of nodes on the system. It is

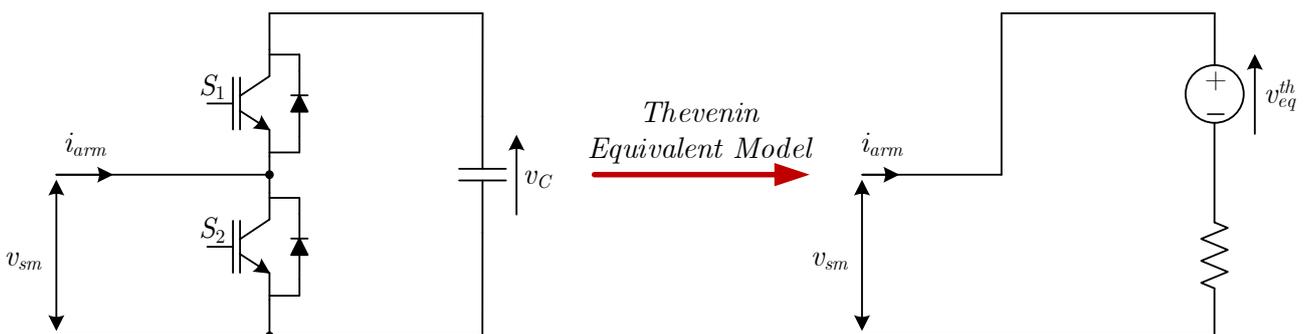


Figure 2.9: Thevenin equivalent SM.

Source: [54]

solved by linear algebraic relations which enables real-time simulation and is ideal for parallelization. Another option for real-time simulation and parallelization is the switching function models that use state-space formulation [55]. This model reduces the system dynamics to a controlled current and voltage source. However, it is computationally intense and does not enable fault study [36].

2.2.2 Reduced order average model

In order to achieve a faster simulation of MMC, reduced-order models have been proposed in the literature. These models are called Average-model (AVM) and consist of reducing the number of state variables inside the model by making some hypotheses. The AVM approximates the switching effects of all SMs in an arm by the continuous voltage source, and it is assumed perfect balancing between the SM capacitor voltages [27, 52, 56, 57, 58]. These models integrate the dynamic of capacitors and their coupling effects with the arm current [55].

AVM are considered as very straightforward and easy to use for control design [55]. The approach of AVM considers the hypothesis that modulation can do SMs capacitor voltage balancing. This hypothesis is the critical point for an accurate representation of a MMC. However, this modeling is suited for many signal analysis, steady-state studies, and power-flow analyses. Indeed average model is robust and easily scalable, as well as it is much faster than a detailed model (about 370 times) and quicker than a simplified equivalent model (about seven times) [57].

For all these reasons, the reduced-order average model will be considered in this thesis to design the controllers.

2.2.3 Derivation of reduced order average model

Regarding mathematical modeling, state-space is used to describe the dynamics of the systems. This approach is often adopted at the general literature and modeling MMC due to the ease of manipulation it offers. Most models presented above can be represented by state-space, where the difference lies in the chosen state variables [55, 56].

Two hypotheses are considered for the MMC circuit modeled for this thesis:

- As aforementioned, considering the hypothesis that modulation can provide SMs capacitor voltage balancing, the reduced-order average model circuit is shown in figure (2.10);
- The voltage on the DC link, imposed over the capacitors, is controlled by the converter at the other end of the DC link, so two ideal voltage sources are connected in series in the DC circuit, each one with $V_{DC}/2$ voltage.

This circuit is the main model considered in this thesis, it is based on [27]. There are no capacitors directly described in this model, so this state-space model neglects the coupling effect between the inductor currents and capacitor voltages. AC current ($i_{v,abc}$), circulating current ($i_{cir,abc}$), total stored energy (W_h), and balancing stored energy (W_v) were chosen as state variables.

From the illustration of a MMC in figure 2.10 the state-space can be constructed. The N SMs connected per arm produce an equivalent voltage source equal to $v_{m,j}$. It is a three-phase converter and each phase ($j = a, b$ and c) is connected with a leg that consists of upper and lower arms ($m = u$ or l).

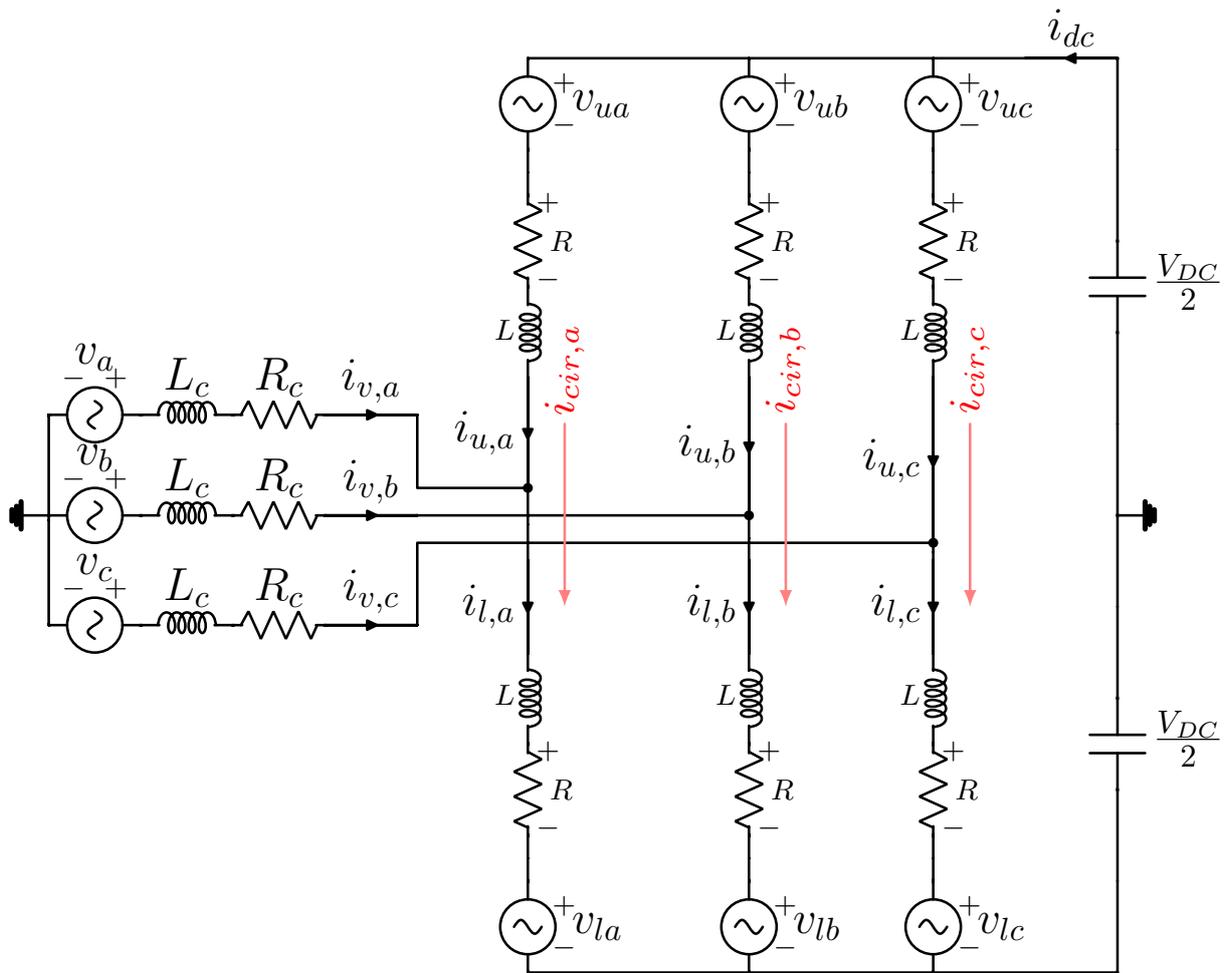


Figure 2.10: Average model of a three-phase MMC.

Source: Author

An inductance L follows the equivalent voltage source in series with resistance R . L needs to consider the external fault criterion, while R summarises the resistive behavior of the MMC (resistive voltage drop across conducting switches, cables, connections, and the inductor resistances). On the AC side, an RL filter is considered per phase (R_c and L_c).

In figure 2.11 it is considered phase j from the MMC average model circuit shown in figure 2.10. Applying Kirchhoff's voltage law on upper arm (figure 2.11(a)), from V_{DC} to $v_{f,j}$ is obtained equation 2.1. If equation (2.1) is equals to zero, equation (2.2) is obtained. About the lower arm (figure 2.11 (b)) from V_{DC} to $v_{f,j}$ there is equation 2.3 and rearranging it is obtained equation 2.4.

$$\frac{V_{DC}}{2} - v_{u,j} - Ri_{u,j} - L\dot{i}_{u,j} + R_c i_{v,j} + L_c \dot{i}_{v,j} - v_{f,j} = 0 \quad (2.1)$$

$$-\frac{V_{DC}}{2} = -v_{u,j} - Ri_{u,j} - L\dot{i}_{u,j} + R_c i_{v,j} + L_c \dot{i}_{v,j} - v_{f,j} \quad (2.2)$$

$$-\frac{V_{DC}}{2} + v_{l,j} + Ri_{l,j} + L\dot{i}_{l,j} + R_c i_{v,j} + L_c \dot{i}_{v,j} - v_{f,j} = 0 \quad (2.3)$$

$$\frac{V_{DC}}{2} = v_{l,j} + Ri_{l,j} + L\dot{i}_{l,j} + R_c i_{v,j} + L_c \dot{i}_{v,j} - v_{f,j}. \quad (2.4)$$

Kirchhoff's current law on the node identified in figure 2.11 defines AC current $i_{v,j}$, related to upper and lower current:

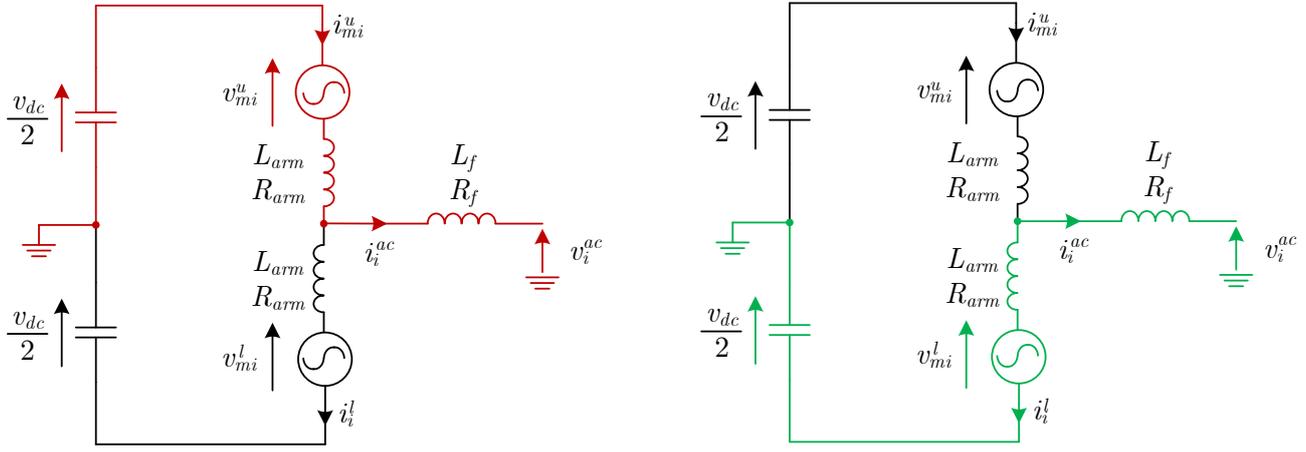


Figure 2.11: Kirchhoff's voltage law for upper arm (a) and lower arm (b) at phase j .
Source: Author

$$i_{v,j} = -i_{u,j} + i_{l,j} \quad (2.5)$$

The arm currents ($i_{u,j}$ and $i_{l,j}$) can be rewritten in terms of circulating current ($i_{cir,j}$) and AC side current ($i_{v,j}$). It is considered that $i_{v,j}$ equally distributed to upper and lower arm and that there are circulating currents flowing between legs, defined in (2.6) and (2.7).

$$i_{u,j} = -\frac{i_{v,j}}{2} + i_{cir,j} \quad (2.6)$$

$$i_{l,j} = \frac{i_{v,j}}{2} + i_{cir,j} \quad (2.7)$$

Adding (2.6) and (2.7) are obtained circulating currents expression in (2.8).

$$i_{cir,j} = \frac{i_{u,j} + i_{l,j}}{2} \quad (2.8)$$

Power-flow equations Adding (2.2) to (2.4):

$$0 = -v_{u,j} + v_{l,j} + R(-i_{u,j} + i_{l,j}) + L(-\dot{i}_{u,j} + \dot{i}_{l,j}) + 2R_c \dot{i}_{v,j} + 2L_c \dot{i}_{v,j} \quad (2.9)$$

Replacing (2.5) in (2.9):

$$L\dot{i}_{v,j} + 2L_c\dot{i}_{v,j} = v_{u,j} - v_{l,j} - Ri_{v,j} - 2R_c i_{v,j} \quad (2.10)$$

Considering the following notation:

$$R_{eq} = R + 2R_c \quad (2.11)$$

$$L_{eq} = L + 2L_c \quad (2.12)$$

Rearranging (2.10) one obtains the current dynamic (2.13), for the phase j from the AC side. This equation describes and enables the control of active and reactive power at AC side.

$$\dot{i}_{v,j} = -\frac{R_{eq}}{L_{eq}}i_{v,j} + \frac{v_{u,j} - v_{l,j}}{L_{eq}} + \frac{2v_{f,j}}{Leq} \quad (2.13)$$

By subtracting (2.4) from (2.2):

$$-V_{DC} = -v_{u,j} - v_{l,j} - R(i_{u,j} + i_{l,j}) - L(\dot{i}_{u,j} + \dot{i}_{l,j}) \quad (2.14)$$

Substituting (2.8) in (2.14):

$$-V_{DC} = -v_{u,j} - v_{l,j} - 2Ri_{cir,j} - 2L\dot{i}_{cir,j} \quad (2.15)$$

Rearranging (2.15) it is obtained the dynamic equation for the circulating current, which describes and enables DC power control.

$$\dot{i}_{cir,j} = -\frac{R}{L}i_{cir,j} - \frac{v_{u,j} + v_{l,j}}{2L} + \frac{V_{DC}}{2L} \quad (2.16)$$

Converter energies equation Even though the average model neglects SM capacitor effect, their combined contribution to converter dynamics is included in the model by the energy expression.

MMC is the first technology of converter to enable independent control of AC and DC current. This control is directly linked to converter power input and output. This power difference results in the SMs capacitors load. In other words, the real operation of a MMC implies voltage changes of SM's capacitor. In this way, SMs will be suitable to synthesize the output DC voltage, and, consequently, the output currents are driven.

Based on this, achieving the voltage on SMs's capacitor results in a certain amount of stored energy per SM. Therefore, the total amount of energy stored (also called in the literature as horizontal balancing) in MMC will be considered as a state, as well as the difference between the energy stored on the upper and lower arms (also called vertical balancing).

- Total energy or horizontal balancing (W_h): describes an energy distribution in horizontal direction (through AC to DC side), summing the energy of each arm, to achieve the desired total converter energy.
- Energy balancing or vertical balancing (W_v): describes an energy distribution through all upper arms in comparison with all lower arms, to achieve equal energy distribution between converter's upper and lower arms.

MMC energy control is mandatory to converter proper operation. Also, it is possible to use the internal energy to propose new control objectives, either for fast frequency support (or inertial support) or for imbalanced operation with different upper and lower arm's energy, as presented in [59].

So, converter total energy derivative is described at equation (2.17), where each equivalent source per arm times arm current are considered. Finally, total converter power is represented by the derivative of energy.

$$\dot{W}_h = \sum_{m=u}^l \sum_{j=a}^c v_{m,j} i_{m,j} \quad (2.17)$$

Equation (2.6) and equation (2.7) replaced at equation (2.17) to obtain the final equation based on $i_{v,j}$ and $i_{cir,j}$ that are chosen as state variables. So, equation (2.18) is obtained.

$$\dot{W}_h = \sum_{j=a}^c v_{u,j} \left(-\frac{i_{v,j}}{2} + i_{cir,j} \right) + \sum_{j=a}^c v_{l,j} \left(\frac{i_{v,j}}{2} + i_{cir,j} \right) \quad (2.18)$$

Considering that the AC and DC power produced by each converter part (upper or lower) the converter balancing energy is defined in equation (2.19):

$$\dot{W}_v = \sum_{j=a}^c v_{u,j} i_{u,j} - \sum_{j=a}^c v_{l,j} i_{l,j} \quad (2.19)$$

Equation 2.6 and equation 2.7 are replaced in equation 2.19 to obtain the final equation based on $i_{v,j}$ and $i_{cir,j}$, which are the chosen state variables. So, equation 2.20 is obtained.

$$\dot{W}_v = \sum_{j=a}^c v_{u,j} \left(-\frac{i_{v,j}}{2} + i_{cir,j} \right) - \sum_{j=a}^c v_{l,j} \left(\frac{i_{v,j}}{2} + i_{cir,j} \right) \quad (2.20)$$

In others words, the energy related state variable W_h corresponds to the total energy stored in the SM capacitors and can also be obtained as:

$$W_h = W_u + W_l \quad (2.21)$$

where W_u is the energy stored in the upper arm SM capacitors and W_l the energy stored in the lower arm SM capacitors. As for the energy balancing W_v it can be obtained as difference between upper and lower arm's stored energy as:

$$W_v = W_u - W_l. \quad (2.22)$$

The stored energy in the upper and the lower arm can be obtained from the SM capacitor's voltage as:

$$W_k = \frac{C_{SM}}{2} \sum_{j=1}^3 \sum_{i=1}^N v_{C,ki,j}^2 \quad (2.23)$$

where k indicates upper u or lower l arms, j the phases of the converter and i indicates the SMs.

Change of reference by Park's transformation Park's transformation is widely used in the electrical power system to simplify three-phase system analyses. Park's transformation uses a rotational matrix that transforms a balanced three-phase system (AC) into a two-phase system (DC). The two-phase system is rotating by a reference frame. The frequency of the rotation is linked with the frequency of one AC phase.

An abc system can be transformed in $dq0$ by using the matrix T bellow

$$T = \frac{2}{3} \begin{bmatrix} \cos(\theta) & \cos(\theta - \frac{2\pi}{3}) & \cos(\theta + \frac{2\pi}{3}) \\ -\sin(\theta) & -\sin(\theta - \frac{2\pi}{3}) & -\sin(\theta + \frac{2\pi}{3}) \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix} \quad (2.24)$$

$$x_{qd0} = T x_{abc} \quad (2.25)$$

and the inverse transformation ($dq0$ to abc) can be obtained by

$$T^1 = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & \frac{1}{2} \\ \cos(\theta - \frac{2\pi}{3}) & -\sin(\theta - \frac{2\pi}{3}) & \frac{1}{2} \\ \cos(\theta + \frac{2\pi}{3}) & -\sin(\theta + \frac{2\pi}{3}) & \frac{1}{2} \end{bmatrix} \quad (2.26)$$

$$x_{abc} = T^{-1}x_{dq0} \quad (2.27)$$

MMC reduced order average model in $dq0$ reference frame Considering Park's transformation matrix T, the three-phase MMC system will turns into $dq0$ reference frame. To illustrate the transformation process (2.13) is rewritten in (2.28).

$$\begin{bmatrix} \dot{i}_{v,a} \\ \dot{i}_{v,b} \\ \dot{i}_{v,c} \end{bmatrix} = \begin{bmatrix} -\frac{R_{eq}}{L_{eq}} & 0 & 0 \\ 0 & -\frac{R_{eq}}{L_{eq}} & 0 \\ 0 & 0 & -\frac{R_{eq}}{L_{eq}} \end{bmatrix} \begin{bmatrix} i_{v,a} \\ i_{v,b} \\ i_{v,c} \end{bmatrix} + \begin{bmatrix} \frac{1}{L_{eq}} & 0 & 0 \\ 0 & \frac{1}{L_{eq}} & 0 \\ 0 & 0 & \frac{1}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{u,a} - v_{l,a} \\ v_{u,b} - v_{l,b} \\ v_{u,c} - v_{l,c} \end{bmatrix} + \begin{bmatrix} \frac{2}{L_{eq}} & 0 & 0 \\ 0 & \frac{2}{L_{eq}} & 0 \\ 0 & 0 & \frac{2}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{f,a} \\ v_{f,b} \\ v_{f,c} \end{bmatrix} \quad (2.28)$$

Using matrix T of Park's transformation in equation (2.28) equation (2.29) is obtained.

$$\begin{bmatrix} \dot{i}_{v,d} \\ \dot{i}_{v,q} \\ \dot{i}_{v,0} \end{bmatrix} = \begin{bmatrix} -\frac{R_{eq}}{L_{eq}} & \omega & 0 \\ -\omega & -\frac{R_{eq}}{L_{eq}} & 0 \\ 0 & 0 & -\frac{R_{eq}}{L_{eq}} \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{v,0} \end{bmatrix} + \begin{bmatrix} \frac{1}{L_{eq}} & 0 & 0 \\ 0 & \frac{1}{L_{eq}} & 0 \\ 0 & 0 & \frac{1}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{u,d} - v_{l,d} \\ v_{u,q} - v_{l,q} \\ v_{u,0} - v_{l,0} \end{bmatrix} + \begin{bmatrix} \frac{2}{L_{eq}} & 0 & 0 \\ 0 & \frac{2}{L_{eq}} & 0 \\ 0 & 0 & \frac{2}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{f,d} \\ v_{f,q} \\ v_{f,0} \end{bmatrix} \quad (2.29)$$

Taking into account that in the equilibrium of balanced systems, the zero components are equal to zero (boxed terms in (2.29)), then equation (2.29) can be rewritten as a system (2.30), which describes the AC current state variables that should be controlled.

$$\begin{bmatrix} \dot{i}_{v,d} \\ \dot{i}_{v,q} \end{bmatrix} = \begin{bmatrix} -\frac{R_{eq}}{L_{eq}} & \omega \\ -\omega & -\frac{R_{eq}}{L_{eq}} \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \end{bmatrix} + \begin{bmatrix} \frac{1}{L_{eq}} & 0 \\ 0 & \frac{1}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{u,d} - v_{l,d} \\ v_{u,q} - v_{l,q} \end{bmatrix} + \begin{bmatrix} \frac{2}{L_{eq}} & 0 \\ 0 & \frac{2}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{f,d} \\ v_{f,q} \end{bmatrix} \quad (2.30)$$

In the same way, (2.16) can be rewritten as the system (2.31) in the $dq0$ frame. Where $v_{u,0} + v_{l,0} = v_{d0}$ means the DC component in the converter legs. Then, system (2.31) describes the circulating current dynamics in $dq0$ reference that should be controlled.

$$\begin{bmatrix} \dot{i}_{cir,d} \\ \dot{i}_{cir,q} \\ \dot{i}_{cir,0} \end{bmatrix} = \begin{bmatrix} -\frac{R}{L} & \omega & 0 \\ -\omega & -\frac{R}{L} & 0 \\ 0 & 0 & -\frac{R}{L} \end{bmatrix} \begin{bmatrix} i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \end{bmatrix} + \begin{bmatrix} -\frac{1}{2L} & 0 & 0 \\ 0 & -\frac{1}{2L} & 0 \\ 0 & 0 & -\frac{1}{2L} \end{bmatrix} \begin{bmatrix} v_{u,d} + v_{l,d} \\ v_{u,q} + v_{l,q} \\ v_{d0} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \frac{v_{dc}}{2L} \end{bmatrix} \quad (2.31)$$

Concerning the converter total stored energy in (2.18) and energy balancing at (2.20), these values on the referential $f = d, q, 0$ are presented in (2.32) and (2.33), respectively.

$$\begin{aligned}
\dot{W}_h &= \frac{3}{2} \sum_{f=d}^0 v_{u,f} \left(-\frac{i_{v,f}}{2} + i_{cir,f} \right) + \frac{3}{2} \sum_{f=d}^0 v_{l,f} \left(\frac{i_{v,f}}{2} + i_{cir,f} \right) \\
&= -\frac{3}{4} v_{u,d} i_{v,d} + \frac{3}{2} v_{u,d} i_{cir,d} - \frac{3}{4} v_{u,q} i_{v,q} + \frac{3}{2} v_{u,q} i_{cir,q} + \frac{3}{4} v_{l,d} i_{v,d} + \frac{3}{2} v_{l,d} i_{cir,d} + \\
&\quad + \frac{3}{4} v_{l,q} i_{v,q} + \frac{3}{2} v_{l,q} i_{cir,q} + 3 i_{cir,0} v_{d,0}
\end{aligned} \tag{2.32}$$

$$\begin{aligned}
\dot{W}_v &= \frac{3}{2} \sum_{f=d}^0 v_{u,f} \left(-\frac{i_{v,f}}{2} + i_{cir,f} \right) - \frac{3}{2} \sum_{f=d}^0 v_{l,f} \left(\frac{i_{v,f}}{2} + i_{cir,f} \right) \\
&= -\frac{3}{4} v_{u,d} i_{v,d} + \frac{3}{2} v_{u,d} i_{cir,d} - \frac{3}{4} v_{u,q} i_{v,q} + \frac{3}{2} v_{u,q} i_{cir,q} - \frac{3}{4} v_{l,d} i_{v,d} - \frac{3}{2} v_{l,d} i_{cir,d} - \\
&\quad + \frac{3}{4} v_{l,q} i_{v,q} - \frac{3}{2} v_{l,q} i_{cir,q}
\end{aligned} \tag{2.33}$$

Finally, considering the state vector as $x = [i_{v,d} \ i_{v,q} \ i_{cir,d} \ i_{cir,q} \ i_{cir,0} \ W_h \ W_v]^T$ and the controller input as $u = [v_{u,d} \ v_{u,q} \ v_{l,d} \ v_{l,q} \ v_{d0}]^T$, the three-phase MMC can be represented by the bilinear form shown in (2.34) and at (2.36).

$$\dot{x} = Ax + \sum_{k=1}^{\rho} B_k u_k x + b_k u_k + z \tag{2.34}$$

where, considering $\rho = 5$.

The model in system (2.36) can be summarized in (2.35).

$$\left\{ \begin{array}{l}
\dot{i}_{v,d} = -\frac{R_{eq}}{L_{eq}} i_{v,d} + \omega \cdot i_{v,q} + \frac{v_{u,d} - v_{l,d}}{L_{eq}} + \frac{2v_{f,d}}{L_{eq}} \\
\dot{i}_{v,q} = -\frac{R_{eq}}{L_{eq}} i_{v,q} - \omega \cdot i_{v,d} + \frac{v_{u,q} - v_{l,q}}{L_{eq}} + \frac{2v_{f,q}}{L_{eq}} \\
\dot{i}_{cir,d} = -\frac{R}{L} i_{cir,d} + \omega \cdot i_{cir,q} - \frac{v_{u,d} + v_{l,d}}{2L} \\
\dot{i}_{cir,q} = -\frac{R}{L} i_{cir,q} - \omega \cdot i_{cir,d} - \frac{v_{u,q} + v_{l,q}}{2L} \\
\dot{i}_{cir,0} = -\frac{R}{L} i_{cir,0} - \frac{v_{d0}}{2L} + \frac{V_{DC}}{2L} \\
\dot{W}_h = -\frac{3}{4} v_{u,d} i_{v,d} + \frac{3}{2} v_{u,d} i_{cir,d} - \frac{3}{4} v_{u,q} i_{v,q} + \frac{3}{2} v_{u,q} i_{cir,q} + \\
\quad + \frac{3}{4} v_{l,d} i_{v,d} + \frac{3}{2} v_{l,d} i_{cir,d} + \frac{3}{4} v_{l,q} i_{v,q} + \frac{3}{2} v_{l,q} i_{cir,q} + 3v_{d0} i_{cir,0} \\
\dot{W}_v = -\frac{3}{4} v_{u,d} i_{v,d} + \frac{3}{2} v_{u,d} i_{cir,d} - \frac{3}{4} v_{u,q} i_{v,q} + \frac{3}{2} v_{u,q} i_{cir,q} + \\
\quad - \frac{3}{4} v_{l,d} i_{v,d} - \frac{3}{2} v_{l,d} i_{cir,d} - \frac{3}{4} v_{l,q} i_{v,q} - \frac{3}{2} v_{l,q} i_{cir,q}
\end{array} \right. \tag{2.35}$$

$$\begin{aligned}
\begin{bmatrix} \dot{i}_{v,d} \\ \dot{i}_{v,q} \\ \dot{i}_{cir,d} \\ \dot{i}_{cir,q} \\ \dot{i}_{cir,0} \\ \dot{W}_h \\ \dot{W}_v \end{bmatrix} &= \begin{bmatrix} \frac{-R-2R_c}{L+2L_c} & \omega & 0 & 0 & 0 & 0 & 0 \\ -\omega & \frac{-R-2R_c}{L+2L_c} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{R}{L} & \omega & 0 & 0 & 0 \\ 0 & 0 & -\omega & -\frac{R}{L} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{R}{L} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} + \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{3\omega}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 & 0 \\ -\frac{3\omega}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} v_{u,d} + \\
&+ \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} v_{u,q} + \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 & 0 \\ -\frac{3}{4} & 0 & -\frac{3}{2} & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} v_{l,d} + \\
&+ \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & -\frac{3}{2} & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} v_{l,q} + \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{v,d} \\ i_{v,q} \\ i_{cir,d} \\ i_{cir,q} \\ i_{cir,0} \\ W_h \\ W_v \end{bmatrix} v_{d,0} + \\
&+ \begin{bmatrix} \frac{1}{L+2L_c} \\ 0 \\ -\frac{1}{2L} \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} v_{u,d} + \begin{bmatrix} 0 \\ \frac{1}{L+2L_c} \\ 0 \\ -\frac{1}{2L} \\ 0 \\ 0 \\ 0 \end{bmatrix} v_{u,q} + \begin{bmatrix} -\frac{1}{L+2L_c} \\ 0 \\ -\frac{1}{2L} \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} v_{l,d} + \begin{bmatrix} 0 \\ -\frac{1}{L+2L_c} \\ 0 \\ -\frac{1}{2L} \\ 0 \\ 0 \\ 0 \end{bmatrix} v_{l,q} + \\
&+ \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -\frac{1}{2L} \\ 0 \\ 0 \end{bmatrix} v_{d,0} + \begin{bmatrix} \frac{2v_{f,d}}{L+2L_c} \\ \frac{2v_{f,q}}{L+2L_c} \\ 0 \\ 0 \\ \frac{V_{DC}}{2L} \\ 0 \\ 0 \end{bmatrix} \tag{2.36}
\end{aligned}$$

Controlling Modular Multilevel Converters

The control of MMC has additional challenges in comparison with other converters topology. The control method may have to deal with

- Externally, manage active and reactive power flow, AC and DC voltage,
- Internally, deal with converter dynamics as circulating currents, SM capacitor voltage, arm balancing, phase balancing, and converter energy control.

MMCs also have a complex modeling technique because of the high number of Submodule (SM), which requires simultaneous control to attain capacitor voltage balancing. There are many MMC modeling approaches, and models that directly affect the control design. In this thesis, a mathematical model based on the average arm is used to develop the controllers, and a switching model is used

to verify controls performances. Concerning the average model, there are many approaches in the literature. In [25], the average model considers a switching function model that accurately includes each SM's capacitors' dynamic.

Additionally, in [26], authors introduce a continuous model where arms are represented by variable voltage sources function. However, a more complex average model will increase the system order, as well as the complexity of the proposed solution. In this way, the average model used in this research is based in [27], which consider per arm, an equivalent SM voltage.

A switching model is simulated with the proposed controller to verify the control performance. The switching model has a low-level controller, which properly attain SMs voltage balancing. The sorting algorithm implemented in the low-level control is based on the standard technique proposed by [24].

Concerning control, most of the existing results on the control strategy for MMCs consist of linear controllers, such as vector control, which may not have guaranteed stability. This is because only one point of operation is considered in its design and also because the system's nonlinearities are approximated [28, 29, 30].

In this point of view, one may cite works as [31], where the nonlinear MMC model is first linearized, and then linear controllers are designed for it. In a different way, [27] proposes a discrete-time bilinear model of an MMC, controlled by a sum-of-squares decomposition method, following a nonlinear analysis.

These studies are motivated by the relevance of designing nonlinear controllers that can assure stability throughout large electrical grid operation regions, including rigorous stability analysis [32, 33]. The next chapter will discuss with more detail about modeling and control to MMC.

2.3 Control designs for MMC systems

The control algorithm regulates systems' variables, in order to attain application requirements. System operation and user requests may change the power demand and voltage levels. Furthermore, the control provides equipment protection from current and voltage over nominal values. Also, it must provide system stability and suitable responses during transients resulting in all expected operating conditions. In addition, control can address AC grid support: inertial and frequency stabilization to low-inertia grids [60], and voltage stabilization to high-impedance grids [24].

Besides the above mentioned applications, MMC controller will also deal with circulating current, most about the second harmonic suppression goal [61], and capacitor voltage balancing. Arm current also needs to be measured and controlled once it is directly related to SM capacitor voltage.

As discussed above, and highlighted by [24], when using MMC topology, there are additional concerns with dynamics that the control must take into account. They are summarized below:

- upper level controls: they are common for two-level VSC controller.
 - DC voltage to ensure low level losses and no damage to the cables' insulation.
 - AC voltage, in weak AC grids.
 - Active power transfer to attend the power demand.
 - Reactive power requirement.

- second-harmonic circulating current suppression
- SM capacitor voltage balancing
- arm, phase, pole balancing
- energy charge

The literature states the above mentioned controllers by two-level: high-level control and low-level control, as summarized in figure 2.12, adapted from [62]. The high-level control comprehends the power flow between the DC and AC sides. The power flow is given by setting voltage references for upper and lower arms. These definitions also comprehend DC voltage, AC voltage, and frequency. Low-level control of MMC deals with internal converter aspects as control of circulating current, SM capacitor voltage regulation, and arm energy balancing. These aspects rely on the management of SMs switching. A proper switch method may attend the requested arm voltage and ensure SMs capacitor balance [63, 52].

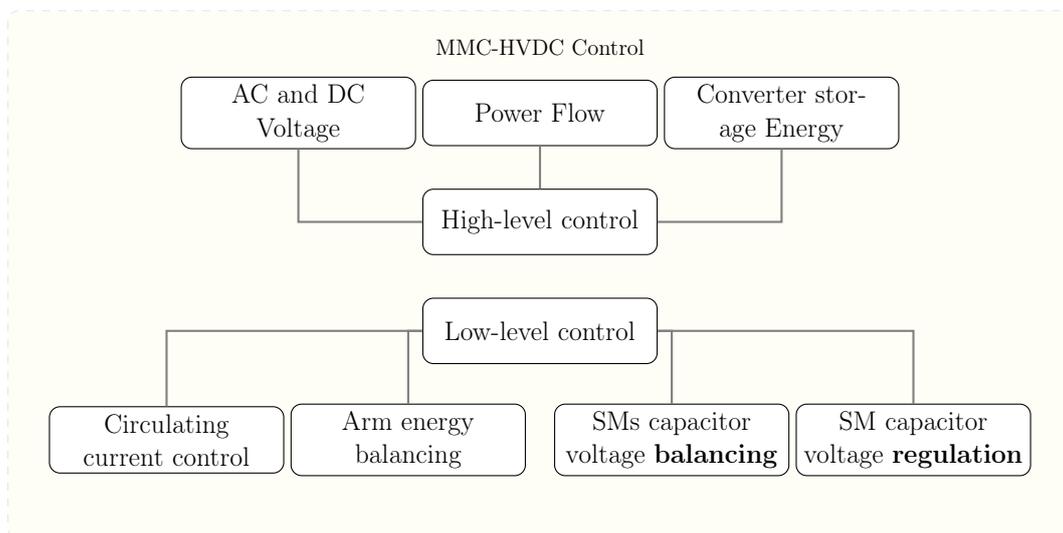


Figure 2.12: MMC-HVDC necessary controls.

Source: Author

The literature has investigated the control aspects, which are particular to the use of MMC. Several methods are addressed to MMCs' control, as [61, 50, 64]. They are mostly based on PWM approach and standard linear control, using an open-loop or closed-loop approach.

Circulating current control One of the goals of the control in the MMC applications is the circulating currents suppression. They flow through the converter phase legs of the MMC and come from the voltage differences among the phase legs [65]. The circulating current controller is often mentioned in the literature as "inner" or "inner-loop". In circulating current, there are DC and harmonic components. DC components play a crucial role in the DC power dispatch, while the fundamental frequency component can transport energy between the upper and lower arms [65]. The remaining circulating current components result in current signal depreciation and the increased capacitor voltage ripple, mainly the second harmonic component [61, 65].

The open-loop approach is based on the estimation of internal parameters, such as the value of the SM capacitor voltages, total voltage per arm, and arm current. In [61], a new controller is proposed, like circulating current suppressing controller (CCSC). The control is based on an open-loop modulation that uses SM

capacitor voltage. CCSC control is integrated to DC-loop control in stationary $\alpha\beta\theta$ frame. A proportional-resonant regulator is integrated due to the internal model principle. The authors point out that the CCSC methods suppress just the second harmonic component. However, they highlight that this component is the dominant one at circulating current. Therefore, the proposed controller focuses on the second harmonic, while the DC component is neglected, also because it has no effect on circulating current. Finally, the control achieves a steady-state performance, which has a compromise with dynamic performance. In [50] and [66], a dq reference frame control is implemented to suppress the second harmonic on circulating current. It was combined with a Phase shifted carrier PWM with switching frequency reduction. The proposed controller is efficient in suppressing the double harmonic circulating current and, as a consequence, improve SM capacitor voltage balancing.

In [65], a thorough investigation demonstrates the interaction between arm currents and capacitor voltages. It is derived from an equation describing circulating current components, and the analytical expression is verified by experimental results. The authors conclude that second-order harmonic is directly proportional to the amplitude of the AC side current. They can validate the analytical equation on a 10 kVA prototype with five SM per arm. Finally, the results improve the sizing of the components: arm inductor and the SM capacitors. This improvement may reduce the alternating components in the circulating currents.

Capacitor voltage balancing control strategy In an MMC, the SM capacitor voltages deviate from their nominal value during regular operation. This is the result of different conduction intervals for each SM. So, a method to attain voltages' balancing is required to have a proper converter operation. The technique needs to charge or discharge particular SM to achieve the desired nominal value of capacitor voltage [24]. This control is often implemented within the modulation strategy [67]. However, it can be implemented by a sorting control method [68, 69, 70, 71, 40].

Capacitor voltage balancing by the modulation, concern for adjusting the modulation reference wave to accomplish a proper SM switching, which maintains the capacitor voltage balanced.

The proposal presented by [67] is a simplified control technique in order to control the voltage of capacitors that are used in the DC bus of a three-phase three-level Neutral-Point Clamped (NPC) rectifier. In addition, it is highlighted that SVM-PWM is the best technique applied to converters. Most voltage balancing techniques are based on modifying the switching sequences, including extra hardware and modified SVM-PWM hexagon. The extra hardware included in the NPC converters not only makes the system expensive, but also adds complex calculation. The modification in the SVM-PWM hexagon used to balance the capacitor voltage affects the parameters on the source and load side beyond acceptable limits. Therefore, the authors concluded that the research reported in the literature is not sufficient with regard to capacitor voltage balance of a three-phase NPC bidirectional rectifier using optimized switching sequences. In this way, the researcher proposes a new modulation technique that reduces the potential variations of the neutral point and keeps the parameters of the source side and the load side within the acceptable and without the need for extra hardware. The results presented through the simulation demonstrate the effectiveness of the proposed control algorithm. One of the main points is that no additional hardware is needed for the stable operation of the NPC rectifier, which results in reduced volume and reduced component costs. The DC bus capacitor voltages

are balanced within a narrow band. The voltage balancing effect of the DC bus capacitor is reflected on the source side and the load side.

In the **sorting control method**, the capacitor voltage balancing is separated from the modulation strategy. The modulation manages the number of active SMs, and the sorting control select which SMs will switch to perform the voltage balancing among submodules. In [72] the goal is to equalize and stabilize the SM capacitor voltages. The SM selection method, combined with the stored energy estimation, is proposed. A single-phase control is proposed, for the purpose of being scalable for the number of the converter phase. This approach provides the balancing of stored energy in each arm. However, small oscillation changes are not totally suppressed by this method. In [73], MMC control is accomplished by using a state observer. Two controllers are proposed, and a comparison with an open-loop control is performed. One uses the state observer to estimate the total voltage per arm, and the other, the voltage balancing method is used with the state estimation of each SM voltage. The results show that both propositions improve voltage balancing control methods in comparison with the open-loop approach.

In [68] it is presented a sorting control method to minimize voltage fluctuation on submodule capacitors under low-frequency carrier modulation. The authors combine a sorting algorithm that selects submodules to be activated with a common-mode voltage and circulating current injection. The proposed methods can reduce energy fluctuation, and attain effective capacitor voltage balancing thanks to using the sorting algorithm. Furthermore, the circulating current fluctuation is decreased.

The authors of [40] highlight that phase-shift modulation has an equal power distribution between submodules resulting in a suitable inner current control and DC capacitor voltage balance. However, this method has a weak harmonic performance. Thus, the paper presents a phase-disposition modulation, combined with a hysteresis controller and a sorting algorithm, to control capacitor voltages balance, inner current control, and individual control of the DC capacitor voltages. Moreover, a hysteresis controller drives circulating currents into the desired range, arm voltage balancing, and individual voltage capacitors properly controlled are achieved.

Converter energy control In [29], the authors deal with the total energy problem. The method is based on a rotating reference frame and uses a circulating current suppression technique. The proposed method is efficient in eliminating the oscillation on converter legs energy, and as a consequence, reduces voltage oscillation. This reduction is obtained by injection of differential current with a second harmonic component. The authors consider that it is the main drawback of the proposed method. Furthermore, in [74], besides controlling the total energy, they propose a difference in energy control. The energy control is obtained by the regulation of positive, negative, and zero sequences of circulating currents in dq0 reference frame, for both once and twice the fundamental frequency. The authors highlight that it is possible to cancel the oscillating terms of total energy and difference energy by driving circulating current to zero. For example, they are using the circulating current suppressing controller proposed by [66]. Although the method proposed by the authors consists of implementing a different reference to converter energy. This methodology effectively improve the capacitor oscillation reduction in comparison with [26] and improve the circulating current suppression in comparison with [66].

A full control system was proposed by [28]. The control is based on maximum

and minimum functions to perform the submodules' selection. The proposed method can decouple DC voltage from submodules' voltage, enabling a different set point for DC bus and active submodules. Author call attention that there are no significant results on system dynamics from the energy balancing controller proposed by [49]; on the other hand, circulating current suppression presented by [75], adequately supply arm energy balancing. The control proposition can drastically reduce submodules switching, per circle.

The previously mentioned researches focused on power and internal control aspects. However, there is another aspect to be addressed by AC-DC converter controllers: DC voltage bus control. There are three external aspects to be controlled (DC voltage bus, active and reactive power). However, technical restrictions allow each station to control just two of these aspects. Most of the mentioned researchers consider DC-bus voltage constant or controlled by another station. In [30], DC-bus voltage is attained by submodules' capacitor voltage. The converter energy model attains the solution in two ways: one in which stored energy does not depend on the DC-bus level and the other one which does. The presented solution can be used in multiterminal connections on the station, which control DC-bus voltage.

Nonlinear multivariable control Besides, most of the researches presented above develop MMC controller based on cascaded control (e.g., PID control) [42]. This bias results from the simplification of the system in subsystems and step-by-step building and a well-known technique to implement control tuning [76]. In this case, each control loop is often associated with different response times, where the faster gives the reference to the slower. Furthermore, cascaded controls are designed to a specific operation point, on the other hand, the nonlinear one is designed to a wide operation region. Accordingly to this, there are solutions to MMC controllers which differ from conventional cascade control based.

In [77], a current and energy control, as well as energy balancing of a bilinear state-space MMC model, is achieved by a nonlinear multivariable control. All MMC internal parameters are modeled as a periodic bilinear time-varying system. The authors demonstrate a Periodic Linear Quadratic Regulator (PLQR), using currents and energies estimation by Least Squares (LS). The Linear-Quadratic problem is solved by an optimal time-invariant state feedback control law. The control is performed in a 430 MVA MMC. Converter start up and arm balancing are showed.

In [27], the proposed MMC control is based on sum-of-square decomposition method. A bilinear discrete model with rotating reference frame is used for the design. A quadratic Lyapunov function is proposed to ensure system stability. Besides, an optimization process took place to maximize the convergence region of Lyapunov function. A three-phase switching model, with 41 levels, is used to validate the proposed control. State trajectories are shown. At last, a comparison with a PI controller is provided. The authors highlight that the proposed control is more demanding and need more computational effort. However can be easily implemented in real time.

A model-based nonlinear control is shown in [78], where is considered an MMC average model where a resulting submodule is represented per arm. A nonlinear coordinate transformation is used to point candidate states as output. The authors performed system linearization, based on the candidates output.

Multivariable control uses a nonlinear multivariable model. These methods request advanced control strategies to define the control laws and perform stability analyses [52]. The convenience of using a multivariable control approach is to

design a direct control strategy of all the converter's state variables. State-space equations of the MMC system are integrated. Moreover, it allows the demonstration of the proposed scheme's suitability to asymptotically stabilize the MMC's complicated dynamics.

Stability analyses is substantial for the study of dynamic system. On this thesis the stability of an equilibrium point will be investigated. Equilibrium point stability is usually achieved through Lyapunov theory [79]:

- An equilibrium point is stable if all solutions starting at nearby point, stay nearby, and;
- An equilibrium point is asymptotically stable if all solutions starting at a nearby point tend to the equilibrium point and time goes to infinity.

Since each operating point (P_e and Q_e) defines a different value for states), it is convenient to proceed with a change of variables, where the state x will be replaced by its error \tilde{x} plus their steady state value \bar{x} .

$$x \triangleq \tilde{x} + \bar{x}$$

This change of variable is convenient because for all operating point \tilde{x} its reference is zero. To attain this goal, the control can be designed focusing on asymptotically stabilize state error ($\tilde{x} = 0$), and time go to infinity. Thus, state x will assume their reference value, \bar{x} .

In this thesis, two multivariable controls, based on Lyapunov theory, are addressed to achieve the MMC control challenges:

- **Chapter 4:** A nonlinear approach based on Feedback Linearization and Backstepping, and;
- **Chapter 5:** A bilinear approach based on Quadratic Feedback control.

Feedback linearization approach Considering a nonlinear system as

$$\begin{aligned} \dot{x} &= f(x) + G(x)u \\ y &= h(x) \end{aligned} \quad (2.37)$$

the Feedback Linearization consists on finding a state feedback control, as

$$u = \alpha(x) + \beta(x)v \quad (2.38)$$

and a change of variables

$$z = T(x) \quad (2.39)$$

that transform the nonlinear system into an equivalent linear system. The feedback linearization of the MMC is investigated by [31]. The nonlinear model is presented, and an input-output feedback linearization is accomplished. However, the authors utilize linear controllers, Proportional-resonant (PR) and PI controller, to regulate the linearized system states. The zero-dynamic stability is investigated and proved. Furthermore, the proposed control well succeed to track reference, providing faster dynamic response and smooth transients for step response. In [80] the feedback linearization control based on Lyapunov theory is addressed for a DC/DC converter, in the context of multi-terminal HVDC. System model is bilinear in a state space representation. Controllability and stability

are investigated. The system is modeled as a bilinear approach of an average dynamic model and computer simulations are addressed. The proposed control stabilize the MMC system. In addition, the authors designed a quadratic feedback control which will be further discussed along this chapter.

As presented above by equations 2.37-2.39, the proposed control is model dependent [81]. Thus the model design and parametric errors affect the control performance. It is possible to verify these effects by robustness validations. Furthermore, it is possible to ensure a degree of robustness, often stronger than linear controls, as said by Lemma 9.1 [79]. Accordingly, a nonlinear controller is able to operate in a wide region.

Quadratic Feedback control approach Electrical circuits based on switching devices like MMC are often mathematically modeled as bilinear systems [77, 27, 80, 82, 83]. The system is described by linear differential equations and the control inputs are the coefficients. The general representation of bilinear system consists of:

$$\dot{x} = Ax + \sum_{k=1}^{\rho} (u_k B_k x + u_k b_k) \quad (2.40)$$

Considering a bilinear system in which the state variables are $x \in \mathbb{R}^n$, and the input variables are $u \in \mathbb{R}^{\rho}$.

The design of nonlinear control for the bilinear system is a tough problem, even worse for higher dimension systems [84]. To control this class of system raises many challenges, mostly: manage all states altogether, what results in states which are dynamically coupled.

In [84] it is derived conditions for the existence of a control Lyapunov function for a general bilinear system. The authors deals with two dimensional bilinear systems with one control input. It is presented a necessary and sufficient condition which ensures that the presented design condition can be satisfied. The condition is that $V(x) = x^T P x$, based on [85, 86], with a symmetric and positive definite matrix P is a quadratic Lyapunov control function for the system in equation 2.40 if and only if equation 2.41 is valid.

$$Y(x) := x^T (A^T P + P A) x \leq 0 \forall x \in M := \left\{ x \in \mathbb{R}^n \mid x \neq 0, \sum_{k=1}^{\rho} \{(B_k x + b_k)^T P x\}^2 \neq 0 \right\} \quad (2.41)$$

Thus, the stated control Lyapunov function law ensures the global asymptotic stability of the closed-loop system. In [80] asymptotic stability is guaranteed to a bilinear DC/DC converter, through a quadratic feedback control. The control assumptions were similar to the presented above by [84]. The model of DC/DC converter has dimension four. A change of variable is performed and control is designed to drive error \tilde{x} to be zero, implying x to \bar{x} . The control simulations are performed on matlab. The authors consider the bilinear controller, for the presented system with dimension four, more accessible to implement than the feedback linearization approach. However, also highlight that feedback linearization is broader known and has established theory on the literature.

Thesis boundary conditions The context created in this introduction surrounds the thesis proposition. The two above mentioned control approaches will take place in the following chapters. Additionally, asymptotic stability has been established. The controllers are designed for the three-phase MMC converters.

They are based on the bilinear average model proposed by [77, 27]. The computer algebra systems, MAPLE and Mathematica 11.2, are the computational software used to attain the math computation. Furthermore, MATLAB R2019b at the SIMULINK Simscape Electrical environment simulates a switching MMC model and average-model. The MMC simulated on Simscape has a sorting algorithm implemented, based on [24].

2.4 Chapter conclusion

This chapter discussed the main points about MMC operational principles. The use of full-bridge SM instead of half-bridge SM would improve DC cable fault protection, although it increases switching losses. Modulation and sorting algorithm handle the voltage balancing across arms' SM. Furthermore, the modeling aspect concerning the decrease of the computational requirement for reduced-order models is discussed. Additionally, the mathematical modeling of the reduced-order average model was presented and used to develop the controllers proposed in this thesis. Finally a section concerning the control designs for MMC systems is presented.

Chapter 3

MMC Linear Control and Test System

As discussed in chapter 2, comparing MMC converters in respect to other VSCs, there are additional dynamics that controller must take into account: circulating current control, SM capacitor voltage balancing, and stored internal energy .

In this research, the three-phase MMC switching model uses phase-shift modulation. Here it is considered that the SM capacitor voltage balancing is solved by the modulation interface, which will be further analyzed. Among the drawbacks of using the MMC, this thesis has addressed the points of circulating current management, and stored internal energy and its balancing.

In the next chapters of this thesis, a reduced-order average model was used to develop the proposed control and to make the mathematical stability analysis. Meanwhile, a switched model was tested on Matlab Simscape Electrical to verify its performance. Two multivariable controllers are presented to solve the MMC control challenge. In addition, this chapter demonstrates, for comparison purposes, a cascaded control based on PI.

The cascade control presented here is adapted from the control proposed on [28]. These modifications are necessary to have the same state variables and control inputs as the proposed nonlinear controllers.

Two test systems with two different voltage levels are presented — one in medium voltage and the other in high-voltage. The goal is to verify nonlinear control performance and tuning for each particular case. The medium-voltage system is a 60 kV DC voltage and nominal power of 50 MVA , based on the system proposed in [27]. Meanwhile, the high-voltage is a 400 kV DC and 450 MVA , based on [87].

Simulations with average-model and with switching-model were performed. MMC state references are described in this chapter.

This chapter focuses on the performance of the MMC models using the PI controller adapted from [28].

3.1 Equilibrium points for state variables and control inputs

This section will establish the equilibrium point for states and the corresponding control inputs values (\bar{x} and \bar{u}). However, since references may change in response to grid variations or disturbances, here it will be highlighted the corresponding modifications.

Current i_{vj} is defined in the previous chapter in rotating dq reference frame. Park's transformation was used to transform symmetrical and balanced AC system equations (2.28) into the synchronized rotating dq reference frame of (2.30),

which is recalled here:

$$\begin{bmatrix} \dot{i}_{vd} \\ \dot{i}_{vq} \end{bmatrix} = \begin{bmatrix} -\frac{R_{eq}}{L_{eq}} & \omega \\ -\omega & -\frac{R_{eq}}{L_{eq}} \end{bmatrix} \begin{bmatrix} i_{vd} \\ i_{vq} \end{bmatrix} + \begin{bmatrix} \frac{1}{L_{eq}} & 0 \\ 0 & \frac{1}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{ud} - v_{ld} \\ v_{uq} - v_{lq} \end{bmatrix} + \begin{bmatrix} \frac{2}{L_{eq}} & 0 \\ 0 & \frac{2}{L_{eq}} \end{bmatrix} \begin{bmatrix} v_{fd} \\ v_{fq} \end{bmatrix}$$

In the rotating reference frame the power in the PCC can be described by (3.1).

$$S_e = P_e + jQ_e = \frac{3}{2}(v_{fd} + jv_{fq})(i_{vd} - ji_{vq}) \quad (3.1)$$

$$P_e = \frac{3}{2}(v_{fd}i_{vd} + v_{fq}i_{vq}) \quad (3.2)$$

$$Q_e = \frac{3}{2}(-v_{fd}i_{vq} + v_{fq}i_{vd}) \quad (3.3)$$

It is assumed that the rotating frame is aligned with the alternating terminal voltage, thus the voltage v_a is synchronized on the d axis. Thanks to this consideration, v_{fq} is equal to zero. Following this, the AC active and reactive power definitions are rewritten in (3.4) and (3.5).

$$P_e = \frac{3}{2}v_{fd}i_{vd} \quad (3.4)$$

$$Q_e = -\frac{3}{2}v_{fd}i_{vq} \quad (3.5)$$

As it is possible to see, active and reactive power flow are directly linked with states i_{vd} and i_{vq} . Thus they are used to define reference values. \bar{P}_e and \bar{Q}_e are the power references and are defined by the consumption demand. The desired values for the AC currents are defined in (3.6) and (3.7) as functions of the active and reactive power references coming from higher level controllers.

$$\bar{x}_1 = \bar{i}_{vd} = \frac{2\bar{P}_e}{3v_{fd}} \quad (3.6)$$

$$\bar{x}_2 = \bar{i}_{vq} = \frac{2\bar{Q}_e}{3v_{fd}} \quad (3.7)$$

Since components dq of circulating current in an MMC do not produce useful power and increase the converter losses, they should be minimized. For this reason, their references are taken as zero:

$$\bar{x}_3 = \bar{i}_{cir d} = 0 \quad (3.8)$$

$$\bar{x}_4 = \bar{i}_{cir q} = 0 \quad (3.9)$$

The desired values for control inputs can be defined by system equation (2.31) (recalled below) in the equilibrium point of the steady-state, thus $\dot{x} = 0$.

$$\begin{bmatrix} \dot{i}_{cir d} \\ \dot{i}_{cir q} \\ \dot{i}_{cir 0} \end{bmatrix} = \begin{bmatrix} -\frac{R}{L} & \omega & 0 \\ -\omega & -\frac{R}{L} & 0 \\ 0 & 0 & -\frac{R}{L} \end{bmatrix} \begin{bmatrix} i_{cir d} \\ i_{cir q} \\ i_{cir 0} \end{bmatrix} + \begin{bmatrix} -\frac{1}{2L} & 0 & 0 \\ 0 & -\frac{1}{2L} & 0 \\ 0 & 0 & -\frac{1}{2L} \end{bmatrix} \begin{bmatrix} v_{ud} + v_{ld} \\ v_{uq} + v_{lq} \\ v_{d0} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \frac{v_{dc}}{2L} \end{bmatrix}$$

In this way, (2.31) becomes (3.10), (3.11) and (3.12).

$$-\frac{R_{\bar{c}}}{L} \bar{i}_{cir d} + w \cdot \bar{i}_{cir q} - \frac{\bar{v}_{ud} + \bar{v}_{ld}}{2L} = 0 \quad (3.10)$$

$$-w \cdot \bar{i}_{cir d} - \frac{R_{\bar{c}}}{L} \bar{i}_{cir q} - \frac{\bar{v}_{uq} + \bar{v}_{lq}}{2L} = 0 \quad (3.11)$$

$$-\frac{R_{\bar{c}}}{L} \bar{i}_{cir 0} - \frac{\bar{v}_{d0}}{2L} + \frac{V_{DC}}{2L} = 0 \quad (3.12)$$

Replacing (3.8) and (3.9) in (3.10), we obtain:

$$\bar{v}_{ud} = -\bar{v}_{ld} \quad (3.13)$$

Also, replacing (3.8) and (3.9) in (3.11) obtains:

$$\bar{v}_{uq} = -\bar{v}_{lq} \quad (3.14)$$

Thus, replacing (3.13) and (3.14) in (2.30), at the equilibrium point, it becomes (3.15), (3.16), (3.17) and (3.18).

$$-\frac{R_{eq\bar{c}}}{L_{eq}} \bar{i}_{vd} + w \cdot \bar{i}_{vq} + \frac{2\bar{v}_{ud}}{L_{eq}} + \frac{2v_{fd}}{L_{eq}} = 0 \quad (3.15)$$

$$-\frac{R_{eq\bar{c}}}{L_{eq}} \bar{i}_{vd} + w \cdot \bar{i}_{vq} - \frac{2\bar{v}_{ld}}{L_{eq}} + \frac{2v_{fd}}{L_{eq}} = 0 \quad (3.16)$$

$$-w \cdot \bar{i}_{vd} - \frac{R_{eq\bar{c}}}{L_{eq}} \bar{i}_{vq} + \frac{2\bar{v}_{uq}}{L_{eq}} + \frac{2v_{fq}}{L_{eq}} = 0 \quad (3.17)$$

$$-w \cdot \bar{i}_{vd} - \frac{R_{eq\bar{c}}}{L_{eq}} \bar{i}_{vq} - \frac{2\bar{v}_{lq}}{L_{eq}} + \frac{2v_{fq}}{L_{eq}} = 0 \quad (3.18)$$

Collecting terms on (3.15), (3.16), (3.17), (3.18) and (3.12) the reference to the control inputs \bar{v}_{ud} , \bar{v}_{ld} , \bar{v}_{uq} , \bar{v}_{lq} and \bar{v}_{d0} are obtained:

$$\bar{v}_{ud} = \frac{R_{eq\bar{c}}}{2} \bar{i}_{vd} - \frac{wL_{eq}}{2} \cdot \bar{i}_{vq} - v_{fd} \quad (3.19)$$

$$\bar{v}_{ld} = -\frac{R_{eq\bar{c}}}{2} \bar{i}_{vd} + \frac{wL_{eq}}{2} \cdot \bar{i}_{vq} + v_{fd} \quad (3.20)$$

$$\bar{v}_{uq} = \frac{wL_{eq}}{2} \cdot \bar{i}_{vd} + \frac{R_{eq\bar{c}}}{2} \bar{i}_{vq} - v_{fq} \quad (3.21)$$

$$\bar{v}_{lq} = -\frac{wL_{eq}}{2} \cdot \bar{i}_{vd} - \frac{R_{eq\bar{c}}}{2} \bar{i}_{vq} + v_{fq} \quad (3.22)$$

$$\bar{v}_{d0} = -2R_{\bar{c}} \bar{i}_{cir 0} + V_{DC} \quad (3.23)$$

The desired value for the zero component of the circulating current ($\bar{i}_{cir 0}$) comes from the equilibrium point at steady-state of equation (2.18), where derivative of the desired value is zero ($\dot{\bar{x}} = 0$). In (2.18) replacing (3.19) and (3.21) and collecting terms to obtain (3.24).

$$\bar{x}_5 = \bar{i}_{cir 0} = \frac{V_{DC} - \sqrt{V_{DC}^2 - 4R(\bar{i}_{vd}\bar{v}_{ud} + \bar{i}_{vq}\bar{v}_{uq})}}{4R} \quad (3.24)$$

In (3.24), one of the roots is unfeasible since it takes the MMC to a very high dissipating mode, so the other is chosen.

The reference for SMs' energy is linked with SMs' capacitor voltage, and it can be expressed as in equation (3.25).

$$V_{DC} - 2Ri_{cirj} - 2L\dot{i}_{cirj} = 2NV_C^{SM} \quad (3.25)$$

Applying Park's transformation (T) in equation (3.25), the equilibrium point for capacitors' voltage is:

$$V_C^{SM} = \frac{V_{DC} - 2R\bar{x}_5}{2N} \quad (3.26)$$

then, the stored energy per SM can be calculated as:

$$W_C^{SM} = \frac{1}{2}C_{SM}(V_C^{SM})^2 \quad (3.27)$$

By equation (3.27), considering all active SMs, the desired total energy of the converter is obtained in equation (3.28).

$$\bar{x}_6 = \bar{W}_h = 6 \cdot N \cdot W_C^{SM} = \frac{3C_{SM} \cdot (V_{DC} - 2R\bar{x}_5)^2}{4N} \quad (3.28)$$

Due to the symmetric configuration of the converters, upper and lower arms must have the same stored energy in steady-state, so the reference for the energy balance (\bar{W}_v) is defined as zero.

$$\bar{x}_7 = \bar{W}_v = W_u - W_l = 0 \quad (3.29)$$

The state reference and the stability condition defined above fuel the control development and simulations which will be presented in this thesis.

3.2 PI controller

A cascaded-control for the MMC is described in this section, which is based on a PI and is adapted from [25]. The modifications were necessary to obtain the same control inputs as the proposed nonlinear controllers, thus attaining a proper and fair performance comparison.

The result in [25] was chosen as the standard to be compared due to similarities in the control's objectives. The authors proposed an MMC control system, based on converter's stored internal energy. Furthermore, it points out the decoupling between the DC voltage produced by the converter and the voltage imposed by the DC bus. This result is also achieved by both nonlinear controllers proposed in this thesis.

An MMC converter with the same configuration as presented in figure 2.1 is considered by [25]. From there, equations (3.30) and (3.31) per phase j are obtained.

$$\frac{V_{DC}}{2} = v_{uj} + L\dot{i}_{uj} + Ri_{uj} - L_c\dot{i}_{vj} - Ri_{vj} + v_{fj} \quad (3.30)$$

$$\frac{V_{DC}}{2} = v_{lj} + L\dot{i}_{lj} + Ri_{lj} + L_c\dot{i}_{vj} + Ri_{vj} - v_{fj} \quad (3.31)$$

In the original control proposed by [25], there are two key variables which combine the controller inputs $v_{m,j}$, presented as: ($V_{convacj}$ and $V_{convdcj}$). They are respectively the total voltage on the leg j and the average voltage between upper and lower arm. They are presented in equation (3.32) and equation (3.33).

$$V_{conv_{acj}} = \frac{v_{lj} - v_{uj}}{2} \quad (3.32)$$

$$V_{conv_{dcj}} = v_{uj} + v_{lj} \quad (3.33)$$

Subtracting and adding (3.30) and (3.31), and also replacing the definition in (3.32) and (3.33) the equations (3.34) and (3.35) are obtained.

$$v_{fj} - v_{conv_{acj}} = \left(\frac{L}{2} + L_c\right) \dot{i}_{vj} + \left(\frac{R}{2} + R_c\right) i_{vj} \quad (3.34)$$

$$V_{DC} - v_{conv_{dcj}} = 2L\dot{i}_{cirj} + 2Ri_{cirj} \quad (3.35)$$

So, the following controllers in dq rotating reference frame are proposed to control AC current from (3.34).

$$\bar{v}_{conv_d} = -(\bar{i}_{vd} - i_{vd})C_{i_{ac}} + v_{fd} - \left(\frac{L}{2} + L_c\right) \omega i_{vq} \quad (3.36)$$

$$\bar{v}_{conv_q} = -(\bar{i}_{vq} - i_{vq})C_{i_{ac}} + v_{fq} - \left(\frac{L}{2} + L_c\right) \omega i_{vd} \quad (3.37)$$

Also, to control circulating current of equation (3.35), the control in equation (3.38) is proposed.

$$\bar{v}_{conv_{dc}} = -(\bar{i}_{cirj} - i_{cirj})C_{i_{cir}} + \frac{V_{DC}}{2} \quad (3.38)$$

where C_x is the PI control function in Laplace domain, in equation (3.39).

$$C_x = k_p^x + \frac{k_i^x}{s} \quad (3.39)$$

where x represents each of the considered states.

In [25] the relation between power variation and energy stored on SM capacitors are provided as:

$$C_{arm} \frac{d(v_{C_{tot_{uj}}}^2 + v_{C_{tot_{lj}}}^2)}{dt} = P_{ej}^{DC} - P_{ej}^{AC} \quad (3.40)$$

$$C_{arm} \frac{d(v_{C_{tot_{lj}}}^2 - v_{C_{tot_{uj}}}^2)}{dt} = i_{cirj} v_{conv_{acj}} \quad (3.41)$$

The control of total energy (W_h) provides the regulation of energy exchange between AC and DC sides. It is obtained through the desired value of DC circulating current \bar{i}_{cir0} by the PI control derived from (3.40) as shown in (3.42). Meanwhile, energy balancing (W_v) balance the energy between upper and lower arms, by the desired values of AC components of the circulating currents $i_{cir_{dq}}$. The PI controller is derived from (3.41) and shown in (3.43).

$$\bar{i}_{cir0} = ((\bar{W}_h - W_h) C_{W_h} + P_e^{AC}) \frac{1}{V_{DC}} \quad (3.42)$$

$$\bar{i}_{cir_{dq}} = (\bar{W}_v - W_v) \frac{C_{W_v}}{V_{conv_{acdq}}} \quad (3.43)$$

In this thesis it is proposed an adaptation of the control shown above, from [25]. The power flow controllers consist in considering the control inputs $v_{m,j}$

separately. Equations (3.32) and (3.43) consider the combined voltage v_{uj} and v_{lj} , while in this thesis they are considered separately. Therefore, each control input, i.e. the arms' equivalent voltage ($v_{m,j}$), is derived below.

From the previous chapter, the power-flow equation (2.13) can be written as (3.44).

$$\frac{v_{lj} - v_{uj}}{2} = \frac{-L_{eq}\dot{i}_{vj}}{2} - \frac{R_{eq}i_{vj}}{2} + v_{fj} \quad (3.44)$$

So, Park's transformation is applied to equation (3.44), and by a change of variables it is obtained the AC current control (3.45) and (3.46).

$$\frac{\tilde{v}_{ld} - \tilde{v}_{ud}}{2} = -(\bar{i}_{vd} - i_{vd})C_{iac} + v_{fd} \quad (3.45)$$

$$\frac{\tilde{v}_{lq} - \tilde{v}_{uq}}{2} = -(\bar{i}_{vq} - i_{vq})C_{iac} + v_{fq} \quad (3.46)$$

In the same way, equation (2.16) can be written as (3.47). A change of variables and Park's transformation on (3.47), produces circulating currents' control (3.48), (3.49) and (3.50).

$$v_{uj} + v_{lj} = -2L\dot{i}_{cirj} - 2Ri_{cirj} + V_{DC} \quad (3.47)$$

$$\tilde{v}_{ud} + \tilde{v}_{ld} = -(\bar{i}_{cir d} - i_{cir d})C_{i_{cir d}} \quad (3.48)$$

$$\tilde{v}_{uq} + \tilde{v}_{lq} = -(\bar{i}_{cir q} - i_{cir q})C_{i_{cir q}} \quad (3.49)$$

$$\tilde{v}_{d0} = -(\bar{i}_{cir 0} - i_{cir 0})C_{i_{cir 0}} \quad (3.50)$$

Collecting terms from (3.45), (3.46), (3.48) and (3.49), one obtains the uncoupled control inputs at (3.51), (3.52), (3.53), and (3.54).

$$\tilde{v}_{ud} = -\frac{1}{2}(\bar{i}_{cir d} - i_{cir d})C_{i_{cir d}} + (\bar{i}_{vd} - i_{vd})C_{iac} \quad (3.51)$$

$$\tilde{v}_{uq} = -\frac{1}{2}(\bar{i}_{cir q} - i_{cir q})C_{i_{cir q}} + (\bar{i}_{vq} - i_{vq})C_{iac} \quad (3.52)$$

$$\tilde{v}_{ld} = \frac{1}{2}(\bar{i}_{cir d} - i_{cir d})C_{i_{cir d}} + (\bar{i}_{vd} - i_{vd})C_{iac} \quad (3.53)$$

$$\tilde{v}_{lq} = \frac{1}{2}(\bar{i}_{cir q} - i_{cir q})C_{i_{cir q}} + (\bar{i}_{vq} - i_{vq})C_{iac} \quad (3.54)$$

Concerning total energy W_h and balancing energy W_v , the controller proposed by [25] in (3.42) and (3.43) is simplified and used. Where total energy's control provides the reference for $i_{cir 0}$, which regulates DC power output, while the energy balance control provides $i_{cir d}$ reference.

$$\bar{i}_{cir 0} = -(\bar{W}_h - W_h)C_{W_h} \quad (3.55)$$

$$\bar{i}_{cir d} = -(\bar{W}_v - W_v)C_{W_v} \quad (3.56)$$

Therefore, all states of a three-phase MMC can be controlled by the cascade-control adapted from [25]. Including energy states which aren't directly controlled by controller inputs.

The PI controllers developed in this section are summarized by the block diagrams in figure 3.1 to figure 3.5. Also, the firing pulses generation is depicted in figure 3.6 based on phase-shift PWM.

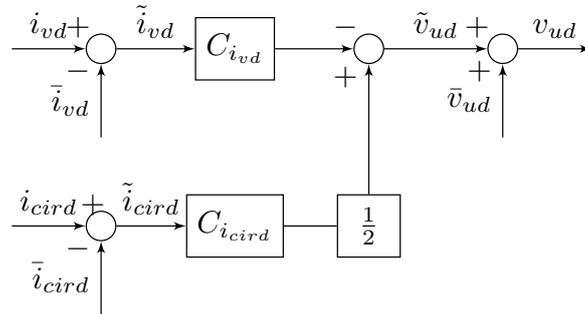


Figure 3.1: Block diagram of control input v_{ud} .

Source: Author

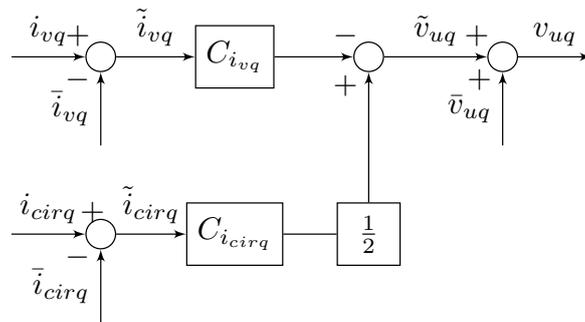


Figure 3.2: Block diagram of control input v_{uq} .

Source: Author

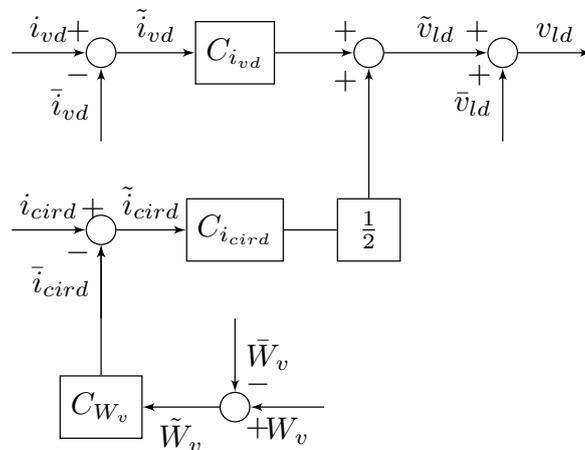
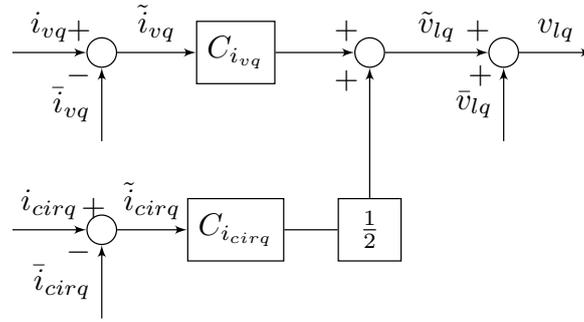


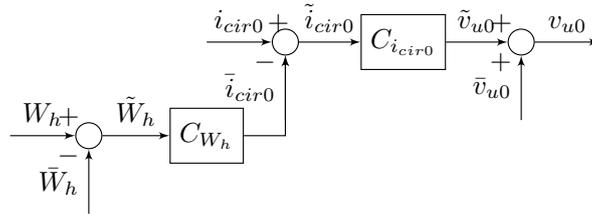
Figure 3.3: Block diagram of control input v_{ld} .

Source: Author

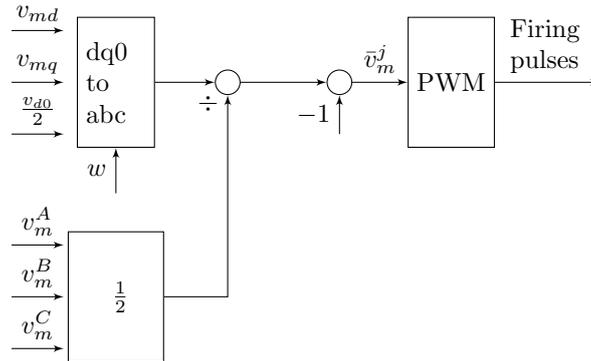
where v_{md} is v_{ud} and v_{ld} , and so on.

Figure 3.4: Block diagram of control input v_{lq} .

Source: Author

Figure 3.5: Block diagram of control input v_{u0} .

Source: Author

Figure 3.6: Block diagram of firing pulses to m arms.

Source: Author

3.2.1 Tuning

The PI controllers were tuned to present a speed of convergence close to the controllers proposed in this thesis. By setting the desired time constant τ_i , the parameters k_p^x and k_i^x can be computed as presented in [88] at chapter 8.4. Considering the proportional-integral PI controller in (3.39), it enables states to track their references:

$$C_x = k_p^x + \frac{k_i^x}{s}$$

where k_p^x and k_i^x are the proportional and integral gains for state x . As described in [88], the power controller's gains can be obtained in term of the desired time constant for the closed-loop system τ_i , as shown in (3.57) and (3.58).

$$k_p^x = \frac{L_c}{\tau_i} \quad (3.57)$$

$$k_i^x = \frac{R_c}{\tau_i} \quad (3.58)$$

For smaller τ_i , the output current controllers track faster the references, which are obtained from the active and reactive power references. However, τ_i must be large enough to attain the system dynamic requirement, as to be ten times the converter's switching frequency. As [88] mentioned, τ_i uses to be selected in the range of 0.5 ms to 5 ms. This choice is linked with the application's requirements and the converter's switching frequency.

The tuning of circulating currents' PIs is not much exploited on literature. In this thesis it is tuned considering the time constant as well as arm impedance, as shown in (3.59) and (3.60).

$$k_p^x = \frac{L}{\tau_i} \quad (3.59)$$

$$k_i^x = \frac{R}{\tau_i} \quad (3.60)$$

Moreover, gains drive the circulating currents to follow their respective reference values, given by the outer loop controllers, and maintain q component for the circulating current in its reference value, which is set to zero.

As a result of a limited literature available for the tuning of PIs used to control the energy on the MMC, this task is carried out by an trial and error approach. It is considered for the total energy and energy balance controllers, a slower response in comparison with currents. Such to avoid undesired interactions between inner and outer controllers.

First of all, the total energy controller is tuned; this controller sets the reference for the circulating current i_{cir0} . Finally, energy balancing controller is tuned and set the reference to $i_{cir d}$.

The parameters for both controllers were set using Matlab - Simulink by adjusting the desired response.

3.3 Simulation test of MMC with the PI controller at switching-model and average-model

This section presents simulations for the MMC with 41 levels with the PI controller proposed in the previous section. First of all, it is presented simulations for a medium-voltage system described by an average arm model presented in section 2.2.3. In this case, a state-space simulation is carried out on Matlab/Simulink. Additionally, a switching model is also developed. The switching model is built using the Matlab Simscape Electrical environment. The model uses twenty half-bridge SMs per arm and a phase-shift PWM modulation. Finally, a high-voltage system is simulated by the switching model. Therefore, this section and the next sections comprises the following tests:

- Medium-voltage system
 - average arm model
 - * four-quadrant power operation
 - * changes on converter energy
 - switching model

- * four-quadrant power operation
- * changes on converter energy
- high-voltage
 - Switching model
 - * four-quadrant power operation
 - * changes on converter energy

3.4 Medium-voltage system test with PI controller

In figure 3.7 a 50 MVA HVDC connection is shown. The main AC grid is connected to symmetric monopole DC line/cable, by an AC-DC MMC converter. The MMC, highlighted by the red dashed line, is detailed in figure 2.1 for the switching model and in figure 2.10 for the reduced-order average model.

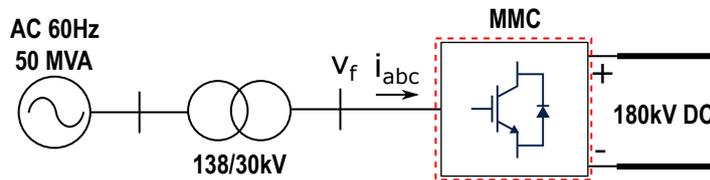


Figure 3.7: Medium-voltage system test.

The detailed switching model of the three-phase MMC converter with 41 levels, with the proposed PI, is tested using the Matlab Simscape Electrical environment. The system test is adapted from [87]. The original DC voltage was changed to 180 kV to amplify the capacity to inject reactive power. System's parameters are presented in Table 3.1, and the results are shown in the dq reference frame. The pulse generator used is a phase-shift PWM.

Table 3.1: Parameters of simulated medium-voltage system and PI control gains.

Parameter	Value	Parameter	Value
S_{MMC}	50 MVA	$k_p^{i_{vdq}}$	50
V_{AC}	30 kV	$k_i^{i_{vdq}}$	1120
V_{DC}	180 kV	$k_p^{i_{cir0}}$	28
L_c	5 mH	$k_i^{i_{cir0}}$	1000
L	14 mH	$k_p^{W_h}$	300
R_c	0.03 Ω	$k_i^{W_h}$	-25
C_{SM}	3 mF	$k_p^{W_v}$	0.8
Freq	60 Hz	$k_i^{W_v}$	0.1
R	0.5 Ω		
N	20		

Figure 3.8, figure 3.12, and figure 3.17 comprehend eight graphics each. At each figure, the first graphic depicts the active and reactive power demand, and the seven states follow it $x = [i_{vd} \ i_{vq} \ i_{cir0} \ i_{cirq} \ i_{cir0} \ W_h \ W_v]$ and their desired value \bar{x} denoted by (Ref.). All that three figures shows the simulation of the MMC average model in the medium-voltage level with the PI controller presented above. The step changes on active and reactive power (P_e and Q_e) shown at 1st graphic comprehend the four-quadrant operation with the maximum power injection, 70% of nominal power, respecting the capability curve.

Figure 3.8: Four-quadrant operation of MMC average model with PI controller.

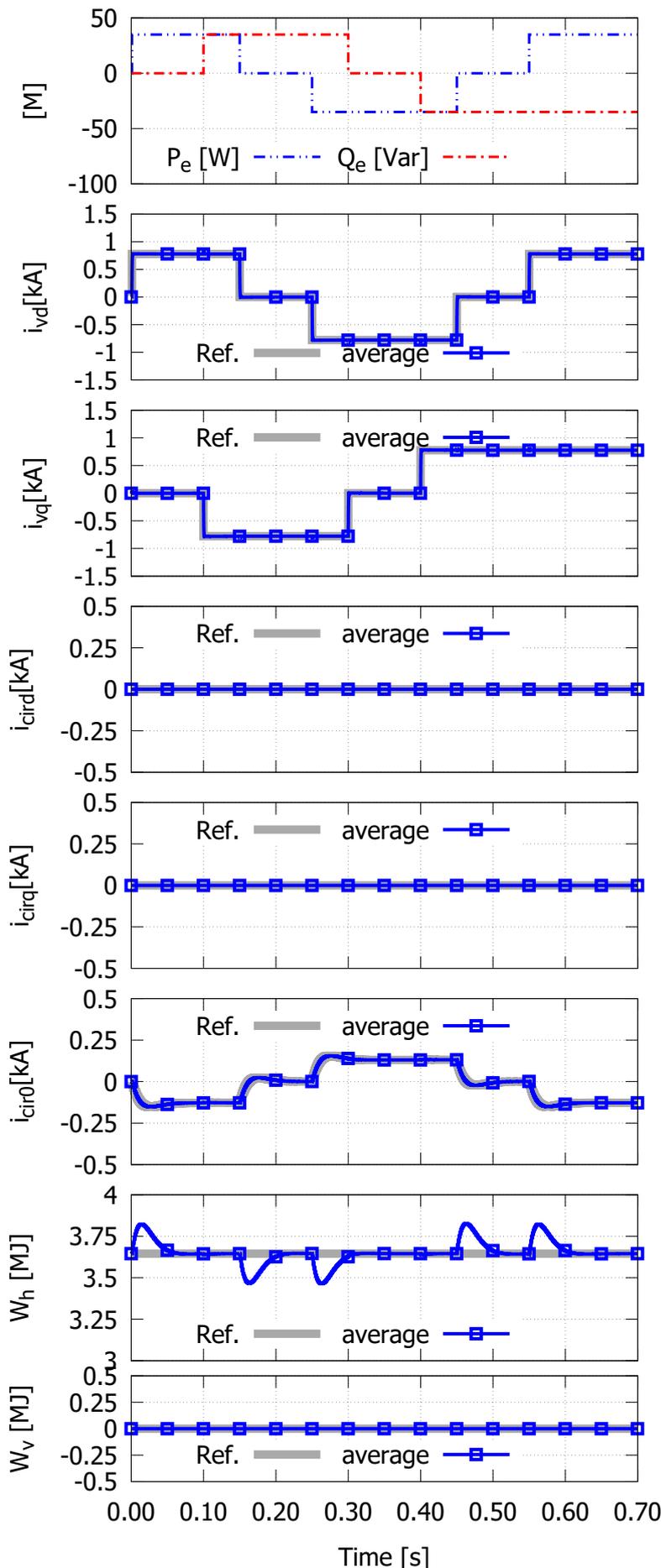


Figure 3.9 is a detail from figure 3.8. It shows states i_{vd} and i_{vq} under the active

Four-quadrants operation average-model medium-voltage At $t = 0.05$ s P_e turns to 35 MW, which is followed by the related states: i_{vd} (2nd graphic) and i_{cir0} (6th graphic). State i_{vq} in 3rd graphic, faces a small transient which is shown in detail in figure 3.9. State W_h (7th graphic) is affected and presents a transient of 50 ms. The same behaviour is observed in all the active power changes, at $t = 0.15$ 0.20 0.35 0.40s.

Meanwhile, Q_e turns to 35 MW at $t = 0.10$ s, where the directly linked state, i_{vq} in the 3rd graphic, follows the new reference in 1 ms. The direct component of AC current, i_{vd} , faces a fast transient associated with reactive power changes, see detail at figure 3.10. The same pattern is seen at all change of reactive power.

Furthermore, circulating currents i_{cirdq} remain on their references during all changes (4th and 5th graphic). However, total energy W_h deal with transients linked with changes in i_{cir0} , which can be explained because this current manages the DC output power, which affects the stored energy.

power step at $t = 0.05$ s. State i_{vd} needs less than 1 ms to track its reference, and presents no overshoot. As a consequence, i_{vq} presents a transient, and returns to its reference when $i_{vd} = \bar{i}_{vd}$.

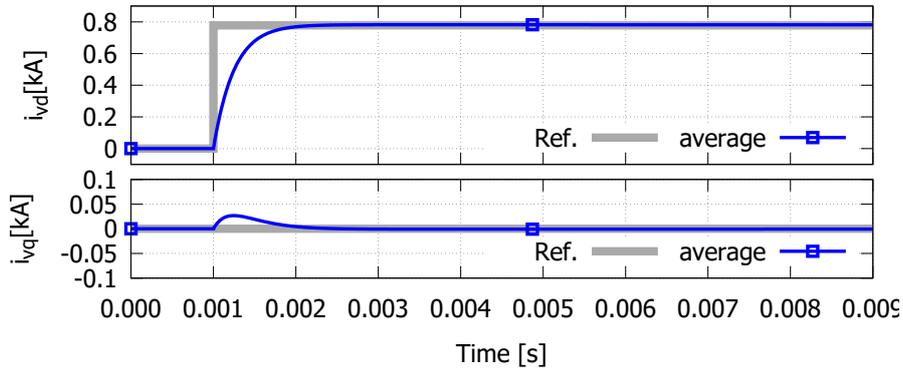


Figure 3.9: Detail of step on active power, from figure 3.8.

Source: Author

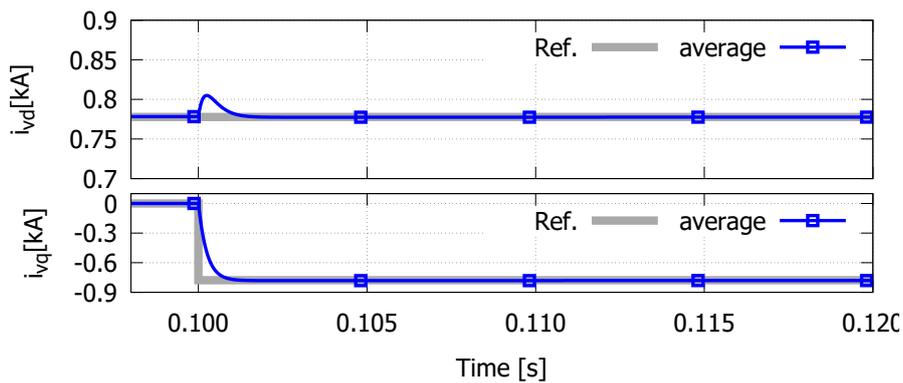


Figure 3.10: Detail of step on reactive power, from figure 3.8.

Source: Author

It is clear that the PI can drive the states of the MMC average-model to track their references. In figure 3.11, i_{cir0} is shown in detail and it is possible to see the state tracking its reference without delays.

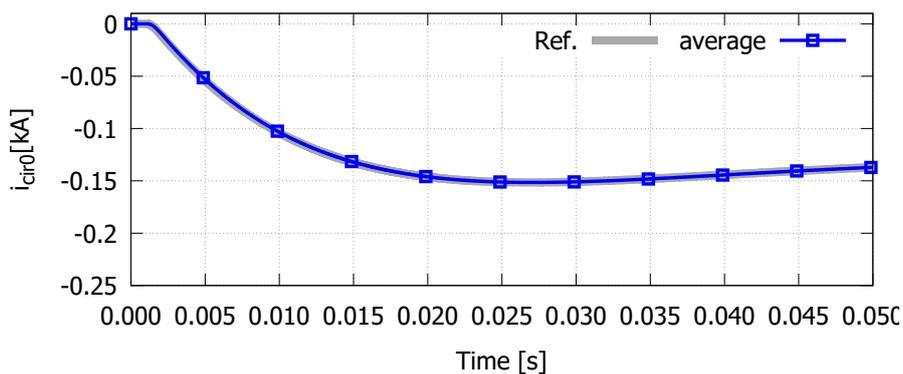
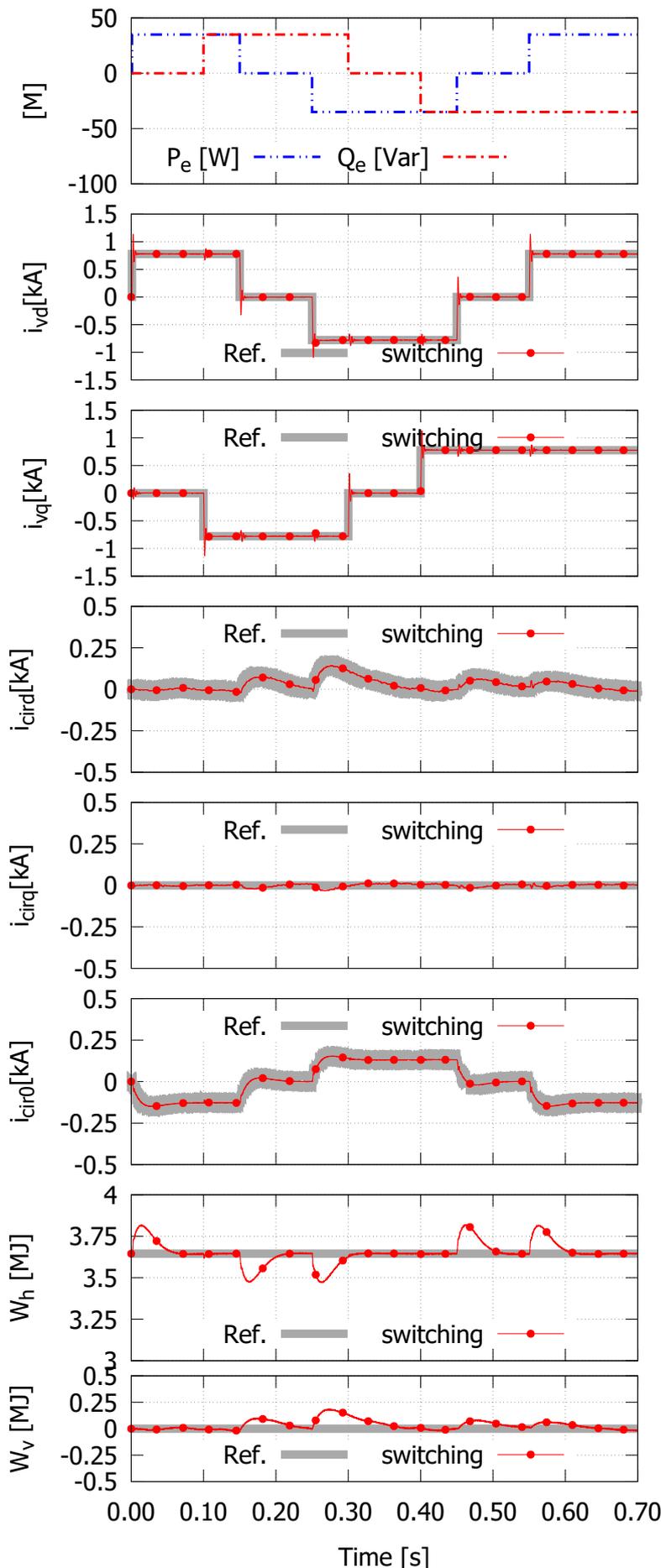


Figure 3.11: Detail of state i_{cir0} while a step on active power, from figure 3.8.

Source: Author

Figure 3.12: Four-quadrant operation of MMC switching-model with PI controller.



Still on figure 3.12, the dq component of circulating currents ($i_{cir dq}$) present an

Four-quadrants operation switching-model medium-voltage In figure 3.12, a switching model is simulated with the proposed PI controller. It is possible to see that states follow their references (Ref.).

In the same way as presented in the average model (figure 3.8), there are coupling effects between i_{vd} and i_{vq} (2nd and 3rd graphic). However the effects here were larger, and are detailed in figure 3.13 and figure 3.14. There it may be seen that, at each active power step ($t = 0.05\ 0.15\ 0.20\ 0.35\ 0.40\ s$) while i_{vd} reacts to track the new reference, i_{vq} oscillates around its reference. Similarly, when there are changes on i_{vq} , i_{vd} also oscillates around its reference, as for example, following reactive power steps, i_{vd} oscillates around its reference.

If compared with the average model at figure 3.8, it is possible to see that reference of direct component of circulating current ($i_{cir d}$ Ref.) and circulating current reference ($i_{cir 0}$ Ref.) present small oscillations which came from SMs switching, at 4th and 6th graphics.

overshoot at the inversion of the power-flow direction at $t = 0.20$ s, to $P_e = -35$ MW and $Q_e = 35$ MVar where they react more powerfully even causing an unbalancing between upper and lower arms energy (W_v at 8th graphic). Finally, W_h (7th graphic) shows a stronger reaction for each change of active power in comparison with the average-model.

Figure 3.13 is a detail from figure 3.12. Show state i_{vd} and i_{vq} under the active power step at $t = 0.05$ s. State i_{vd} need 10 ms to track their references, and present an overshoot. In comparison with the average-model in figure 3.8, i_{vd} switching response is ten times slower and there is overshoot. Figure 3.13 also shows that i_{vq} deals with a slow transient, and takes 50 ms to re-track the reference, substantially large than average-model.

It is important to highlight that PI controllers' gains were set the same for both the average-model and switching-model, aiming to have suitable performance in both models and fair comparison between them. However, the gains' adjust may improve the speed of convergence of the response on the switching-model.

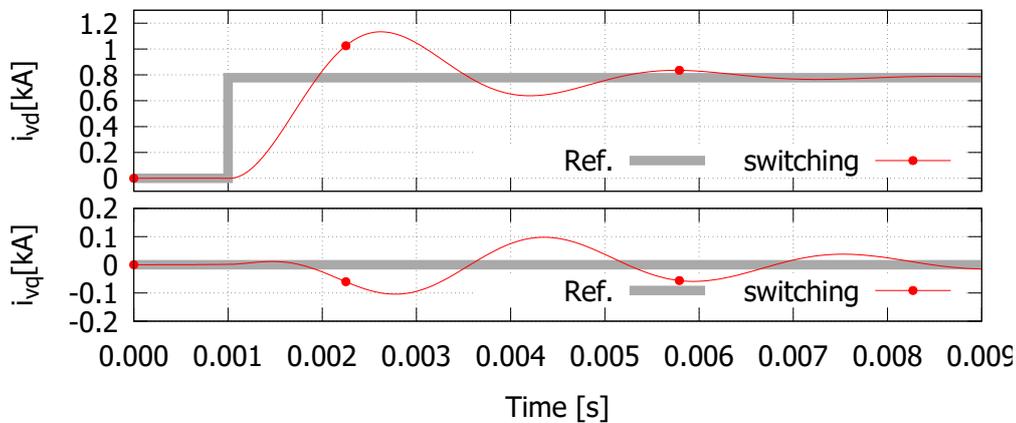


Figure 3.13: Detail of step on active power, from figure 3.12.

Source: Author

Figure 3.14 presents the detail of the reactive step from figure 3.12. States i_{vd} and i_{vq} are displayed. For the reactive step, i_{vd} faces a transient and takes longer than 50 ms to re-track the reference. Quadrature-component, directly linked with reactive power, needs around 10 ms to follow its reference. As mentioned before, it presents a slower dynamic in comparison with the average-model.

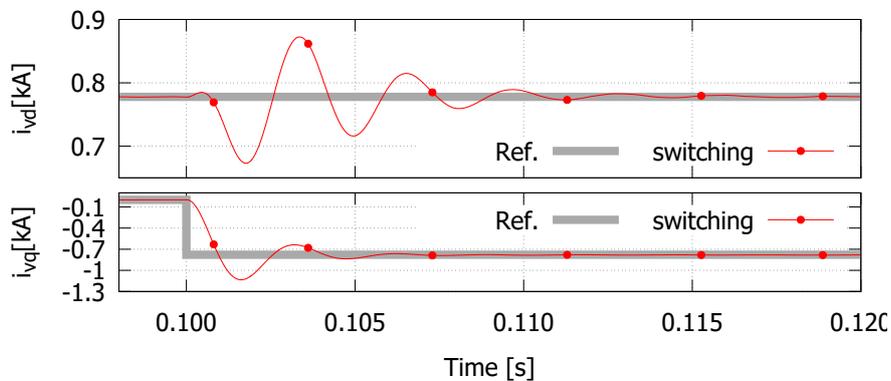


Figure 3.14: Detail of step on reactive power, from figure 3.12.

Source: Author

It is clear that PI can drive well the states of the MMC average-model to track their references. In figure 3.15, i_{cir0} is shown in detail and it is possible to see that state following its reference without delays. In addition, small oscillation can be seen in the reference and, as a consequence, in the state i_{cir0} .

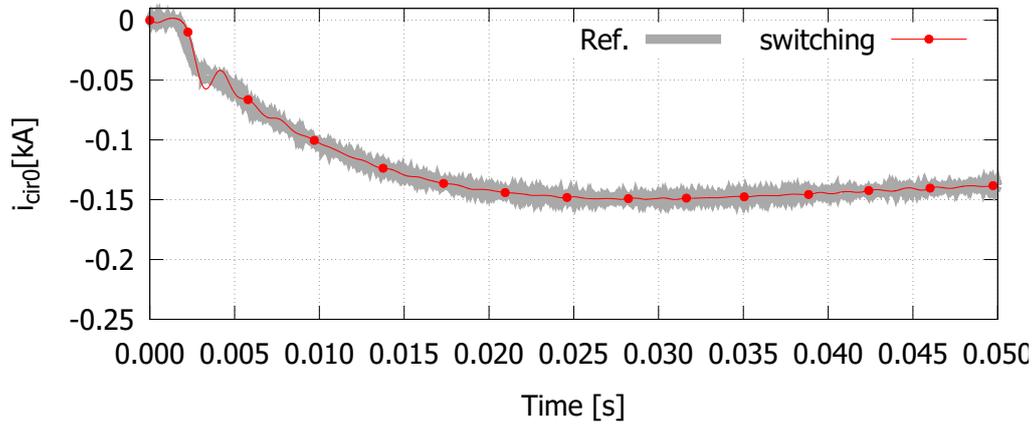


Figure 3.15: Detail of state i_{cir0} while a step on active power, from figure 3.12.
Source: Author

Figure 3.16 presents state W_v , where a fluctuation around the reference is noticed. Once again, switching-model presents a slower dynamic in comparison with average-model.

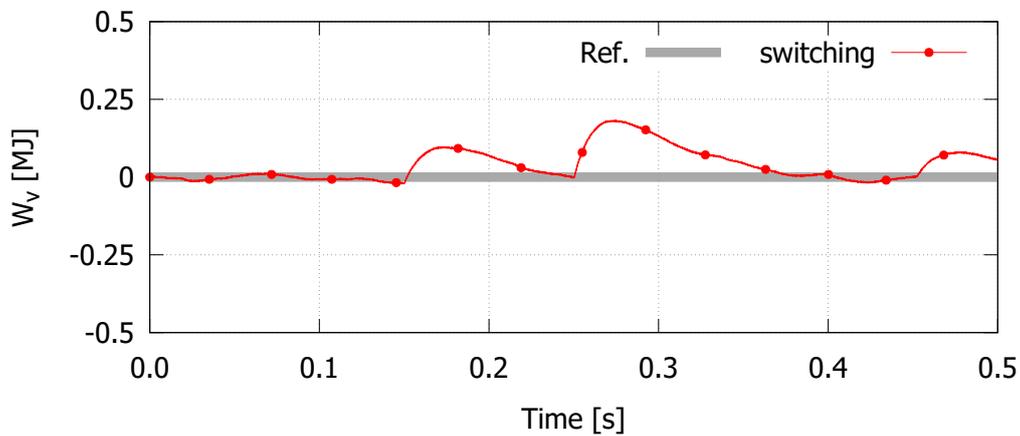
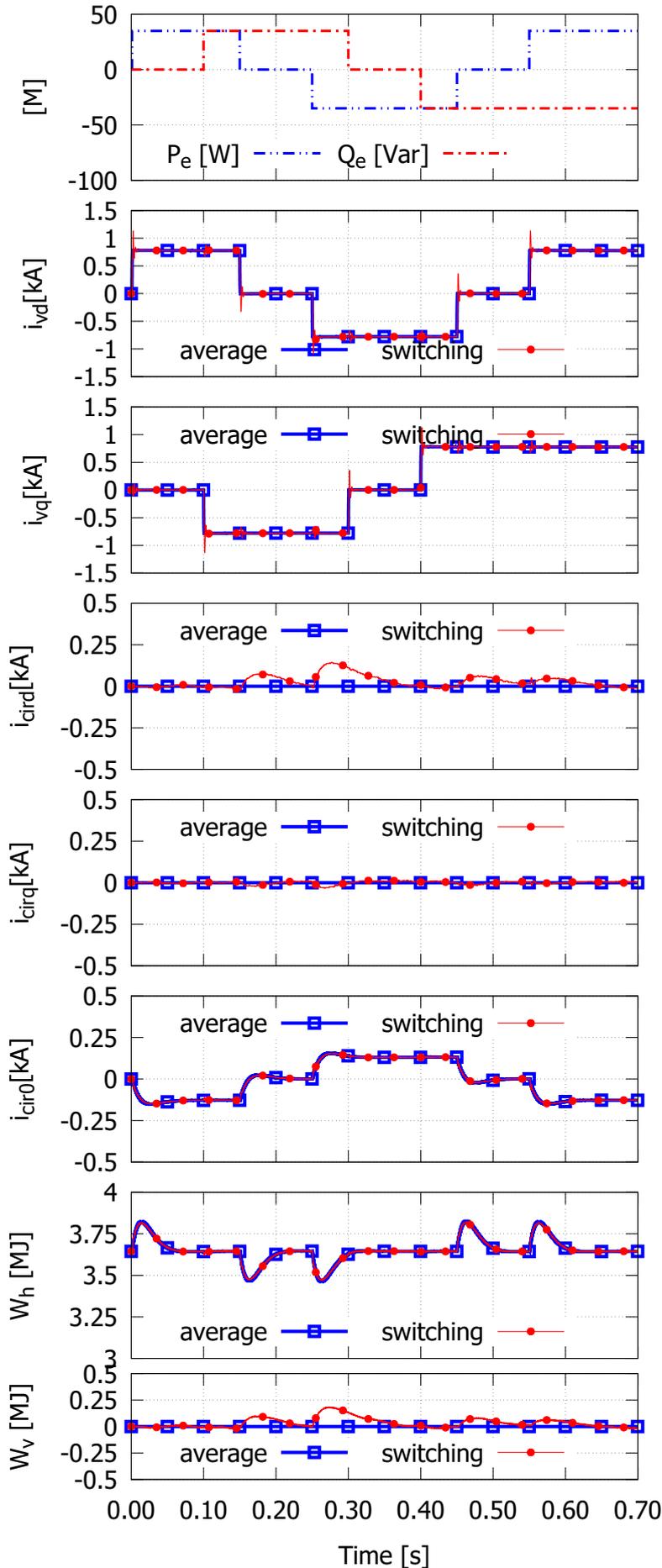


Figure 3.16: Detail of state W_v .

Source: Author

Figure 3.17: Switching-model and average-model comparison.



Four-quadrants operation of average-model and switching-model for comparison Figure 3.17 shows the states' response from average-model (figure 3.8) and switching-model (figure 3.12) without their references (Ref.).

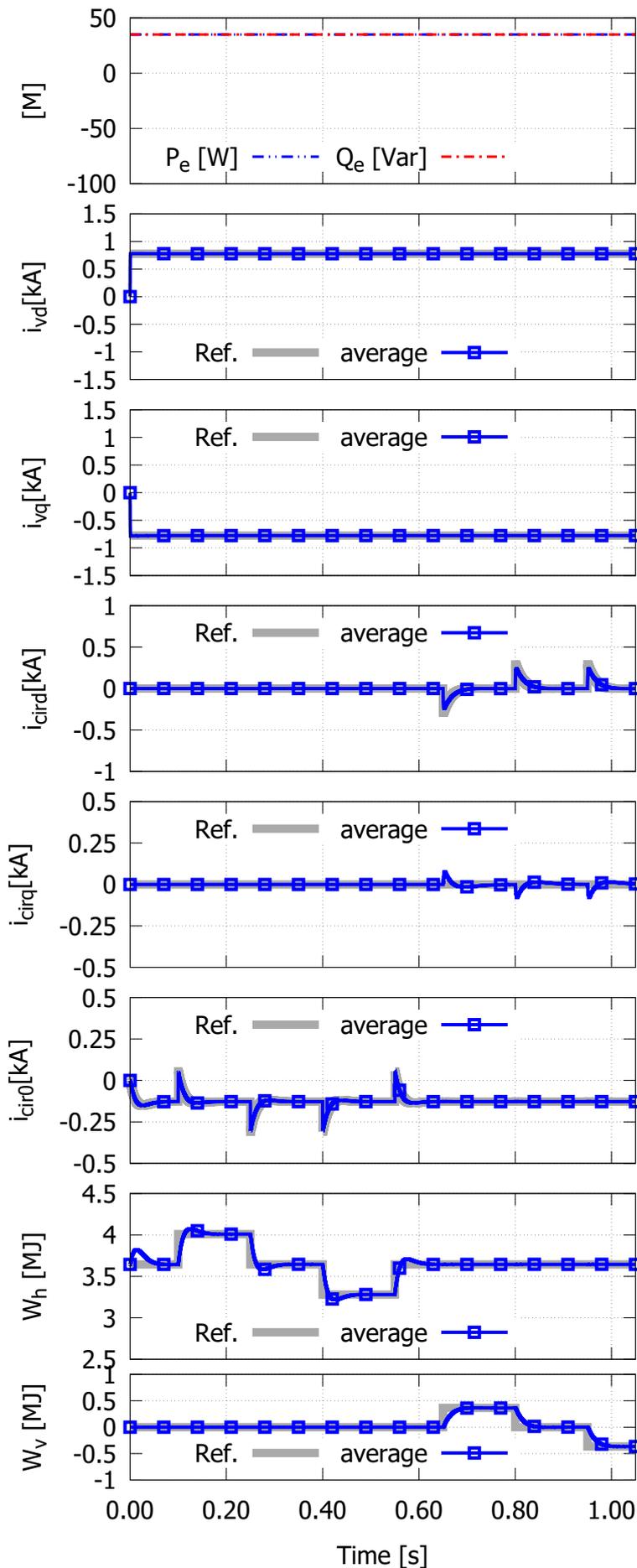
At figure 3.8 and 3.12 PI control states, are at their desired values, however present distinct references for each models, on states $i_{cir d}$ and $i_{cir 0}$. This is a result of the additional dynamics from SMs switching, in which affect equations on (3.55) and (3.56) directly linked to above mentioned states.

At $i_{cir d}$ and $i_{cir 0}$ (4th and 6th graphic) it is possible to see the difference between responses for average and switching models.

Total energy W_h in the switching model presents larger overshoot compared with average model.

At energy balancing W_v at 8th graphic, unbalance caused by oscillations at $t = 0.20$ s can be seen on the switching model. However, this can't be seen at the average model.

Figure 3.18: Energy change at MMC average-model with PI controller.



Change on converter energy W_h and W_v average-model medium-voltage Figure 3.18, figure 3.21 and figure 3.22 also comprehend the eight graphics containing power and states' response. However, in these tests the PI control response for energy steps were analyzed. Power is set to 70 % of nominal power at $t = 0.01 s$, and step changes in total energy are applied at $t = [0.1 0.2 0.25 0.35 s]$, while balancing energy is changed at $t = [0.4 0.50 0.55 s]$.

In figure 3.18 the performance of the average-model MMC with PI controller is evaluated for a change in converter energy. The operation point is changed at $t = 0.01 s$, where $P_e = 35 MW$ and $Q_e = 35 MVar$. The designed PI control tested here allows the decoupling between DC voltage produced by the converter and the voltage imposed by the DC bus. As a result, it is possible to set the reference to converter energy without compromising system operation.

In this way, an increase in total energy is defined at $t = 0.10$ s at W_h (7th graphic). To attain energy's desired reference, i_{cir0} increases momentarily around the reference at $t = [0.10 \ 0.35$ s] and decreases to accomplish energy discharge at $t = [0.20 \ 0.25$ s], as a result of control designed in (3.55).

An change is imposed for W_v (8th graphic) at $t = 0.65$ s. State variables $i_{cir d}$ and $i_{cir q}$ swing until the energy balancing (W_v) track the new reference.

It is important to highlight that the tests done at figure 3.18 are not a conventional converter operating point (as delivery active and reactive power) and consists on a additional achievement where set point of converter energy can be modified to achieve grid requirements, as ancillary services.

Figure 3.19 presents a zoom from figure 3.18. It is possible to see that the speed of convergence of W_h is around 200 ms, with a minor overshoot. Meanwhile \bar{i}_{cir0} momentarily changes to attain the new energy demand.

In figure 3.20 it is shown the detail of W_v increase. In this case, $\bar{i}_{cir d}$ temporally changes to drive W_v to \bar{W}_v . Also, $i_{cir q}$ is affected and re-tracks the reference in 10 ms. This agrees with the assumption of states $i_{cir dq}$ to be used to manage the energy distribution between legs.

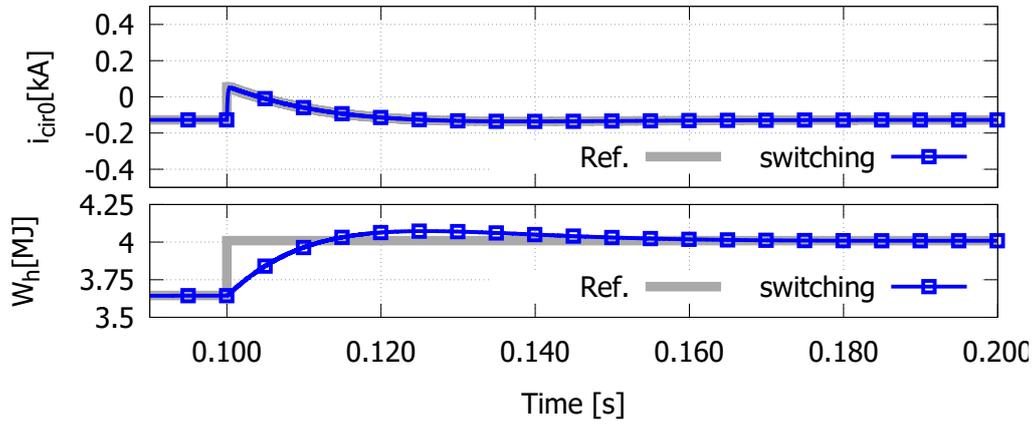


Figure 3.19: Detail from figure 3.18 of increase in energy W_h .

Source: Author

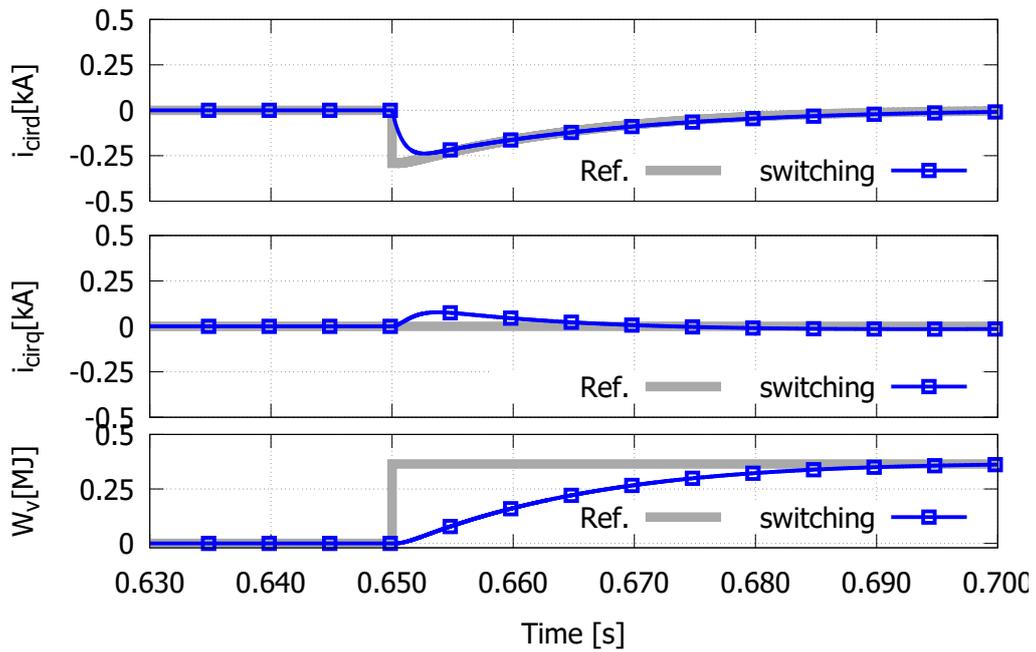
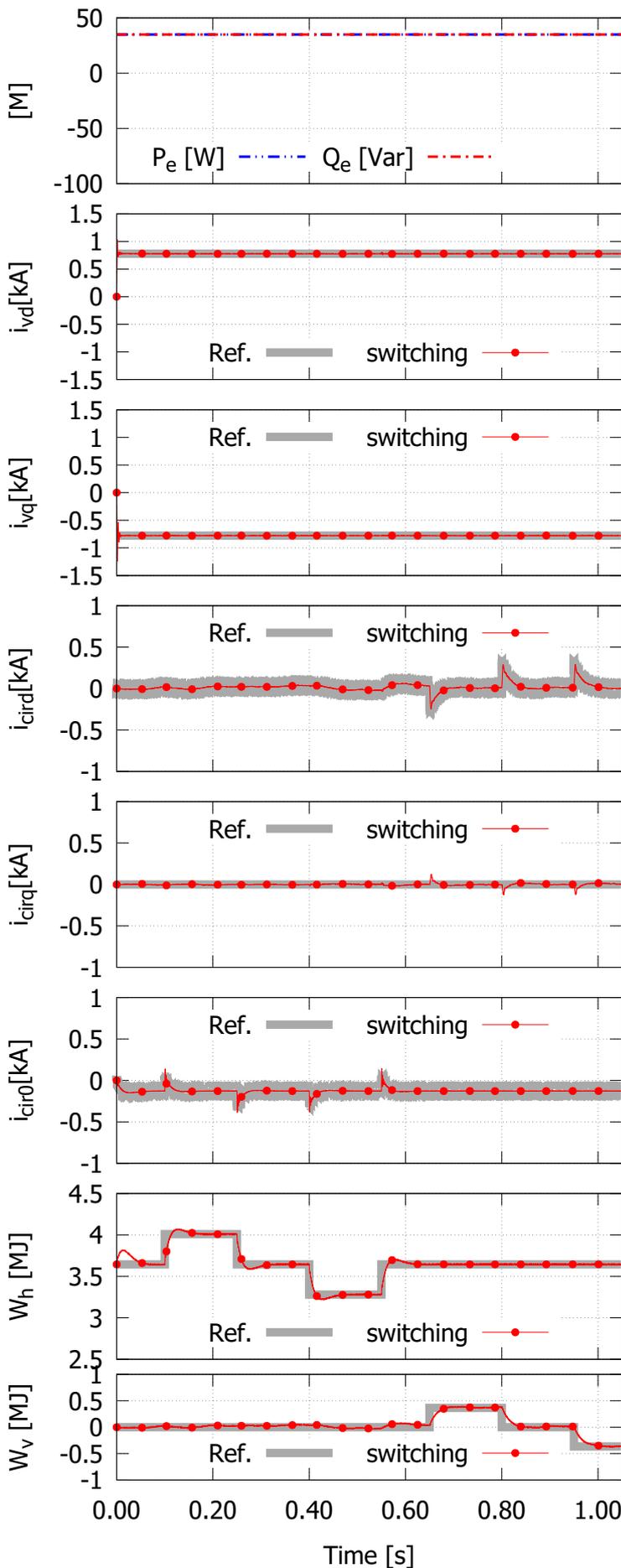


Figure 3.20: Detail from figure 3.18 of increase in energy balancing W_v .

Source: Author

Figure 3.21: Energy change at MMC switching-model with PI controller.



Change on converter energy W_h and W_v switching-model medium-voltage In figure 3.21, the switching-model is simulated under changes on converter energy. The increase in total energy at $t = 0.10$ s at W_h (7th graphic) is linked with the changes on i_{cir0} . The same behaviour can be seen at $t = [0.25 \ 0.40 \ 0.55 \text{ s}]$ where W_h decreases.

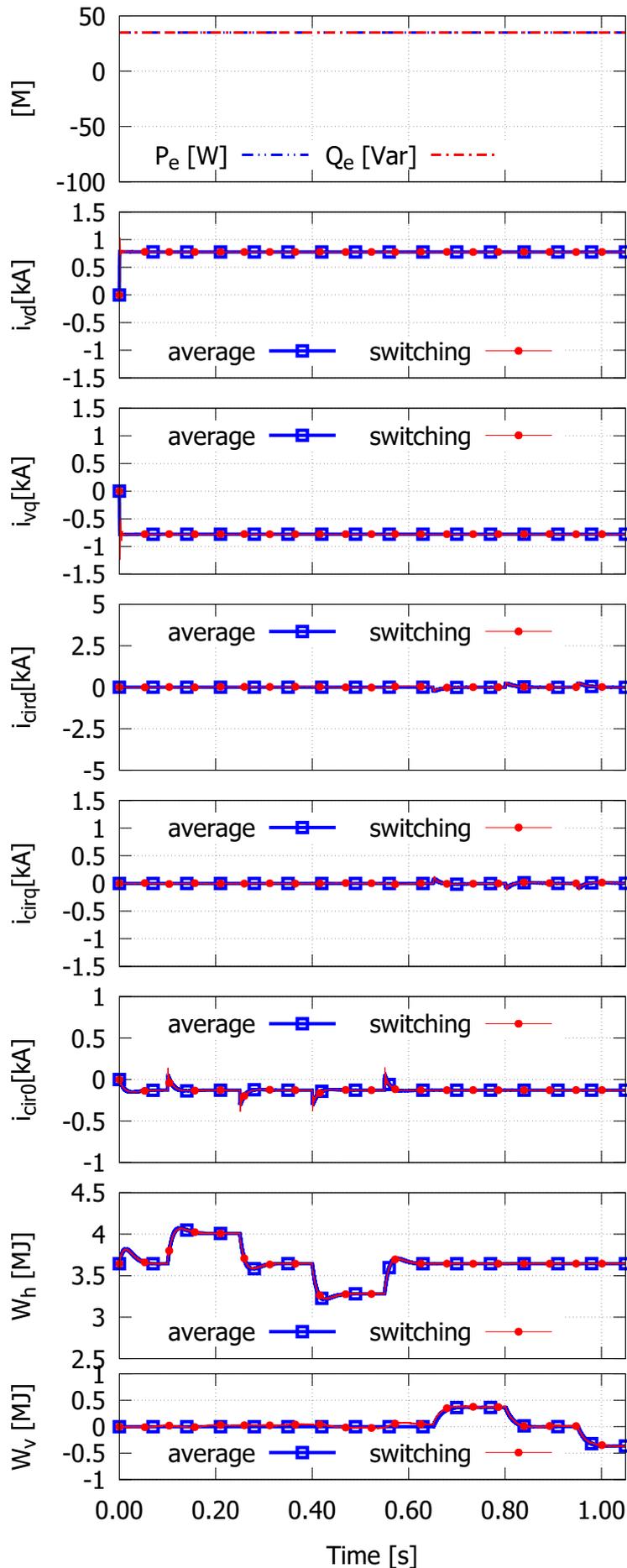
State i_{cir0} on 4th graphic has its reference changed to reach the desired value of W_v , as designed in equation (3.56). Also, i_{cirq} lightly swings around its reference at each change on W_v , indicating the share of responsibility to i_{cirdq} to promote energy balancing.

State i_{cir0} and state W_h are not affected by changes on energy balancing W_v .

The speed of convergence for all changes is close to the one presented by the average model.

The reference of i_{cir0} presents a small oscillation here. This may come from the switching devices effect.

Figure 3.22: Average-model and switching-model comparison.



Energy changes for average-model and switching-model Figure 3.22 merges responses from figures 3.18 and 3.21. In both previous results for energy change, states track their reference. As it is possible to see on the 6th graphic of figure 3.22, there are distinct references for i_{cir0} at each model. Concerning the reaction of i_{cir0} for each energy change, states' response for each model, match in duration and range.

The difference noticed at i_{cir0} references comes from the divergence between real switching resistance and the equivalent value of SMs resistance at an arm (R), considered in the average model, also, the additional dynamic from switching SMs.

3.4.1 Control Effort

The chosen gains directly affect the control effort, which can be measured by the overshoots in transients on the control output. Figures 3.23 and 3.24 present average and switching model comparison, however they have similar performances, except in few moments where switching model presents a minor opposite overshoot which will be emphasized in the next comment. So, the following comments are suitable for both models.

In figure 3.23 and figure 3.24 are presented the control output signals (v_{ud} , v_{uq} , v_{ld} , v_{lq} and v_{d0}) for the two above presented tests. In figure 3.23, changes in active and reactive power produce a transient on control inputs which are not larger than three times of the desired value of v_{ud} and v_{uq} . Meanwhile, v_{ld} and v_{lq} present overshoots around thirteen times of the desired values. In the other hand, v_{d0} did not presented pronounced transients.

In figure 3.24, the changes in total energy ($t = [0.10 \ 0.25 \ 0.40 \ 0.55]s$) have a major effect on v_{d0} because it drives the DC power output. For balancing energy changes at $t = [0.65 \ 0.80 \ 0.95]s$ the control inputs v_{ud} , v_{uq} , v_{ld} and v_{lq} overshoots are not larger than twice their respective desired values.

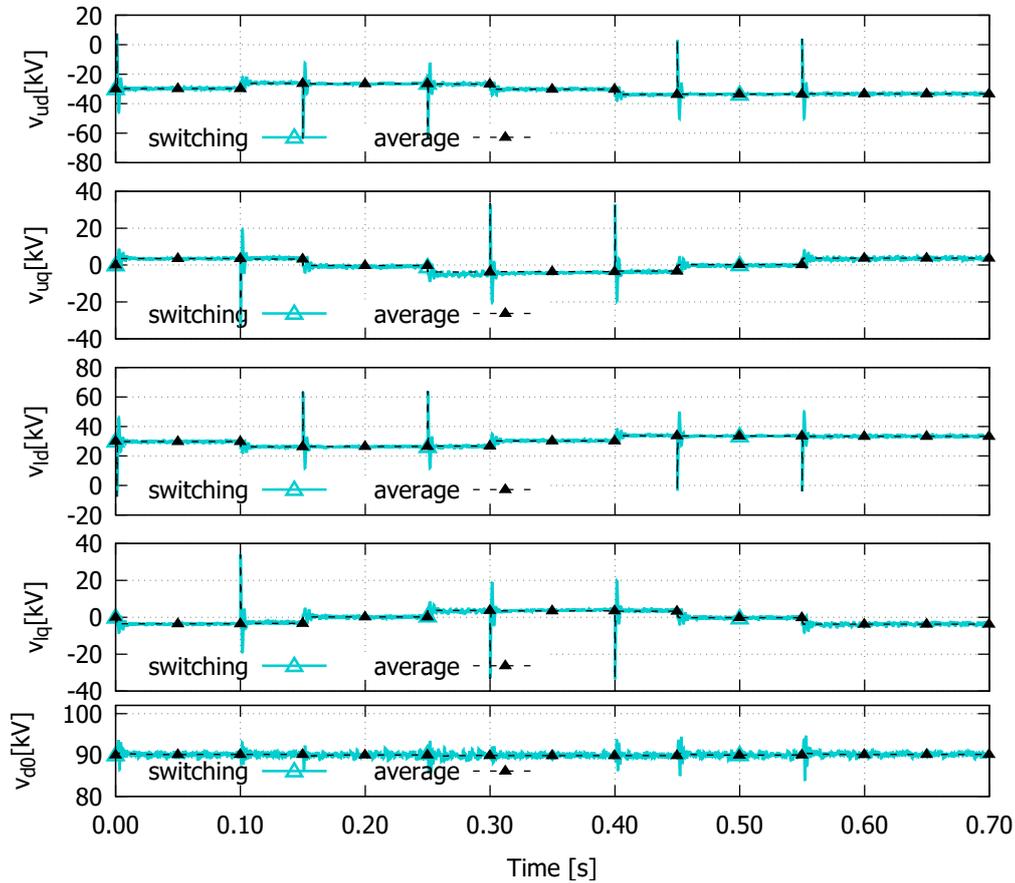


Figure 3.23: Control inputs of average and switching model for the operating points presented in figure 3.17.

Source: Author

The results presented before aim to compare the performance of the average-model and switching-model. Furthermore, the switching-model will be further analyzed because of the additional dynamics that come from SMs switching.

Figure 3.26 shows the voltage at each SM and figure 3.25 shows $dq0$ component of circulating currents for the operating point of P_e and Q_e equal to 70% of nominal power.

At the switching-model simulated here, it is not designed a controller to stabi-

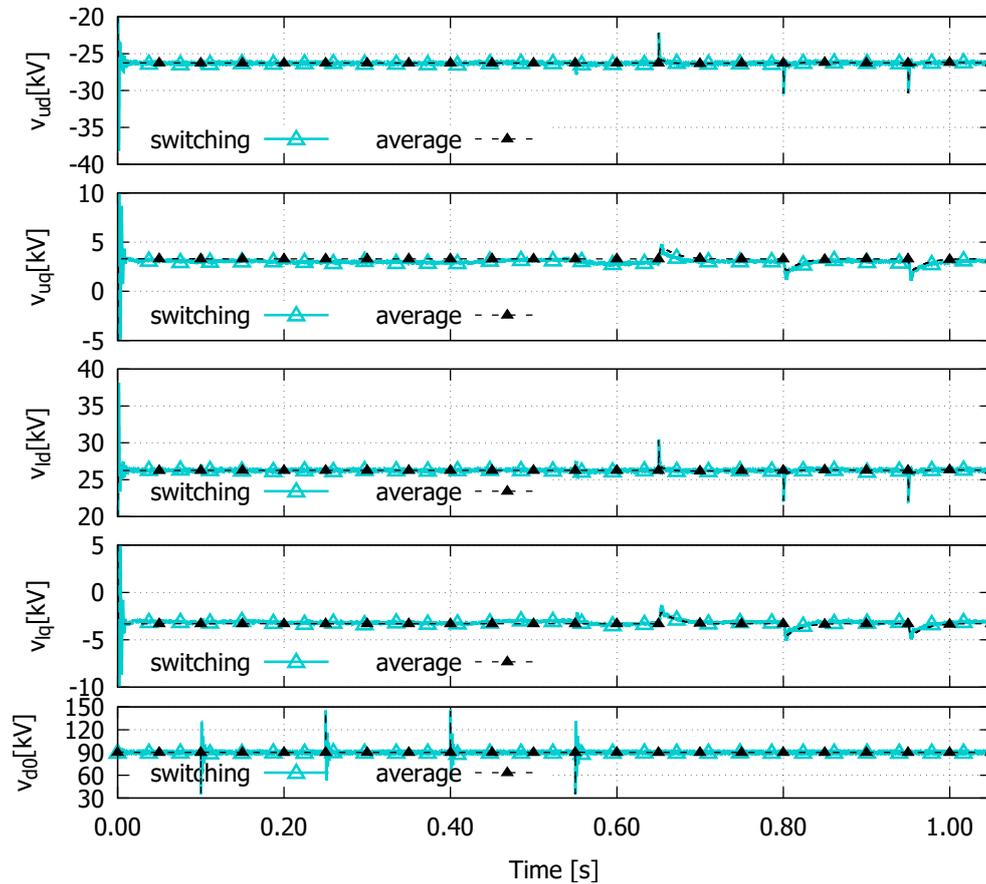


Figure 3.24: Control inputs of average and switching model for the operating points presented in figure 3.22.

Source: Author

lize the double-fundamental frequency component of circulating currents. However it is possible to see in figure 3.25 that components dq are controlled around references, zero. They are amplified at each operating point change, however become smaller in steady state. Meanwhile component zero has small oscillation and follows the fundamental component.

Because of the sorting algorithm implemented, it is possible to notice a suitable balancing between each SM voltage. At the right part of the figure is presented a zoom in time from 0.32 s to 0.38 s. By this, it is clear that the voltage range in one SM changes for each period and even when they are bypassed, keeping a constant value of voltage.

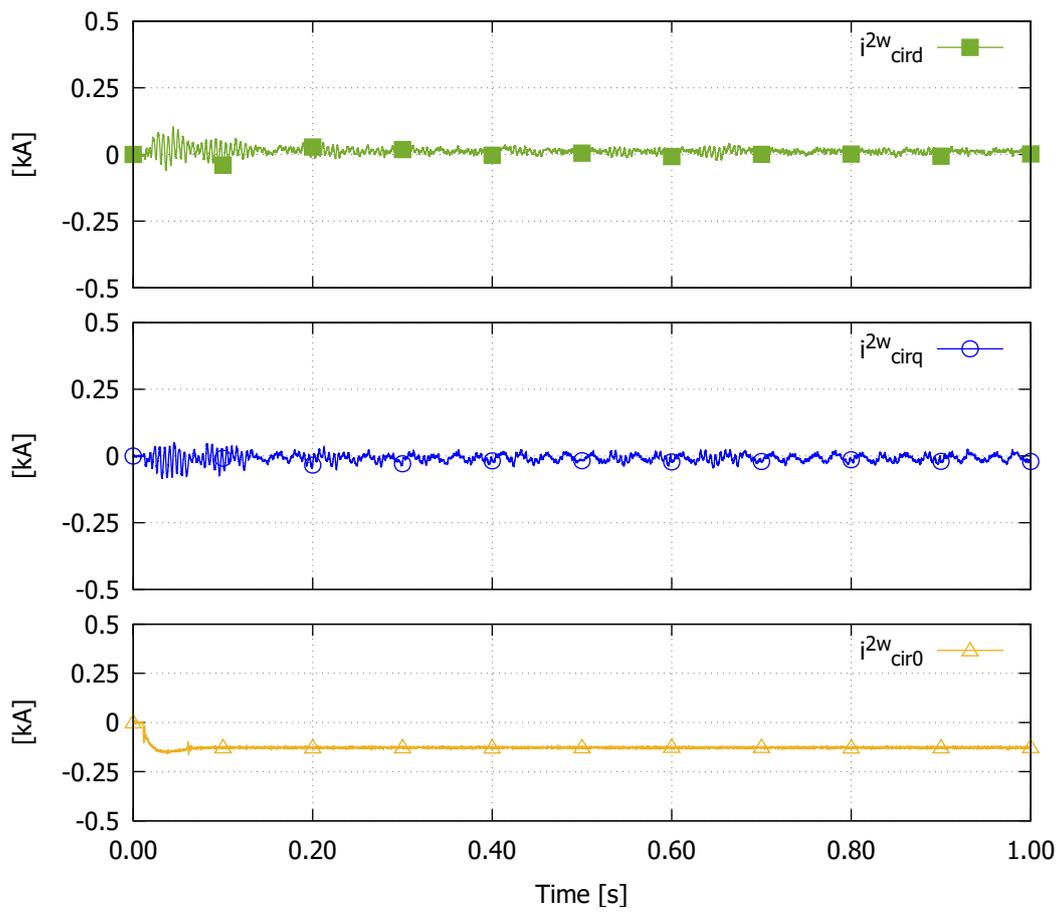


Figure 3.25: Double-fundamental frequency component of circulating currents at medium-voltage switching model with PI controller.

Source: Author

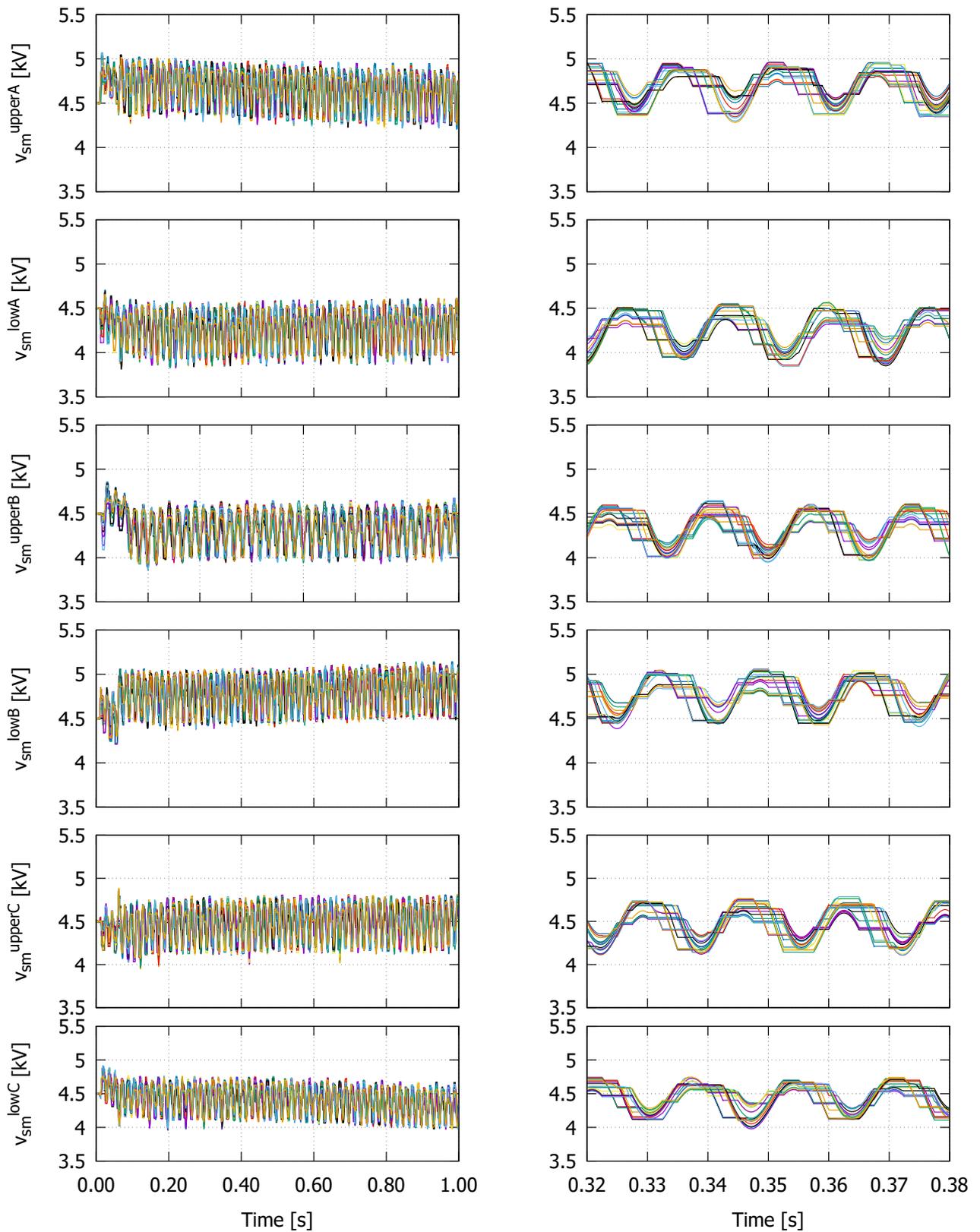


Figure 3.26: Voltage of each SM per arm of medium-voltage system with PI controller.
Source: Author

3.4.2 Robustness over parameters' uncertainties and voltage fluctuation on medium-voltage system with PI controller

Robustness The robustness test considers the control's sensitivity over parameter uncertainties. This section shows different scenarios with parameter uncertainties considered.

It is essential to highlight that the manufacture of power electronics provides devices from low to high tolerance errors, directly affecting costs. Practical lower tolerances are 10%, and can be increased to a tolerance of less than 0.1%. The literature points to SMs capacitance tolerance error as the key to a proper MMC design, as mentioned by [89].

In this section's test, the simulations go beyond practical tolerance error, aiming to overstress the control performance. For each one, the parameters R , R_c , L , L_c and C_{SM} change (one at a time) in $\pm 10\%$ and $\pm 20\%$ from their nominal values. Meanwhile, the control remains the same, i.e., as designed using nominal values. At $t = 0.005$ s a change in active power is performed, while at $t = 0.01$ s a change in reactive power.

Figure 3.27 shows the state variables with $\pm 10\%$ and $\pm 20\%$ of arm resistance (R). This test PI controller drives all state variables to the desired value even with the arm resistance error. Additionally, for changes in R_c figure 3.28 shows that PI performs the state reference. However, i_{circd} and W_v present a small deviation in the test where R_c is equal to -20% of nominal value.

In figure 3.29 there is a response for changes in arm inductance L . Once again, there are light overshoot for state i_{circd} and W_v , but they can be neglected. The other state variables are well controlled by PI. Meanwhile, changes of $+20\%L_c$ result in a response of i_{circd} and W_v , which differ from the other scenarios.

For SM, capacitor uncertainties presented in figure 3.31 state variables face distinct response in transients. However, track the reference in steady-state. Most of the transient comes from the initial value of W_h , which is linked with SM capacitance value; there is a high speed of convergence to the desired value. Also, $\pm 20\% C$ affect the speed of W_v , and consequently i_{circd} .

Voltage fluctuation The voltage fluctuation is also analyzed in this section. This test consider (1) a over (under) AC voltage from nominal value at the PCC; (2) a over (under) from nominal DC voltage. The $\pm 10\%$ and $\pm 5\%$ from nominal value are considered.

- Fluctuation in AC voltage result over-signal in state variables i_{vd} and i_{vq} . The other state variables are not affected by the voltage change (see figure 3.32);
- Fluctuation in DC voltage has a similar effect of change in SM capacitors. This is a result of the desired value for W_h in equation (3.28) where V_{DC} play a crucial role.

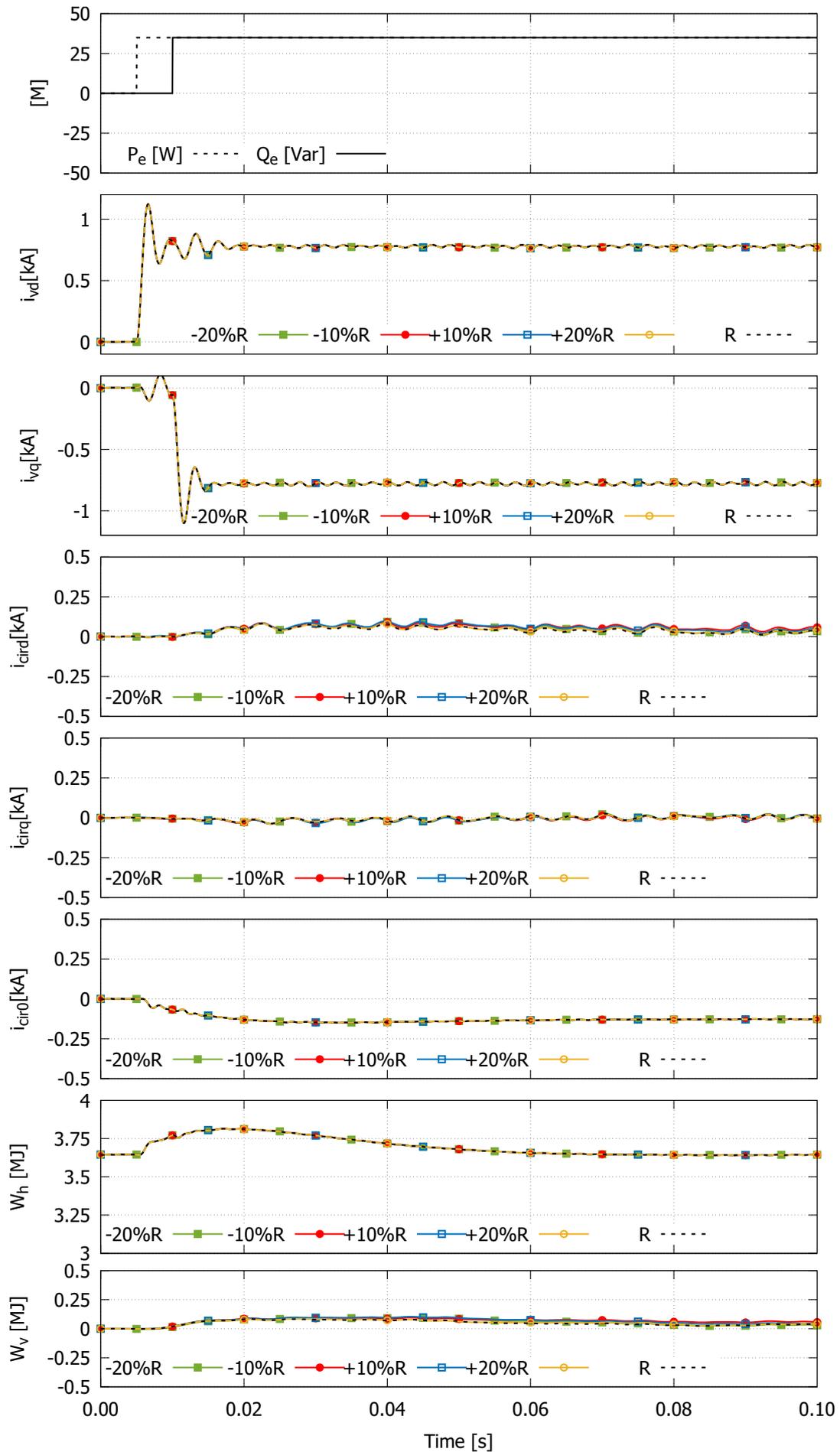


Figure 3.27: The system state over variation of parameter R of medium-voltage system with PI controller.
Source: Author

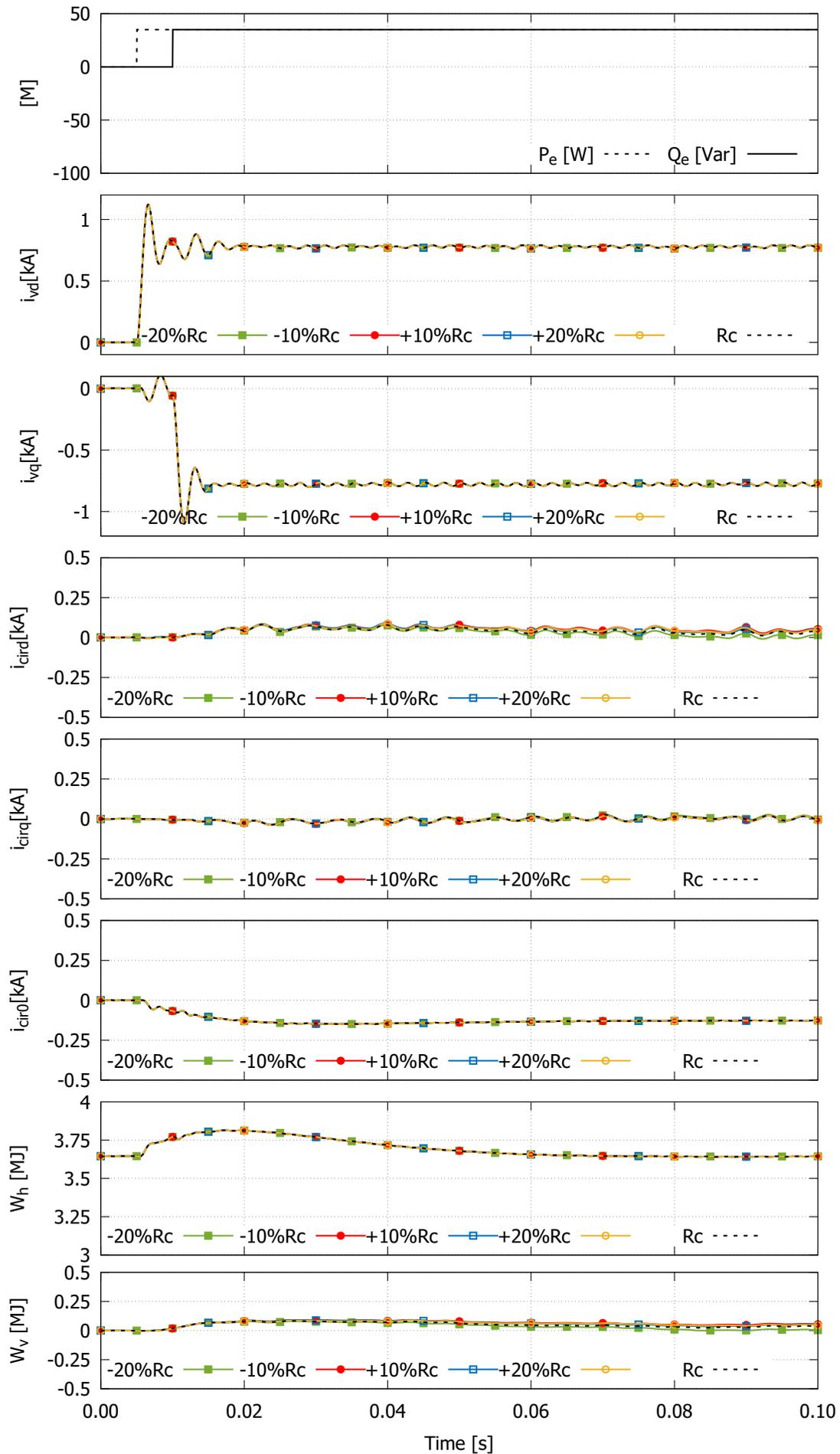


Figure 3.28: The system state over variation of parameter R_c of medium-voltage system with PI controller.

Source: Author

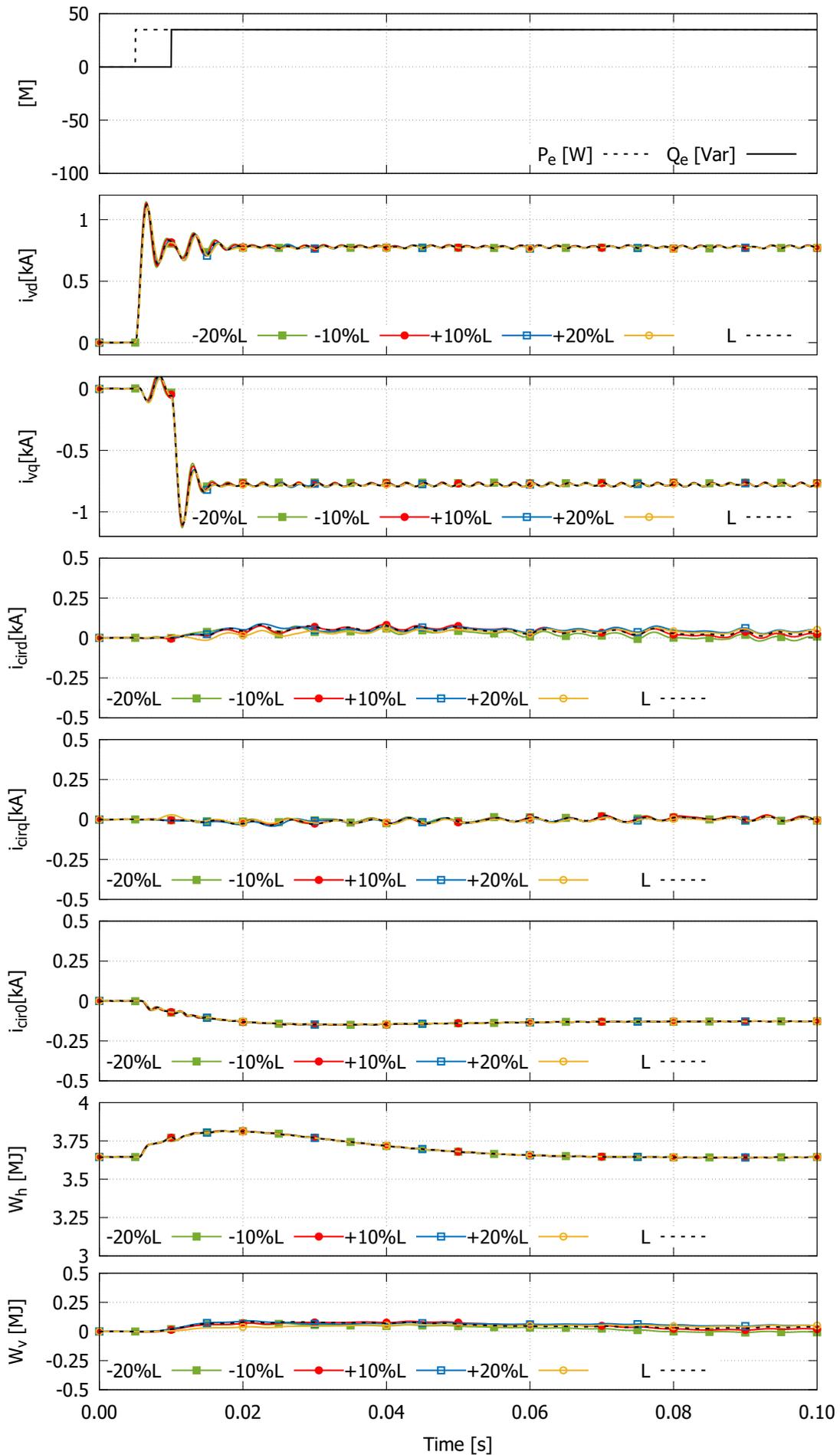


Figure 3.29: The system state over variation of parameter L of medium-voltage system with PI controller.
 Source: Author

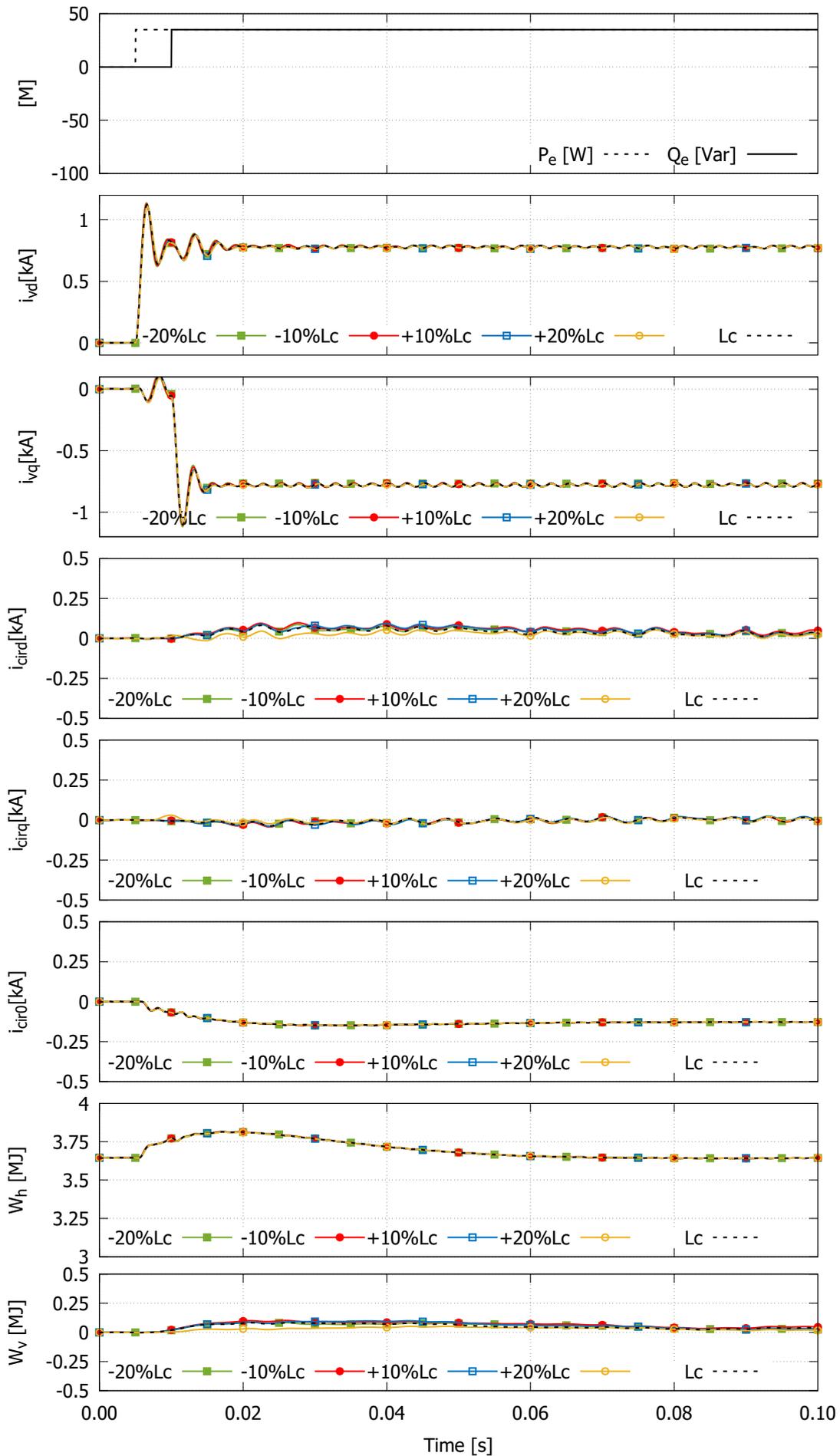


Figure 3.30: The system state over variation of parameter L_c of medium-voltage system with PI controller.

Source: Author

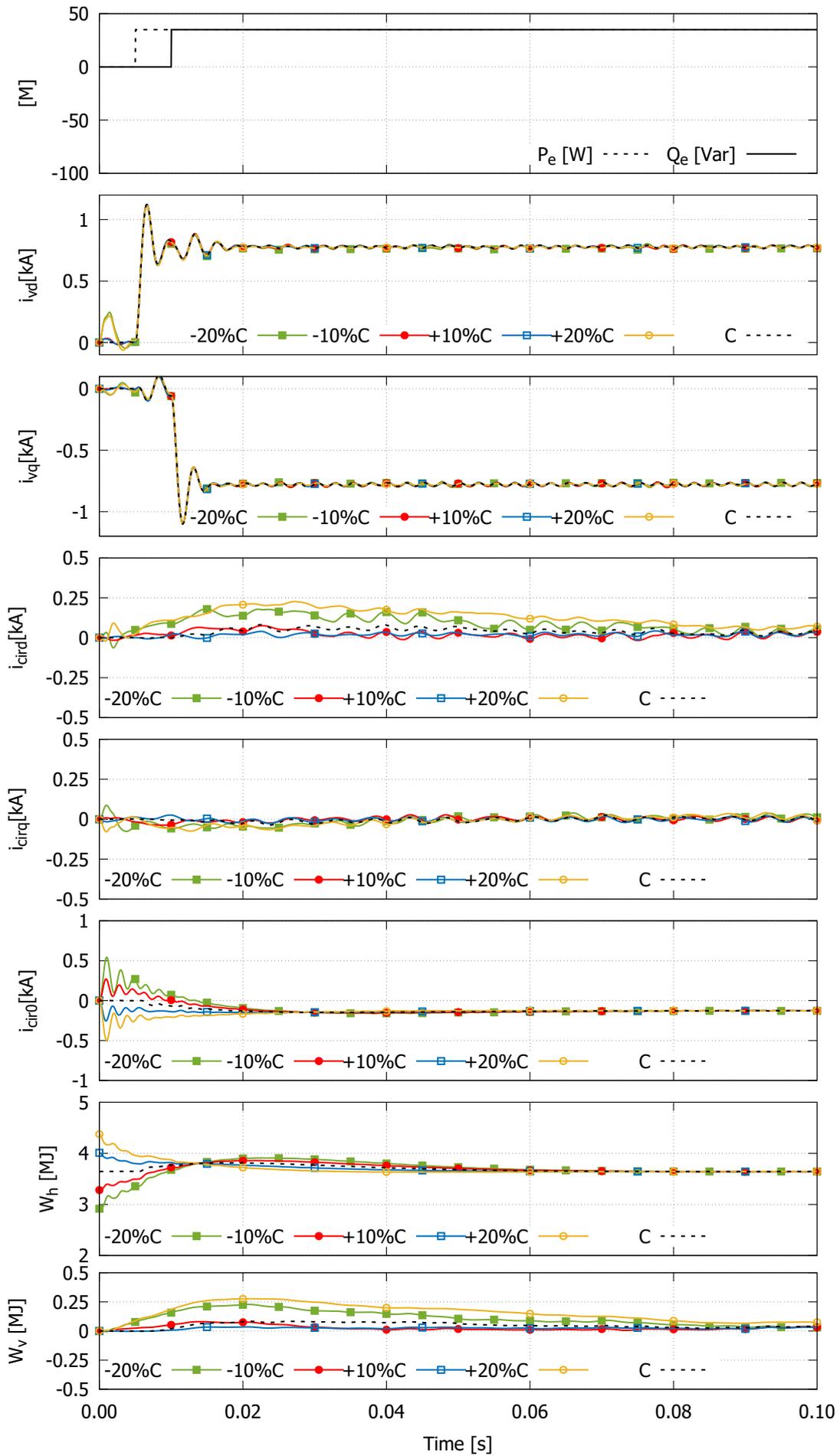


Figure 3.31: The system state over variation of parameter C of medium-voltage system with PI controller.
 Source: Author

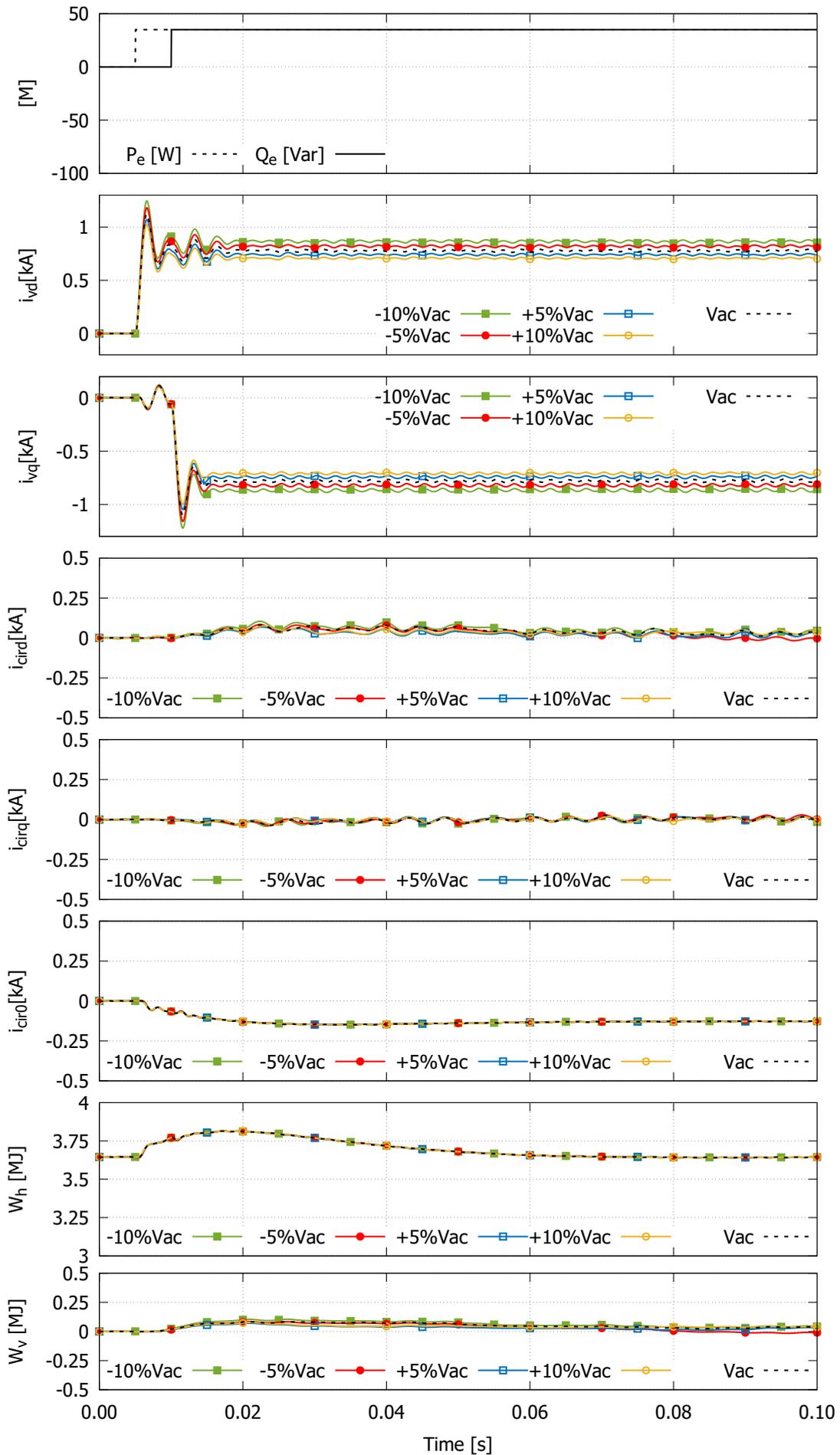


Figure 3.32: The system state over variation in the voltage at the PCC of medium-voltage system with PI controller.

Source: Author

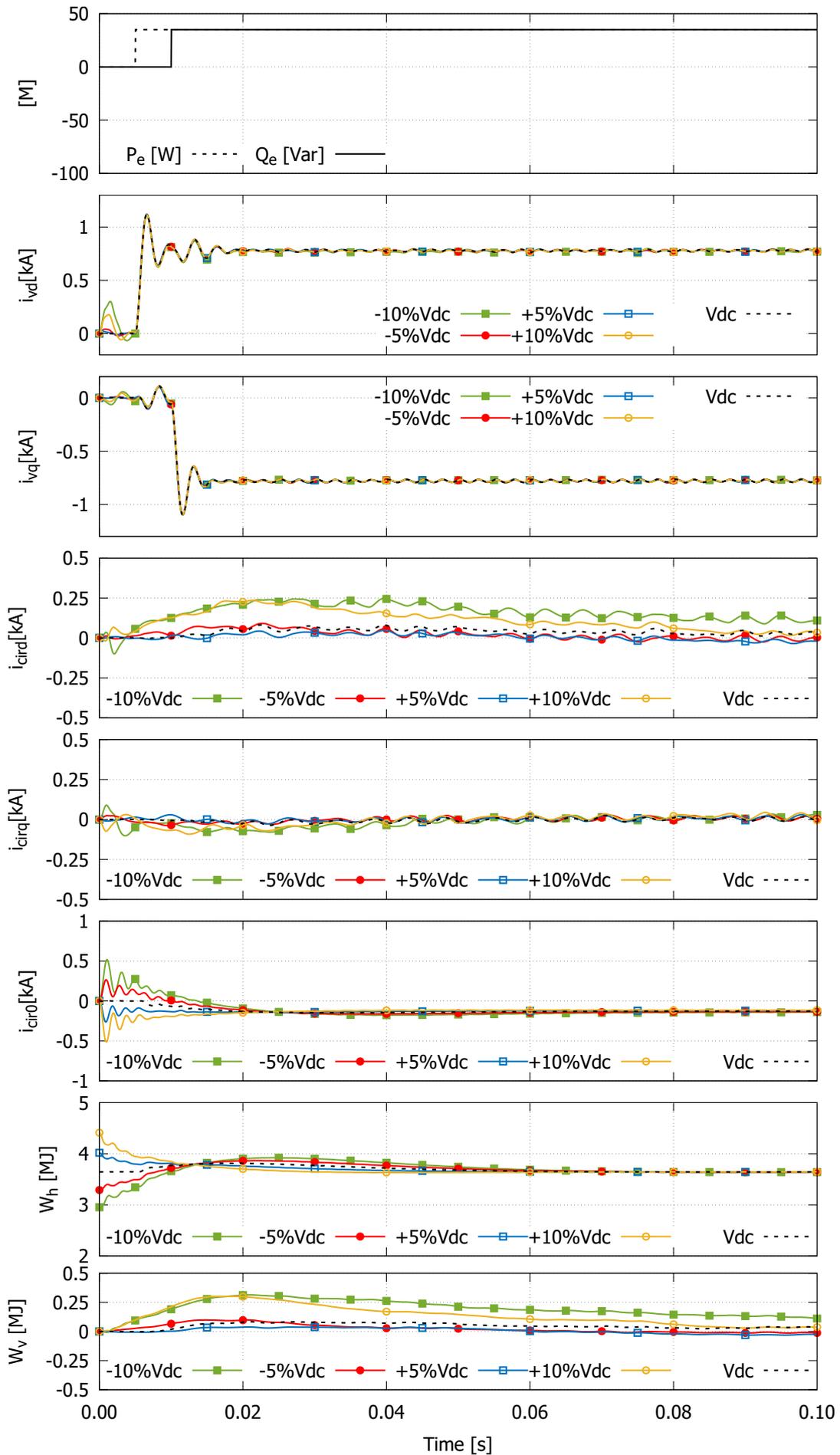


Figure 3.33: The system state over variation in DC voltage of medium-voltage system with PI controller.

Source: Author

3.5 High-voltage system test with PI controller

A high-voltage system is also analysed, aiming to verify controllers' characteristics concerning these systems. In figure 3.34 a 450 MVA HVDC connection is shown. The main AC grid is connected to symmetric monopole DC line/cable, by an AC-DC MMC converter.

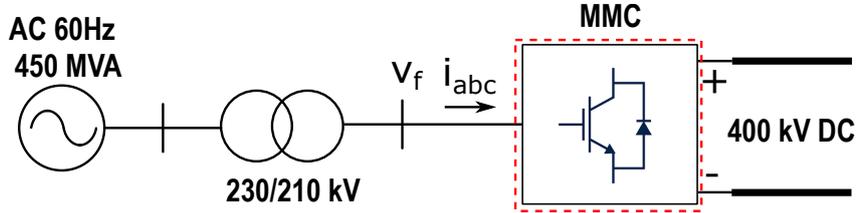


Figure 3.34: System diagram of 400 kV system.

Source: Author

A detailed switching model of the three-phase MMC converter with twenty SMs per arm, with the PI controller proposed in this chapter, is tested using the Matlab Simscape Electrical environment. The system test is originally proposed in [87]. The pulse generator used is a phase-shift PWM with a sorting algorithm, and system's parameters are presented in Table 3.2.

For the tuning process, the gains for state variables i_{vdq} and $i_{cir dq}$ are obtained such as to have the same time constant of medium-voltage system. $k_p^{W_h}$ becomes smaller because the response with (-0.5) has a high overshoot, and $k_i^{W_v}$ becomes larger once the previous gain (0.1) presents steady state error for state W_v .

Table 3.2: Parameters of simulated high-voltage system and PI controller gains.

Parameter	Value	Parameter	Value
S_{MMC}	450 MVA	$k_p^{i_{vdq}}$	120
V_{DC}	400 kV	$k_i^{i_{vdq}}$	37453
V_{AC}	210 kV	$k_p^{i_{cir dq}}$	80
C_{SM}	3 mF	$k_i^{i_{cir dq}}$	1000
L	40 mH	$k_p^{i_{cir 0}}$	300
L_c	12 mH	$k_i^{i_{cir 0}}$	1000
R_c	1 Ω	$k_p^{W_h}$	-0.3
R	0.5 Ω	$k_i^{W_h}$	-25
N	20	$k_p^{W_v}$	0.8
Freq	60 Hz	$k_i^{W_v}$	20

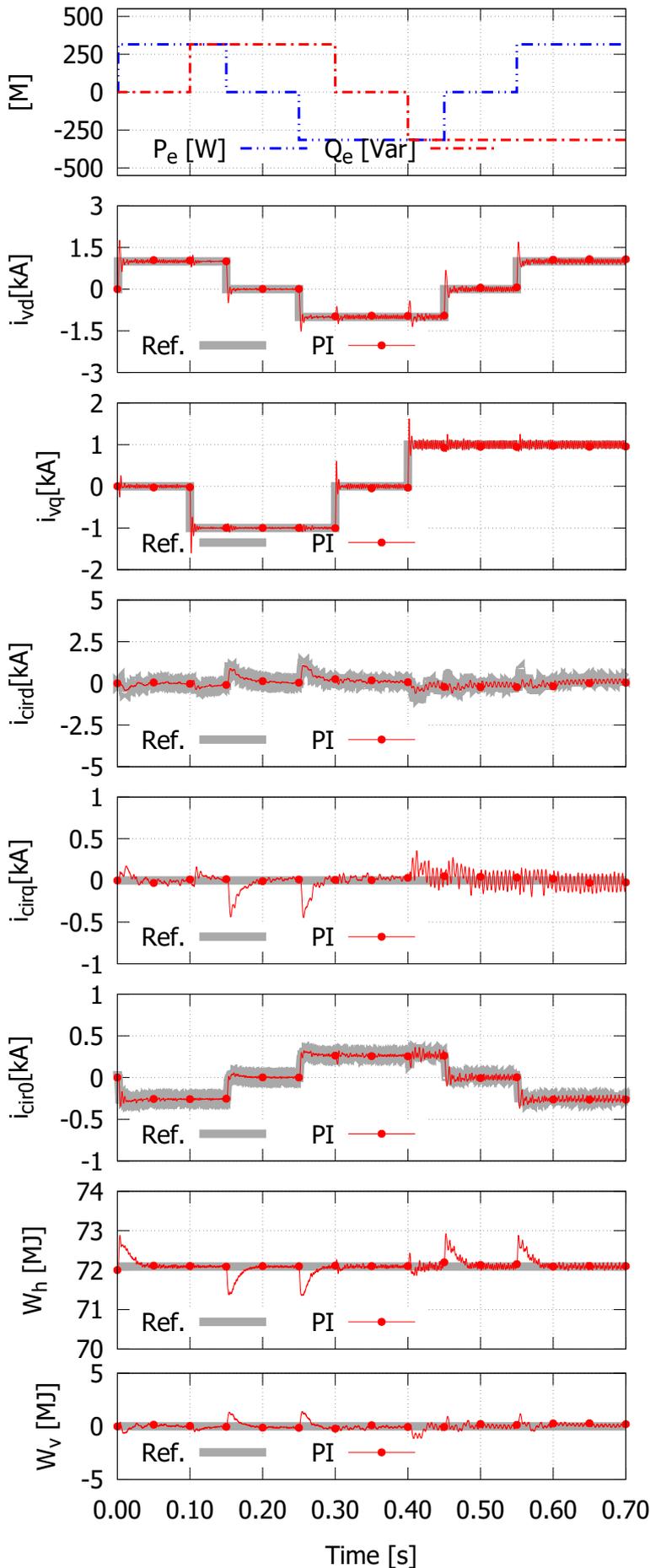
Figure 3.35 presents the four-quadrants operation for the high-voltage system with PI controller. A set of steps in active and reactive power is reproduced in the 1st graphic. Previous section uses 70 % of active and reactive power for this test. Here this operation condition will be maintained, which for this system implies the limits of $P_e = \pm 315 MW$ and $Q_e = \pm 315 MVar$. It means, the voltage is ten times bigger than medium-voltage system.

This test presents larger overshoot and oscillation when compared with the medium-voltage system. Furthermore, the author would like to highlight that the process of tuning was harder than for the medium-voltage system, and it was not possible to define a set of gains in which all operating points performed well. As a result, for the five first operating point (until 0.40 s), all states variables present a smooth response. On the other hand, when the power flow has changed its

direction (for the following three operating points), state variables present large oscillations.

The performance variation concerning operating points for PI controllers is as expected. An important feature to be addressed is the fact that the PI may need to re-adjust the control gains and parameters to keep following a new grid reference and to correctly perform stability, while controllers based on nonlinear theory gains can work in a broader region and consequently need less tuning.

Figure 3.35: Four-quadrants operation of high-voltage system with proposed PI controller.



Four-quadrants operation of high-voltage system with PI controller. State variables i_{vdq} (2nd and 3rd graphics) track all the new references in less than 10 *ms* and present a small overshoot. State variable i_{cird} follows well its reference.

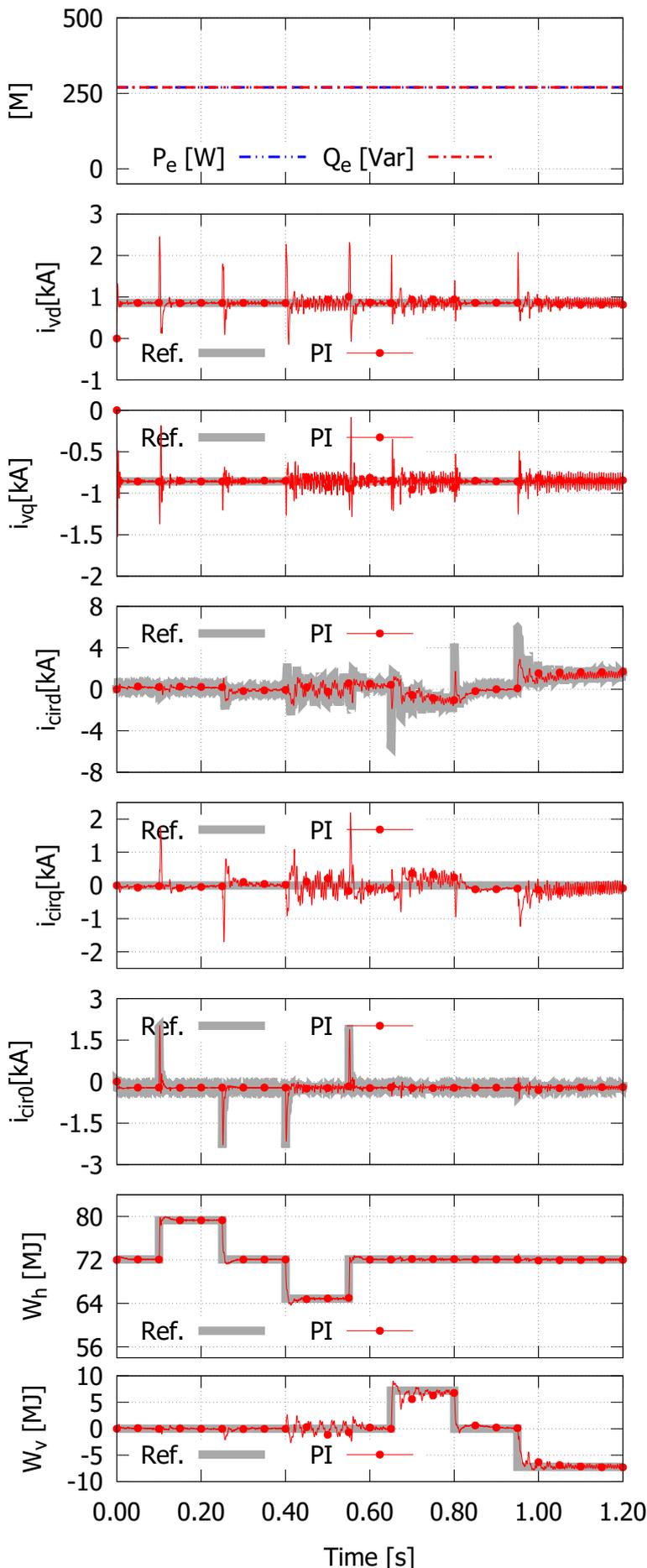
At 4th graphic the state variable i_{cirq} performs different operating points. As mentioned above, it is possible to see two different behaviours: first smooth, and then noisily response, what points out the need for a tuning improvement.

The i_{cird} tracks well its reference, related with active power changes. Meanwhile, total energy and energy balance face transients for each P_e step.

Even though the controller deal with oscillation response for the operating point after $t = 0.40$ s, PI can drives all state variables to their desired value (Ref.).

Figure 3.37 shows the control effort for this test. Steps in active and reactive power produce a proportional control effort. This will be further discussed in this section.

Figure 3.36: Energy steps for high-voltage system with proposed PI controller.



Energy changes of high-voltage system with PI controller. In figure 3.36, steps in total energy of $\pm 10\%$ are defined at 0.10 s and 0.40 s. During the total energy increase (from 0.10 s to 0.25 s) most state variables present overshoots, however they also present a high speed of convergence to re-track their references. Otherwise for the total energy decrease, state variables have an oscillating response.

During the imbalances of W_v (overloading upper/lower arms), PI controller can drive states to their new reference value.

Figure 3.38 shows the control effort resulting from this test. Changes in the total energy and energy balancing are distributed among control inputs. Furthermore v_{d0} participates most on the changes of total energy than those of energy balancing. This is a direct result of the energy model in equation (2.32) and equation (2.33).

Additionally from figure 3.37, the effort linked with each change in active

power is distributed among inputs, most for v_{ud} and v_{ld} (e.g. 0.15 s). Likewise, change on reactive power result in a more pronounced overshoot at v_{uq} and v_{lq} (e.g. 0.10 s). Also, v_{d0} react for each i_{cir0} change, which is linked with active power changes. These behaviors is result of the model, respectively described in equation (2.30) and equation (2.31).

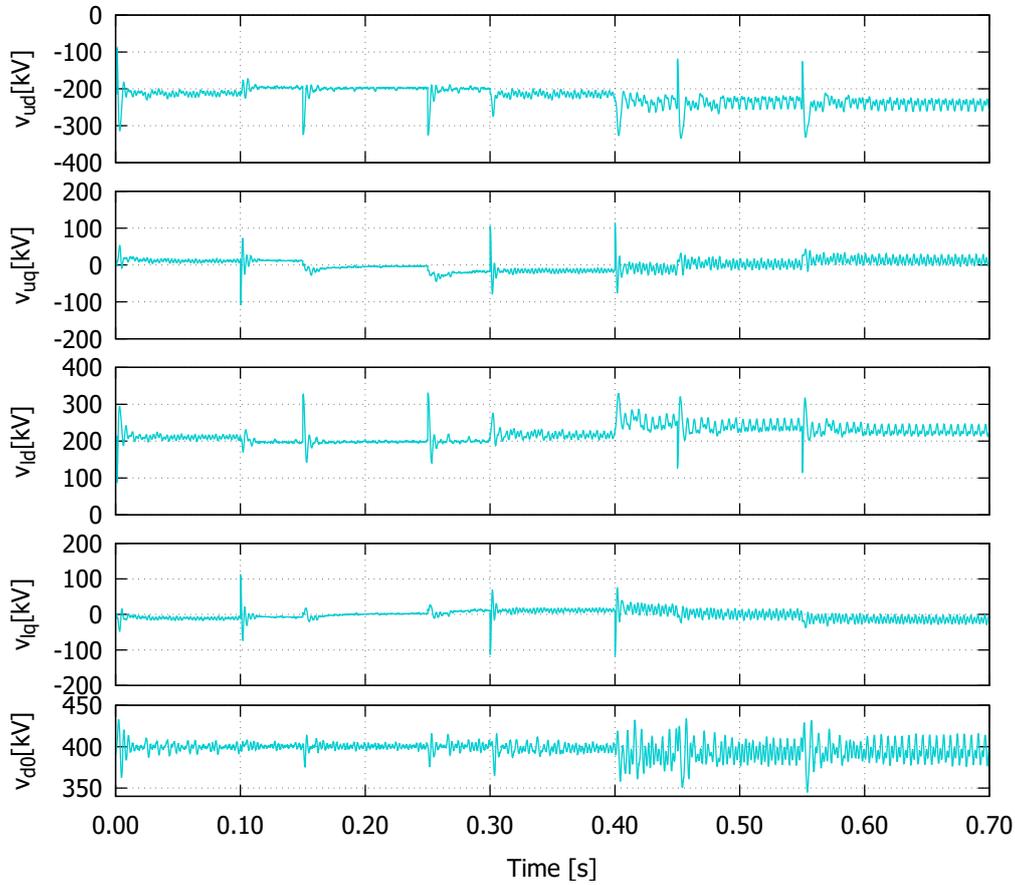


Figure 3.37: Control effort of four-quadrant operation of PI controller.

Source: Author

There are compromises to be considered while choosing an MMC model. Some of them are directly related to internal dynamics. The model used in this research considers the control of the energy summation at all upper arms to be equal to lower arms energy summation, which is called energy balancing W_v . However, an ideal balancing condition is to have the energy balanced individually per arm. So, figure 3.39 demonstrates how energy performed per arm. For this test, the operating point was set as $P_e = 315 MW$ and $Q_e = 315 MVar$ at 0.05 s. There it is possible to see the share of energy in the arms. After the transient caused by power injection, arms are well balanced in 450 ms. Furthermore total energy in upper (lower) arms are presented in figure 3.40. The summation of energy in upper (lower) arms (W_u and W_l) is controlled on the desired value and are balanced just after the transient caused by the power injection.

For the same operation point, double-fundamental frequency components of circulating currents are presented in figure 3.41. It is possible to verify that during the transient the three components present large oscillations, however, they become small and close to zero for components dq ($i_{cir dq}^{2w}$) and around reference of the fundamental for zero component (i_{cir0}^{2w}).

At last, figure 3.42 shows SMs capacitors voltages per arm, in the left graphics and a detail at right graphics (zoom on time from right graphics). It is verified that voltages are well balanced by the implemented sorting algorithm.

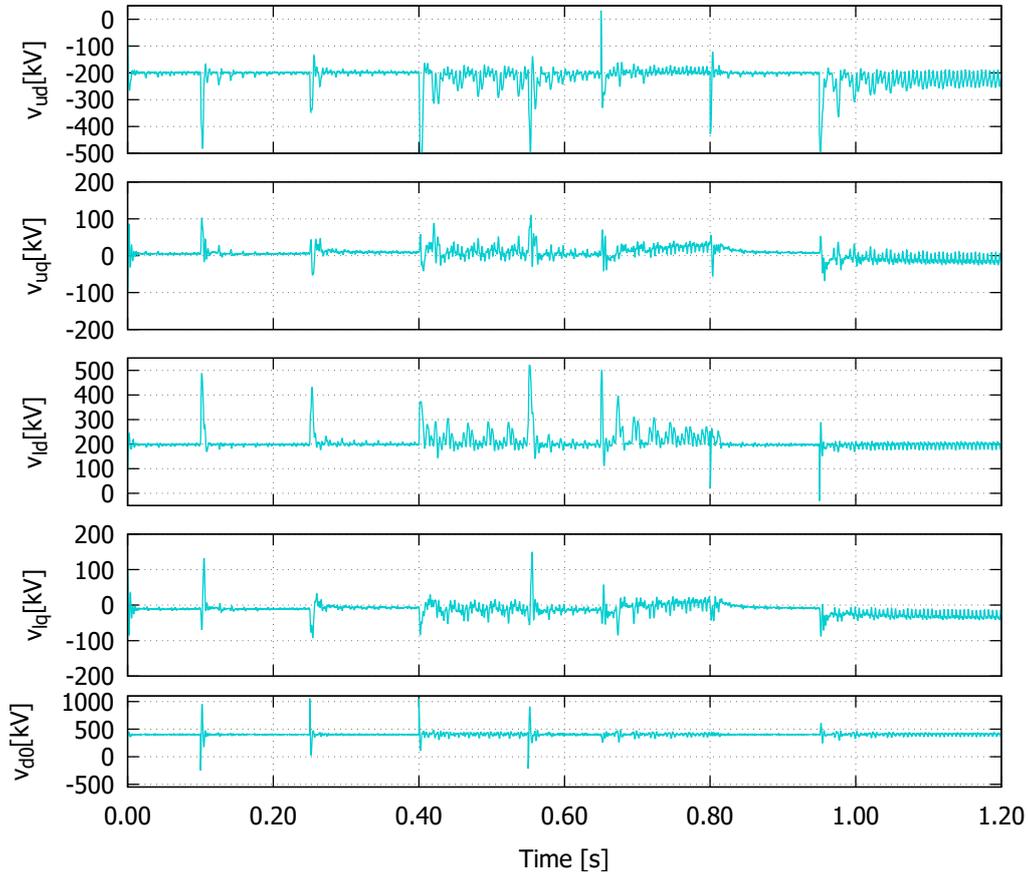


Figure 3.38: Control effort of changes in energy of PI controller.

Source: Author

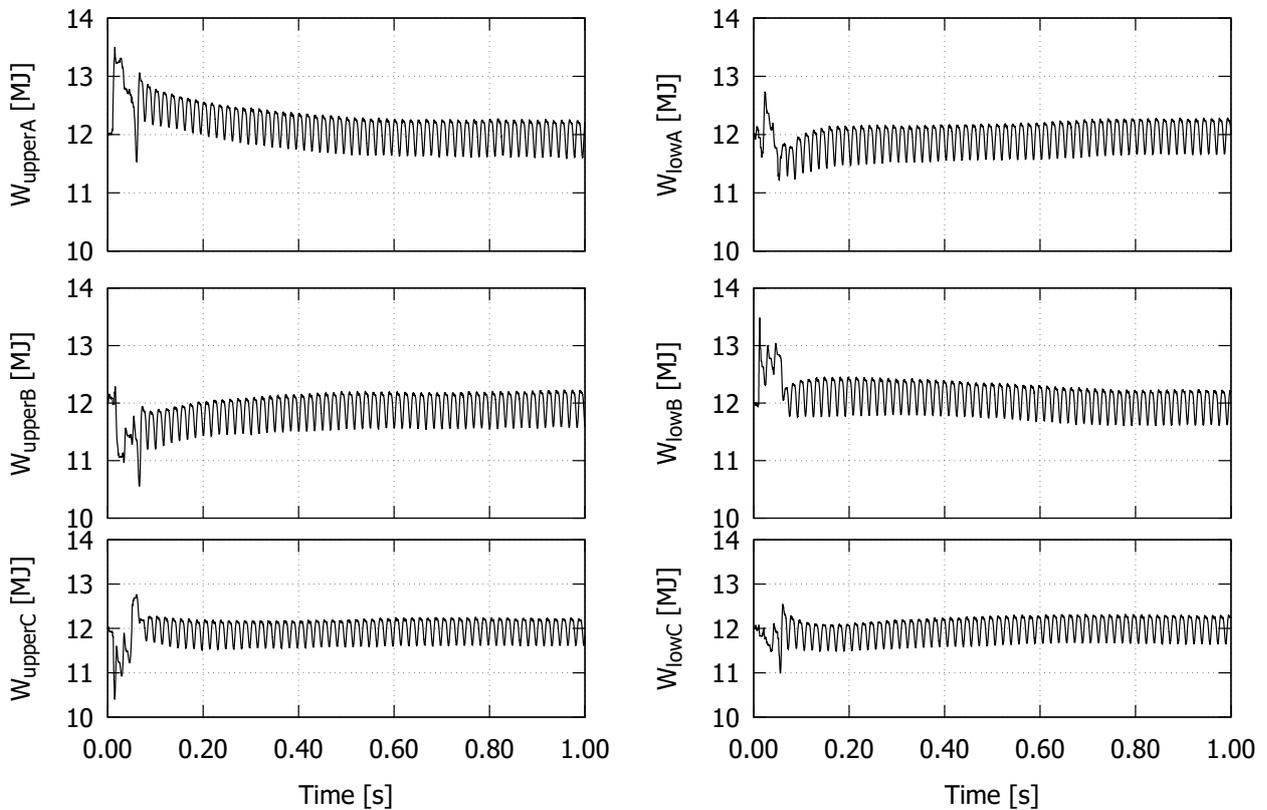


Figure 3.39: Share of energy among arms with PI controller.

Source: Author

3.5.1 Robustness over parameters' uncertainties and voltage fluctuation on high-voltage system with PI controller

Robustness The test presented in section 3.4.2 is performed here, considering the high-voltage system.

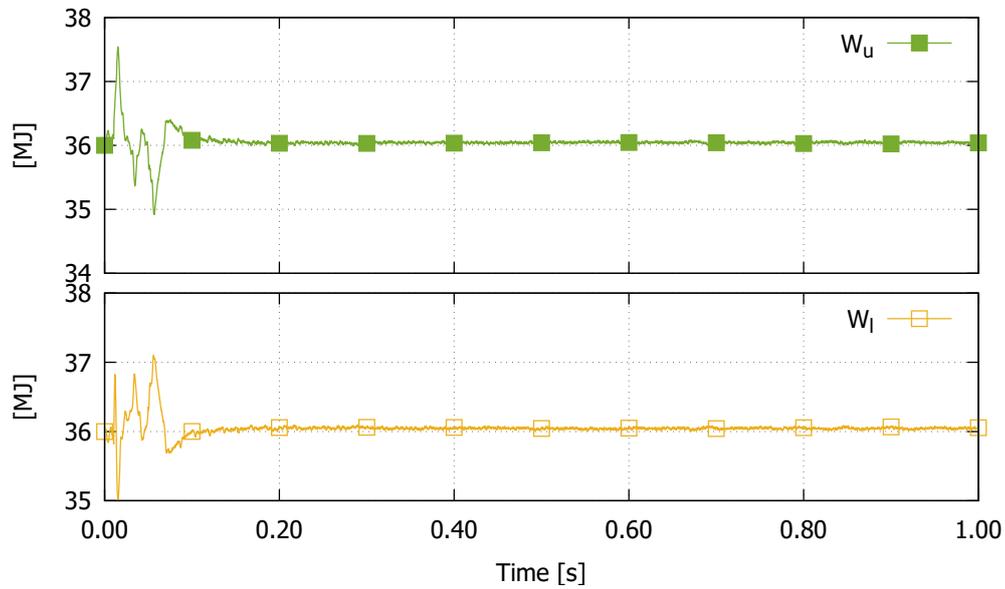


Figure 3.40: Total energy in the three upper arms (W_u) and the three lower arms (W_l) with PI controller.

Source: Author

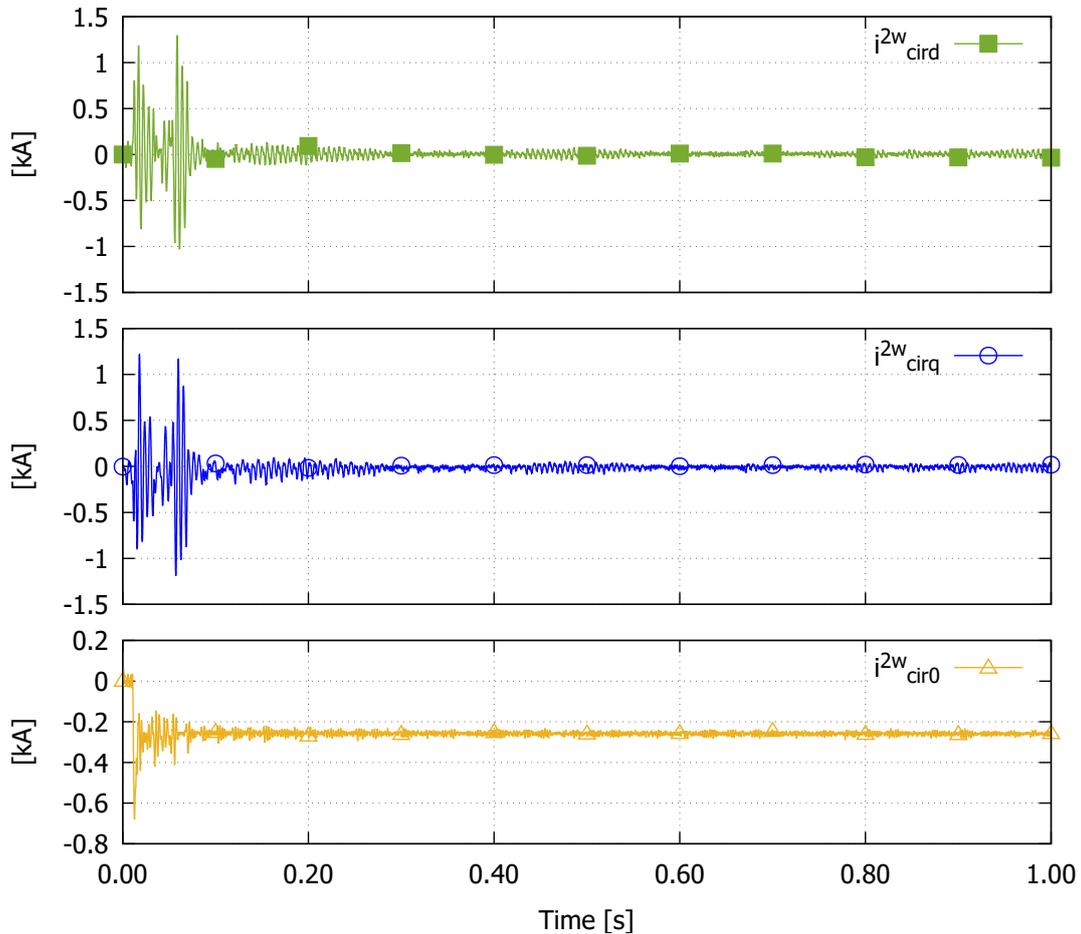


Figure 3.41: Double-fundamental frequency component of circulating currents at high-voltage switching model with PI controller.

Source: Author

The R , L , R_c and L_c parameters' uncertainties are kept as $\pm 10\%$ and $\pm 20\%$ from the nominal values, however changes in SM capacitors is reduced to $\pm 10\%$ and $\pm 5\%$. The reduction is proposed here, once state variables' response becomes oscillatory during the transient, prejudicing the analyses.

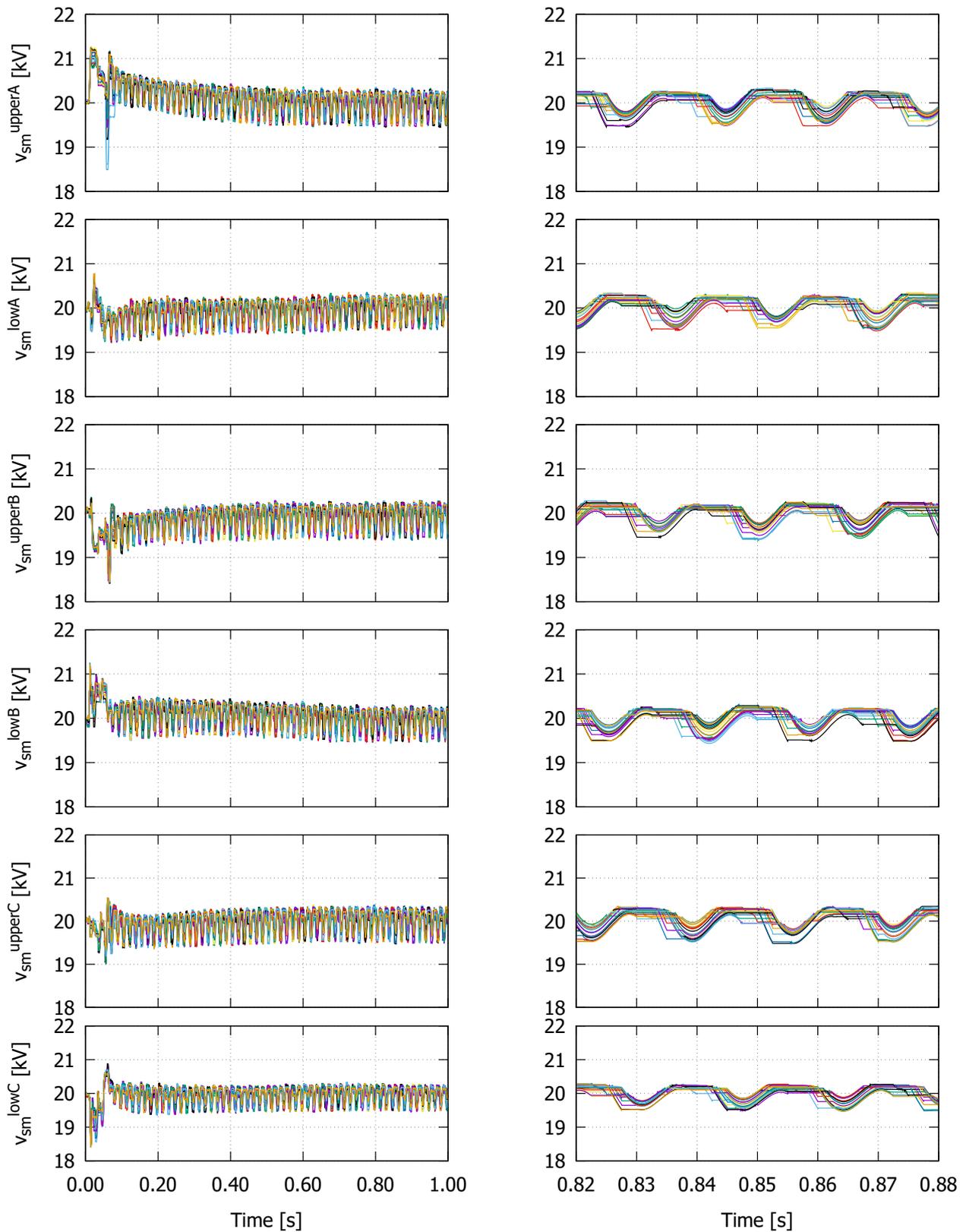


Figure 3.42: SMs capacitor voltage per arm and equivalent detail from PI controller.
Source: Author

Variations of $\pm 10\%$ and $\pm 20\%$ in arm resistance (R) is proposed and state variables response presented in figure 3.43. This test shows that the PI controller can drive all state variables to the desired value, even with the arm resistance error.

In figure 3.44, there are state variables over variation in R_c . As in the medium-voltage system, PI drive state to their reference. However, in this test, variables $i_{cir d}$ present a small deviation, but it can be neglected.

Figure 3.45 there is a response for changes in arm inductance L . As the

medium-voltage, there are light deviations for state $i_{cir d}$ and W_v . They can be neglected once they are too small. PI well controls the other state variables.

Changes in L_c are well performed by the PI controller. This case differs from medium-voltage, where $i_{cir d}$ and W_v present deviation from the desired value in transients.

Finally, for the changes in SMs capacitor, the state variables response has a larger overshoot in comparison with medium-voltage, as shown in figure 3.47. The states are most affected by the increase of $+10\%C$, when, even in steady-state, they present oscillatory response for most state variables.

Voltage fluctuation Voltage fluctuations are performed at the PCC. It is tested $\pm 10\%V_{ac}$ and $\pm 5\%V_{ac}$, and figure 3.48 shows the result. State variables i_{vd} and i_{vq} present over-signal and oscillatory response for the increase in V_{ac} . On the other hand, the decrease in V_{ac} result in a response just with over-signal.

State variables $i_{cir dq0}$ has a oscillatory response during transient however track the reference in steady-state. At last, W_v is light affected.

State variables response over changes in V_{dc} are presented in figure 3.49. System states deal with over-shoot during transients, and PI drive states to their references in steady-state. However for the increase of $+10\%V_{dc}$, state variables $i_{cir dq0}$ and W_v has a large oscillatory response which may affect MMC operation.

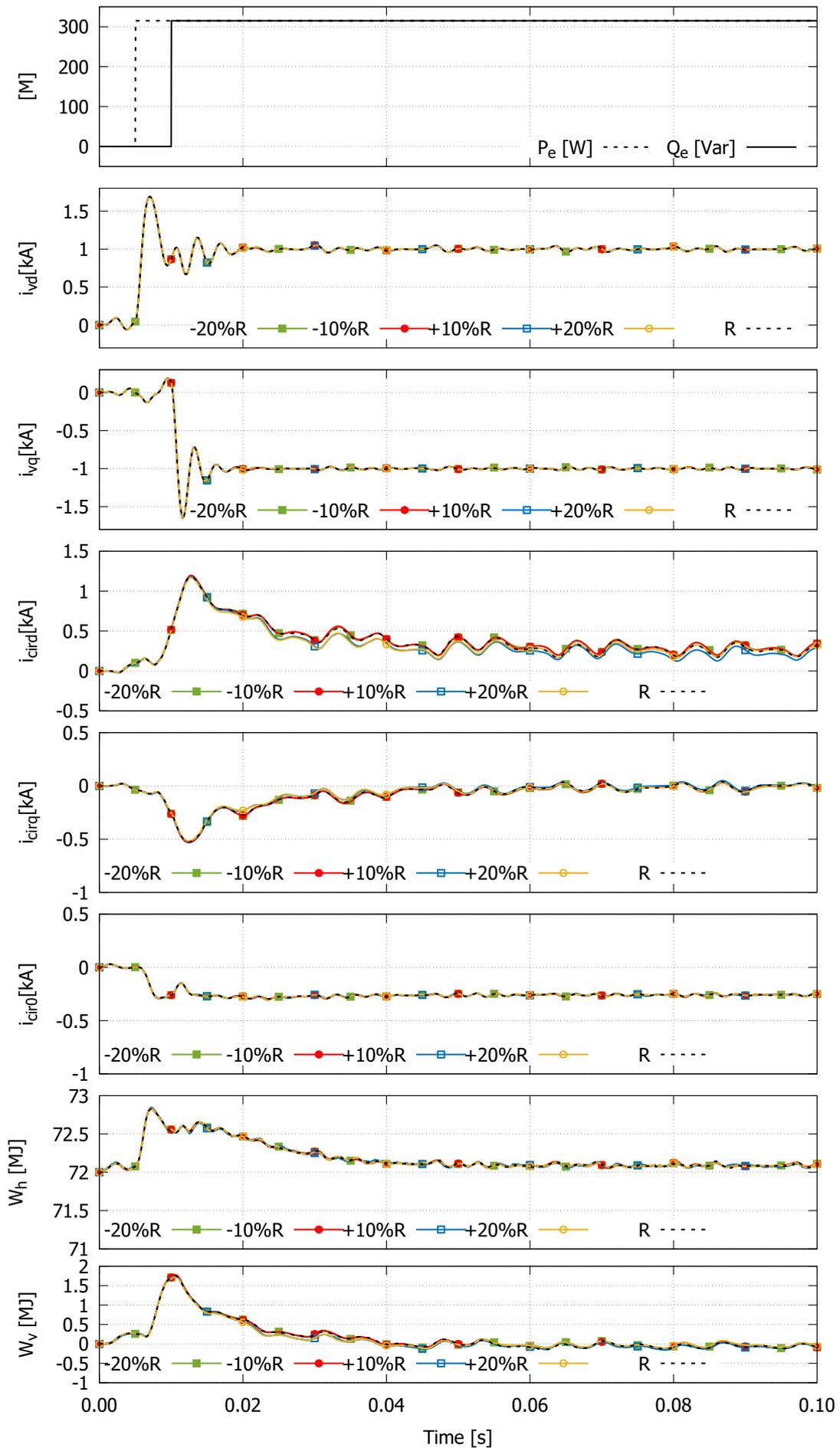


Figure 3.43: The system state over variation of parameter R of high-voltage system with PI controller.

Source: Author

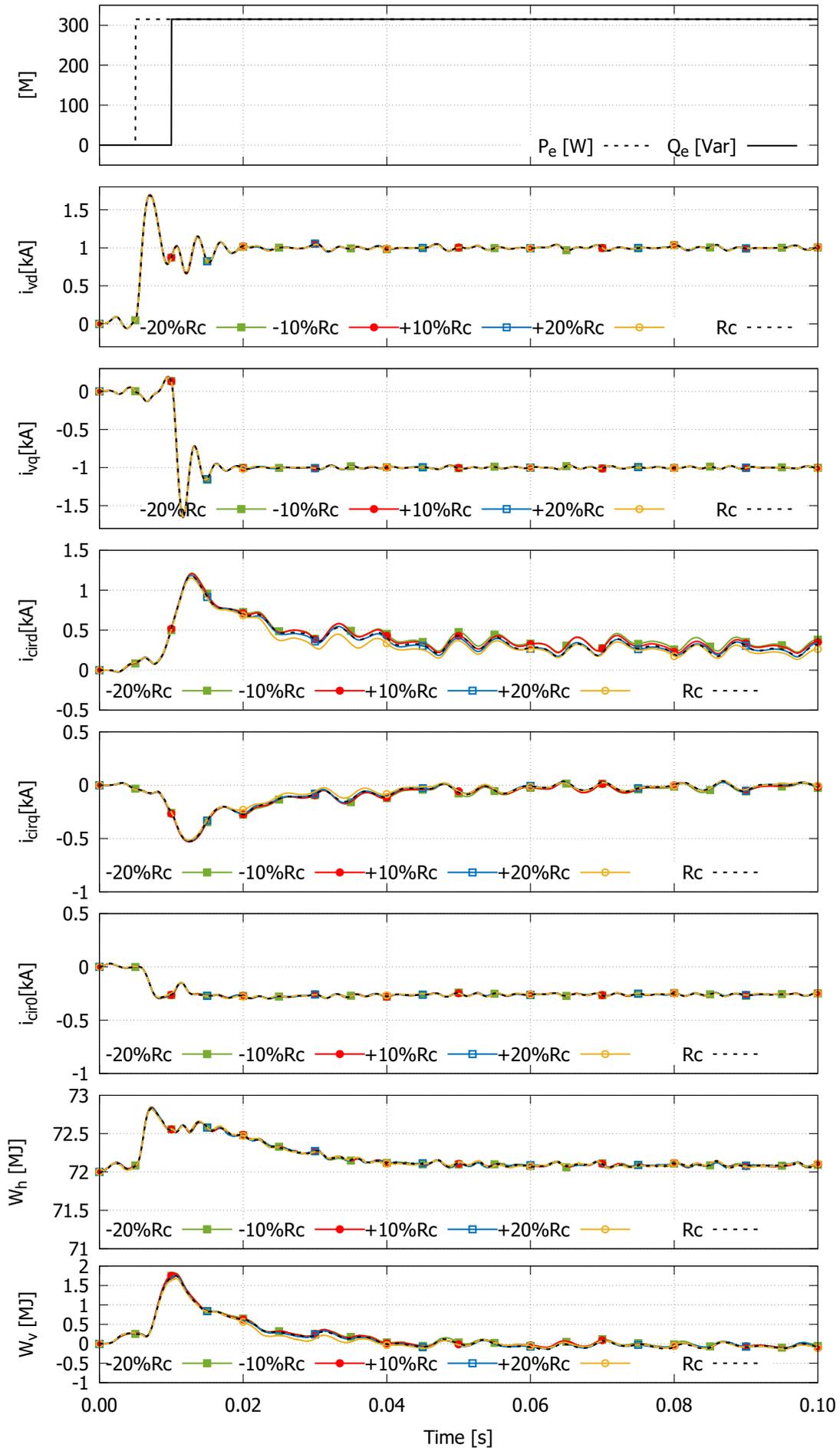


Figure 3.44: The system state over variation of parameter R_c of high-voltage system with PI controller.

Source: Author

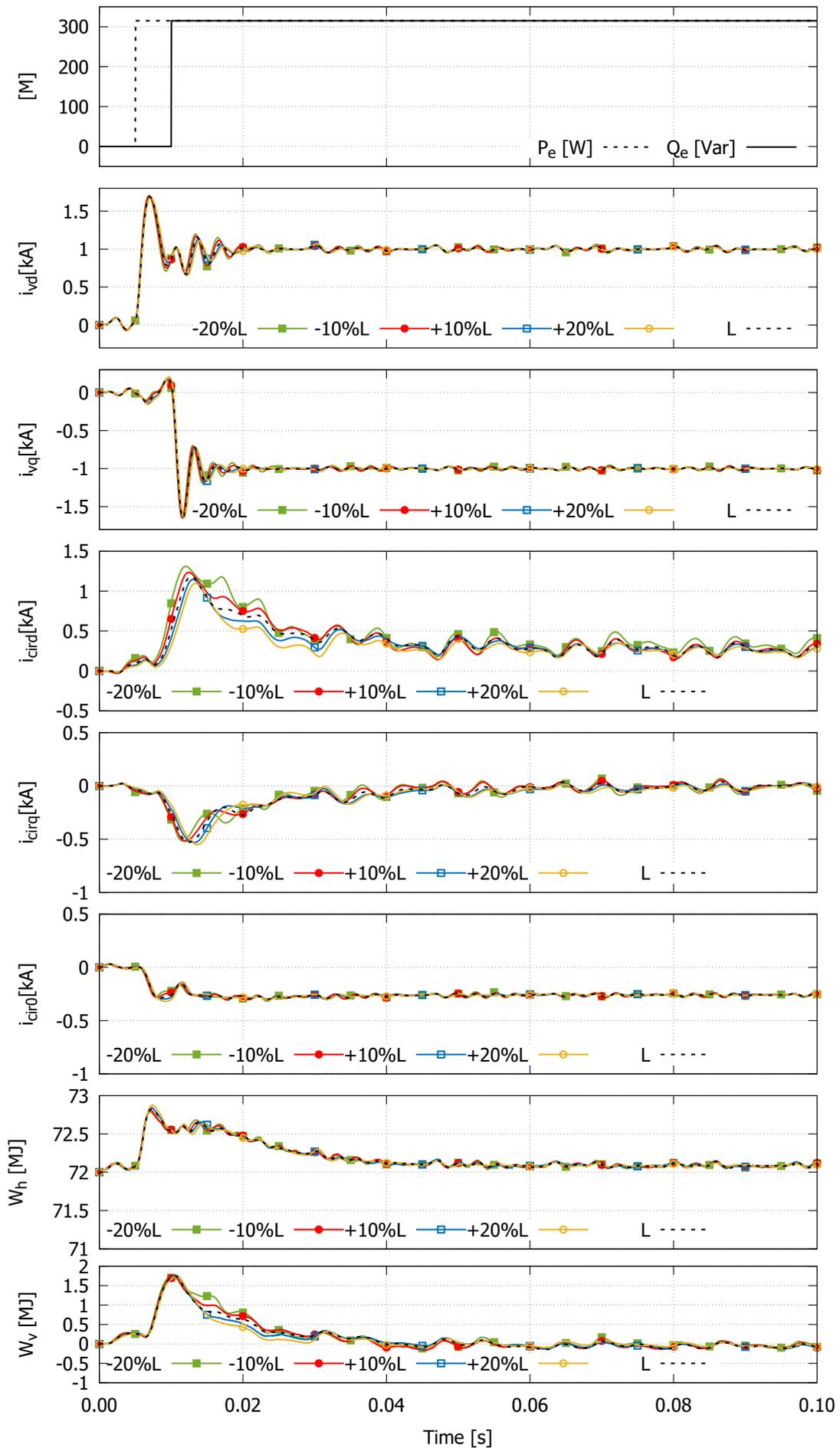


Figure 3.45: The system state over variation of parameter L of high-voltage system with PI controller.

Source: Author

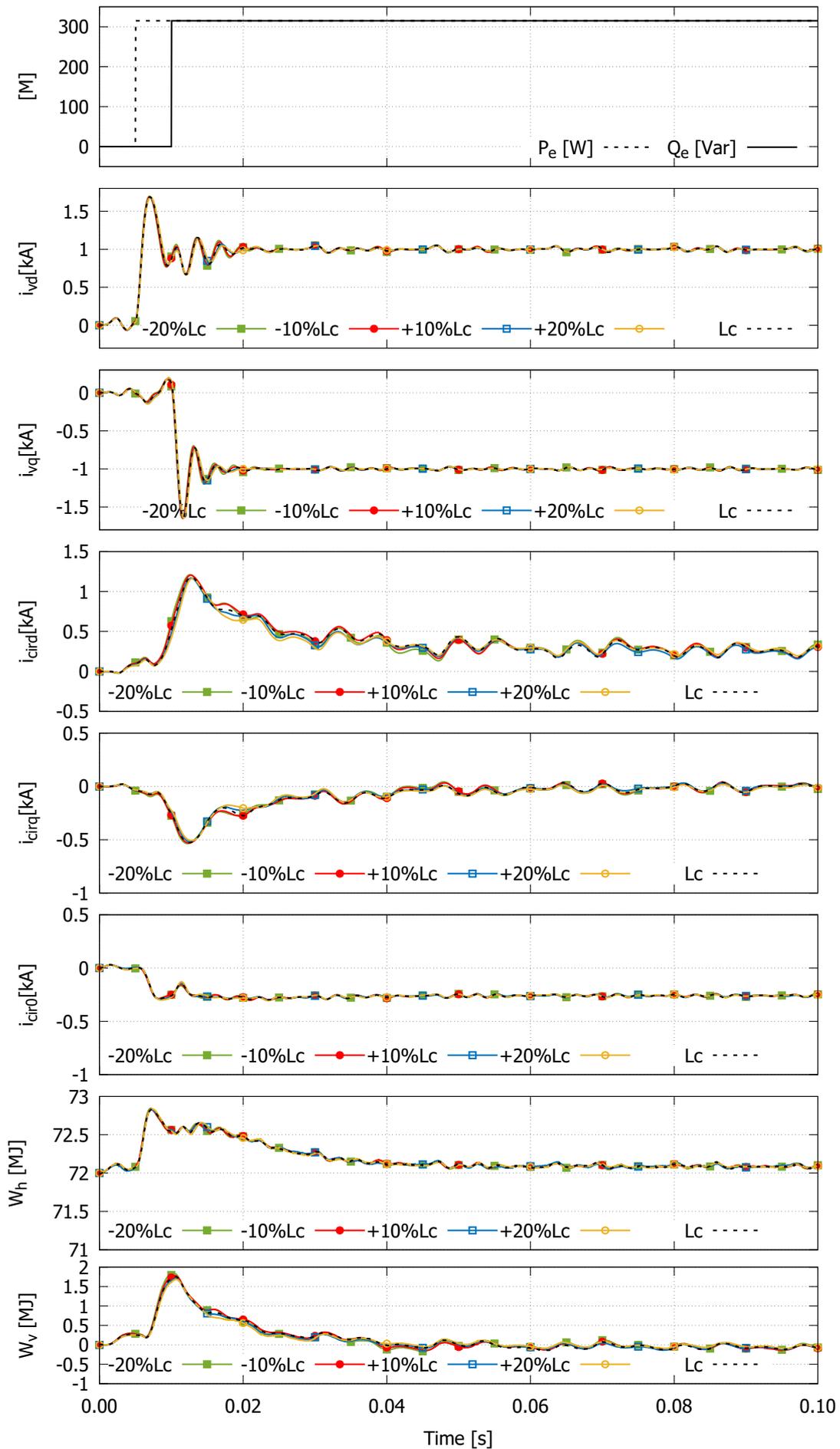


Figure 3.46: The system state over variation of parameter L_c of high-voltage system with PI controller.

Source: Author

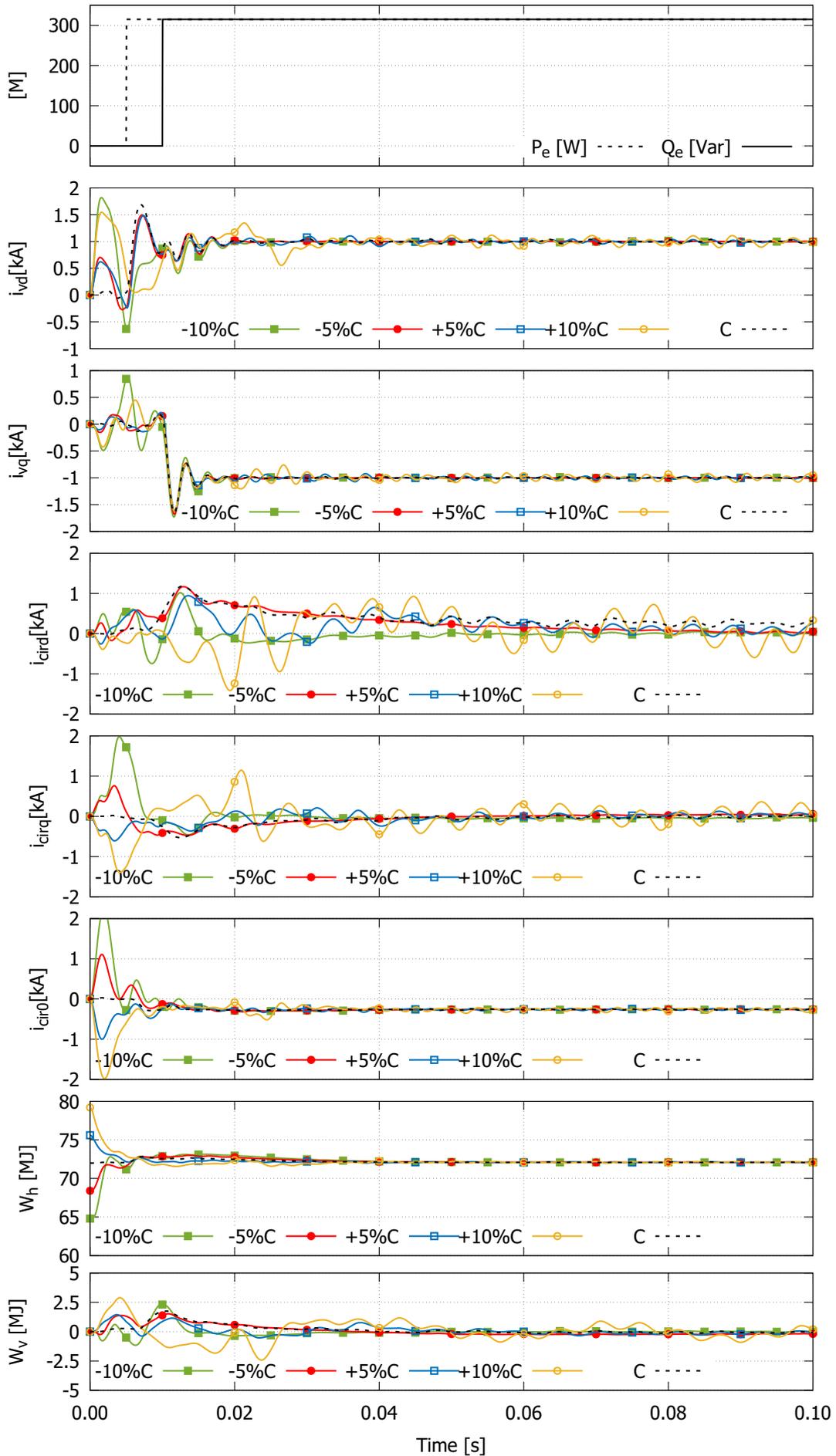


Figure 3.47: The system state over variation of parameter C of high-voltage system with PI controller.

Source: Author

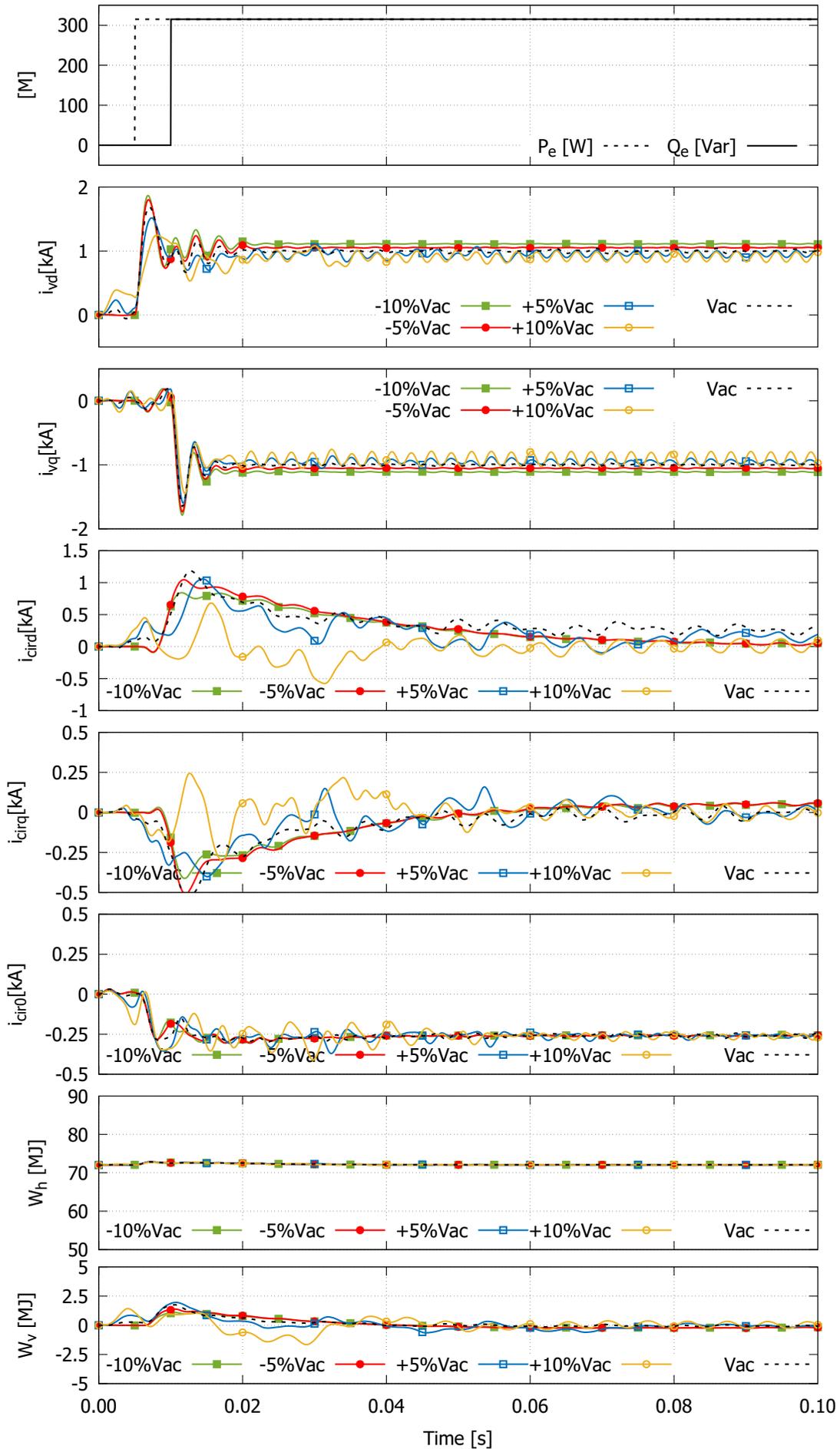


Figure 3.48: The system state over variation in the voltage at the PCC of high-voltage system with PI controller.

Source: Author

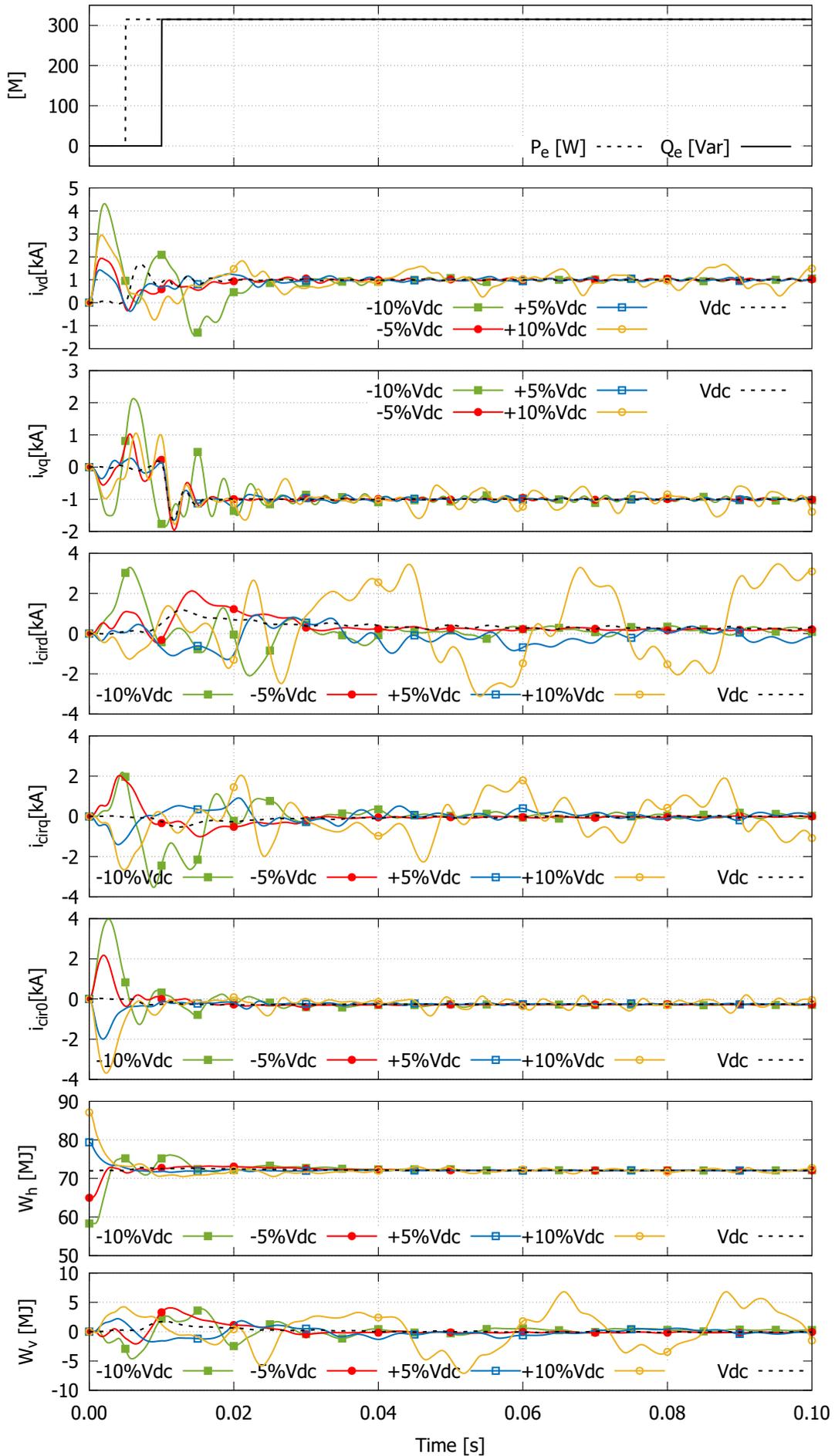


Figure 3.49: The system state over variation in DC voltage of high-voltage system with PI controller.

Source: Author

3.6 Chapter conclusion

This chapter presented the design of the PI controller, adapted from [25]. This chapter defines the state desired values and control inputs references. In addition, there is a description of the tuning procedure.

An average and a switching MMC models in medium-voltage with the PI controller. They present suitable performance for a set of operating points and energy steps, where states have a high speed of convergence and light overshoots. The tests also show the associated control efforts. Average and switching models present equivalent performance which allows the use of the average model if a more simple model is required.

It is essential to highlight that the PI controller's gains were set to have the same responses for the average-model and switching-model aiming to have suitable performance in both models and fair comparison. However, the controller gains adjust may improve the response on the state variables $i_{cir d}$ and W_v from the switching-model.

Although both models present similar performance, the focus will be on the switching model when analyzing the internal dynamics.

Additionally, a high-voltage model is simulated with the PI controller, with a set of operating points and energy steps. Concerning internal dynamics, PI accomplish the balancing between submodule capacitors' voltage and the balancing between W_u and W_l .

The robustness over parameter uncertainties shows that the PI controller can drive state variables even for changes of $\pm 20\%$ in R , R_c , L , and L_c . Additionally, uncertainties in the SMs capacitor are harmful to the state variables, especially for the high-voltage system.

Voltage fluctuation of V_{ac} and V_{dc} has a moderate effect over the medium-voltage system, however more harmfully for the high-voltage system. The desired value for the zero component of the circulating current (\bar{i}_{cir0}) comes from the equilibrium point at steady-state of equation (2.18), where ($\dot{\bar{x}} = 0$). In (2.18) replacing (3.19) and (3.21) and collecting terms to obtain (3.24).

Chapter 4

Nonlinear control

This chapter presents the nonlinear control design with formal stability proof for an MMC, which is critical for interaction between AC and DC grids. Lyapunov theory is used to develop the proposed controller, which is based on Backstepping and Feedback Linearization techniques, and to perform the stability analysis. The proposed controller allows to asymptotically stabilize the MMC system. The proposed algorithm allows to manage the converter in a wide range of operation points, by means of arbitrary tuning assignment. Robustness and performances of proposed control are verified by means of Matlab Simscape Electrical simulations, including active and reactive power reference variations and grid imbalance conditions. A detailed MMC switching model, of $450MVA$ is considered on Matlab validation. A phase-shift PWM is considered with a sorting algorithm. In addition, MMC's internal energy is also controlled, what can contribute to help in the high-speed frequency control by using of this energy for synthetic inertia.

In this chapter, the control design is firstly presented, followed by the main mathematical results. Then, the control is implemented on a switched model. The performance over power flow changes, energy unbalance conditions, robustness over parameter uncertainties, and robustness over DC and AC voltage fluctuation are analyzed. Management of circulating current and the voltage balancing are shown on abc referential. To conclude, the tuning procedure and control effort are discussed.

4.1 Nonlinear controller in the context of MMC

Most of the existing results on the control strategy for MMCs consist of linear controllers, as vector control (nested Proportional Integral - PI - controllers), with stability not defined. This because only one point of operation is considered in its design, and because the system's nonlinearities are disregarded [28, 29, 30].

In this point of view, one may cite works as [31], where the nonlinear MMC model is first linearized, and then linear controllers are designed for it. In a different way, [27] proposes a discrete-time bilinear model of an MMC, controlled by a sum-of-squares decomposition method, following a nonlinear analysis. These studies are motivated by the relevance of designing nonlinear controllers that can assure stability throughout large electrical grid operation regions, including rigorous stability analysis [32, 33].

This chapter presents a nonlinear controller for a MMC based on Lyapunov theory. The resulting nonlinear scheme is independent of the operation point since it uses the full nonlinear model. The controller compensates several nonlinear components and imposes desired closed loop dynamics. For this reason, there is a decoupling on resulting closed loop system, and tuning becomes effortless, be-

cause its parameters represent these desired dynamics. The proposed controller is also robust, what can be seen by the fact that it was developed using the averaged model but simulations were carried out using a more complex switched model. Finally, the fact that the system is underactuated is clearly exploited such that the controller steers the actuated states, that are on their turn used to drive the underactuated states to desired values. This backstepping procedure creates a clear structure on which states are driven by individual control inputs or other states. The resulting closed loop system can then provide fast ancillary services (sub second) that will be capital for future power grids, like fast frequency response and synthetic inertia, for a wide range of operation points.

4.2 Mathematical model - Recalling main definitions

Here again we consider the circuit shown in figure (2.10) with the average model of the MMC in the $dq0$ reference frame presented by system (2.35).

The system states are the AC currents in the d and q axis ($i_{v,d}$ $i_{v,q}$), circulating currents in the d , q and 0 axis ($i_{cir,d}$ $i_{cir,q}$ $i_{cir,0}$), total energy (W_h) and energy balancing (W_v) and are summarised as

$$x = [i_{v,d} \ i_{v,q} \ i_{cir,d} \ i_{cir,q} \ i_{cir,0} \ W_h \ W_v]$$

The controller inputs are the equivalent voltage produced per arm. $v_{u,d}$ is the direct component of equivalent voltage of the upper arm, $v_{u,q}$ is the quadrature component of equivalent voltage of the upper arm, $v_{l,d}$ is the direct component of equivalent voltage of the lower arm, $v_{l,q}$ is the quadrature component of equivalent voltage of the lower arm, and v_{d0} is the zero component of equivalent voltage in upper an lower arm. In $dq0$ reference that will be

$$u = [v_{u,d} \ v_{u,q} \ v_{l,d} \ v_{l,q} \ v_{d0}]$$

At the switching model, the controller inputs are the voltage waveforms to be sent to the modulation scheme. The modulation scheme is responsible for generating the gating signals to the SMs IGBTs to produce the desired output voltage at the converter terminals. In this chapter we use phase-shift PWM modulation.

4.3 Control Objective

The control objective is to stabilize the MMC system. In order to achieve this objective it is used a backstepping procedure where states $i_{v,dq}$ and $i_{cir,dq0}$ are directly controlled to steer states W_h and W_v . Therefore, an important characteristic of the MMC presented in the model above is that there are seven states and just five control inputs. So, the system is under-actuated with five actuated states and two free-dynamic states. In this chapter the actuated states were selected as $[i_{v,d} \ i_{v,q} \ i_{cir,d} \ i_{cir,q} \ i_{cir,0}]$ and therefore the behaviour of $[W_h \ W_v]$ are considered as free-dynamic states. To tackle this problem, it is used a combination of input-output feedback linearization and backstepping.

4.3.1 The Actuated States

Next, the error from a state $x_i \ \forall i \in \{1 \dots 7\}$ and its reference \bar{x}_i is represented by \tilde{x}_i , as shows (4.1):

$$\tilde{x}_i \triangleq x_i - \bar{x}_i \quad \forall i \in \{1 \dots 7\} \quad (4.1)$$

First, it is considered the control design for state $i_{v,d}$. So, it is proposed a first Lyapunov function (4.2):

$$V_{i_{v,d}} = \frac{1}{2}(i_{v,d} - \bar{i}_{v,d})^2 + \beta_{v,d}\xi_{v,d}^2 \quad (4.2)$$

with $\xi_{v,d}$ given by:

$$\dot{\xi}_{v,d} = \tilde{i}_{v,d}$$

Its time derivative is:

$$\begin{aligned} \dot{V}_{i_{v,d}} = \tilde{i}_{v,d} \cdot \left(-\frac{R_{eq}\tilde{i}_{v,d}}{L_{eq}} - \frac{R_{eq}\bar{i}_{v,d}}{L_{eq}} + \omega\tilde{i}_{v,q} + \omega\bar{i}_{v,q} + \frac{v_{u,d}}{L_{eq}} - \frac{v_{l,d}}{L_{eq}} + \frac{2v_{f,d}}{L_{eq}} \right) + \\ + \beta_{v,d}\xi_{v,d}\tilde{i}_{v,d} \end{aligned} \quad (4.3)$$

The time derivative of Lyapunov function must be smaller than zero to assure asymptotic stabilization for state $i_{v,d}$, the following equation is defined:

$$-\alpha_{i_{v,d}} \cdot \tilde{i}_{v,d} = -\frac{R_{eq}\tilde{i}_{v,d}}{L_{eq}} - \frac{R_{eq}\bar{i}_{v,d}}{L_{eq}} + \omega\tilde{i}_{v,q} + \omega\bar{i}_{v,q} + \frac{v_{u,d}}{L_{eq}} - \frac{v_{l,d}}{L_{eq}} + \frac{2v_{f,d}}{L_{eq}} + \beta_{v,d}\xi_{v,d} \quad (4.4)$$

with constants $\alpha_{i_{v,d}}, \beta_{i_{v,d}} \in \mathbb{R}_+^*$.

Collecting terms from (4.4), the following expression for $v_{u,d}$ is obtained in (4.5). The control input $v_{l,d}$, which was not designed yet, needs to be considered in a future step to finally establish the control law $v_{u,d}$.

$$\begin{aligned} v_{u,d} = R_{eq}\bar{i}_{v,d} + R_{eq}\tilde{i}_{v,d} - L_{eq}\omega\tilde{i}_{v,q} - L_{eq}\omega \cdot \bar{i}_{v,q} + \\ - 2v_{f,d} - L_{eq}\alpha_{i_{v,d}}\tilde{i}_{v,d} - L_{eq}\beta_{i_{v,d}}\xi_{v,d} + v_{l,d} \end{aligned} \quad (4.5)$$

Thus, a Lyapunov function for state $i_{cir,d}$ is proposed in (4.6), and its time derivative shown in (4.7).

$$V_{i_{cir,d}} = \frac{1}{2}(i_{cir,d} - \bar{i}_{cir,d})^2 \quad (4.6)$$

$$\dot{V}_{i_{cir,d}} = \tilde{i}_{cir,d} \left(-\frac{R_{eq}\tilde{i}_{cir,d}}{L} - \frac{R_{eq}\bar{i}_{cir,d}}{L} + \omega\tilde{i}_{cir,q} + \omega\bar{i}_{cir,q} - \frac{v_{u,d}}{2L} - \frac{v_{l,d}}{2L} \right) \quad (4.7)$$

In order to obtain a suitable Lyapunov function's derivative, one may define the control law $v_{l,d}$ as:

$$\begin{aligned} v_{l,d} = -\frac{R_{eq}}{2} \cdot (\bar{i}_{v,d} + \tilde{i}_{v,d}) + \frac{L_{eq}\omega}{2} \cdot (\tilde{i}_{v,q} + \bar{i}_{v,q}) + v_{f,d} + \frac{L_{eq}\alpha_{i_{v,d}}}{2} \cdot \tilde{i}_{v,d} + \\ + \frac{L_{eq}}{2}\beta_{i_{v,d}}\xi_{v,d} + Lw \cdot (\tilde{i}_{cir,q} + \bar{i}_{cir,q}) + L\alpha_{i_{cir,d}}\tilde{i}_{cir,d} - R \cdot (\tilde{i}_{cir,d} + \bar{i}_{cir,d}) \end{aligned} \quad (4.8)$$

such that the time derivative of the Lyapunov function becomes:

$$\dot{V}_{i_{cir,d}} = -\alpha_{i_{cir,d}} \cdot \tilde{i}_{cir,d}^2 \quad (4.9)$$

where we define the constant $\alpha_{i_{cir,d}} \in \mathbb{R}_+^*$. By (4.6) and (4.9), one can assure exponential stability for state $i_{cir,d}$ towards its reference.

Replacing (4.8) in (4.5), the control law $v_{u,d}$ is defined as:

$$v_{u,d} = \frac{R_{eq}}{2} \cdot (\bar{i}_{v,d} + \tilde{i}_{v,d}) - \frac{L_{eq}\omega}{2} \cdot (\tilde{i}_{v,q} + \bar{i}_{v,q}) - v_{f,d} - \frac{L_{eq}\alpha_{i_{v,d}}}{2} \cdot \tilde{i}_{v,d} + \frac{L_{eq}}{2} \beta_{i_{v,d}} \xi_{v,d} + L\omega \cdot (\tilde{i}_{cir,q} + \bar{i}_{cir,q}) + L\alpha_{i_{cir,d}} \tilde{i}_{cir,d} - R \cdot (\tilde{i}_{cir,d} + \bar{i}_{cir,d}) \quad (4.10)$$

Applying these control laws, (4.8) and (4.10) in (4.3), the time derivative of the Lyapunov function becomes:

$$\dot{V}_{i_{v,d}} = -\alpha_{i_{v,d}} \cdot \tilde{i}_{v,d}^2 \quad (4.11)$$

By (4.2) and (4.11), and calling upon La Salle's theorem one can assure asymptotic stability for the state $i_{v,d}$ towards its reference. In addition, calling upon theorem 4.6 in [79], it is possible to show that this stability is indeed exponential for states $i_{v,d}$ and $\xi_{v,d}$. The same procedure presented above is considered for states $i_{v,q}$ and $i_{cir,q}$. The following Lyapunov functions are considered:

$$V_{i_{v,q}} = (i_{v,q} - \bar{i}_{v,q})^2 + \frac{1}{2} \beta_{v,q} \xi_{v,q}^2 \quad (4.12)$$

$$V_{i_{cir,q}} = (i_{cir,q} - \bar{i}_{cir,q})^2 + \frac{1}{2} \beta_{cir,q} \xi_{cir,q}^2 \quad (4.13)$$

with $\xi_{v,q}$ and $\xi_{cir,q}$ given by:

$$\xi_{v,q} = i_{v,q} - \bar{i}_{v,q}$$

$$\xi_{cir,q} = i_{cir,q} - \bar{i}_{cir,q}$$

Considering the time derivative of the Lyapunov functions from (4.12) and (4.13), the control laws $v_{l,q}$ and $v_{u,q}$ can be obtained as:

$$v_{l,q} = -R \cdot (\tilde{i}_{cir,q} + \bar{i}_{cir,q}) - L\omega \cdot (\tilde{i}_{cir,d} + \bar{i}_{cir,d}) - \frac{R_{eq}}{2} \cdot (\bar{i}_{v,q} + \tilde{i}_{v,q}) + L\beta_{i_{cir,q}} \xi_{cir,q} - \frac{L_{eq}\omega}{2} \cdot (\tilde{i}_{v,d} + \bar{i}_{v,d}) + v_{f,q} + \frac{L_{eq}\alpha_{i_{v,q}}}{2} \cdot \tilde{i}_{v,q} + \frac{L_{eq}\beta_{i_{v,q}}}{2} \cdot \xi_{v,q} + L\alpha_{i_{cir,q}} \tilde{i}_{cir,q} \quad (4.14)$$

$$v_{u,q} = -R \cdot (\tilde{i}_{cir,q} + \bar{i}_{cir,q}) - L\omega \cdot (\tilde{i}_{cir,d} + \bar{i}_{cir,d}) + \frac{R_{eq}}{2} \cdot (\bar{i}_{v,q} + \tilde{i}_{v,q}) + L\beta_{i_{cir,q}} \xi_{cir,q} + \frac{L_{eq}\omega}{2} \cdot (\tilde{i}_{v,d} + \bar{i}_{v,d}) - v_{f,q} + \frac{L_{eq}\alpha_{i_{v,q}}}{2} \cdot \tilde{i}_{v,q} - \frac{L_{eq}\beta_{i_{v,q}}}{2} \cdot \xi_{v,q} + L\alpha_{i_{cir,q}} \tilde{i}_{cir,q} \quad (4.15)$$

Control laws (4.14) and (4.15), with $\alpha_{i_{cir,q}}$, $\alpha_{i_{v,q}}$, $\beta_{i_{cir,q}}$ and $\beta_{i_{v,q}}$ positive constants, leads to the Lyapunov functions' time derivatives:

$$\dot{V}_{i_{cir,q}} = -\alpha_{i_{cir,q}} \cdot \tilde{i}_{cir,q}^2 \quad (4.16)$$

$$\dot{V}_{i_{v,q}} = -\alpha_{i_{v,q}} \cdot \tilde{i}_{v,q}^2 \quad (4.17)$$

As before, (4.12), (4.13), (4.16) and (4.17) with La Salle's theorem assure asymptotic stabilization of states $i_{cir,q}$ and $i_{v,q}$ towards their references. Again, it is possible to show that stabilization of states $i_{v,q}$, $\xi_{v,q}$, $i_{cir,q}$ and $\xi_{cir,q}$ are exponential.

At last, concerning state $i_{cir,0}$, a Lyapunov function is proposed in (4.18) with time derivative (4.19).

$$V_{i_{cir,0}} = \frac{1}{2}(i_{cir,0} - \bar{i}_{cir,0})^2 \quad (4.18)$$

$$\dot{V}_{i_{cir,0}} = \tilde{i}_{cir,0} \cdot \left(-\frac{R_{\tilde{}}}{L} i_{cir,0} - \frac{R_{\bar{}}}{L} i_{cir,0} - \frac{v_{d0}}{2L} + \frac{V_{DC}}{2L} \right) \quad (4.19)$$

Rearranging (4.19), the control law $v_{d,0}$ is obtained in (4.20), which leads to (4.21).

$$v_{d0} = 2L\tilde{i}_{cir,0}\alpha_{i_{cir,0}} - 2R \cdot (\bar{i}_{cir,0} + \tilde{i}_{cir,0}) + V_{DC} \quad (4.20)$$

$$\dot{V}_{i_{cir,0}} = -\alpha_{i_{cir,0}} \cdot \tilde{i}_{cir,0}^2 \quad (4.21)$$

Again, it is possible to show that $\tilde{i}_{cir,0}$ exponentially converges to zero. By the procedure described above, the five available control inputs ($v_{u,d}$, $v_{u,q}$, $v_{l,d}$, $v_{l,q}$ and v_{d0}) were defined respectively in (4.10), (4.15), (4.8), (4.14) and (4.20). Moreover, exponential stabilization was obtained by design for all actuated states ($i_{v,d}$, $i_{v,q}$, $i_{cir,d}$, $i_{cir,q}$ and $i_{cir,0}$).

4.3.2 Free-dynamic States

The total converter's energy W_h and balance energy W_v do not have a exclusive control input as the other states. So a backstepping procedure was used in their cases. For this reason, virtual inputs are proposed as $i_{cir,0}^*$ and $i_{cir,d}^*$.

The variable $i_{cir,0}^*$ is used as a reference for $i_{cir,0}$, and will be applied to steer W_h to its desired equilibrium. Thus, it is now defined the state error $\tilde{i}_{cir,0}$ in (4.22), where \tilde{W}_h is the error from total converter's energy W_h and its equilibrium value \bar{W}_h . In a similar way, because $i_{cir,d,q}$ represent the flow inside the converter, it is possible to transfer energy between converters' arms. So, $i_{cir,d}^*$ is chosen to be used as a control signal for W_v . It is then defined the error between the state and its reference as in (4.23).

$$\begin{cases} \tilde{i}_{cir,0} = i_{cir,0} - i_{cir,0}^* \\ i_{cir,0}^* = \bar{i}_{cir,0} + \alpha_W \tilde{W}_h + \beta_{W_h} \xi_{W_h} \end{cases} \quad (4.22)$$

$$\begin{cases} \tilde{i}_{cir,d} = i_{cir,d} + i_{cir,d}^* \\ i_{cir,d}^* = \bar{i}_{cir,d} + \alpha_{W_v} \cdot W_v + \beta_{W_v} \cdot \xi_{W_v} \end{cases} \quad (4.23)$$

where α_{W_h} , α_{W_v} , β_{W_h} and β_{W_v} are positive constants, and ξ_{W_h} and ξ_{W_v} will be defined latter.

Therefore, the total converter energy (W_h) dynamic is rewritten considering the predefined control inputs introduced in (4.8), (4.10), (4.14), (4.15) and (4.20) and the virtual input (4.22).

It is important to emphasize that the remaining states do not rely on the two energy states. For this reason, these two are considered as zero dynamics (similarly could be seen as a cascaded system) of the feedback linearization of the remaining states [79]. To analyze these zero dynamics, it is now considered $\tilde{i}_{v,d} = 0$, $\tilde{i}_{v,q} = 0$, $\tilde{i}_{cir,d} = 0$, $\tilde{i}_{cir,q} = 0$ and $\tilde{i}_{cir,0} = 0$. Based on this, it is now defined the state ξ_{W_v} and we rewrite $\dot{\tilde{W}}_h$ as (4.24).

$$\begin{aligned} \dot{\xi}_{W_h} &= W_h - \bar{W}_h \triangleq \tilde{W}_h \\ \dot{\tilde{W}}_h &= \frac{3}{2}\tilde{i}_{v,d}v_{f,d} + \frac{3}{2}\tilde{i}_{v,q}v_{f,q} - \frac{3}{4}R_{eq}\tilde{i}_{v,d}^2 - \frac{3}{4}R_{eq}\tilde{i}_{v,q}^2 + 3\tilde{i}_{cir,0}v_{DC} - 3R\tilde{i}_{cir,d}^2 + \\ &\quad - 3R\tilde{i}_{cir,q}^2 - 3R\tilde{i}_{cir,0}^2 + 12R\tilde{i}_{cir,0}\alpha_{W_h}\tilde{W}_h - 3v_{DC}\alpha_{W_h}\tilde{W}_h - 6R\alpha_{W_h}^2\tilde{W}_h^2 \end{aligned} \quad (4.24)$$

the sum of highlighted terms is zero because they represent the elements of the converter's power balance, so (4.24) becomes (4.25). Highlighted terms indeed constitute AC power, DC power, losses in AC elements, and losses in DC elements. Their sum is always zero for physical reasons.

$$\dot{\tilde{W}}_h = 12R\tilde{i}_{cir,0}\alpha_{W_h}\tilde{W}_h - 3v_{DC}\alpha_{W_h}\tilde{W}_h - 6R\alpha_{W_h}^2\tilde{W}_h^2 \quad (4.25)$$

One may now consider the Lyapunov function candidate:

$$V_{W_h} = \frac{1}{2}(W_h - \bar{W}_h)^2 + \frac{1}{2}\xi_{W_h}^2 \quad (4.26)$$

in which derivative is:

$$\dot{V}_{W_h} = 12R\tilde{i}_{cir,0}\alpha_{W_h}\tilde{W}_h^2 - 3v_{DC}\alpha_{W_h}\tilde{W}_h^2 - 6R\alpha_{W_h}^2\tilde{W}_h^3 \quad (4.27)$$

For physical reasons, $12R\tilde{i}_{cir,0} \ll 3v_{DC}$, then, inside a region

$$\|\tilde{W}_h\| < \frac{(3v_{DC} - 12R\tilde{i}_{cir,0})}{6R\alpha_{W_h}} \quad (4.28)$$

Lyapunov function's derivative (4.27) is negative, and as a consequence for a given operation region around the equilibrium point $\xi_{W_h} = 0$ and $\tilde{W}_h = 0$, this Lyapunov function assures asymptotic stability towards this point. Furthermore, the size of this operation region is given by the tuning parameter of α_{W_h} .

Following the same procedure, the zero dynamics represented by W_v are considered with the predefined control inputs (4.8), (4.10), (4.14), (4.15), and (4.20) as:

$$\dot{W}_v = i_{cir,d}^*(-3v_{fd} + R_{eq2}\tilde{i}_{v,d} + 3\omega L_c\tilde{i}_{v,q}) \quad (4.29)$$

where $R_{eq2} = \frac{3(R+R_{eq})}{2}$. Then, using $i_{cir,d}^*$ as an virtual input defined by (4.23) and setting $\tilde{i}_{cir,d} = 0$:

$$\dot{W}_v = -\alpha_{W_v}W_v(3v_{fd} - R_{eq2}\tilde{i}_{v,d} - 3\omega L_c\tilde{i}_{v,q}) - \beta_{W_v}\xi_{W_v}(3v_{fd} - R_{eq2}\tilde{i}_{v,d} - 3\omega L_c\tilde{i}_{v,q}) \quad (4.30)$$

with $\dot{\xi}_{W_v} = W_v$. In the HVDC system, v_{fd} represents a large quantity, while voltage drop across resistance and inductance of PCC are small in comparison to v_{fd} . For physical reasons, the term inside the box is always positive, and it is concluded exponential stability for zero dynamics given by states W_v and ξ_{W_v} , because it is a linear Hurwitz system.

4.4 Main result

One can now state the constructive result built in the previous sections in the form of a theorem.

Theorem 01 *The MMC represented by the system in (2.35), with control inputs given by (4.8), (4.10), (4.14), (4.15) and (4.20) with tuning parameters $\alpha_{i_{vd}}$, $\alpha_{i_{vq}}$, $\alpha_{i_{cir,d}}$, $\alpha_{i_{cir,q}}$, $\alpha_{i_{cir,0}}$, α_{W_h} and $\alpha_{W_v} \in \mathbb{R}_+^*$, is split into an actuated subsystem including states $[i_{v,d} \ i_{v,q} \ i_{cir,d} \ i_{cir,q} \ i_{cir,0}]$, extended by the integral of their dynamics, represented by states $[\xi_{v,d} \ \xi_{v,q} \ \xi_{cir,q}]$. This first subsystem has an exponential stable equilibrium point, represented by (3.6), (3.7), (4.23), (3.9) and (4.22). In addition, the remaining non-actuated subsystem including states $[W_h \ W_v]$ and their extended integral terms $[\xi_{W_h} \ \xi_{W_v}]$ have asymptotically stable equilibrium points (3.28) and (3.29) inside the domain:*

$$\mathcal{D} = \left\{ W_v \in \mathbb{R}_+^*, \ \xi_{W_h}, \xi_{W_v} \in \mathbb{R}, \ \|W_h - \bar{W}_h\| < \frac{(3v_{DC} - 12R\bar{i}_{cir,0})}{6R\alpha_{W_h}} \right\}$$

As a consequence the full system is asymptotic stable inside a domain, which size is given by a tuning parameter.

The proof is based on the composite Lyapunov function:

$$\begin{aligned} V &= V_{i_{v,d}} + V_{i_{v,q}} + V_{i_{cir,d}} + V_{i_{cir,q}} + V_{i_{cir,0}} + V_{W_h} + V_{W_v} \\ &= \frac{1}{2}(i_{v,d} - \bar{i}_{v,d})^2 + \frac{1}{2}(i_{v,q} - \bar{i}_{v,q})^2 + \frac{1}{2}(i_{cir,d} - \bar{i}_{cir,d})^2 + \\ &\quad + \frac{1}{2}(i_{cir,q} - \bar{i}_{cir,q})^2 + \frac{1}{2}(i_{cir,0} - \bar{i}_{cir,0})^2 + \frac{1}{2}(W_h - \bar{W}_h)^2 + \\ &\quad + \frac{1}{2}(W_v - \bar{W}_v)^2 \end{aligned}$$

in which derivative $\dot{V} \leq 0$ by virtue of (4.11), (4.16), (4.9), (4.17) and (4.21), provide $\alpha_{i_{cir,d}}$, $\alpha_{i_{cir,q}}$, $\alpha_{i_{vd}}$, $\alpha_{i_{vq}}$, $\alpha_{i_{cir,0}}$, α_{W_h} and $\alpha_{W_v} \in \mathbb{R}_+^*$. Then, applying theorem 4.6 in 79, it is shown that the actuated states are exponentially stable. Furthermore, the zero dynamics are asymptotically stable inside an operation region given by condition (4.28). Then it is possible to conclude that the whole system is asymptotically stable inside a domain, that will increase its size by reducing design parameter α_{W_h} .

Figure 4.1 summarize the simulation implementation of nonlinear controller.

4.5 Medium-voltage system test with the nonlinear controller

The system presented in figure 3.7 is simulated using the nonlinear control for the switching and average models. The nonlinear control gains are tuned using the switching model, because its extra dynamics may turn the system more sensitive to tuning.

Nonlinear control tuning for medium-voltage system test Control gains imply in system performance. The tuning procedure provides the control gains shown in Table (4.1). These gains are directly linked to the control effort, which is possible

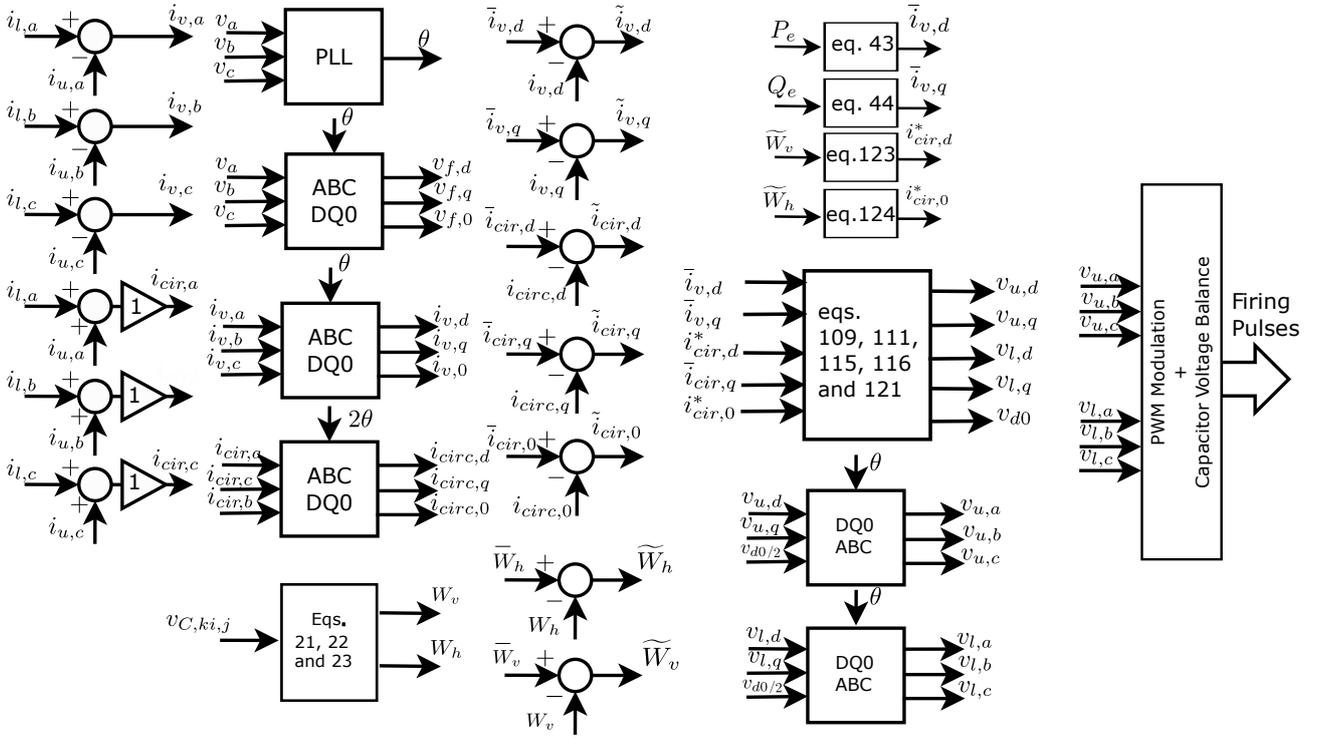


Figure 4.1: Diagram of nonlinear control.

Source: Author

to see on the figure of control inputs. The tuning process shown in this section considers a balancing between the speed of convergence and the overshoots. Indeed, each pair of α s and β s place the corresponding poles.

Tuning β s while α s are equal to zero, enable to set the speed of convergence of the related state variables, i.e. place the poles' modulus:

$$\tau_{i_{vd}} = \frac{1}{\beta_{i_{vd}}}; \quad \beta_{i_{vd}} = 1000 \quad (4.31)$$

$$\tau_{i_{vq}} = \frac{1}{\beta_{i_{vq}}}; \quad \beta_{i_{vq}} = 1000 \quad (4.32)$$

$$\tau_{i_{cirq}} = \frac{1}{\beta_{i_{cirq}}}; \quad \beta_{i_{cirq}} = 1000 \quad (4.33)$$

$$\tau_{W_h} = \frac{1}{\beta_{W_h}}; \quad \beta_{W_h} = 50 \quad (4.34)$$

$$\tau_{W_v} = \frac{1}{\beta_{W_v}}; \quad \beta_{W_v} = 50 \quad (4.35)$$

Adjusting α_s , one obtain the damping ratio, and as consequence, the response of state variables i_{vd} and i_{vq} are improved as shows figure 4.2. It is possibles to verify i_{vd} and i_{vq} convergence for $\alpha_{i_{vd}}$ $\alpha_{i_{vq}}$ equal to 100, 500 and 1000. The speed of convergence is improved by the tuning, however it results in a overshoot in the case of $\alpha = 1000$. The intermediate value (500) is chosen for $\alpha_{i_{vd}}$ and $\alpha_{i_{vq}}$.

State variable i_{cirq} track their reference just by the adjust of $\beta_{i_{cirq}}$. Furthermore, it presents a reduction of noise when $\alpha_{i_{cirq}}$ increases.

State variables $i_{cir,d}$ and $i_{cir,0}$, which are used as virtual inputs, are directly tuned by their α s. For $\alpha_{i_{cir,d}}$ and $\alpha_{i_{cir,0}}$ equals to 1000, there is no steady-state error for these states.

The β_{W_v} and β_{W_h} are tuned to have a slower response compared to the other state variables. They are set to 50, and both W_h and W_v present no steady-state

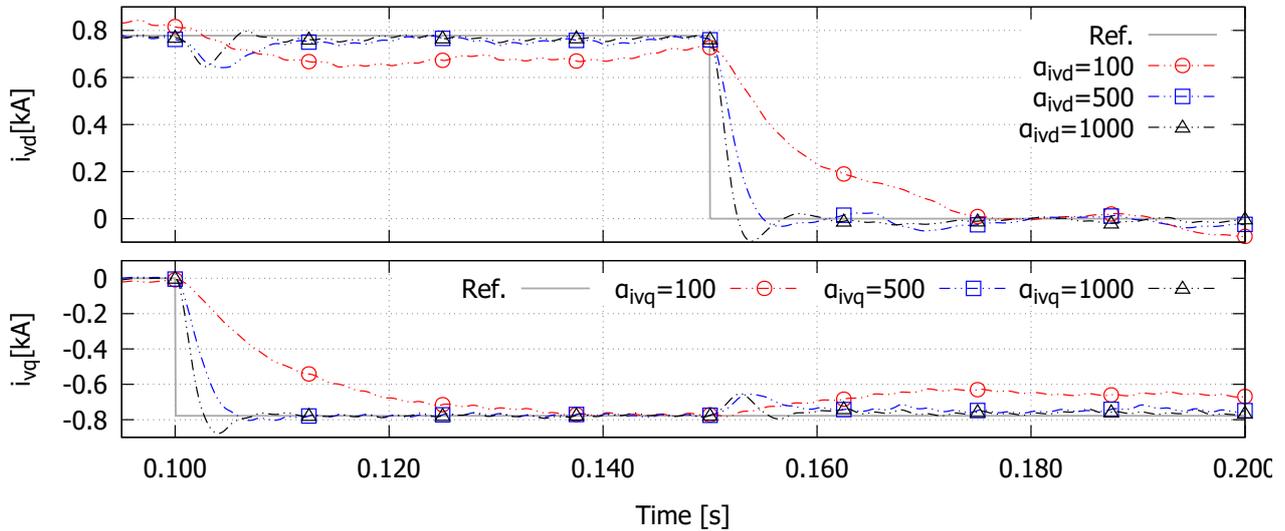


Figure 4.2: Response of state i_{vd} and i_{vq} over tuning of α_s .

Source: Author

error and have high speed of convergence. As a consequence, their respective α_s are set to be equal to 1.

Remark 01 *It is clear that other methods of pole placement could be used, in particular robust techniques as LQR. These possibilities will be tested in future works.*

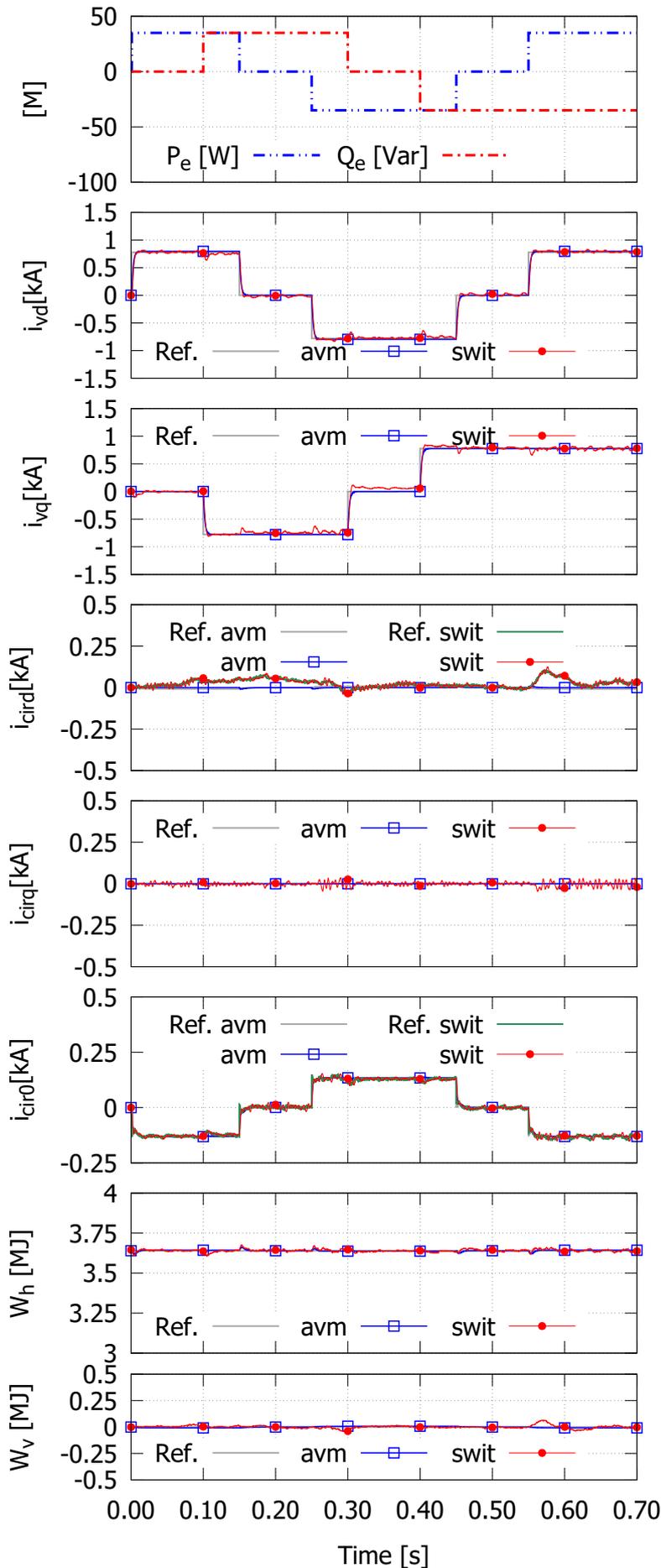
The following results for the medium-voltage system, consider the parameters summarised in table 4.1.

Table 4.1: Parameters of simulated medium-voltage system and nonlinear control gains.

Parameter	Value	Parameter	Value
S_{MMC}	50 MVA	$\beta_{i_{vdq}}$	1000
V_{AC}	30 kV	$\beta_{i_{cirq}}$	1000
V_{DC}	180 kV	β_{W_h}	50
L_c	5 mH	β_{W_v}	50
L	14 mH	$\alpha_{i_{vdq}}$	500
R_c	0.03 Ω	$\alpha_{i_{cir d}}$	1000
C_{SM}	3 mF	$\alpha_{i_{cir q}}$	500
Freq	60 Hz	$\alpha_{i_{cir 0}}$	1000
R	0.5 Ω	α_{W_h}	1
N	20	α_{W_v}	1

Figure 4.3 and figure 4.4 present the performance of the MMC over the proposed nonlinear controller. A four-quadrant operation is presented and also an energy step change. Both average-model (avm) and switching-model (swit) are presented.

Figure 4.3: Four-quadrant operation of the medium-voltage system with the nonlinear controller.



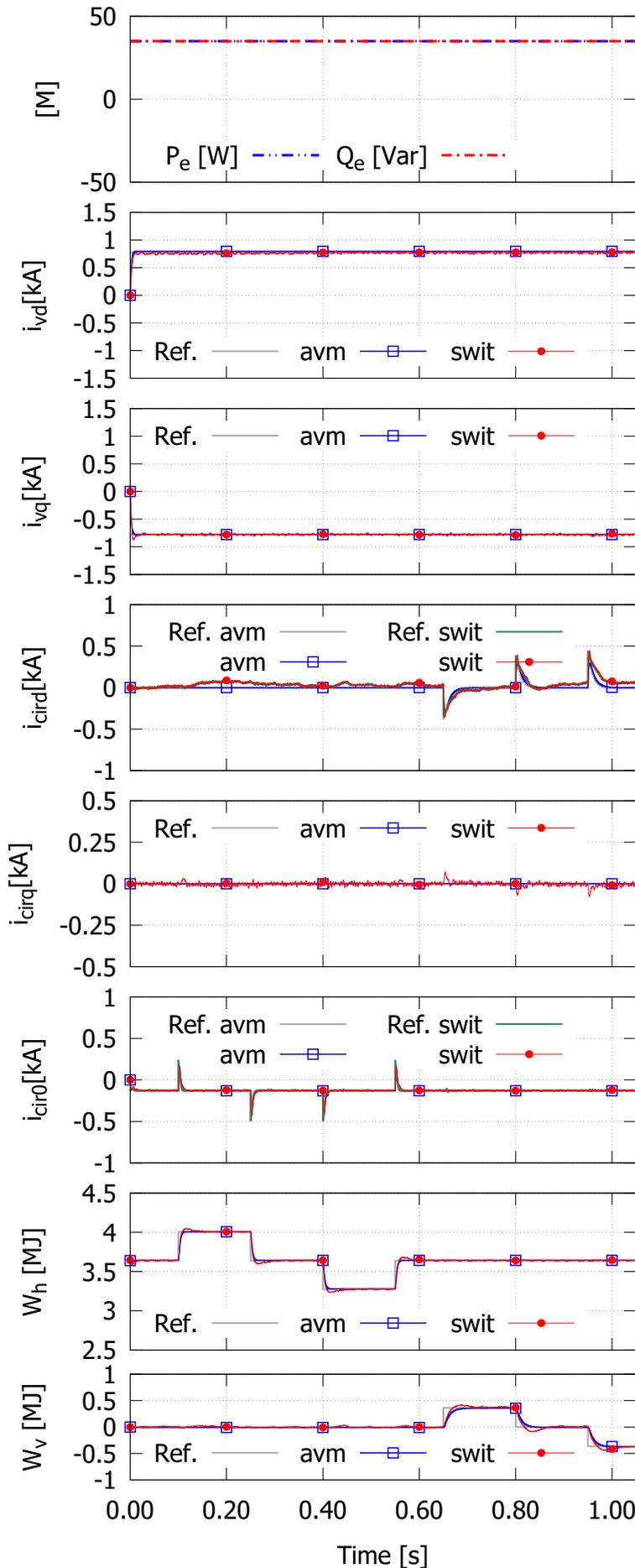
Four-quadrant operation of average and switching models of the medium-voltage system with the nonlinear controller. In figure 4.3 a set of active and reactive power steps are performed. Both average-model and switching-model perform well using nonlinear controller. They present the same speed of convergence and no overshoot.

The switching-model present small oscillations if compared to average-model.

The state variables i_{cird} and i_{cir0} present different reference values (Ref.) between average-model and switching-model. Thus, they are distinguished at the figure.

At 4th graphic, i_{cird} shows a different behaviour for each model, for some operating points. However nonlinear control drives the state variable for the respective desired value. The other state variables present close performance between MMC models.

Figure 4.4: Energy changes of the medium-voltage system with the nonlinear controller.



Energy changes of average and switching models for medium-voltage system with the nonlinear controller. Concerning energy changes, figure 4.4 presents average and switching models' performance with the the nonlinear controller.

Both models achieve their desired values, however switching-model presents a tiny overshoot.

The models' performance has a solid equivalence which allows the use of the average model if a more simple simulation is required.

4.5.1 Robustness over parameters uncertainties and voltage fluctuation for medium-voltage system with nonlinear controller

Robustness Robustness analysis is performed for nonlinear control's sensitivity performance. The parameter uncertainties are considered in this chapter: R , R_c , L , L_c and C_{SM} change (one at a time) in $\pm 10\%$ and $\pm 20\%$ from their nominal values. Real values are used in the control. The operating point is set to 70% of nominal active and reactive power.

Figure 4.5 shows a variation in the arm equivalent resistance R . The state variables present no overshoot neither deviation in steady-state. Additionally, the system's states are also not affected by the deviation on AC side resistance R_c (see figure 4.6).

Figure 4.7 and figure 4.8 point out steady-state error when arms inductance L and AC side inductance L_c are far from the nominal values. That error appears in the AC currents i_{vd} and i_{vq} .

Figure 4.9 shows system's states for changes in SM capacitance. It is possible to see in 7th graphic that the initial value of total energy W_h comes from equation (3.28) which is linked with SM capacitance. However, the nonlinear controller can drive the state variable to the desired reference. Also, the convergence's speed of $i_{cir,d}$ is large.

Therefore, the nonlinear controller proposed in this thesis presented steady-state error when arm inductance L and AC side inductance L_c changes. The state variables most affected were $i_{v,d}$ and $i_{v,q}$. However, these errors can be minimized by the increase of controller gains.

Voltage fluctuation

- Variation in the AC voltage at the PCC result in i_{vd} and i_{vq} with over-signal. The same problem was faced by PI controller, in the test from section 3.4.2. The other state variables are well drive to their reference for all value of V_{ac} ;
- Fluctuation in DC voltage result in slow speed of convergence to $i_{cir,d}$ and W_v . However faster than PI convergence through the same test.

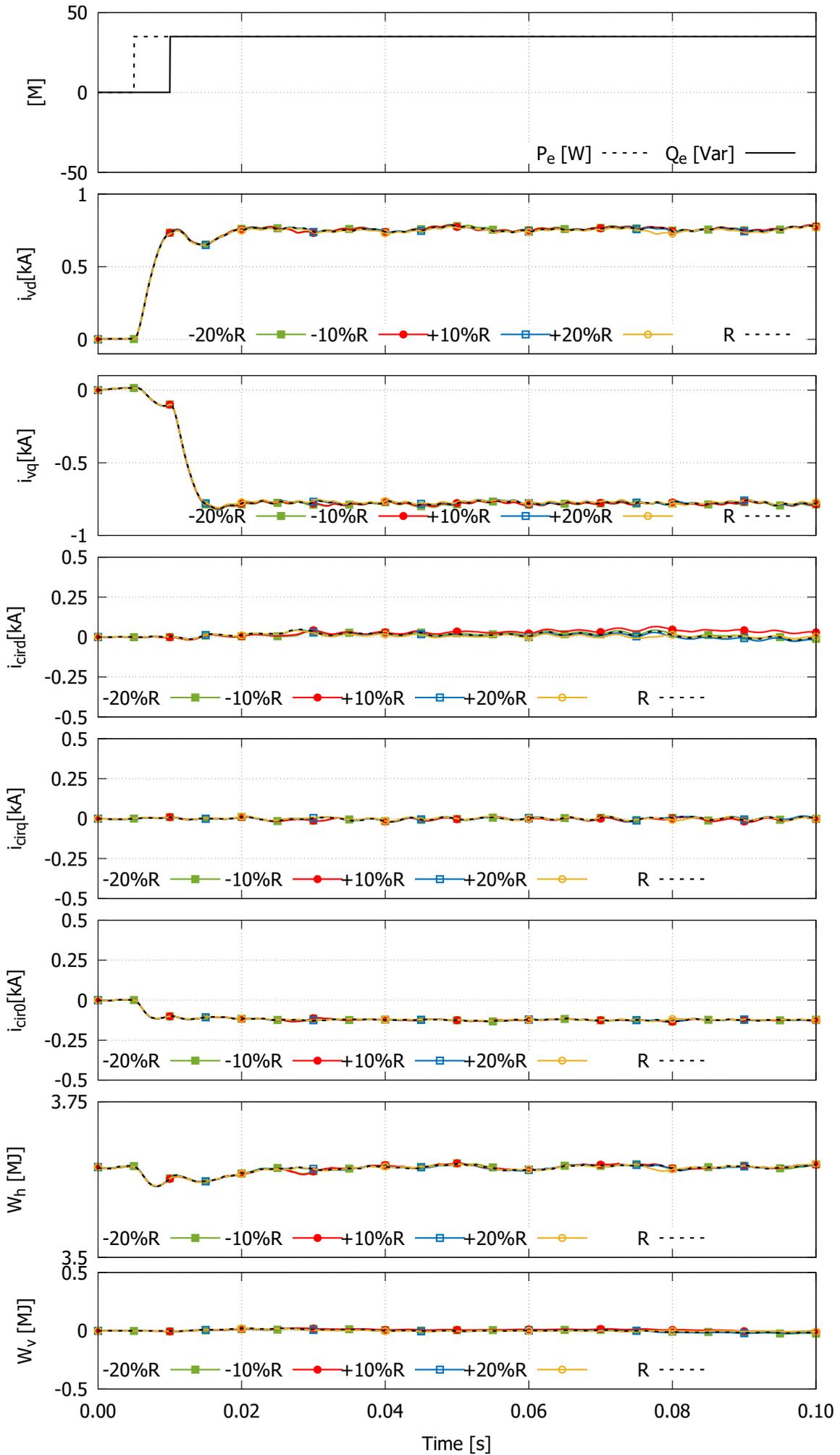
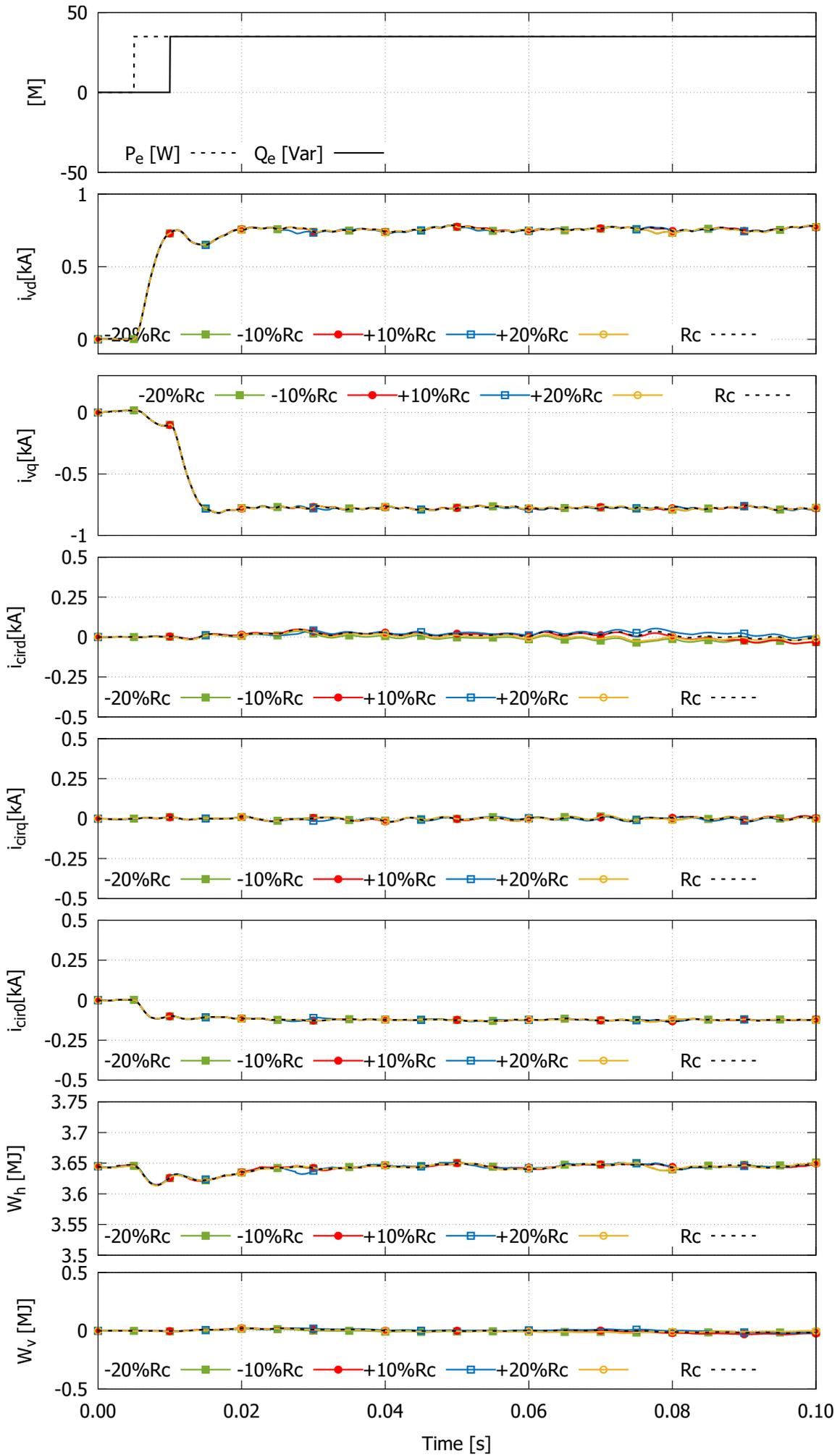


Figure 4.5: The system state over variation of parameter R with nonlinear controller.

Figure 4.6: States over variation of parameter R_c with nonlinear controller.

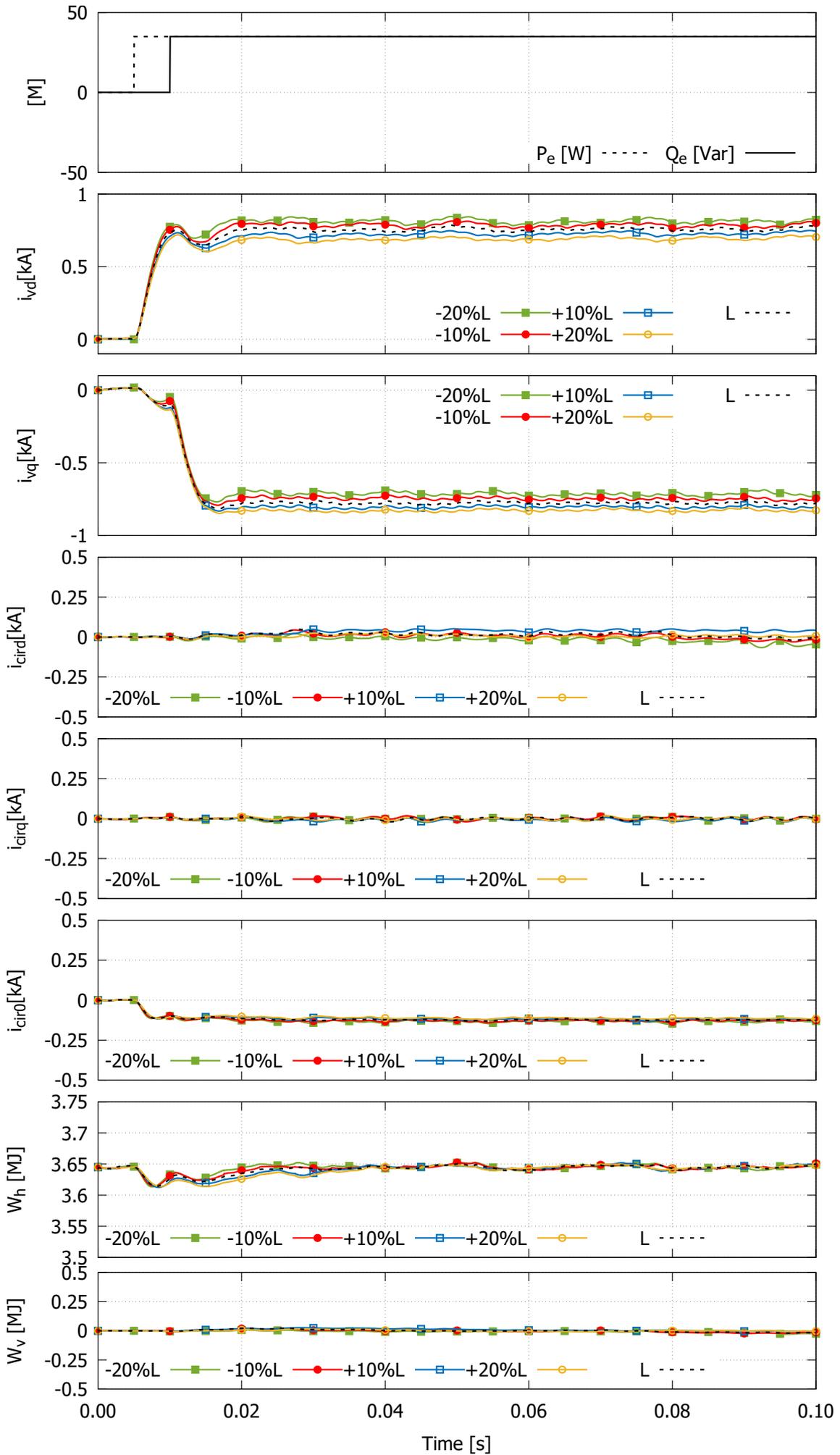
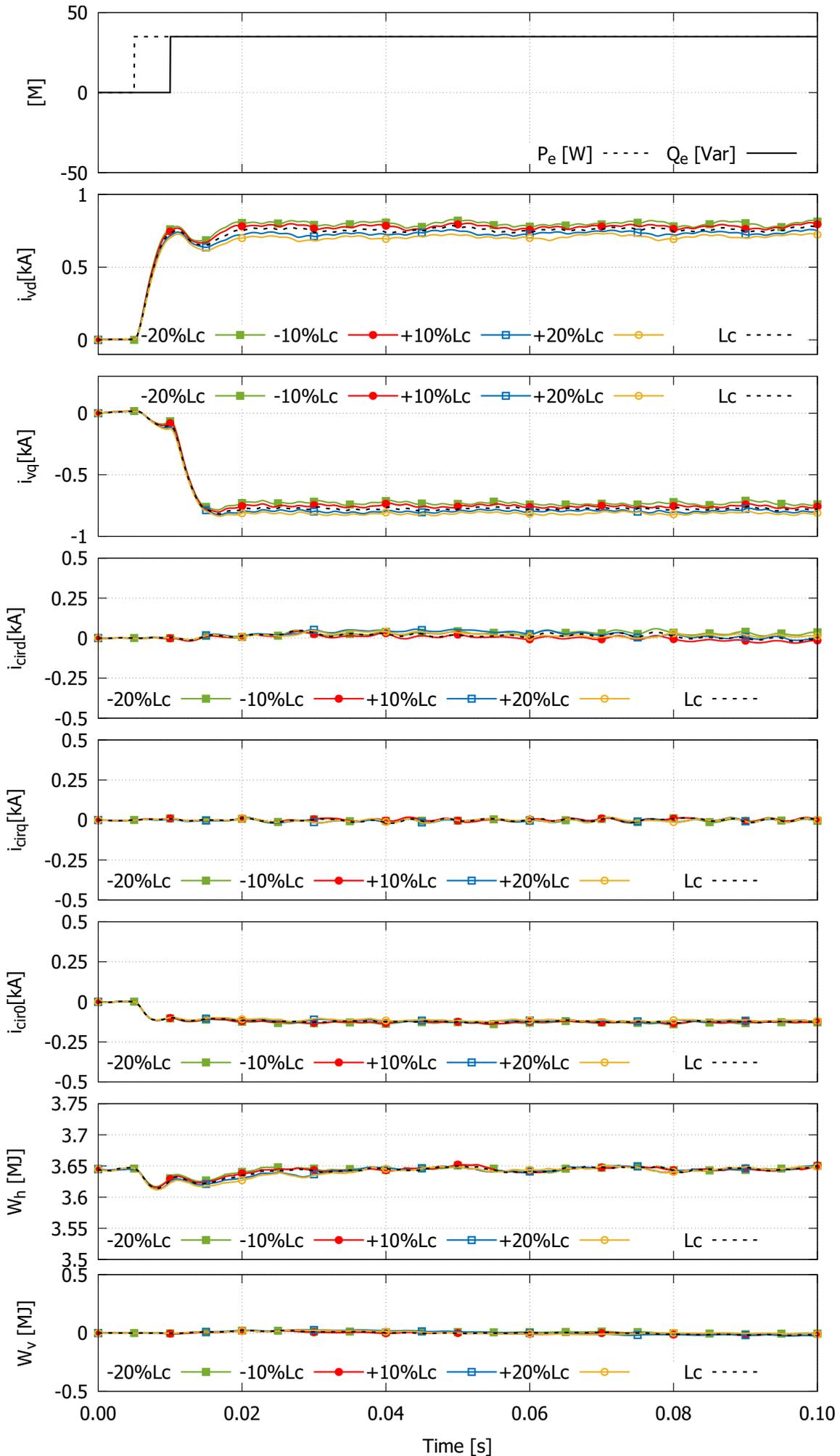


Figure 4.7: States over variation of parameter L with nonlinear controller.

Figure 4.8: States over variation of parameter L_c with nonlinear controller.

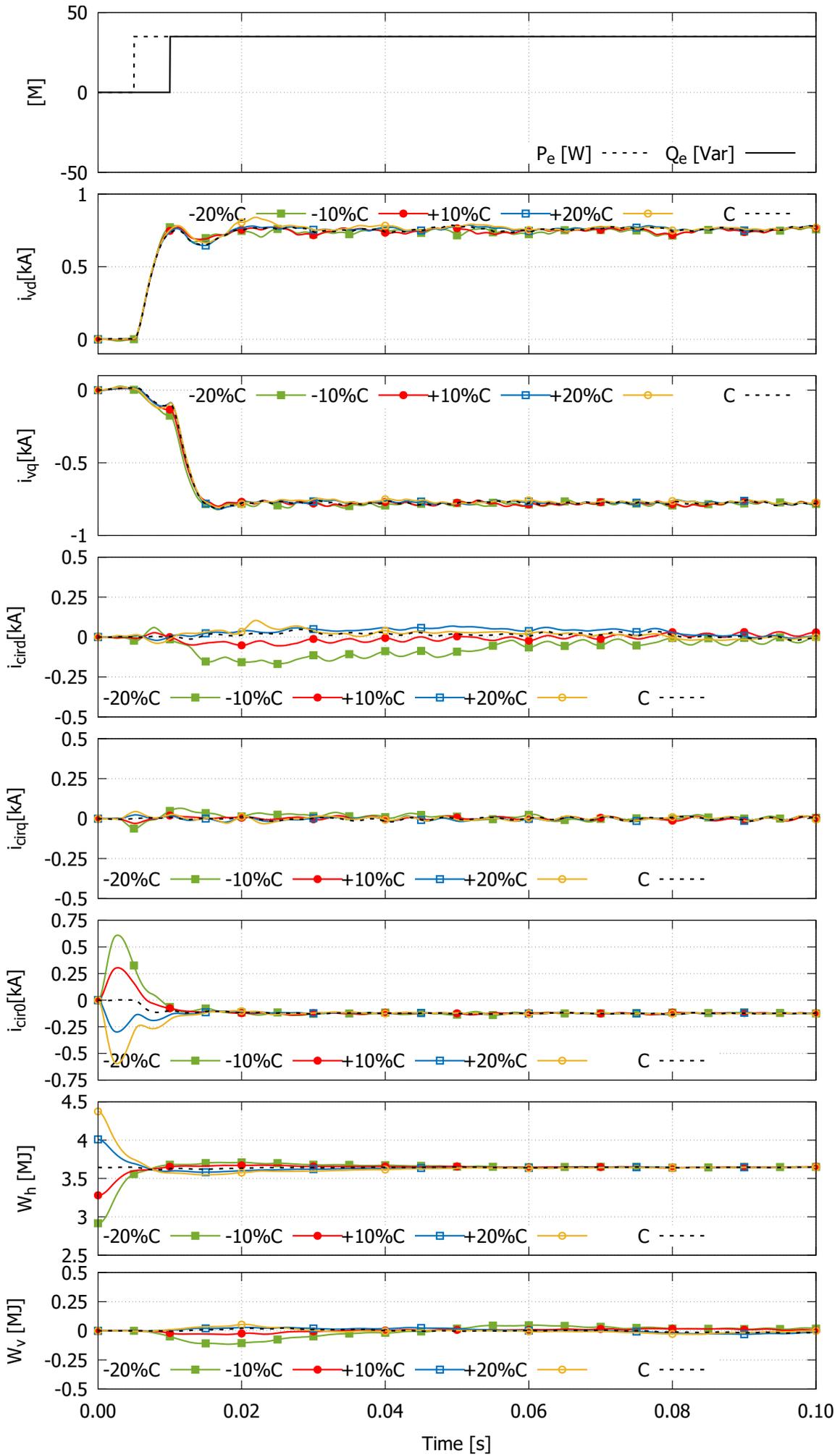


Figure 4.9: States over variation of parameter C with nonlinear controller.

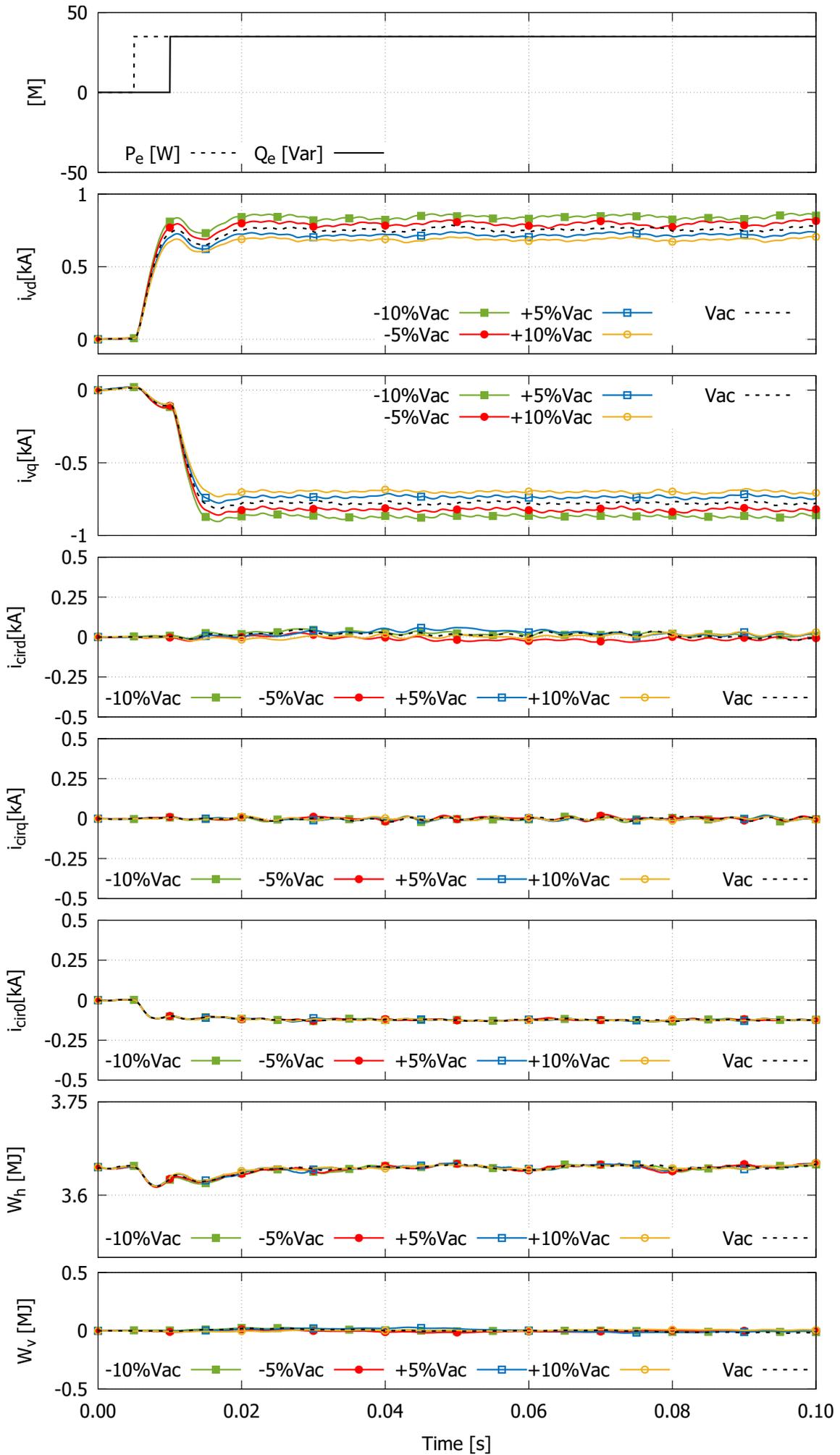


Figure 4.10: Fluctuation of AC voltage at the PCC with nonlinear controller.

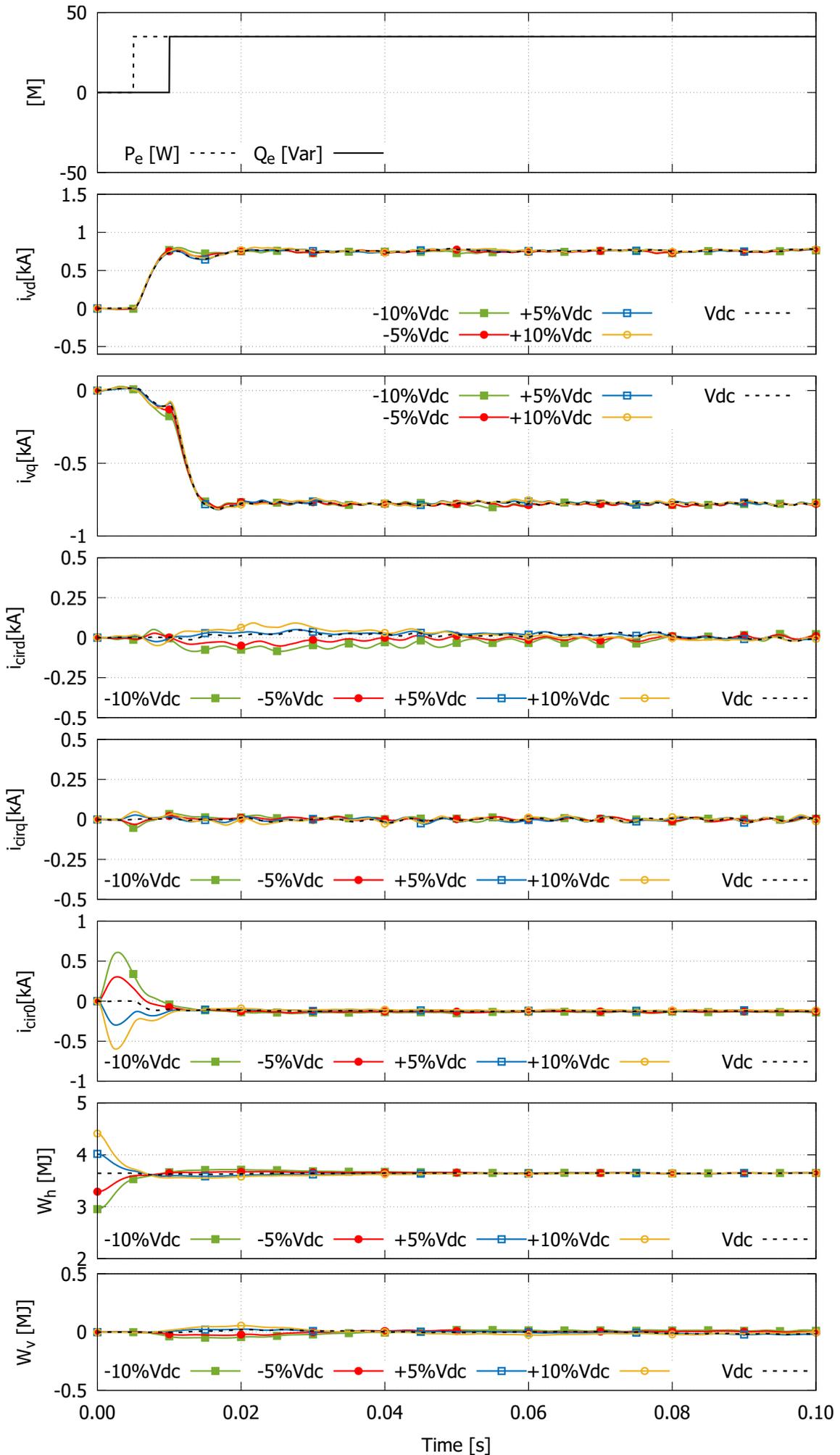


Figure 4.11: DC voltage fluctuation with nonlinear controller.

4.6 High Voltage system test with nonlinear controller

The system presented in figure 3.34 is simulated with the nonlinear controller. In these simulations it is used the switching model. Furthermore, a comparison with the PI controller is carry out.

Nonlinear control tuning for High Voltage system test The same procedure as presented in section 4.5 is accomplished here. Tuning β s while α s are equal to zero, enable to set the speed of convergence of the related state variables. The $\beta_{i_{vd}}$, $\beta_{i_{vq}}$ and $\beta_{i_{cirq}}$ needed to be set ten times bigger than medium-voltage system, once a smaller gain result in a large overshoot with slow state convergence. The β s related to energy are kept the same as medium-voltage system.

$$\tau_{i_{vd}} = \frac{1}{\beta_{i_{vd}}}; \quad \beta_{i_{vd}} = 10000 \quad (4.36)$$

$$\tau_{i_{vq}} = \frac{1}{\beta_{i_{vq}}}; \quad \beta_{i_{vq}} = 10000 \quad (4.37)$$

$$\tau_{i_{cirq}} = \frac{1}{\beta_{i_{cirq}}}; \quad \beta_{i_{cirq}} = 10000 \quad (4.38)$$

$$\tau_{W_h} = \frac{1}{\beta_{W_h}}; \quad \beta_{W_h} = 50 \quad (4.39)$$

$$\tau_{W_v} = \frac{1}{\beta_{W_v}}; \quad \beta_{W_v} = 50 \quad (4.40)$$

Adjusting α s, response of state variables i_{vd} and i_{vq} are improved as shows figure 4.12. It is possible to verify i_{vd} and i_{vq} convergence for $\alpha_{i_{vd}}$ $\alpha_{i_{vq}}$ equal to 500, 1000 and 2000. The speed of convergence is improved by the tuning. The intermediate value (1000) is chosen for $\alpha_{i_{vd}}$ and $\alpha_{i_{vq}}$ in the high voltage system test.

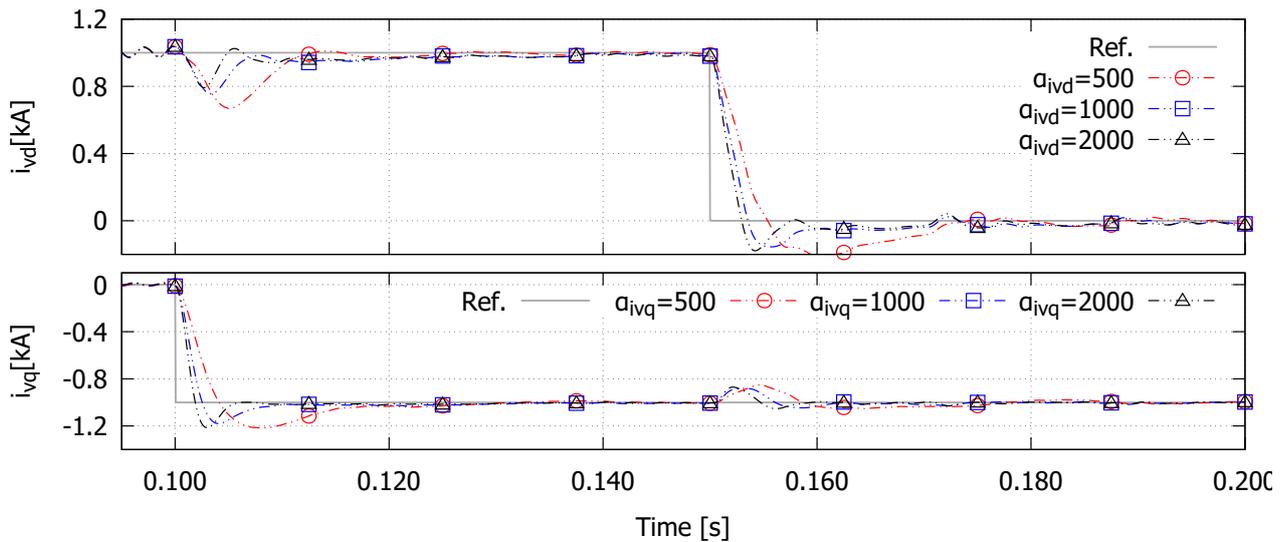


Figure 4.12: Response of state i_{vd} and i_{vq} over tuning of α s.

Source: Author

As in the medium-voltage, in the high voltage system the state variable i_{cirq} track its reference just by the tuning of $\beta_{i_{cirq}}$, and there is a reduction of noise when $\alpha_{i_{cirq}}$ increase. Also, state variables i_{cir0} and i_{cir0} , are directly tuned by their α s. For $\alpha_{i_{cir0}}$ equals to 1000 and $\alpha_{i_{cir0}}$ equals to 2000, there is no steady-state

error for these states. The β_{W_v} and β_{W_h} are both tuned to 50, and both W_h and W_v present no steady-state error and high speed of convergence. Their respective α s are set to be equal to 0.2 reducing the signals' noise.

The following results of high voltage system, use the parameters summarised in table 4.2.

Table 4.2: Parameters of simulated high-voltage system and nonlinear control gains.

Parameter	Value	Parameter	Value
S_{MMC}	450 MVA	$\beta_{i_{vdq}}$	1E4
V_{DC}	400 kV	$\beta_{i_{cirq}}$	1E4
V_{AC}	210 kV	β_{W_h}	50
C_{SM}	3 mF	β_{W_v}	50
L	40 mH	$\alpha_{i_{vdq}}$	1E3
L_c	12 mH	$\alpha_{i_{cir d}}$	1E3
R_c	1 Ω	$\alpha_{i_{cir q}}$	1E3
R	0.5 Ω	$\alpha_{i_{cir 0}}$	2E4
N	20	α_{W_h}	0.2
Freq	60 Hz	α_{W_v}	0.2

4.6.1 Comparison of nonlinear and PI controllers

A detailed switching model of the three-phase MMC converter with 41 levels, depicted in figure 2.1 with the proposed nonlinear control and the PI, is tested using the Matlab Simscape Electrical environment. The system's parameters are presented in table 3.2 and table 4.2, and the results are shown in the dq reference frame.

The performance of the proposed nonlinear control strategy for the MMC was first evaluated through step changes of active and reactive power (P_e and Q_e). All state variables are shown in Figure (4.13), over the power steps. The system is initialized, transmitting zero power.

The considered controllers, nonlinear and PI, provide to the states $i_{cir d}$ and $i_{cir 0}$ different references. So, for those two states it is written *Ref. Non* to indicate Nonlinear controller's reference and *Ref. PI* to identify the PI's references. Remaining states have same references, indicated as *Ref.*

At $t = 0.01$ s, there is an active power step of 70% of the nominal power, see first graphic. It is possible to see a fast response for both controllers, on either output P_e and state i_{vd} on second graphic. The active power step generates an overshoot on state i_{vq} (third graphic). In the same moment, $i_{cir 0}$ (reference and state together) react to transmit the equivalent DC power. For the nonlinear controller, the transient unbalance between AC and DC power (directly related to i_{vd} and $i_{cir 0}$) causes less than 1% of increase in the total energy (W_h at the 7th graphic) until the system regulates the input and output power, which takes 20ms.

Concerning PI controller, the increase in the total energy is slightly larger in comparison with the nonlinear one. However there is a clear compromise between time response and control gains.

Each change in P_e or Q_e implies in a new operating point. On these operating points, PI and nonlinear perform similarly. Then, at $t = 0.40$ s, reactive power become negative, followed by active power, which became positive at $t = 0.45$ s. As a result of the change in the power flow directions, both controllers present oscillations on state variables, PI larger than nonlinear.

At $t = 0.10$ s there is a reactive power step. The directly related state i_{vq} sets to the new reference in less than 10 ms. Remaining states are not affected, and the system can provide the required reactive power.

In figure 4.14 the control performance over free-dynamic state variables is illustrated. The control of converter's energy opens some possibilities concerning very fast ancillary grid services, that will be focused on future research.

Figure 4.14 shows the system performance over converter energy changes. An operating point was set at $t = 0.01$ s, where the active and the reactive power supply 70 % of the nominal power, respecting the capability curve (see 1st graphic). At 8th graphic, on $t = 0.1$ s, the reference for the total energy is increased by 10% of the nominal value. One can see that control drives the concerned states, in order to track the new reference in less than 20ms. It is important to remark that the reference $i_{cir 0}^*$ controls W_h , and at the 5th graph it can be seen that the reference value is accurately tracked by the circulating current.

It is possible to identify a deviation at $i_{cir 0}$ related to changes on W_h . Additionally, an overshoot on $i_{cir d}$ and $i_{cir q}$, which match the steps on balancing energy. That overshoot is necessary to redistribute the energy between the SMs.

At $t = 0.40$ s total energy is reduced by 10%. It is possible to verify that this condition compromises the entire converter operation once state variables start to oscillate around their references. Decrease total energy may imply in the SM capacitor's voltage, which has a crucial role in the entire converter operations. These conditions may need to be further analyzed to be useful for ancillary ser-

vices.

Finally, step changes of $\pm 10\%$ of the nominal total stored energy is applied to the reference of W_v (energy difference between the upper and lower arms), respectively at $t = 0.65\text{ s}$ and $t = 0.95\text{ s}$. It can be seen that the controller is able to track the reference, presenting damped oscillations that settle in 70ms .

Comparing with the PI, the proposed nonlinear controller presented a similar response regarding the performed step tests for total energy and energy difference.

It is important to remark that the desired energy difference between upper and lower arms in normal operation is zero. This step test is used to demonstrate that the proposed controller has the capability of accurately controlling the energy difference independent of the prescribed value, what can be important in unbalanced conditions.

Figure 4.15 shows the controller inputs for the scenario presented on figure 4.13. Each change on power (P_e or Q_e) results on a overshoot at the controller inputs, PI larger than nonlinear. They are considered acceptable.

Figure 4.16 shows the controller inputs for the scenario presented on figure 4.14. These results were produced for W_h and W_v step scenario presented above. Both controllers presenting a suitable control effort.

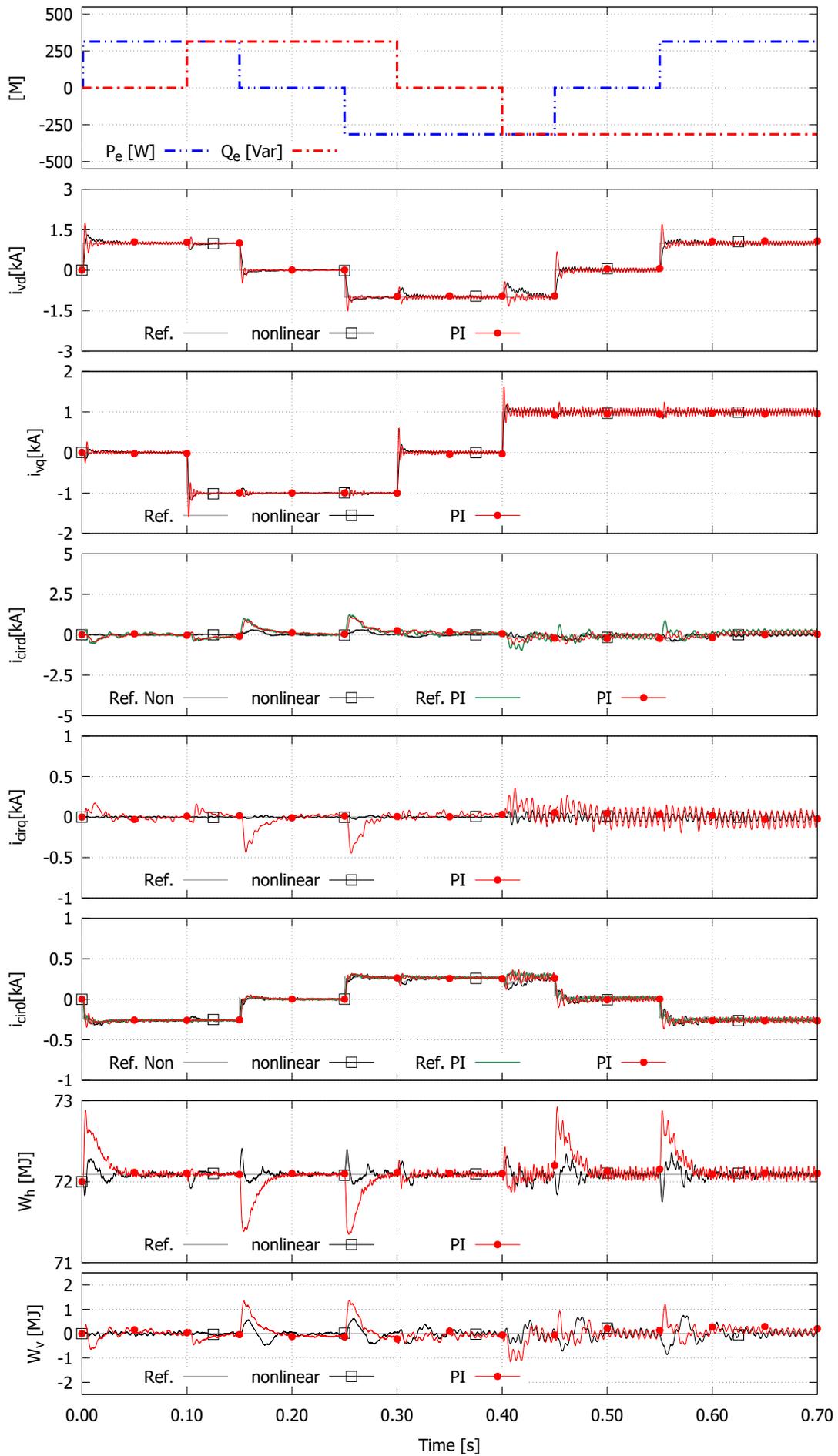


Figure 4.13: Four-quadrant operation of the high voltage system with the nonlinear and PI controller.

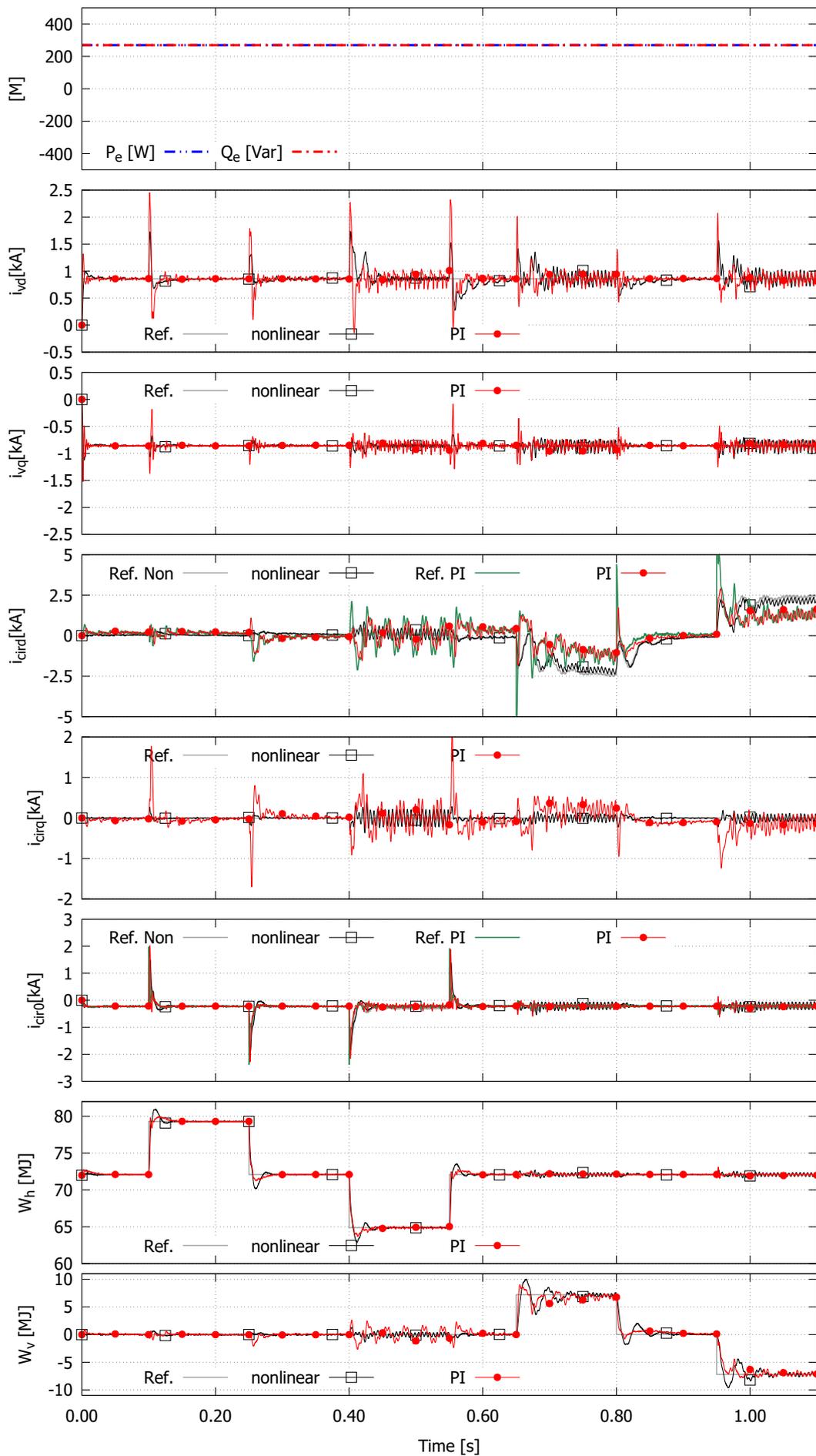


Figure 4.14: State variables response over changes on energy.

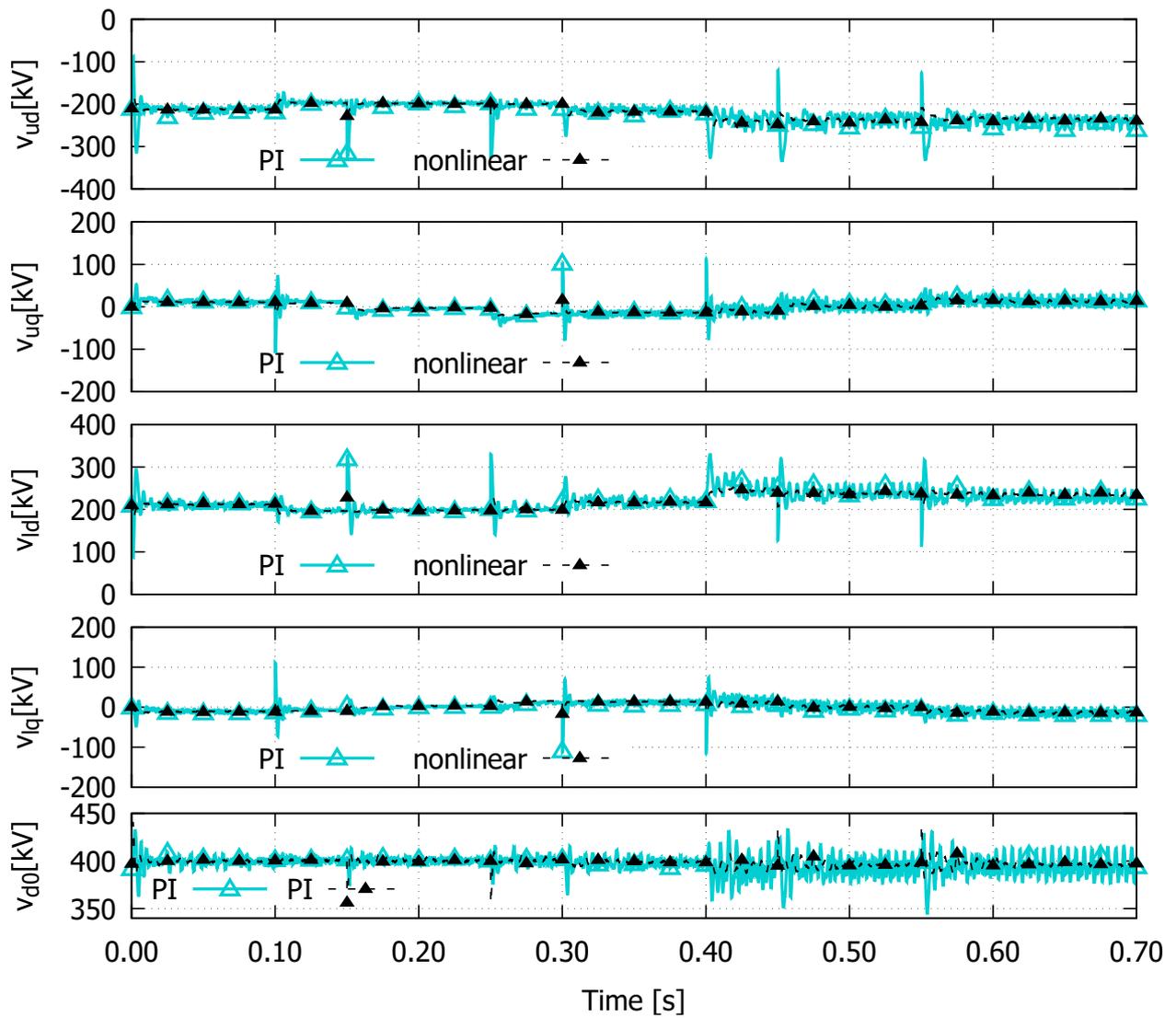


Figure 4.15: Control efforts over power changes.

Source: Author

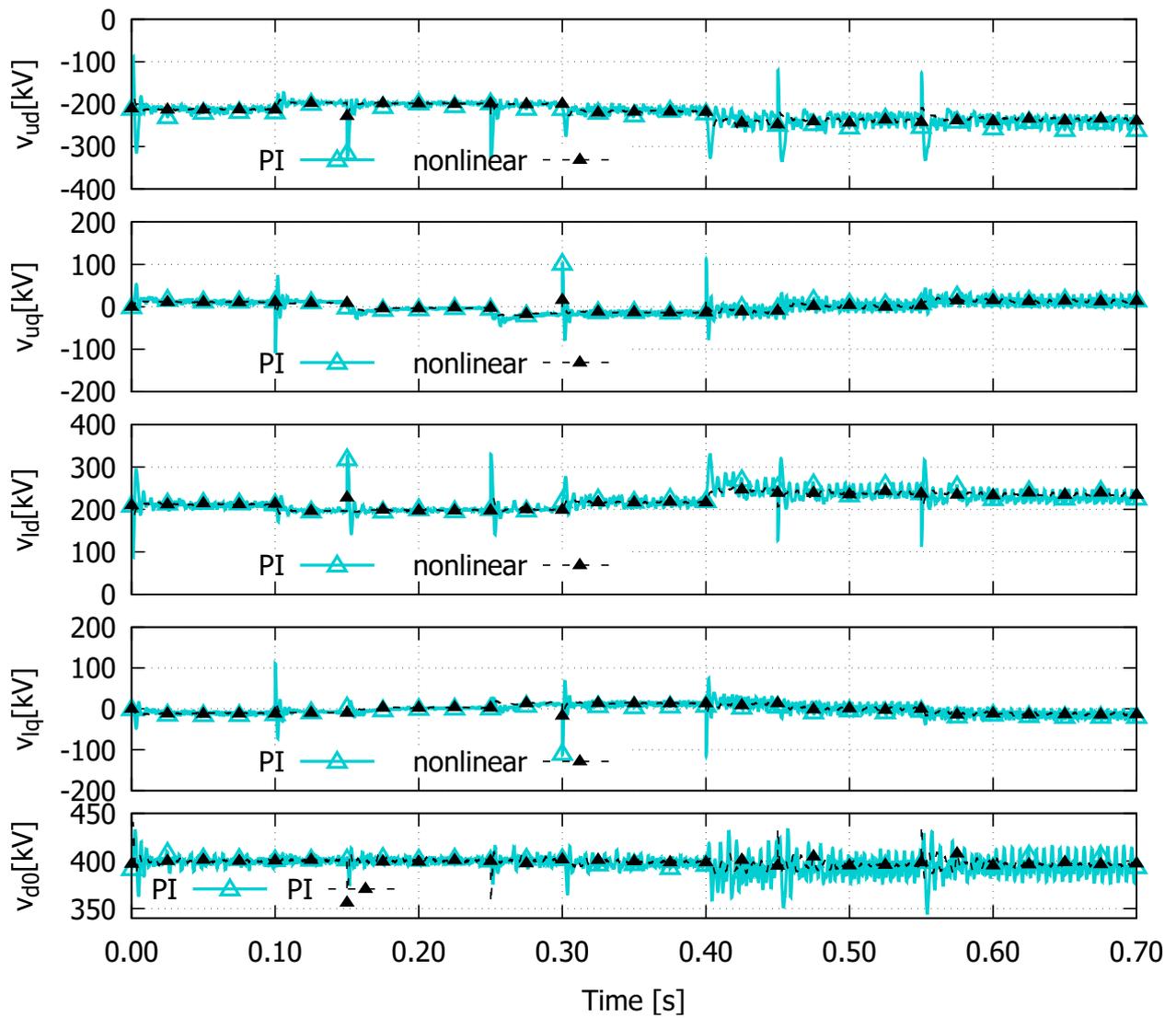


Figure 4.16: Control efforts over energy changes.

Source: Author

Nonlinear control management of internal dynamics As mentioned in chapter 1, there are two main challenges concerning control MMC converters: circulating current management and voltage balancing between arm's capacitors. This section shows how nonlinear controller performs over these challenges.

An operating point is set as $P_e = 315 \text{ MW}$ and $Q_e = 315 \text{ MVar}$ at 0.05 s , and an equal share of energy in the arms is obtained at around $t = 450 \text{ ms}$, as shown in figure 4.17. It is the same convergence speed accomplished by PI controller showed in the previous chapter, figure 4.17.

In figure 4.18, nonlinear controller accomplished the control of total energy in upper (lower) arms. In comparison with PI controller performance (see figure 3.40), the overshoot during the power transient is lower for nonlinear with same convergence speed.

Concerning circulating currents, their performance in dq0 reference frame with the nonlinear controller is presented in figure 4.19. By this result it is possible to conclude that nonlinear controller performs well over the circulating currents, even during changes on the operating point, and have negligible overshoot in comparison with PI controller in figure 3.25.

Figure 4.20 displays the capacitors' voltage attained by nonlinear controller, i.e. the voltage of the twenty SMs in each arm. The figure shows that capacitors' voltages are well balanced and the detail in time between 0.82 s to 0.88 s displays that the sorting algorithm properly switch the SMs. They change the voltage level once per cycle, and are bypassed (keep the voltage for a while). Finally, it is possible to conclude that the nonlinear controller proposed in this thesis can properly balance capacitor's voltage.

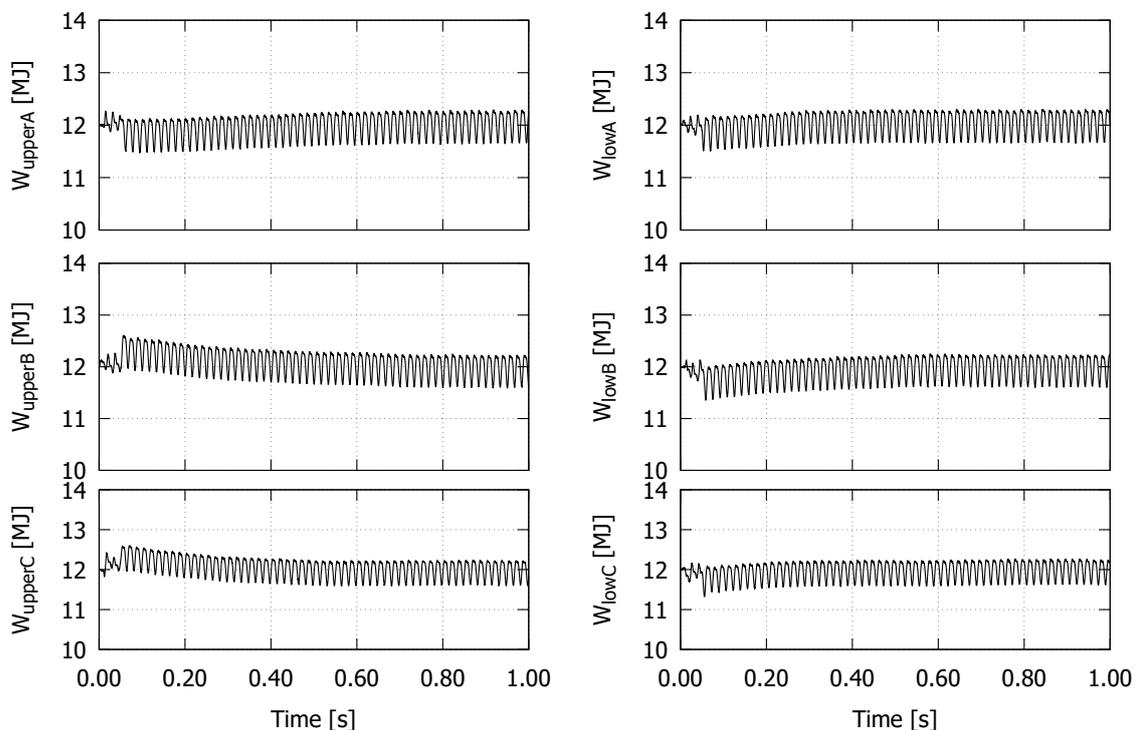


Figure 4.17: Share of energy in each arm with the nonlinear controller.

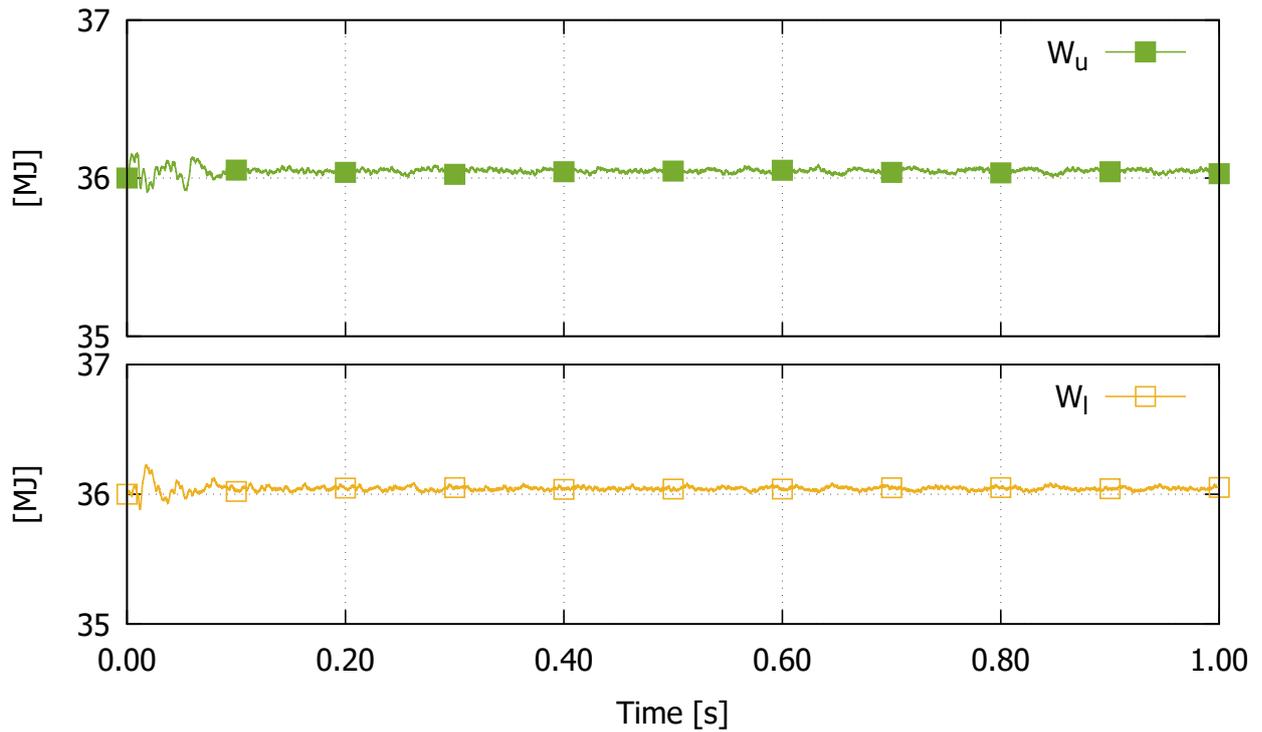


Figure 4.18: Total energy in the three upper arms (W_u) and at the three lower arms (W_l).

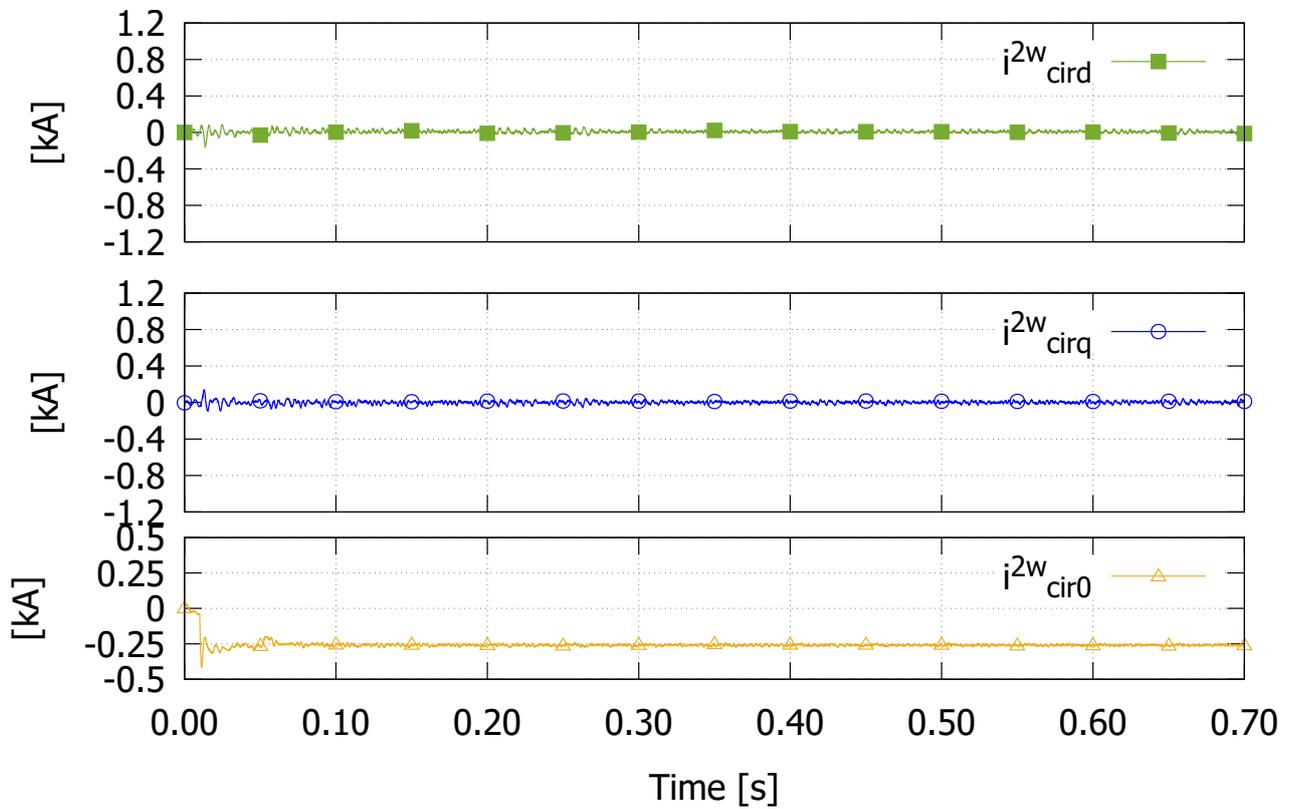


Figure 4.19: Double-fundamental frequency component of circulating currents at high voltage switching model with the nonlinear controller.

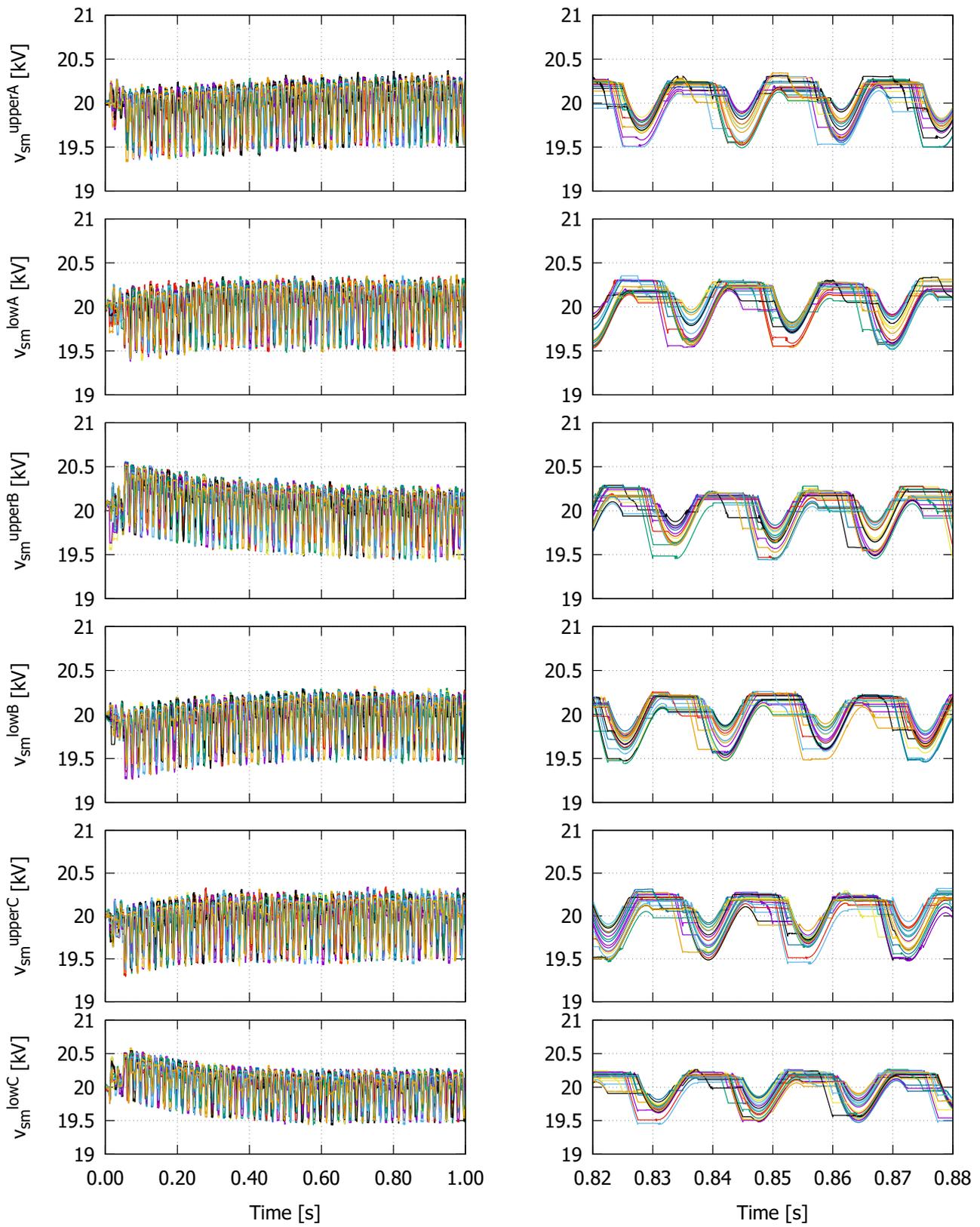


Figure 4.20: SMs' capacitor voltage per arm and equivalent detail in time, accomplished by nonlinear controller.

Source: Author

4.6.2 Robustness over parameters' uncertainties and voltage fluctuation for high-voltage system with nonlinear controller

Robustness This section analyses the control performance under parameters' uncertainties, as first presented in section 3.4.2. In the present simulation scenarios, parameters (R , R_c , L , L_c and C_{SM}) change one at a time from their nominal value to $\pm 10\%$ and $\pm 20\%$. The active and reactive power changes at $t = 0.005$ s and $t = 0.01$ s, respectively.

In figure 4.21 is presented a variation in the arm equivalent resistance R , and in figure 4.22 is presented a variation in AC side resistance. In both cases, the controller is robust over parameter variations. In comparison with the test showed in section 3.5.1, it is possible to see that both PI and nonlinear performs well under parameters' uncertainties.

In figure 4.23 and figure 4.24 there are variations on arms' inductance L and AC side inductance L_c . Both results show tiny deviations during step transients, however it shows high convergence speed for all state variables.

Finally, the controller was more sensitive to changes in SM capacitance, as shown in Figure 4.25. The variations in C were $pm10$ and $pm5$. The state variable i_{vd} , 2^{nd} graphic, has a lower speed of convergence and a larger overshoot. State variables $i_{cir d}$ and $i_{cir q}$ have an oscillating response for an increase C of $+5\%$ and $+10\%$, and slower response for the cases of decreasing C of -5% and -10% . As well, the total energy (W_v) presents the same performance. On the other hand, $i_{cir 0}$ and W_h are well controlled to their desired references.

Voltage fluctuation The performance of the control for voltage's fluctuation is analyzed in this section. P_e and Q_e were settled to 70% of the nominal power, respectively at $t = 0.005$ s and $t = 0.01$ s.

Figure 4.26 shows system's response when voltage at the PCC assumes $\pm 10\%$ and $\pm 5\%$ one at a time. The convergence speed of state variables decreases for the increase in voltage $+10\%$ and $+5\%$. However, they track their reference in a steady-state. On the other hand, circulating currents dq , followed by an energy balancing W_h , present an oscillatory response.

In figure 4.27 states are affected by changes in V_{DC} . States have overshoot and a high speed of convergence.

Moreover, a fluctuation in the AC and DC nominal voltages was performed, and nonlinear control drives, in most cases, the states to their desired value.

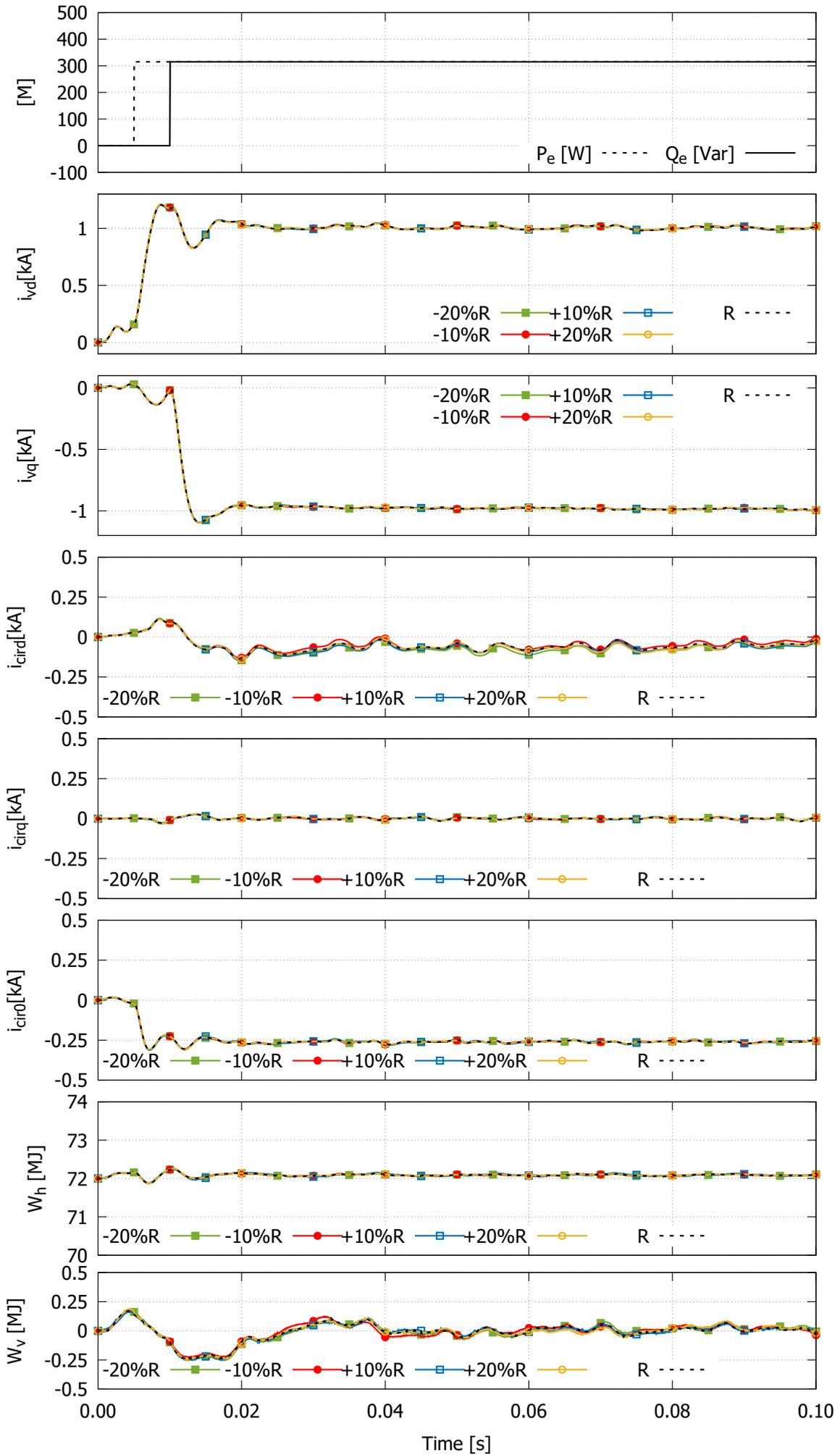


Figure 4.21: The system state over variation of parameter R .

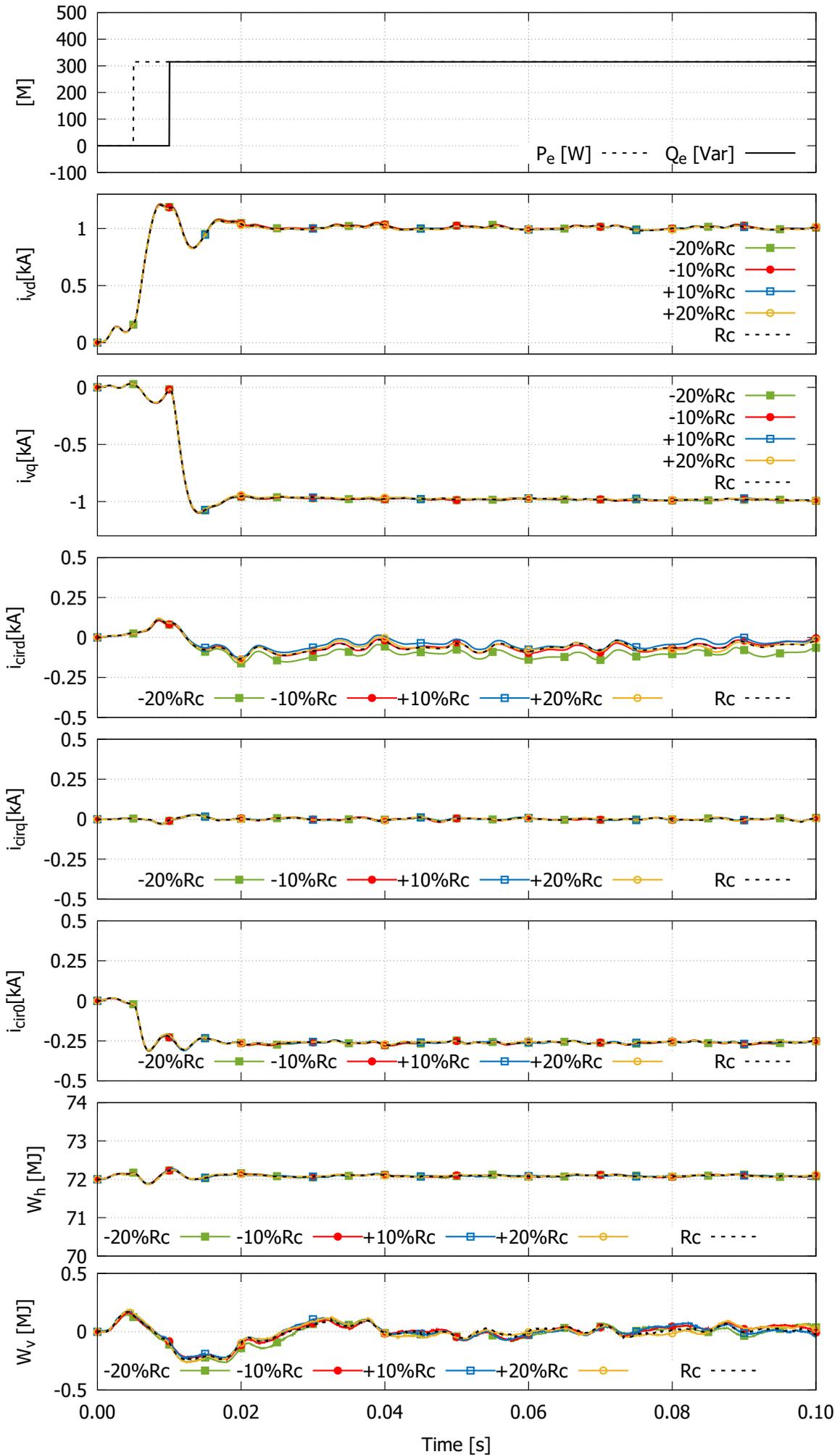
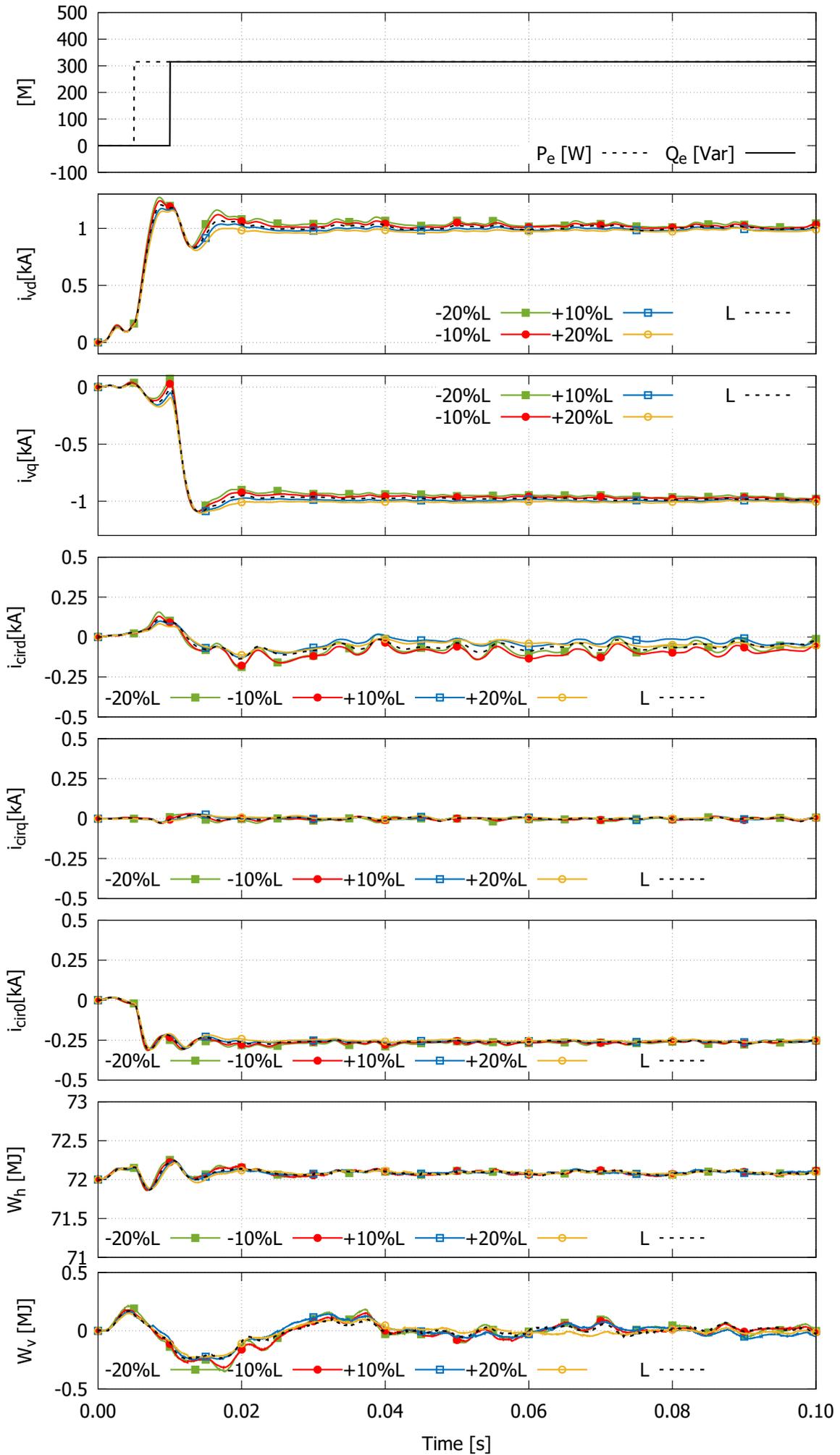


Figure 4.22: States over variation of parameter R_c .

Figure 4.23: States over variation of parameter L .

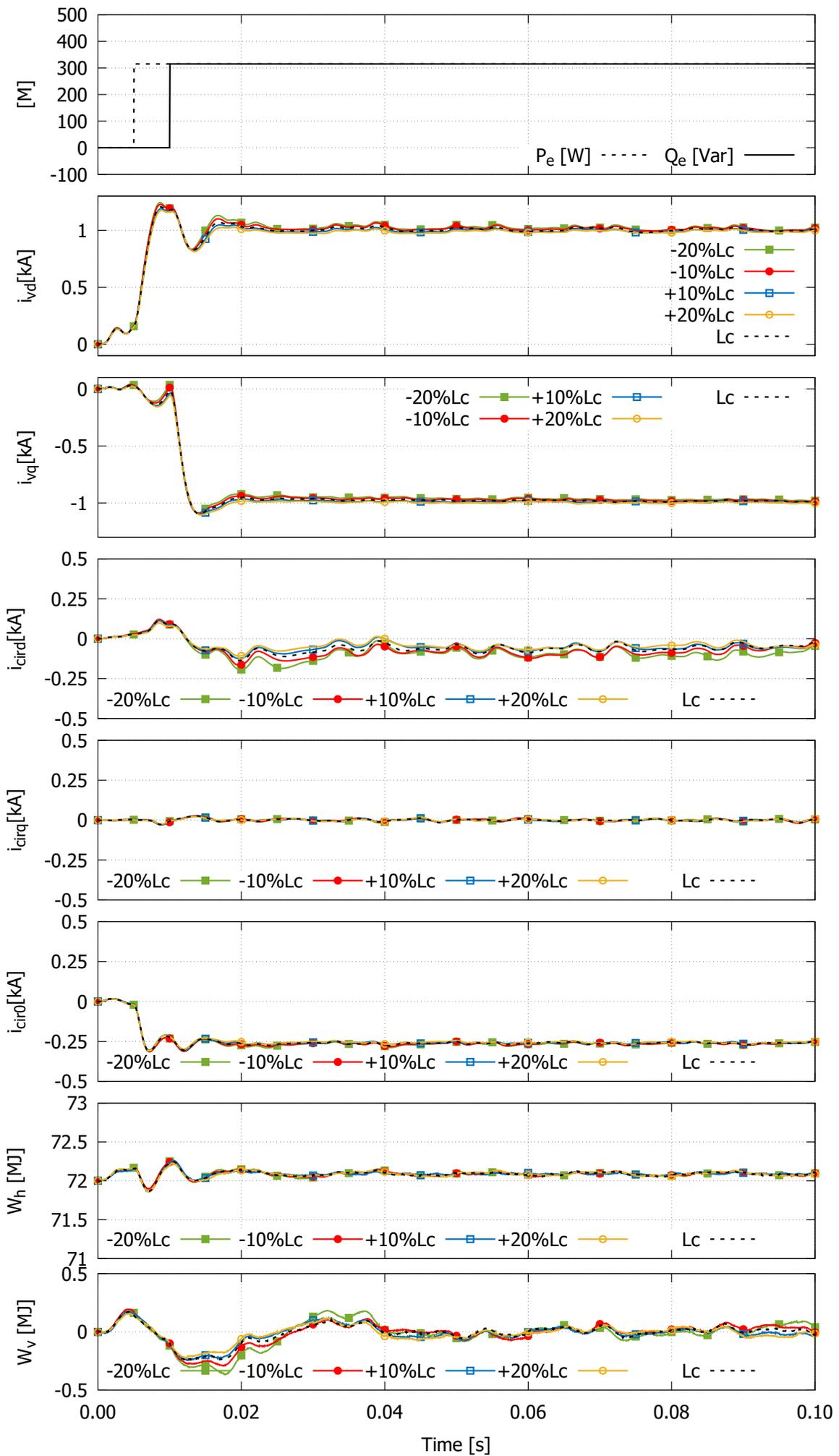


Figure 4.24: States over variation of parameter L_c .

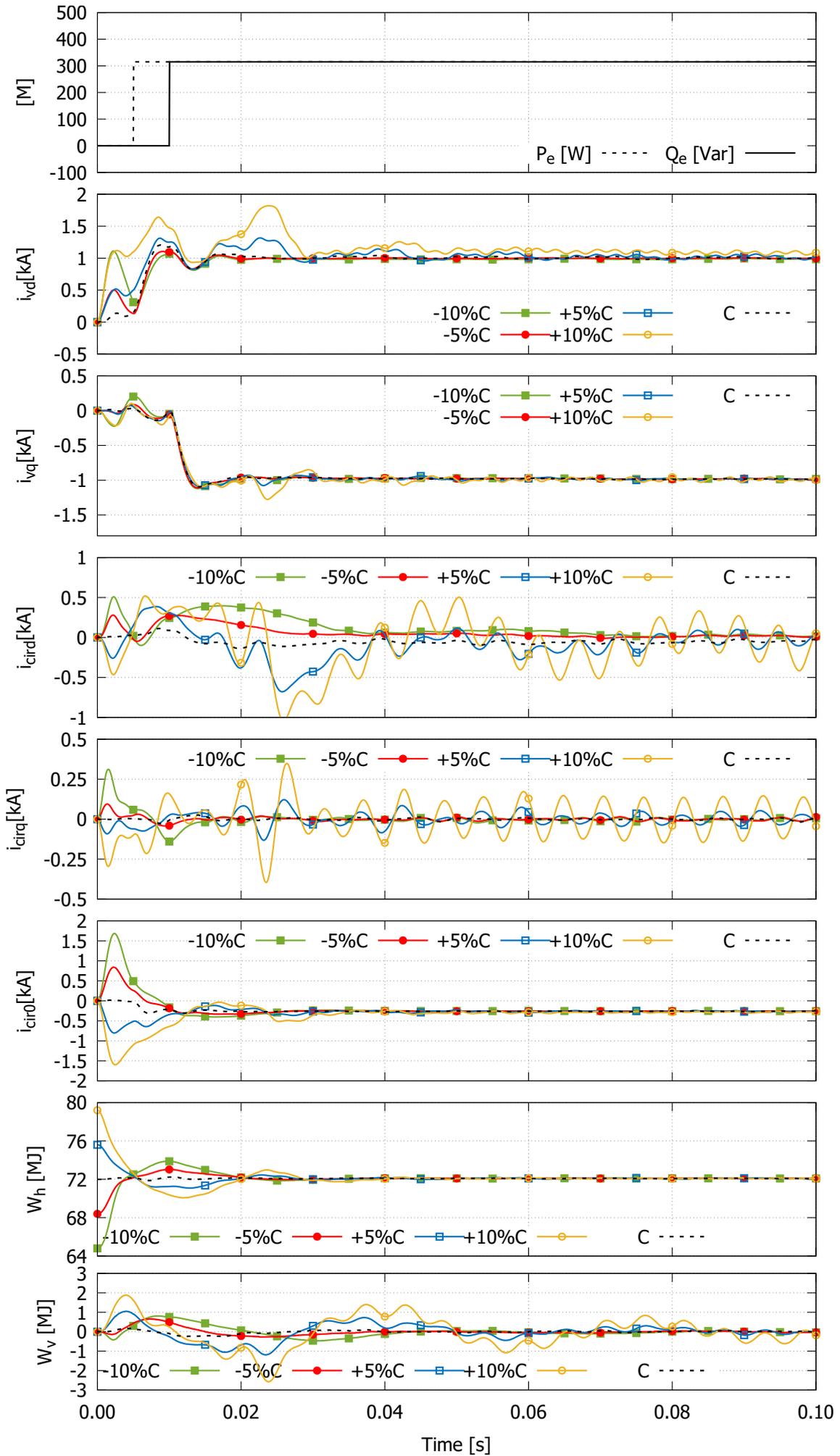


Figure 4.25: States over variation of parameter C .

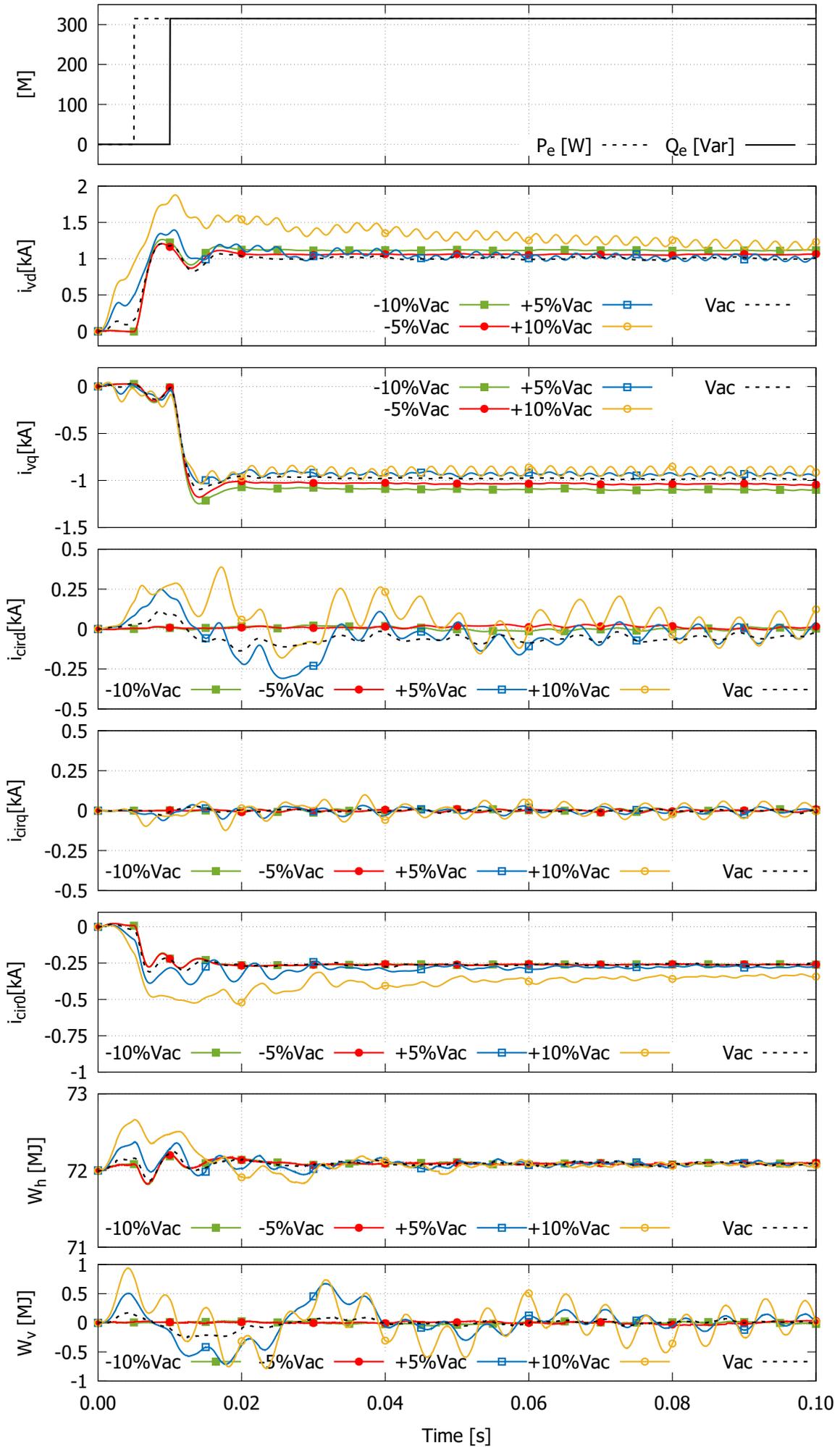
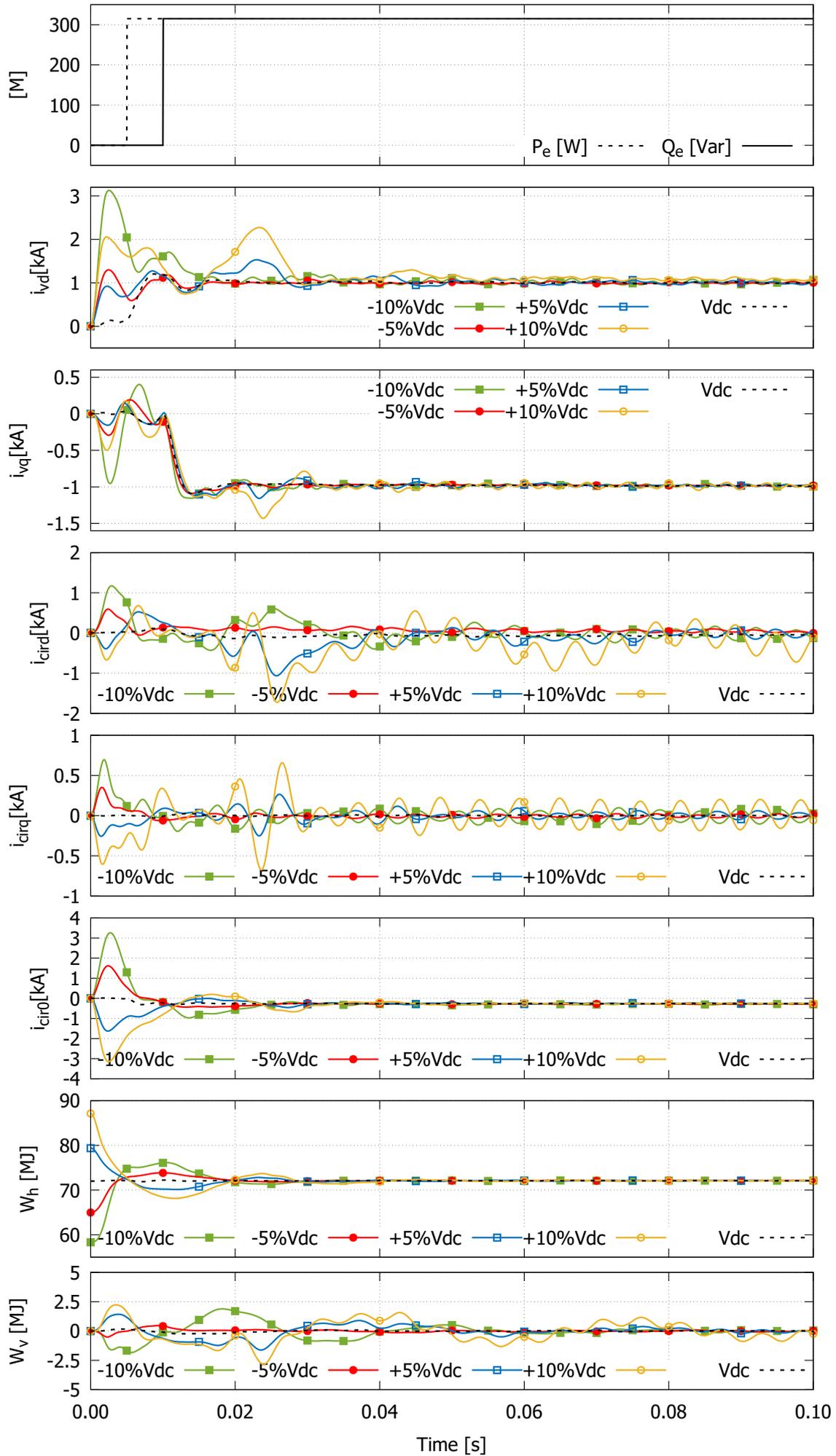


Figure 4.26: Voltage in the PCC changes $\pm 10\%$ and $\pm 5\%$ from the nominal value.

Figure 4.27: DC voltage changes $\pm 10\%$ and $\pm 5\%$ from the nominal value.

4.7 Chapter conclusion

This chapter presented a nonlinear controller for an MMC converter applied for HVDC transmission purposes. The control strategy is designed to control alternating and circulating currents, as well as the converter's stored energy and energy balance. Lyapunov theory is the base to develop the nonlinear control presented in this research, where a rigorous stability analysis is performed to assure proper operation of the grid.

The proposed control performance is tested in a detailed switching MMC model and in average model on the Matlab Simscape Electrical platform. For the proposed control, it is noteworthy that gains are based on the desired state's performances and are straightforward to tune. Moreover, the nonlinear controller has good behavior considering a vast region of operation for the MMC restricted by the system's physical limitations.

Simulations show that the nonlinear controller presents appropriated performance, with small over-signal in transients. The nonlinear control successfully drives the controlled variables to their references, as well as the energy states. The latter being free-dynamics controlled by the designed virtual inputs.

The test of robustness show that nonlinear has a similar performance of PI controller, except for changes in L and L_c at the medium-voltage system with the nonlinear controller. In this case, there is a stationary error in state variables i_{vd} and i_{vq} . This may be solved by tuning nonlinear controller gains.

Chapter 5

Bilinear Quadratic Feedback Control

The present chapter develops a model-based control algorithm for MMCs, including the interesting case of internal energy stabilization. The proposed algorithm is designed following bilinear theory based on quadratic feedback control. The stability of the proposed controller is analyzed through a rigorous procedure based on Lyapunov theory.

Lyapunov's theory is used to formally prove and verify the asymptotic stability for the proposed control, considering the MMC system. This proof is valid for the whole validity region of Lyapunov's function, which has the advantage of allowing an explicit computation of the operation region for the proposed controller [90, 82].

The theoretical results are then evaluated through computer simulations using an MMC average-model and a switching-model in *Simscape Electrical* environment. Furthermore, the chapter accomplishes a comparison with the PI controller presented in chapter 3.

The proposed controller has then shown to control both the converter's currents (circulating and AC) and MMCs' internal energy. The MMC internal dynamics are analysed, as energy per arm, SMs voltage and the double-fundamental frequency component of circulating currents. At last, robustness tests over parameter uncertainties and voltage fluctuation is carried out for the proposed bilinear controller.

The system used in this chapter is the one shown in the system of equations 2.36, and the equilibrium points for state variables and control inputs comes from section 3.1. The system can be summarized as follows:

State vector

$$x = [i_{vd} \ i_{vq} \ i_{cir d} \ i_{cir q} \ i_{cir 0} \ W_h \ W_v]^T$$

Control input

$$u = [v_{ud} \ v_{uq} \ v_{ld} \ v_{lq} \ v_{d0}]^T$$

Bilinear form The MMC system, with state and input vectors defined above, can be re-written in the standard bilinear form:

where, considering $\rho = 5$ for the 5 inputs, to represent a three phase MMC:

$$A = \begin{bmatrix} -\frac{R_{eq}}{L_{eq}} & \omega & 0 & 0 & 0 & 0 & 0 \\ -\omega & -\frac{R_{eq}}{L_{eq}} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{R}{L} & \omega & 0 & 0 & 0 \\ 0 & 0 & -\omega & -\frac{R}{L} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -\frac{R}{L} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$B_1 = \begin{bmatrix} 0 & 0 & 0 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & \dots & 0 \\ -\frac{3}{4} & 0 & \frac{3}{2} & 0 & \dots & 0 \\ -\frac{3}{4} & 0 & \frac{3}{2} & 0 & \dots & 0 \end{bmatrix}$$

$$B_2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \end{bmatrix}$$

$$B_3 = \begin{bmatrix} 0 & 0 & 0 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & \dots & 0 \\ \frac{3}{4} & 0 & -\frac{3}{2} & 0 & \dots & 0 \\ -\frac{3}{4} & 0 & -\frac{3}{2} & 0 & \dots & 0 \end{bmatrix}$$

$$B_4 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{3}{4} & 0 & \frac{3}{2} & 0 & 0 & 0 \\ 0 & -\frac{3}{4} & 0 & -\frac{3}{2} & 0 & 0 & 0 \end{bmatrix}$$

$$B_5 = \begin{bmatrix} 0 & \dots & 0 & 0 & 0 & 0 \\ \vdots & \ddots & \vdots & \vdots & 0 & 0 \\ 0 & \dots & 0 & 0 & 0 & 0 \\ 0 & \dots & 0 & 3 & 0 & 0 \\ 0 & \dots & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$b_1 = \left[\frac{1}{L_{eq}} \quad 0 \quad -\frac{1}{2L} \quad 0 \quad 0 \quad 0 \quad 0 \right]^T$$

$$b_2 = \left[0 \quad \frac{1}{L_{eq}} \quad 0 \quad -\frac{1}{2L} \quad 0 \quad 0 \quad 0 \right]^T$$

$$b_3 = \left[-\frac{1}{L_{eq}} \quad 0 \quad -\frac{1}{2L} \quad 0 \quad 0 \quad 0 \quad 0 \right]^T$$

$$b_4 = \left[0 \quad -\frac{1}{L_{eq}} \quad 0 \quad -\frac{1}{2L} \quad 0 \quad 0 \quad 0 \right]^T$$

$$b_5 = \left[0 \ 0 \ 0 \ 0 \ -\frac{1}{2L} \ 0 \ 0 \right]^T$$

$$z = \left[\frac{2v_{f,d}}{L_{eq}} \ \frac{2v_{f,q}}{L_{eq}} \ 0 \ 0 \ \frac{V_{DC}}{2L} \ 0 \ 0 \right]^T$$

5.1 Bilinear Control Theory

The MMCs, as the majority of power electronic converters, can be represented by a bilinear model [91]. The control inputs are multiplied by the states as shows equation (2.36). Considering a bilinear system in which the state variables are $x \in \mathbb{R}^n$, and the input variables are $u \in \mathbb{R}^\rho$.

5.1.1 Bilinear System Stability - a general case

There are several ways to study the stability of bilinear systems [83]. However, a direct way to prove stability is to apply standard Lyapunov theory [92, 80].

The goal is to find a positive definite Lyapunov function candidate V_g , whose time derivative will be negative definite. Therefore, the candidate $V_g : \mathbb{R}^n \rightarrow \mathbb{R}$ could be defined as a quadratic function as:

$$V_g(x) = x^T P_e x \quad (5.1)$$

Firstly, in a general case, it is sufficient to obtain a positive definite matrix $P_e \in \mathbb{R}^{n \times n}$, in order to prove the first condition for the candidate function. Next, the proof of stability is obtained by the derivation of the Lyapunov function:

$$\begin{aligned} \dot{V}_g(x) &= \dot{x}^T P_e x + x^T P_e \dot{x} \\ &= (Ax + \sum_{k=1}^{\rho} B_k u_k x + b_k u_k)^T P_e x + x^T P_e (Ax + \sum_{k=1}^{\rho} B_k u_k x + b_k u_k) \\ &= x^T [A^T P_e + P_e A] x + 2x^T P_e \sum_{k=1}^{\rho} u_k (B_k x + b_k) \end{aligned} \quad (5.2)$$

where $(B_k u_k x + b_k u_k)^T P_e x = x^T P_e (B_k x + b_k) u_k$.

Now, we use the control law $u_k = -\alpha [B_k x + b_k]^T P_e x$, and the further assumptions that for $k = 1, \dots, \rho$, it is true that $(B_k x + b_k)^T P_e x \neq 0 \ \forall x \neq 0$ and that $x^T [A^T P_e + P_e A] x \leq 0$, see [82]. So, equation (5.2) in closed loop will be:

$$\begin{aligned} \dot{V}_g(x) &\leq -\Phi \|x\|^2 - 2\alpha \sum_{k=1}^{\rho} (x^T P_e (B_k x + b_k))^2 \\ \dot{V}_g(x) &< 0 \end{aligned} \quad (5.3)$$

where the constant $-\Phi = \lambda_{\min}(A^T P_e + P_e A)$ is smaller or equal than zero.

Considering $\alpha > 0$, Lyapunov's theory assures that if the derivative of Lyapunov's function is always strictly negative (negative definite), then the full system is asymptotically stable.

5.1.2 Bilinear System Stability: studied case

Following [90], with the purpose of maintaining the state variable x on a desired operation point \bar{x} , it is performed a change of variables:

$$x \stackrel{\Delta}{=} \tilde{x} + \bar{x}$$

$$u \stackrel{\Delta}{=} \tilde{u} + \bar{u}$$

Changing the variables in equation (2.36), one obtains (5.4).

$$\dot{\tilde{x}} + \dot{\bar{x}} = A(\tilde{x} + \bar{x}) + \sum_{k=1}^{\rho} \{(\tilde{u}_k + \bar{u}_k)(B_k(\tilde{x} + \bar{x}) + b_k)\} + z \quad (5.4)$$

As in the equilibrium point the error between state and their reference is zero ($\tilde{x} = 0$), equation (5.4) can be rewritten into two parts: 1) terms with only the equilibrium states and inputs, that are regrouped in equation (5.5), and 2) remainder terms shown in equation (5.6).

$$\dot{\tilde{x}} = A\bar{x} + \sum_{k=1}^{\rho} \bar{u}_k(B_k\bar{x} + b_k) + z = 0 \quad (5.5)$$

and then:

$$\dot{\tilde{x}} = A\tilde{x} + \sum_{k=1}^{\rho} \bar{u}_k B_k \tilde{x} + \sum_{k=1}^{\rho} (B_k \tilde{x} + B_k \bar{x} + b_k) \tilde{u}_k. \quad (5.6)$$

The evolution of the error states is analysed by the Lyapunov function and its derivative:

$$V(\tilde{x}) = \tilde{x}^T P_e \tilde{x} \quad (5.7)$$

$$\dot{V}(\tilde{x}) = \underbrace{\tilde{x}^T (\tilde{A}^T P_e + P_e \tilde{A}) \tilde{x}}_{1^{st} \text{ Term}} + 2 \underbrace{\left[\sum_{k=1}^{\rho} \tilde{u}_k (B_k \tilde{x} + B_k \bar{x} + b_k) \right]^T P_e \tilde{x}}_{2^{nd} \text{ Term}} \quad (5.8)$$

where: $\tilde{A} = A + \sum_{k=1}^{\rho} \bar{u}_k B_k$. Now we propose the control law:

$$\tilde{u}_k = -\alpha_k [B_k \tilde{x} + B_k \bar{x} + b_k]^T P_e \tilde{x} \quad (5.9)$$

$$u_k = \tilde{u}_k + \bar{u}_k \quad (5.10)$$

Remark 02 Due to the MMC model characteristics (shape of A matrix), not all state variables are present in the first part of equation (5.8). In this way, this part of the Lyapunov's function derivative would only be negative semi-definite. Consequently, its second part will provide the convergence of the remaining states.

Acknowledging these facts, the following procedure based on Lemma 1 of [93] is necessary to design the controller, and access the stability properties of the closed-loop system.

Matrix $\tilde{A} \in \mathbb{R}^{n \times n}$ has two zero eigenvalues: $\lambda_{n-1}(\tilde{A}) = 0$ and $\lambda_n(\tilde{A}) = 0$, such that \tilde{A} admits the Jordan decomposition: $\tilde{A} = U \Lambda U^{-1}$, where $U \in \mathbb{C}^n$ is non-singular and Λ is a diagonal Jordan matrix of \tilde{A} . Considering $\Lambda_R := \text{diag}(\Re(\Lambda_i))$ for all $i \in [1, n-2]$,

then since $\Re(\lambda_i) < 0 \forall i \in [1, n-2]$, there exists a matrix $\Gamma_R \in \mathbb{R}^{n-2 \times n-2}$, symmetric and positive definite, such that $\Gamma_R \Lambda_R + \Lambda_R^T \Gamma_R = -\Phi$, where the diagonal matrices $\Phi \in \mathbb{R}^{n-2 \times n-2}$ and $\Gamma \in \mathbb{R}^{n \times n}$ are positive definite, and constants $\Gamma_1, \Gamma_2 > 0$ as follows:

$$\Phi := \begin{bmatrix} \Phi_1 & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & \Phi_{n-2} \end{bmatrix} \quad (5.11)$$

$$\Gamma := \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & \ddots & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & \Gamma_1 & 0 \\ 0 & 0 & 0 & 0 & \Gamma_2 \end{bmatrix} \quad (5.12)$$

Solving the equation $\Gamma \Lambda + \Lambda^* \Gamma = -Q$, where:

$$Q := \begin{bmatrix} \Phi_1 & 0 & 0 & 0 & 0 \\ 0 & \ddots & 0 & 0 & 0 \\ 0 & 0 & \Phi_{n-2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (5.13)$$

Then, $P_e = U \Gamma U^{-1}$ is Hermitian positive definite since Γ is symmetric positive definite and U^{-1} has full rank, as presented in [93]. It implies that $V(x)$ is a real positive definite function. Next, the derivative of the Lyapunov function, $\dot{V}(\tilde{x})$ is evaluated as:

$$\dot{V}(\tilde{x}) = - \sum_{c=1}^{n-2} \Phi_c \|\tilde{x}_c\|^2 - 2 \left(\sum_{k=1}^{\rho} \alpha_k ((B_k \tilde{x} + B_k \bar{x} + b_k)^T P_e \tilde{x})^2 \right) \quad (5.14)$$

where we can show that $\dot{V}(\tilde{x}) < 0, \forall \tilde{x} \neq 0$.

Theorem 1 *The MMC converter described by the system of equations (2.36), with the bilinear control law described in equation (5.9), and with desired equilibrium point satisfying equation (5.5) and the assumption that for $k = 1, \dots, \rho$, it is truth that $(B_k \tilde{x} + b_k)^T P_e \tilde{x} \neq 0 \forall \tilde{x} \neq 0$, will be asymptotically stabilized to this equilibrium point.*

The proof is standard and is obtained under the positive definite Lyapunov function (5.7) of the error system, in which closed-loop derivative (5.14) is negative definite. Then, by Lyapunov theory, the considered equilibrium point is asymptotically stable.

In order to use the bilinear control defined above, the references for the state variables (see previous chapter) and the steady state inputs must be derived from the desired outputs. Consequently, equation (5.5) is solved to obtain the input reference values (\bar{u}_k) on the equilibrium as equation (5.15), for $c \in [1, n-2]$.

$$\begin{bmatrix} \bar{u}_1 \\ \bar{u}_2 \\ \bar{u}_3 \\ \bar{u}_4 \\ \bar{u}_5 \end{bmatrix} = \begin{bmatrix} \frac{R_{eq}}{2} & -\omega \frac{L_{eq}}{2} & -R & w & 0 \\ \omega \frac{L+L_c}{2} & \frac{R_{eq}}{2} & -\omega L & -R & 0 \\ -\frac{R_{eq}}{2} & \omega \frac{L+L_c}{2} & -R & \omega & 0 \\ -\omega \frac{L+L_c}{2} & -\frac{R_{eq}}{2} & -\omega L & -R & 0 \\ 0 & 0 & 0 & 0 & -2R \end{bmatrix} \begin{bmatrix} \bar{x}_1 \\ \bar{x}_2 \\ \bar{x}_3 \\ \bar{x}_4 \\ \bar{x}_5 \end{bmatrix} + \begin{bmatrix} -v_{fd} \\ -v_{fq} \\ v_{fd} \\ v_{fq} \\ v_{DC} \end{bmatrix} \quad (5.15)$$

Figure 5.1 summarize by a block diagram the implemented bilinear controller.

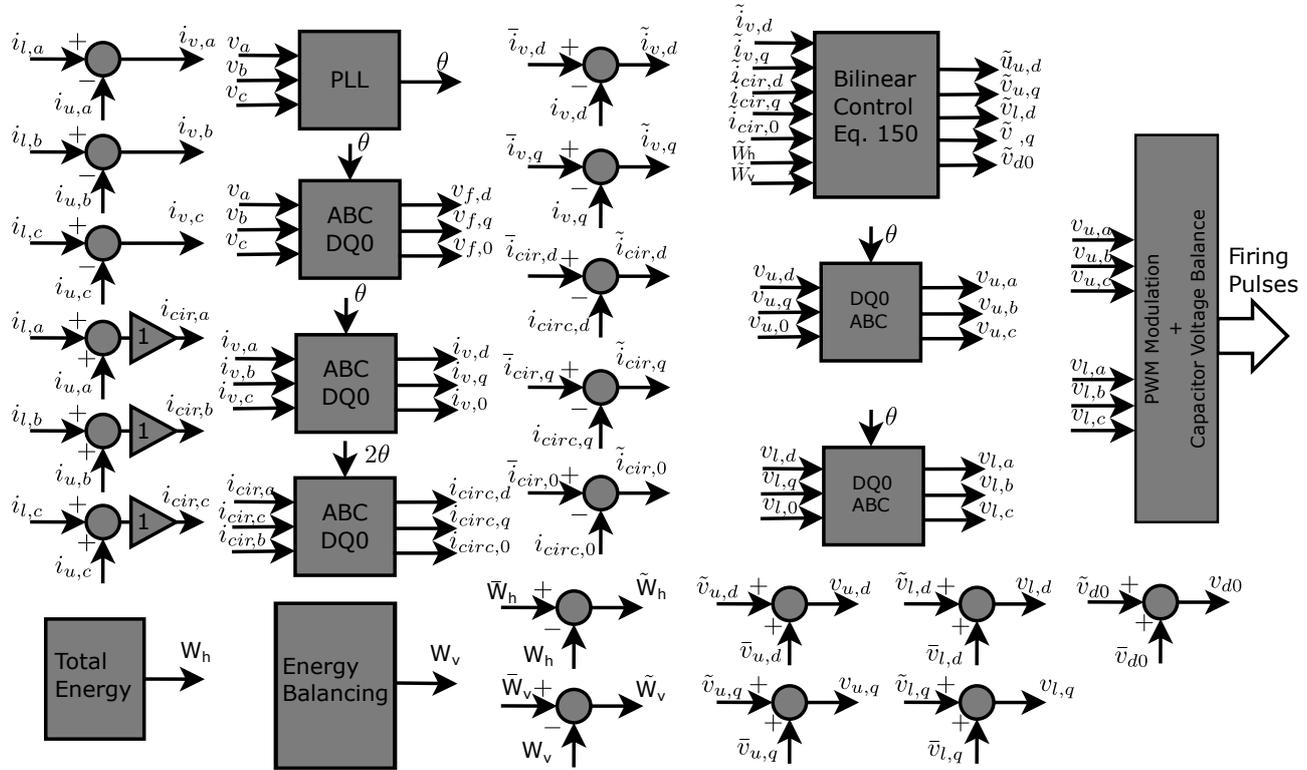


Figure 5.1: Diagram of bilinear controller.

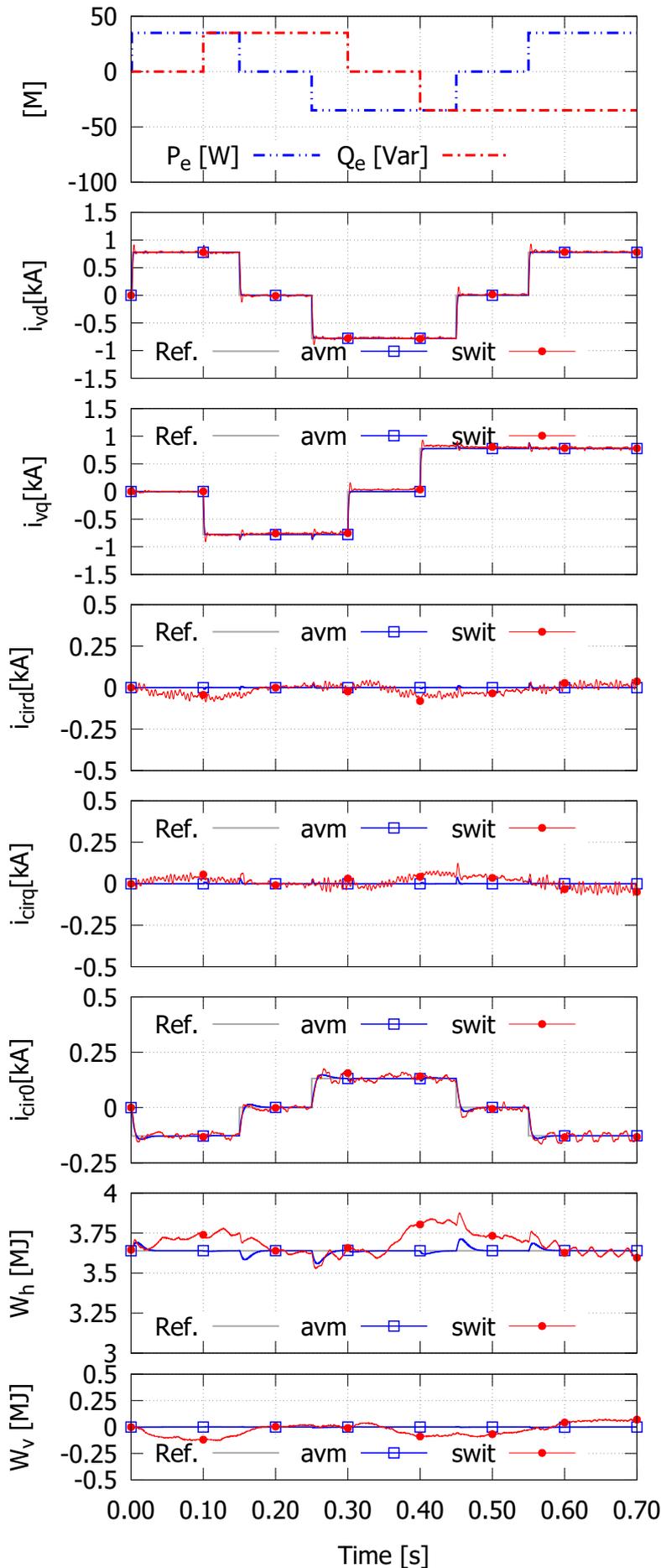
Source: Author

The dynamic performance of the proposed bilinear control strategy applied to an MMC average model is verified by computer simulations using the *Matlab/Simulink* environment. The medium-voltage system is used and the controller gains are presented in Table 5.1. The suitable feedback gains were elected by a trade-off between speed of convergence and overshoot.

Table 5.1: Parameters of simulated system and bilinear control's gains.

Parameter	Value	Parameter	Value
S_{MMC}	50 MVA	α_1	0.5
V_{AC}	30 kV	α_2	0.5
V_{DC}	180 kV	α_3	0.5
L_c	5 mH	α_4	0.5
L	14 mH	α_5	0.5
R_c	0.03 Ω	Γ_1	1
C_{SM}	3 mF	Γ_2	1
Freq	60 Hz	Φ_c	1
R	0.5 Ω		
N	20		

Figure 5.2: Four-quadrant operation for medium-voltage system with bilinear controller.



Four-quadrant operation of the medium-voltage system with bilinear controller. In figure 5.2 eight operating points are performed. A detailed switching-model and an average-model are simulated with bilinear controller.

Bilinear performs well for each new operation point in both models. AC current i_{vd} and i_{vq} (2nd and 3rd graphic) present overshoot for switching-model while average-model doesn't.

The dq components of circulating current present a low speed of convergence by the switching-model. This is the result of a slow dynamic of the energy control. In total energy W_h and energy balancing W_v (7th and 8th graphics).

Figure 5.3: Energy change for medium-voltage system with bilinear controller.

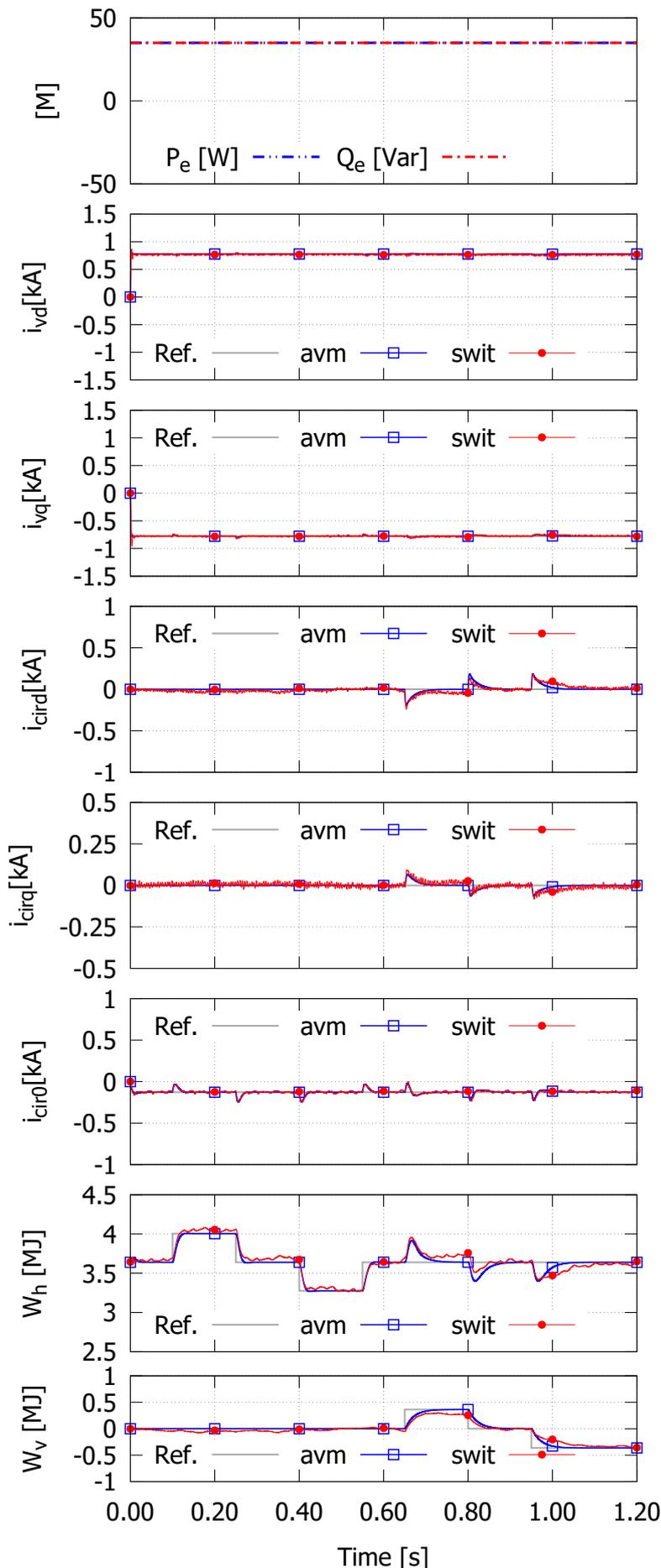


Figure 5.4 shows the voltage balancing attained by the MMC with bilinear con-

Energy change for medium-voltage system with average-model and switching-model with bilinear controller. In figure 5.3 P_e and Q_e are set to 70% of nominal power. Average and switching-model are simulated.

A change in total energy is performed at 0.10 s. Concerning state variable W_h there is no overshoot to track the new reference for both models, however a slow speed of convergence for switching-model is observed. Only state variable i_{cir0} momentarily left its reference to steer total energy to the new reference. The same behaviour is seen for all changes in W_h .

It is possible to observe that the i_{cir0} reference (\bar{i}_{cir0}) comes from equation (3.24). It is different from PI and non-linear controllers, where the desired value of i_{cir0} consider the error on total energy W_h . However, the bilinear control illustrates that this behaviour comes from the fact that input and output power (which are directly linked to W_h) are managed by i_{cir0} , what justify the control strategy used on PI and non-linear control design.

trol. It is possible to observe that balancing is achieved in 1.5 s. In comparison with PI and nonlinear, the bilinear control has a slower response. However, this is directly linked with the slower convergence of energy W_v . The energy per arm, shown in figure 5.5 is also affected and result in a slower convergence, in comparison with the PI and nonlinear.

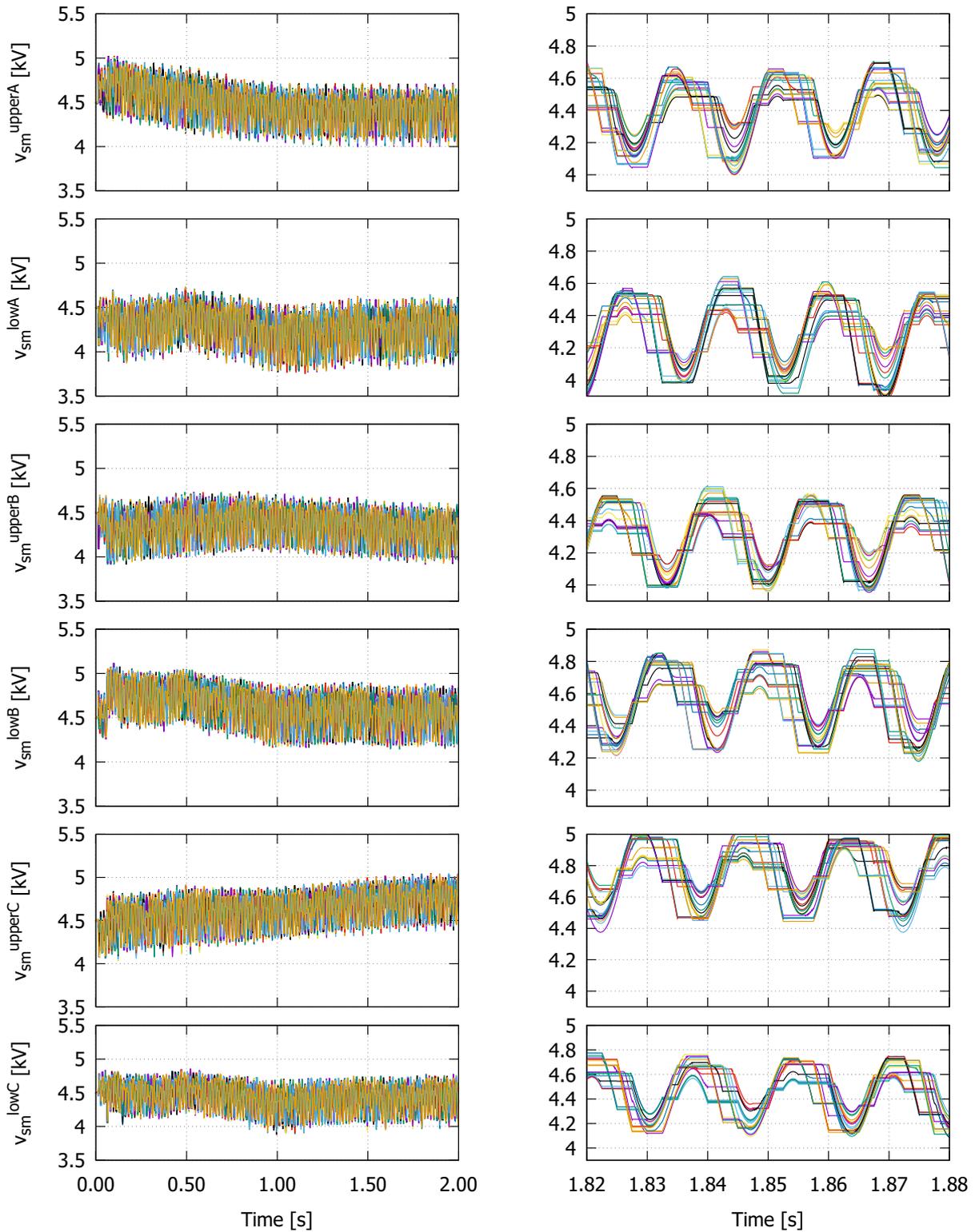


Figure 5.4: SMs voltage balancing per arm with the bilinear control.

Source: Author

Figure 5.6 shows the total energy in upper (lower) arms, using bilinear control. The result achieved differs from the previous controllers once it has an oscillating and slower response.

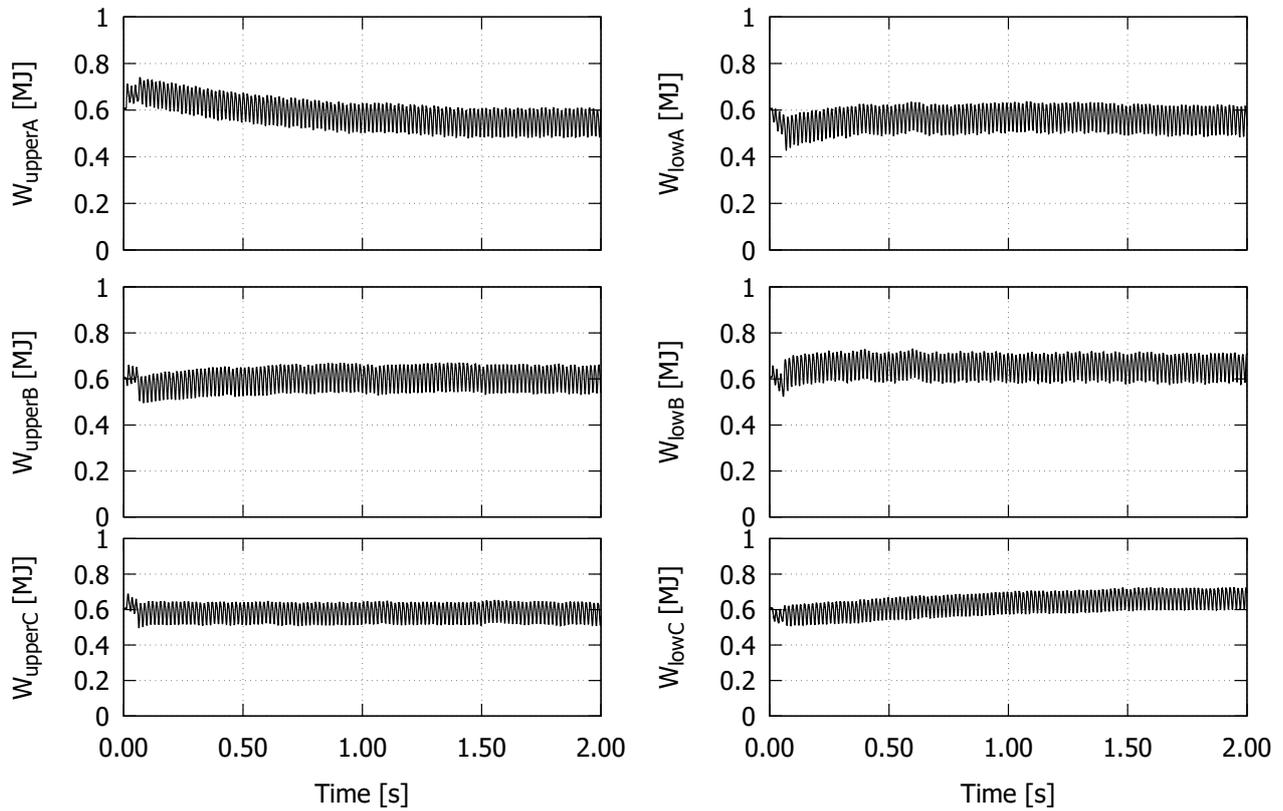


Figure 5.5: Energy per arm of MMC with the bilinear.

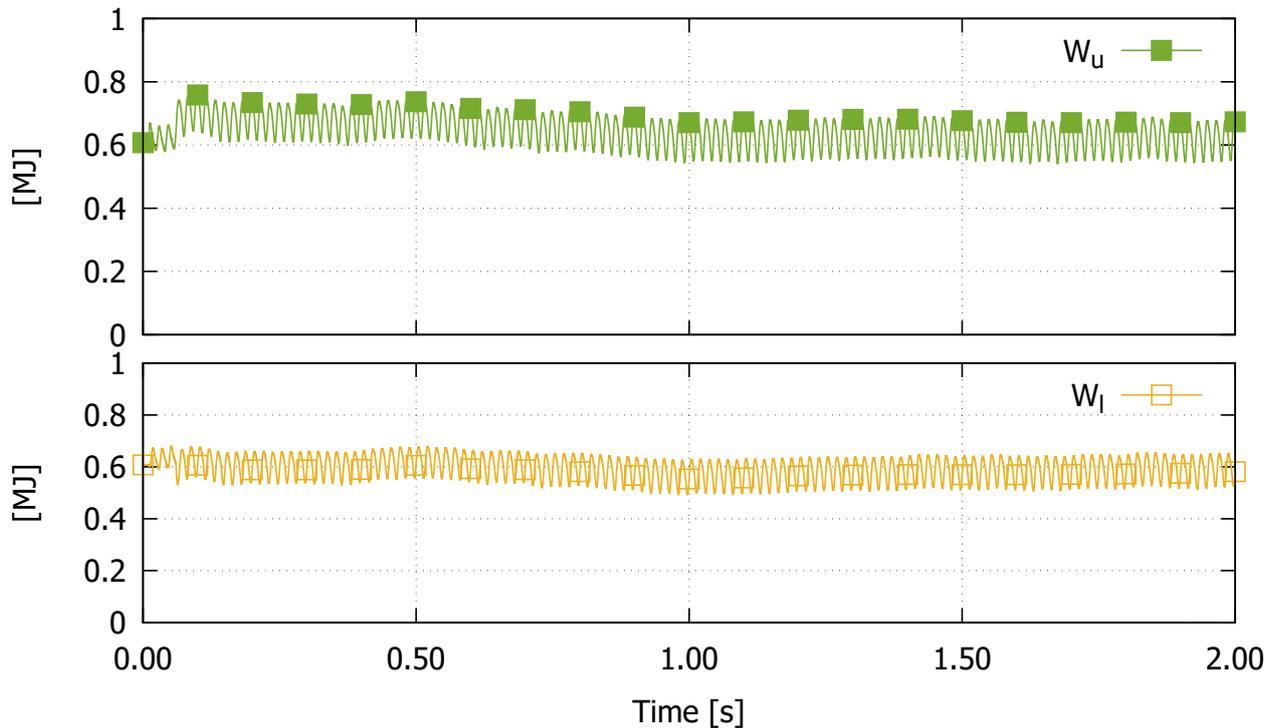


Figure 5.6: Total energy in upper (lower) arms using bilinear controller.

Bilinear controller is able to manage the double-fundamental frequency of circulating currents, as shown at figure 5.7.

Figure 5.8 shows PI and bilinear controllers with four-quadrants operation. The convergence speed for AC currents (i_{vd} and i_{vq}) is high for both controllers, and they present low over-shoot. At 4th graphic, PI follow their reference, and bilinear experienced a slow convergence. In the same way, PI has a higher convergence speed than bilinear for state variable i_{cirq} . Regarding i_{cir0} , both controllers drive

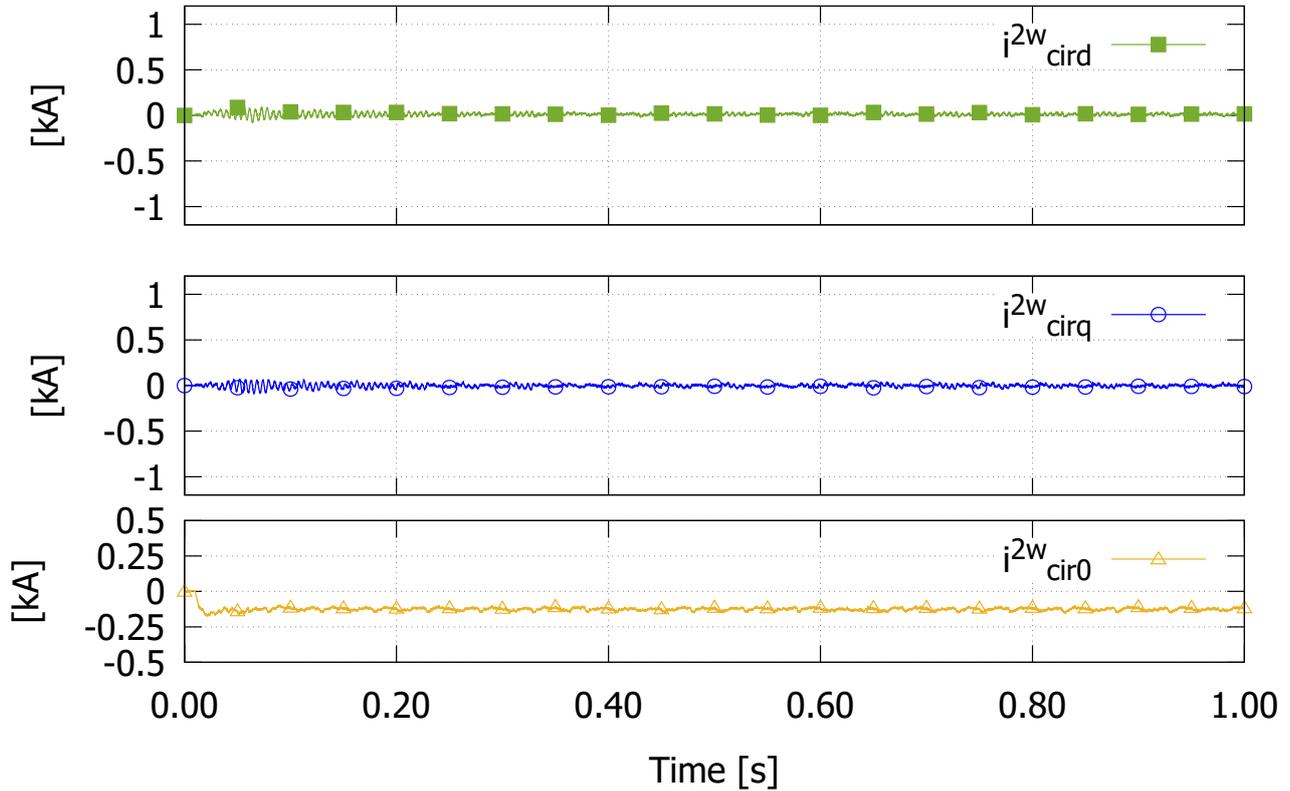


Figure 5.7: Double-fundamental frequency of circulating current with bilinear controller.

the state variable to its desired value. 7th graph shows the total energy of the MMC. As previously mentioned, the convergence speed of state variable W_h with the bilinear controller is linked with gains Γ and Φ . Additionally, state variables are strongly linked, if Γ and Φ are large, larger over-shoot is seen in the other state variables. As a result, changes in P_e and Q_e hinder W_h to reach its reference.

However, the outcome mentioned above does not imply in the speed of convergence for energy changes, as presented in figure 5.9, at the 7th graphic. Here bilinear and PI have similar convergence for total energy changes W_h and energy balancing W_v . Additionally, state variable W_v deals with over-shoot (at 0.65 s, 0.80 s and 0.95 s) for changes in energy balancing.

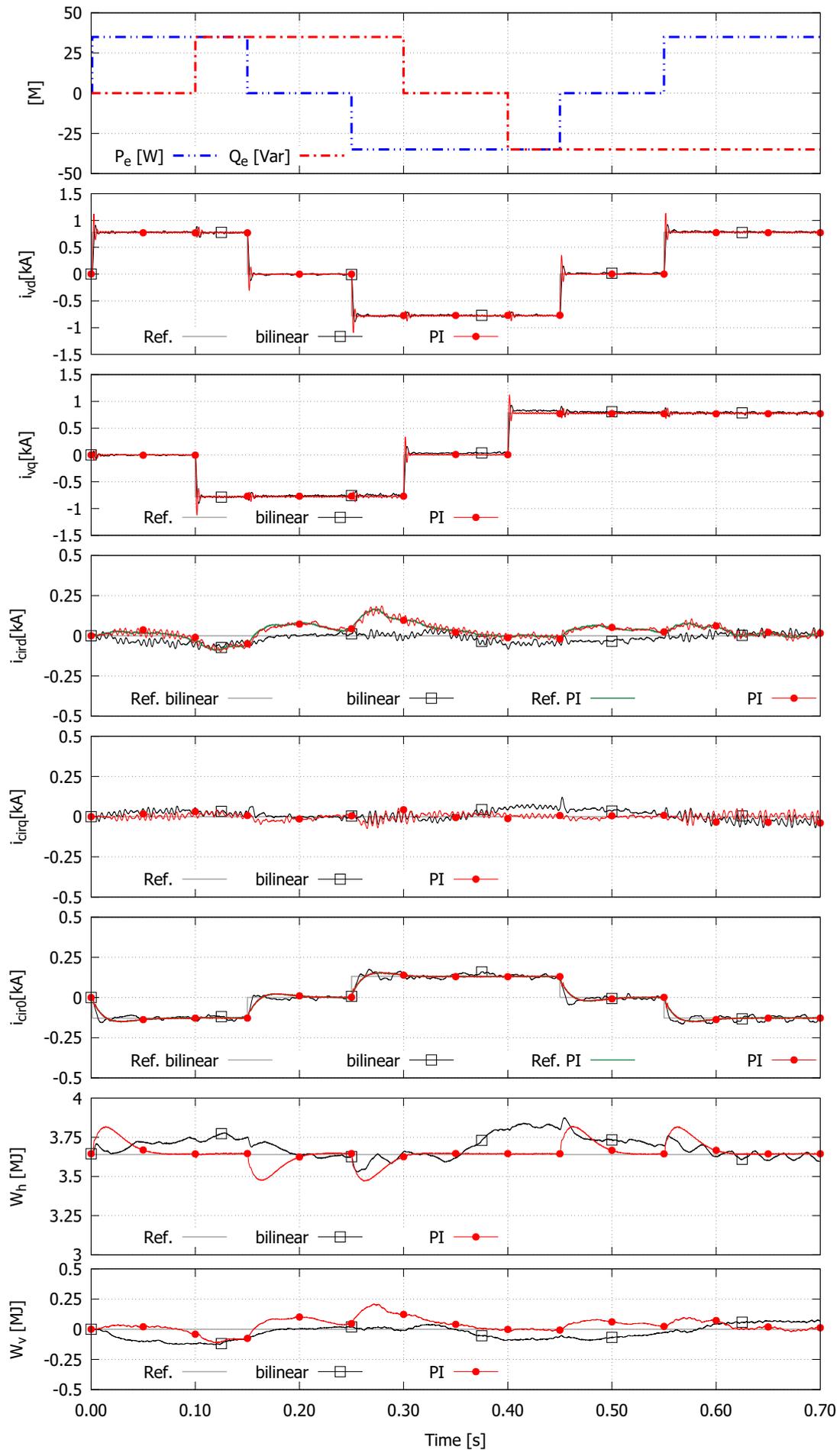


Figure 5.8: A performance comparison between PI and bilinear controller through four-quadrants operation.

Source: Author

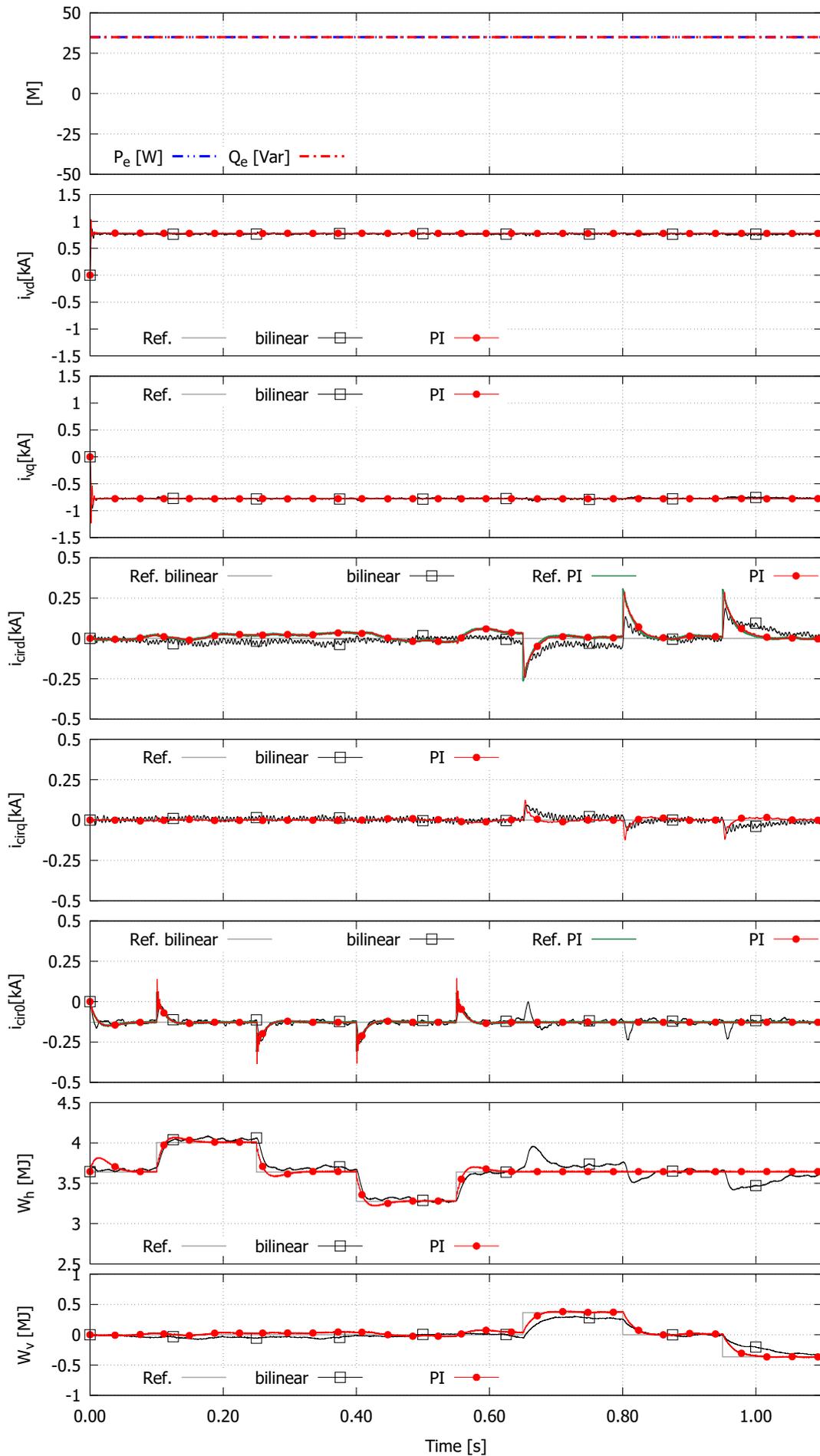


Figure 5.9: A performance comparison between PI and bilinear controller through energy change.

Source: Author

5.2 Robustness over parameters' uncertainties and voltage fluctuation for medium-voltage system with bilinear controller

This section analyses the sensitivity of the bilinear controller over parameter uncertainties. A set of scenarios are created, where parameter uncertainties are considered. For each scenario, one parameter (R , R_c , L , L_c or C_{SM}) assume $\pm 10\%$ or $\pm 20\%$ from their nominal values. Meanwhile, the bilinear controller is computed using the parameters' nominal values. At $t = 0.01$ s the operating point is changed.

In the scenarios with uncertainties in arm resistance (R), bilinear controls well the MMC state variables. In comparison with PI and nonlinear controllers, the bilinear deal with a slower convergence response for total energy W_h , see figure 5.10. Furthermore, in figure 5.11 the bilinear performance is analysed for uncertainties in R_c . Bilinear has suitable performance, similar to PI and nonlinear.

Figure 5.12 and 5.13 consider uncertainties in arm inductance L and AC side inductance L_c . This result in i_{vd} with stationary error; meanwhile, i_{vq} is perfectly driven to its reference for all proposed scenarios. This result differs from PI and nonlinear. Another set of gains was chosen to deal with the stationary error problem, where $\alpha_{1,\dots,4} = 1.5$.

Figure 5.14 and figure 5.15 present state variables i_{vd} and i_{vq} through the robustness test with bilinear controller using a larger gain $\alpha_{1,\dots,4}$. A further investigation needs to be accomplished to improve the total energy W_h response. The state variable W_h is directly linked with gains of Γ and Q . However, a larger Γ and Q result in a high coupling response between state variables. This will be further investigated in futures researches.

For C uncertainties, bilinear achieved similar result of PI (section 3.4.2) and nonlinear (section 4.5.1). The state variables are presented in figure 5.16.

The previous analyses can ensure that the bilinear controller appropriately manages state variables to their desired value. Furthermore, the gains play a crucial role in the bilinear controller performance.

Finally, bilinear performs well face to AC voltage fluctuation, and DC voltage fluctuation. Simulations illustrate the control performance for higher and lower values of nominal voltage in the system's buses.

Figure 5.17 presents state variables with fluctuation in AC voltage. There is a time-varying response during transitory, with a fast convergence to the desired value; Figure 5.18 presents state variables for fluctuation in DC voltage. Bilinear presents similar performance to PI and nonlinear.

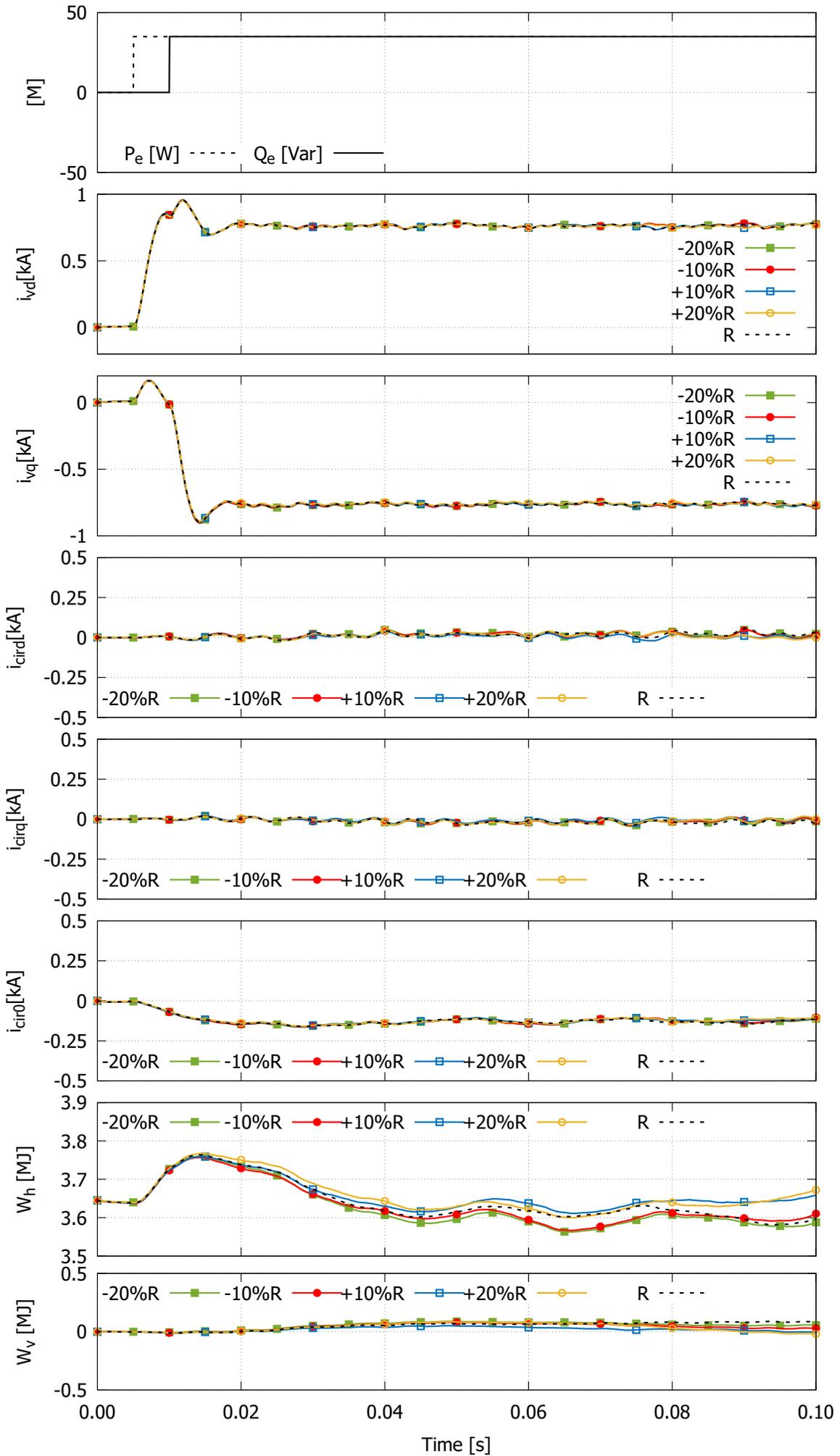


Figure 5.10: The system state over variation of parameter R with bilinear controller. Source: Author

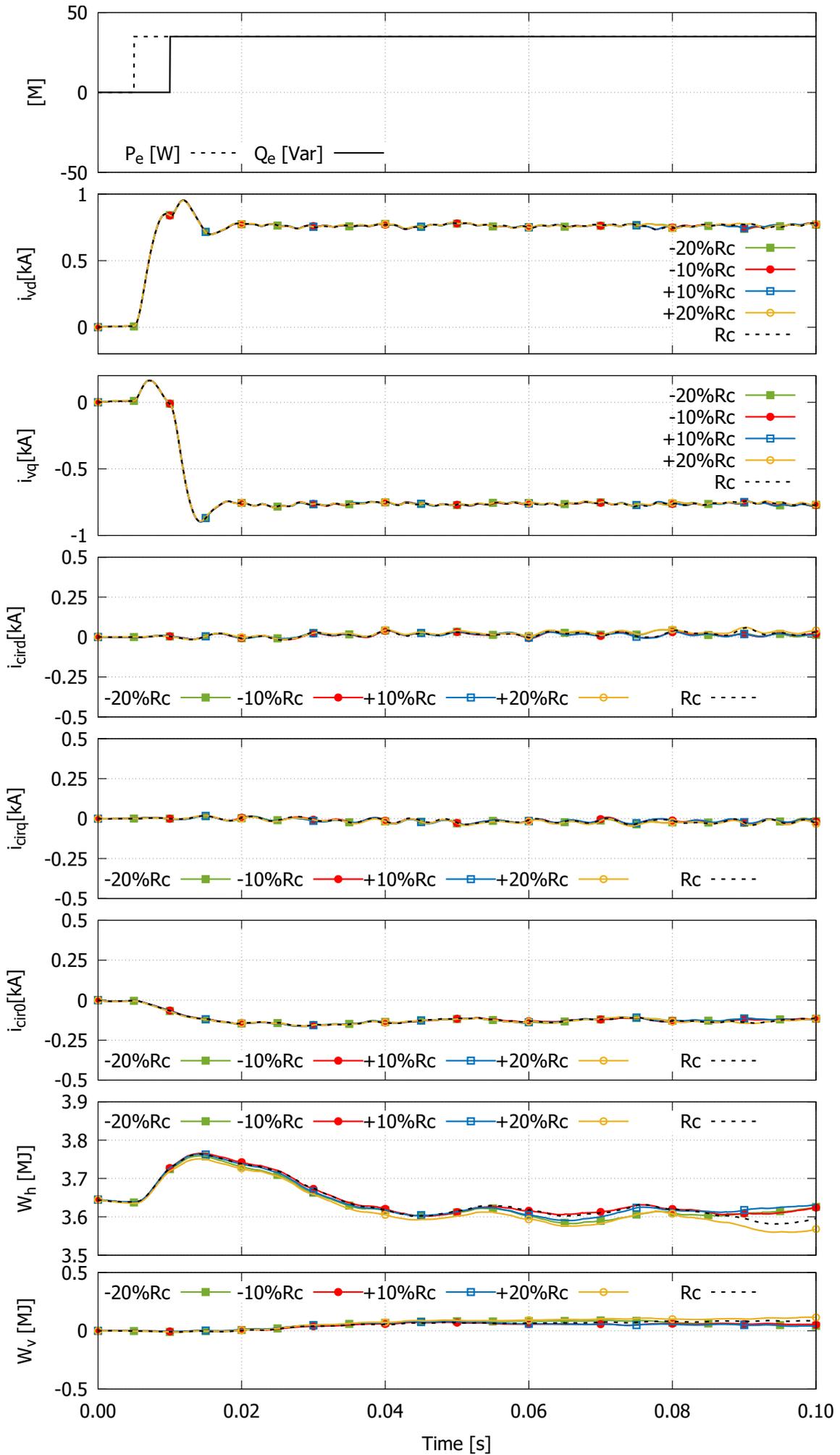


Figure 5.11: States over variation of parameter R_c with bilinear controller.

Source: Author

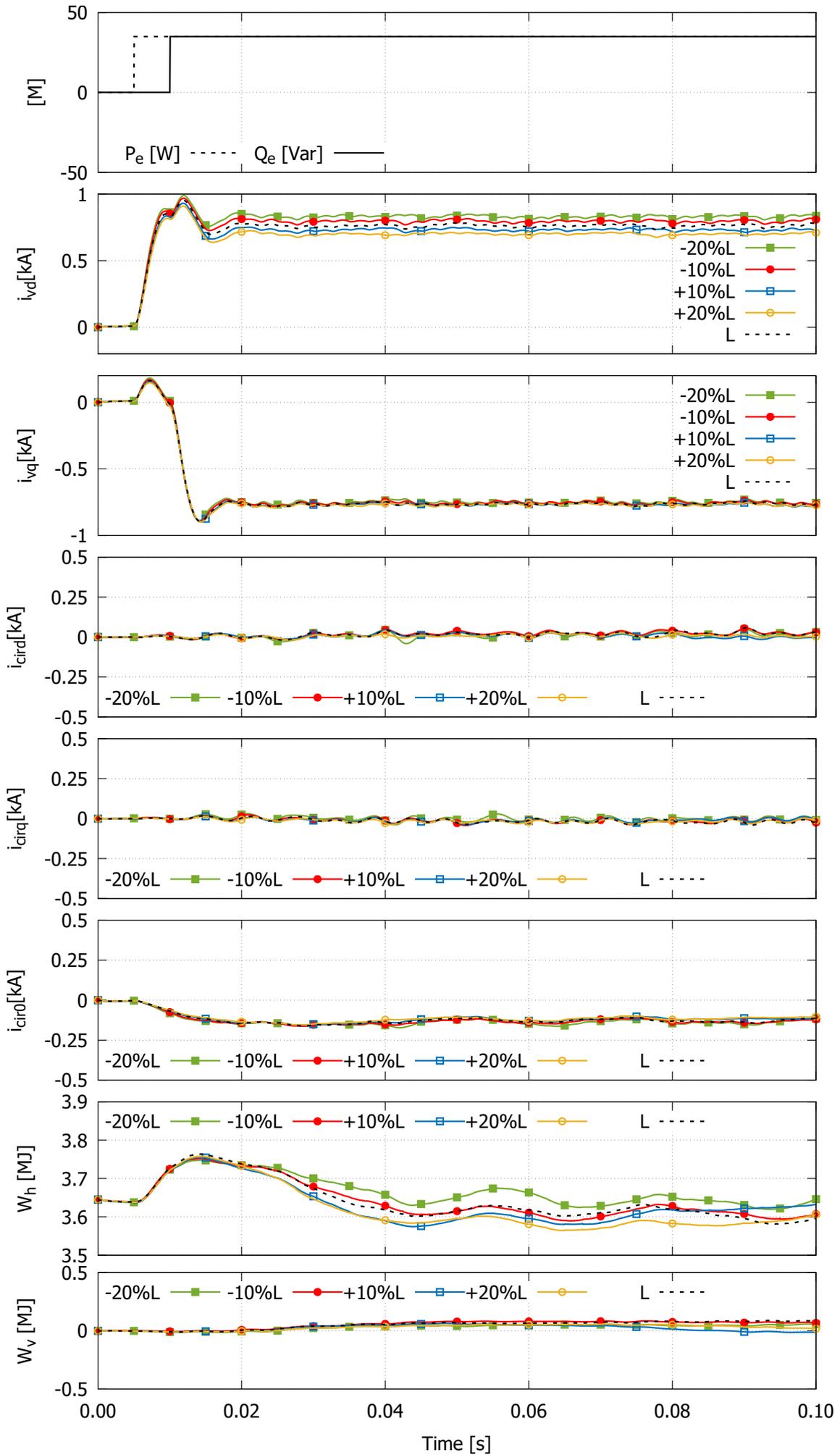


Figure 5.12: States over variation of parameter L with bilinear controller.

Source: Author

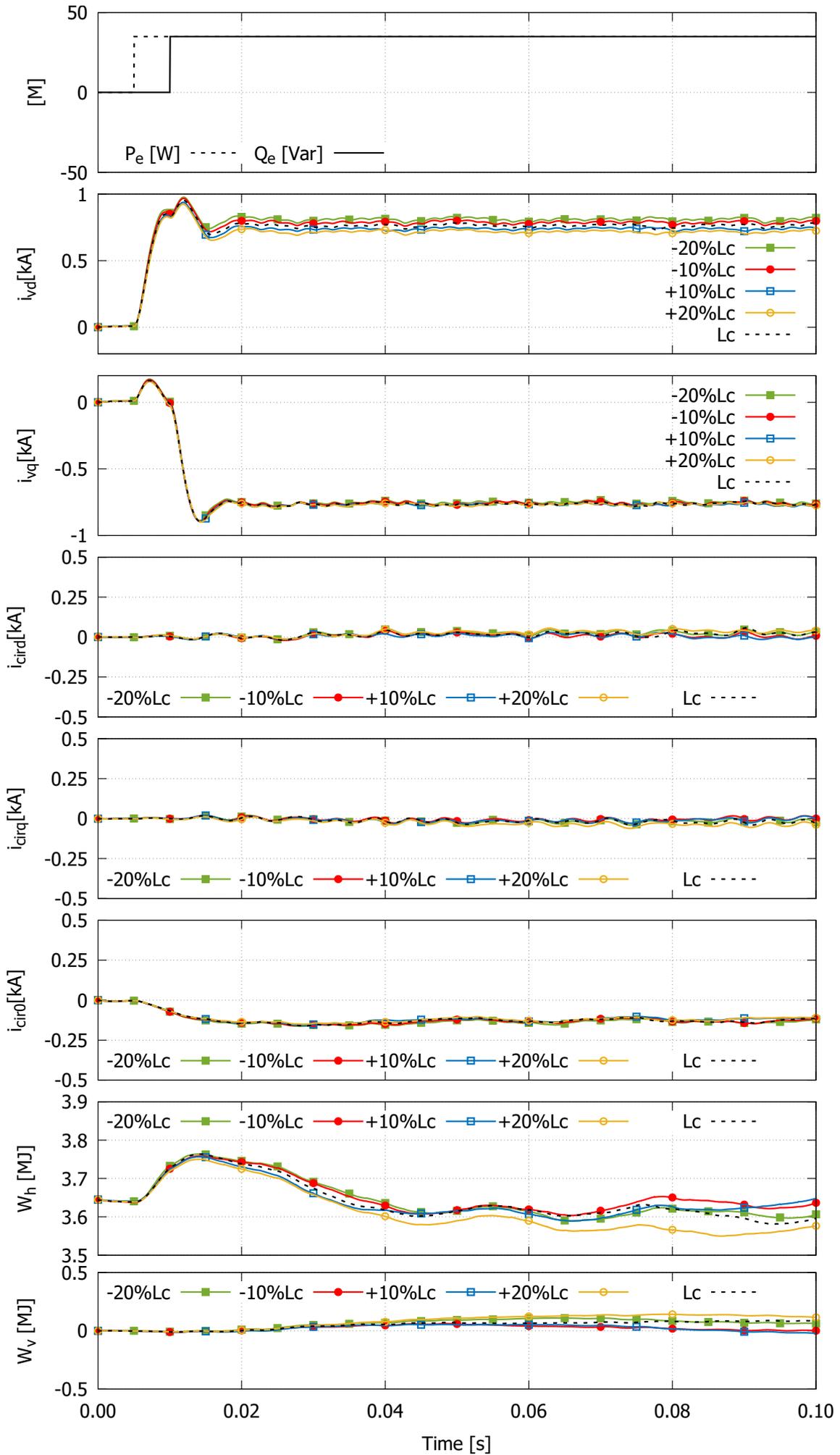


Figure 5.13: States over variation of parameter L_c with bilinear controller.

Source: Author

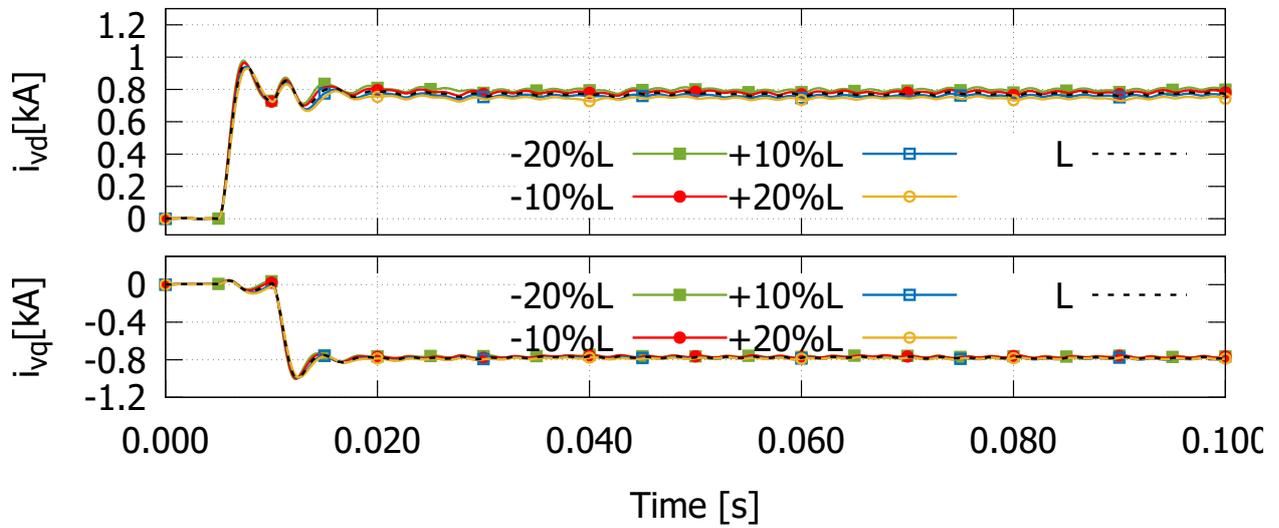


Figure 5.14: Bilinear robustness over uncertainties in L with a larger gain.

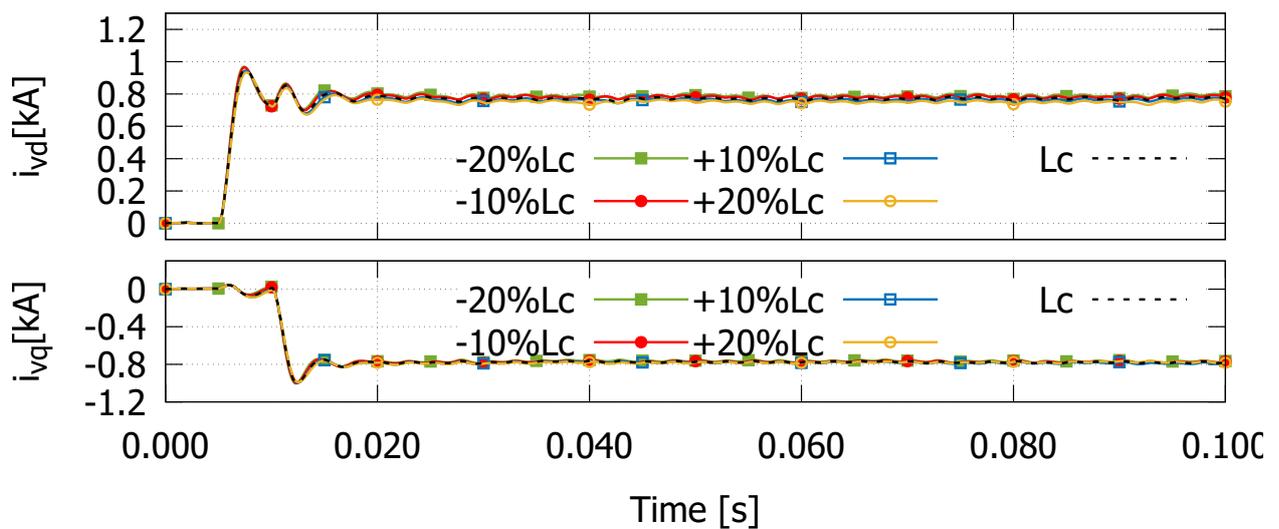


Figure 5.15: Bilinear robustness over uncertainties in L_c with a larger gain.

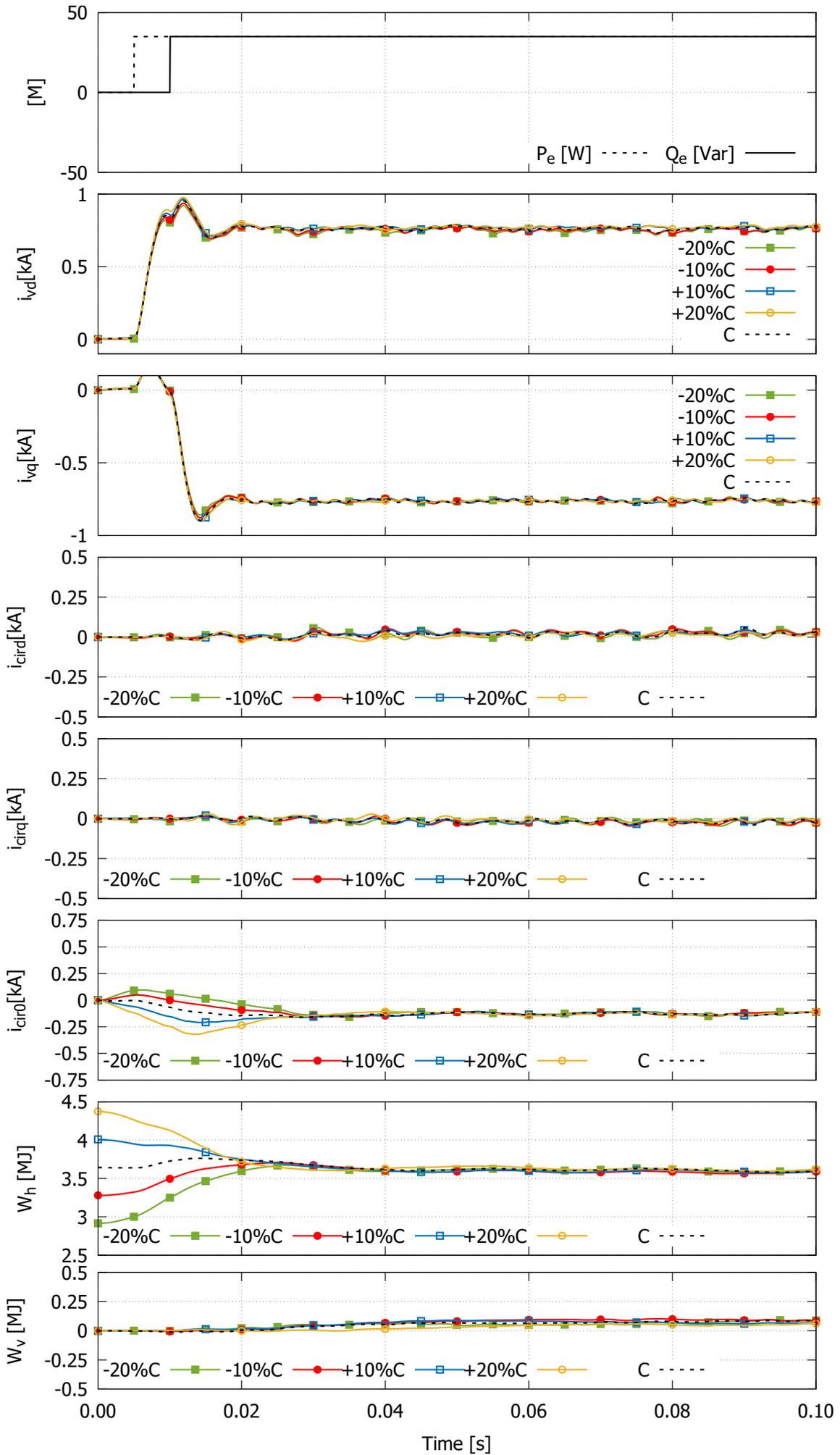


Figure 5.16: States over variation of parameter C with bilinear controller.

Source: Author

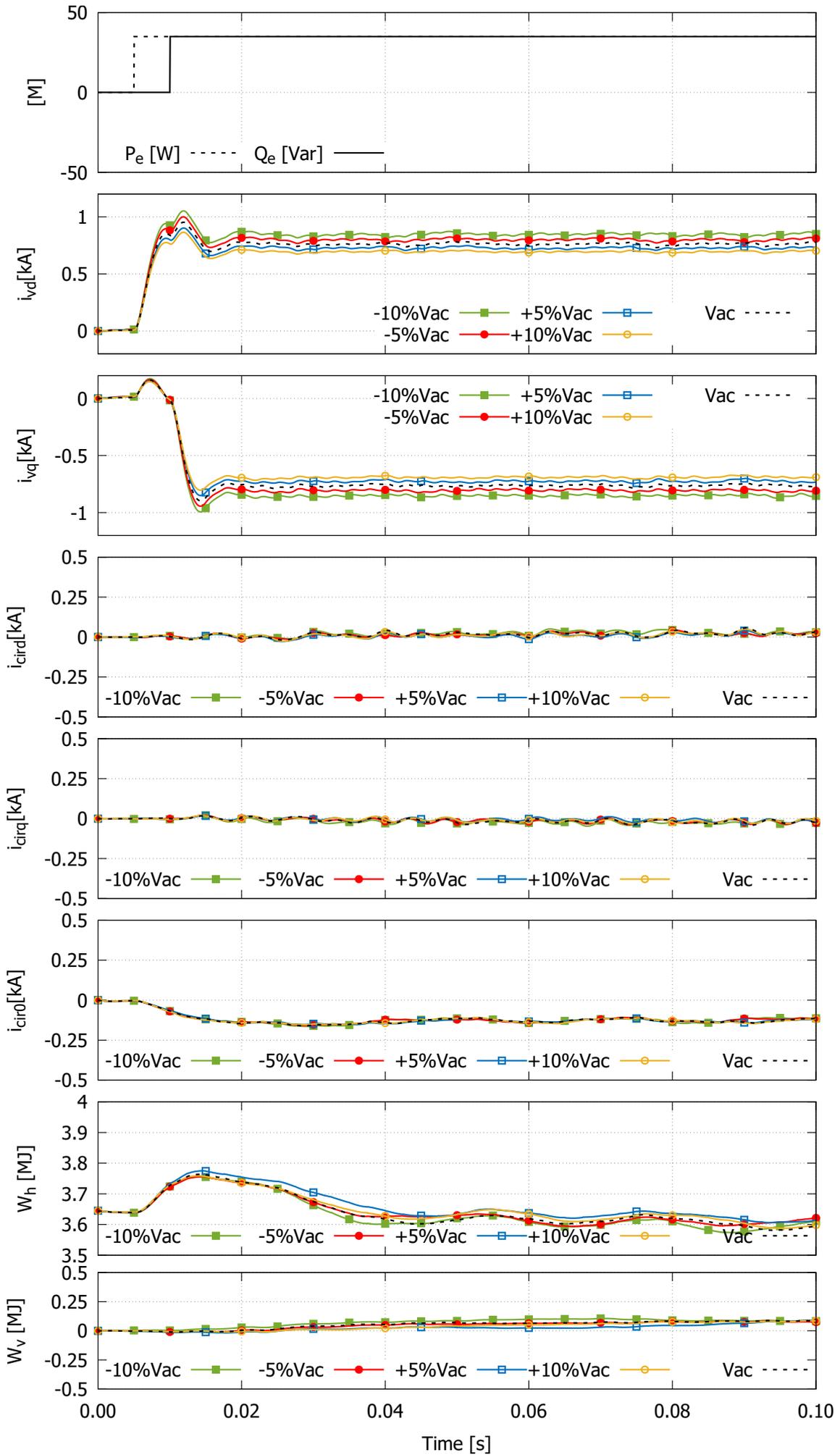


Figure 5.17: Fluctuation of AC voltage with bilinear controller.

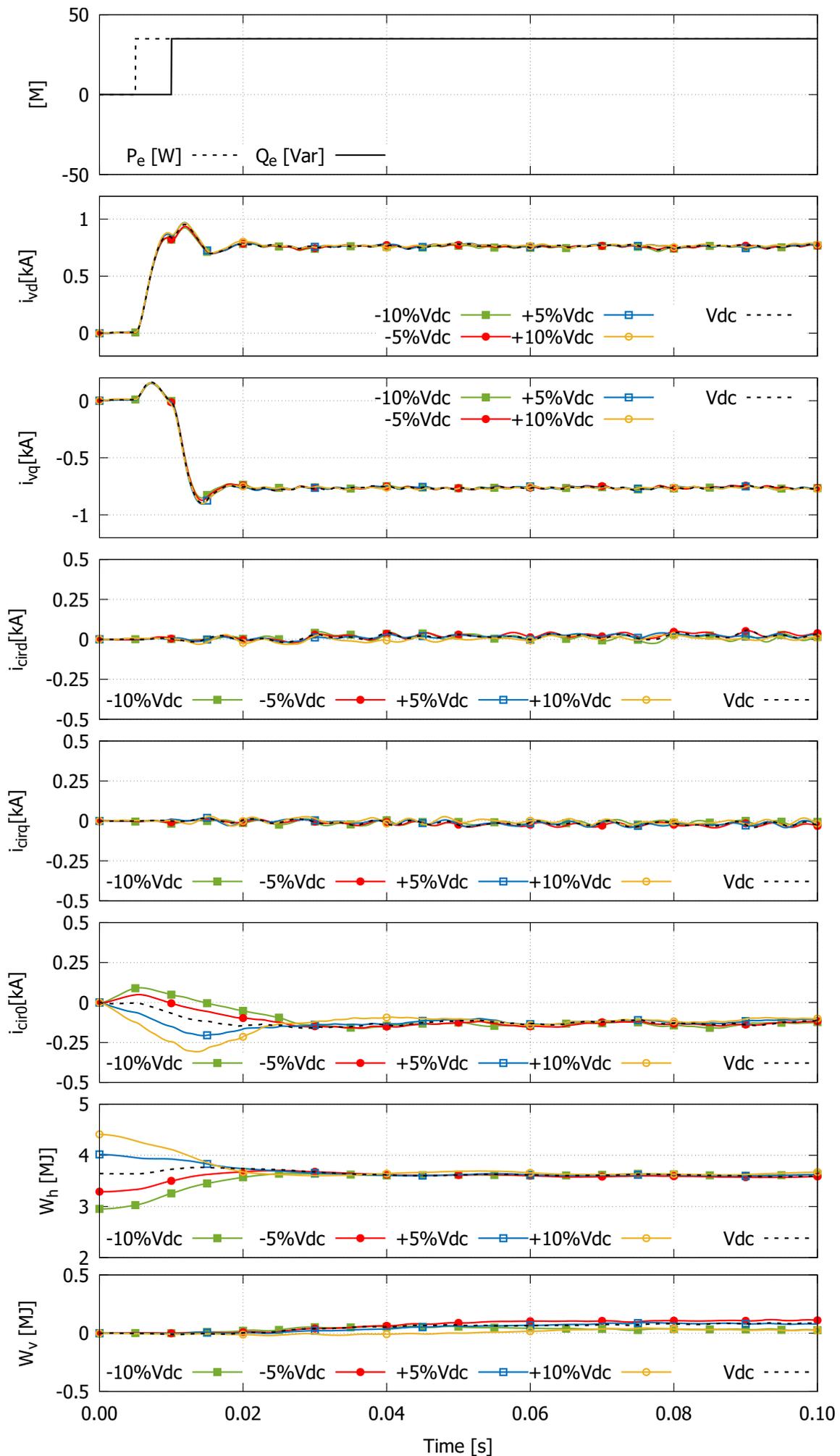


Figure 5.18: Fluctuation of DC voltage with bilinear controller.

5.3 Chapter conclusions

This chapter presented a control algorithm design for MMC converters. An extensive set of operating points are evaluated. Additionally, changes in converter energy are performed. Furthermore, the performance comparison with the PI controller is proposed, where bilinear has a similar performance.

The results include a formal mathematical proof of stability, first for a class of bilinear systems, and then its application for the MMC converter, allowing to stabilize it in a large operating region than linear controllers.

Furthermore, the proposed control strategy allows for the stabilization of all converter's state variables by a single control law.

Control's robustness over parameter uncertainties is accomplished, and bilinear performs well face to uncertainties. However, it is essential to highlight that the gain adjustment needs to consider the uncertainties to be adequately tuned.

Finally, the full state vector using the bilinear controller reaches its desired value for the four-quadrant operation. Additionally, it was accomplished changes in total energy and energy balancing.

Chapter 6

General Conclusion

The electrical grids are becoming more complex worldwide because of a diversity of power generation, more interconnected systems, and an intense energy market. The power generation which comes from renewable increases the number of weak bars in the system. A high number of weak buses can increase the risk of experiencing stability loss. In this way, the demand for ancillary services is growing, for example, increasing the need for systems with synthetic inertia. A solution might be the incorporate to power electronics devices for additional features through the control system. However, in the field of HVDC converters', control for supporting the transmission system's overall stability has yet much to be done. This is an essential issue in electrical grid planning, especially with the huge penetration of renewable connected to the main grid through HVDC. Therefore, this thesis delivers results that contribute to the field of control of MMC converters, that could allow further ancillary services.

Chapter 1 explains the current electrical grid features, as a result of the more interconnected system and the increase of renewable power production. Additionally, it introduces background about power electronics' development and an overview of the technical features attained by each kind of switching device. The chapter points out the last achievement in this field, as the upgrade of the VSC that produces the MMC. That upgrade brings advantages like scalability and lowers switching frequency at devices, in comparison with the VSC. Finally, a short control overview highlights the drawbacks of the MMCs controller and justify the thesis development.

Chapter 2 goes through the technical aspects of the MMC converter. This chapter also includes an overview of modeling and indicates the compromises on simulation speed while using full order models or reduced order models. Furthermore, the detailed overview in control design for MMC is presented, where the achievements obtained by developed nonlinear controllers are emphasized.

Chapter 3 shows the design of a linear control which is used for comparison purposes. The two tests systems are presented, one in medium-voltage and other in high-voltage. Moreover, a comparison between average-model and switching-model using the PI controller is performed. This comparison proves the faithfulness between models for the MMC state variables. Then a high-voltage system is simulated through switching-model and the internal dynamics are analysed. From the internal dynamics, the upper and lower energy balancing is fast accomplished after transients. In spite of this fact, the fact that the controller does not allow to directly control the energy per arms, this is achieved in 400 ms . Finally, the capacitors voltage balancing is well achieved by the implemented sorting algorithm.

Chapter 4 presents a nonlinear controller for an MMC converter applied for HVDC transmission purposes. The control strategy is designed to control not only

the alternating and circulating currents, but also the converter's stored energy and energy balance. Lyapunov theory is the base to develop the nonlinear control presented in this research, where a rigorous stability analysis is performed to assure proper operation of the grid.

The proposed control performance is tested in average model and in a detailed switching MMC model on the Matlab Simscape Electrical platform. For the proposed control, it is noteworthy that gains are based on the desired state's performances and are straightforward to tune. PI and nonlinear controls have similar performances. Moreover, the nonlinear controller has suitable behavior considering a vast region of operation for the MMC restricted by the system's physical limitations.

Robustness over parameters uncertainties are analysed. For changes in R , R_c , L and L_c the control drive state variables to their desired values in steady-state. However the increase on SM capacitors' value C , dq components of circulating current (i_{circdq}) and consequently energy balancing W_v present an oscillatory response.

DC and AC voltages fluctuation affect the speed of convergence for system's state. Meanwhile circulating current has large oscillation when V_{ac} increases, and also oscillates for changes in V_{dc} .

Simulations show that the nonlinear controller presents appropriate performance, with small overshoot in transients. The nonlinear control successfully drives the controlled variables to their references, as well as the energy states. The latter being free-dynamics are controlled by the designed virtual inputs.

Chapter 5 presents a bilinear control for an MMC converter, which directly controls AC and circulating currents and MMC energy. A rigorous mathematical proof is given for its stability, which is based on Lyapunov's theory. This result provides asymptotically stabilization for the three-phases MMC, and the use of a Lyapunov function implies in formal verification of stability and a specific region of attraction for the considered model. Moreover, tuning guidelines are also presented, considering the trade-off between speed of response, coupling effect, and control effort. A sensitivity analysis is also shown. It presents strong robustness properties for realistic parameter's errors.

The bilinear control technique is simulated using an average-model and a switching-model in Simscape Electrical environment. The theoretical and simulation results show that the proposed controller is suitable for the MMC requirements as time response and overshoot, and allows a useful trade-off between power and energy control in the converter. Furthermore, the bilinear control's energy management opens the path to new ancillary services for grid support, for both AC and DC grids, as fast as frequency response or synthetic inertia.

The bilinear control presents rigorous stability proof, and has a well established operating region. In simulations, bilinear control performs well.

Finally, the proposed controllers, nonlinear and bilinear, stabilize well the MMC state variables. Additionally, nonlinear implementation is simple once the relation between the performance of state variables and gains is clear. However, Bilinear has a straightforward solution by a single control law.

6.1 Main Results

- Two nonlinear control algorithms, based on a bilinear mathematical model, are designed for MMC converters;

- These algorithms are able to control AC and DC power flows, total converter's energy and converter energy's balancing at the switching MMC model;
- There are formal stability analysis by Lyapunov theory for both controllers;
- Once the proposed controls are not based on a linearized model, a vast operation region is reachable;
- For the bilinear, compared to other control techniques for MMCs, the proposed control strategy allows stabilizing all converter's state variables by a single control law. The fact that there is a single control law makes the controller much easier to tune than the industry's standard cascaded PI controllers.

6.2 Perspectives for future research

At this point, the thesis met some challenges related to the converter energy controller, and the future topics to be addressed are:

- To use the control in an MTDC grid, also controlling V_{DC} ;
- To expand to an MTDC grid fully controlled by bilinear;
- To use MMC control as a fault detector and protection;
- For certain MTDC operating points, it will be defined the distance until the voltage collapses in each bar;
- To use the SM energy storage to provide ancillary services, such as inertial, frequency and voltage support for the grid.

6.3 Publication

Main publication

- **Oliveira G.C.**, Damm G., Monaro R.M., Luís F. N. Lourenço, Carrizosa M.J., Françoise Lamnabhi-Lagarrigue *Nonlinear Control for Modular Multilevel Converters with Enhanced Stability Region and Arbitrary Closed Loop Dynamics*. International Journal of Electrical Power & Energy Systems. *October, 2020*

Other publications

- Prezotto G.C., Suzuki N.Y., **Oliveira G.C.**, Monaro R.M., Di Santo S.G. *Simulação de um Disjuntor de Corrente Contínua para Aplicações em Alta Tensão*. 12th Latin-American Congress on Electricity Generation and Transmission, Mar del Plata - Argentina, 2017

- Suzuki N.Y., Lacerda V.A., **Oliveira G.C.**, Monaro R.M., Coury D.V. *Comparação de Métodos para Seleção de Parâmetros de Conversores Modulares Multiníveis*. 12th Latin-American Congress on Electricity Generation and Transmission, Mar del Plata - Argentina, 2017
- Suzuki N.Y., Monaro R.M., **Oliveira G.C.**, Di Santo S.G. *Desenvolvimento de um Sistema Microcontrolado para Controle de um Conversor de um Sistema HVDC*. Simpósio Brasileiro de Sistemas Elétricos, Natal- RN - Brazil, 2016
- Funabashi V., Monaro R.M., **Oliveira G.C.**, Di Santo S.G. *Sistema Microcontrolado para o Controle em Tempo Real do Ângulo de Ataque das Pás de Turbinas Eólicas*. Simpósio Brasileiro de Sistemas Elétricos, Natal - RN - Brazil, 2016

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Appendix A

Introduction en Français

A.1 Contrôle des convertisseurs modulaires à plusieurs niveaux

Le contrôle de MMC présente des défis supplémentaires par rapport à la topologie d'autres convertisseurs. La méthode de contrôle doit faire face à :

- En externe, la gestion du flux de puissance active et réactive, ainsi que les tensions AC et DC;
- En interne, la gestion de la dynamique du convertisseur comme les courants de circulation, la tension du condensateur SM, l'équilibrage des demi-bras, l'équilibrage de phase et le contrôle de l'énergie du convertisseur.

MMCs ont également une technique de modélisation complexe en raison du nombre élevé de Submodule (SM), qui nécessite un contrôle simultané pour atteindre l'équilibrage de la tension du condensateur. Il existe de nombreuses approches de modélisation MMC et les modèles affectent directement la conception des commandes. Dans cette thèse, un modèle mathématique basé sur le demi-bras moyen est utilisé pour développer les contrôleurs, et un modèle de commutation est utilisé pour vérifier les performances des contrôles. Concernant le modèle moyen, il existe de nombreuses approches dans la littérature. Dans [25], le modèle moyen considère un modèle de fonction de commutation qui inclut avec précision la dynamique des condensateurs de chaque SM.

De plus, dans [26], il existe un modèle continu où les demi-bras sont représentés par la fonction de sources de tension variables. Cependant, un modèle moyen plus complexe augmentera l'ordre du système, donc la complexité de la solution proposée. De cette façon, le modèle moyen utilisé dans cette recherche est basé sur [27], qui utilise une tension SM équivalente, par demi-bras.

Un modèle de commutation est simulé à l'aide du contrôleur proposé pour vérifier les performances du contrôle. Le modèle de commutation a un contrôleur de bas niveau, qui atteint correctement l'équilibrage de tension des SM. L'algorithme de tri implémenté dans le contrôle de bas niveau est basé sur la technique standard proposée par [24].

Concernant le contrôle, la plupart des résultats existants sur la stratégie de contrôle pour MMCs consistent en des contrôleurs linéaires, en tant que contrôle vectoriel. Ainsi, un seul point de fonctionnement est pris en compte dans sa conception puisque les non-linéarités du système sont ignorées [28, 29, 30].

De ce point de vue-là, on peut citer des travaux comme [31], où le modèle non linéaire MMC est d'abord linéarisé, puis des contrôleurs linéaires sont conçus pour cela. D'une manière différente, [27] propose un modèle bilinéaire en temps discret d'une MMC, contrôlé par une méthode de décomposition en somme des carrés, suite à une analyse non linéaire.

Ces études sont motivées par la pertinence de concevoir des contrôleurs non linéaires qui peuvent assurer la stabilité dans les grandes régions d'exploitation du réseau électrique, y compris une analyse de stabilité rigoureuse [32, 33]. Le chapitre suivant abordera plus en détail la modélisation et le contrôle de MMC.

A.2 Objectif principal de la thèse

L'objectif principal de cette thèse est de développer une méthode de contrôle MMC adaptée pour assurer la stabilité de l'état du système, en particulier les courants de circulation et l'énergie stockée par le convertisseur.

Objectifs spécifiques Les objectifs spécifiques suivants doivent être atteints:

- Développer une méthode de contrôle capable de minimiser les courants de circulation et l'énergie stockée par le convertisseur pour un convertisseur MMC;
- Prouver la stabilisation du système;
- Évaluer la robustesse du contrôle pour la variation des paramètres du convertisseur;
- Évaluer les impacts des gains de contrôle sur la dynamique du convertisseur.

A.3 Principales contributions

Les principales contributions de cette thèse sont de présenter deux nouveaux contrôleurs non linéaires appliqués à la MMC. Les techniques proposées permettent de contrôler les tensions AC et DC, les courants de circulation et l'énergie totale et d'équilibrage du convertisseur. Des preuves mathématiques sont présentées pour sa stabilité, qui est basée sur la théorie de Lyapunov. Ces contrôleurs fournissent une stabilisation asymptotique pour les triphasés MMC.

A.4 Conclusion générale

Les réseaux électriques sont de plus en plus complexes dans le monde en raison d'une diversité de production d'électricité, de systèmes plus interconnectés et d'un marché de l'énergie intense. La production d'électricité d'origine renouvelable augmente le nombre de barres faibles dans le système. Un nombre élevé de bus faibles peut augmenter le risque de perte de stabilité. De cette manière, la demande de services auxiliaires augmente, par exemple, augmentant le besoin de systèmes à inertie synthétique. Une solution pourrait être l'incorporation pour alimenter les appareils électroniques pour des fonctionnalités supplémentaires via le système de contrôle. Cependant, dans le domaine des convertisseurs HVDC, il reste encore beaucoup à faire pour contrôler la stabilité globale du système de transmission. C'est une question essentielle dans la planification du réseau électrique, en particulier avec l'énorme pénétration des énergies renouvelables connectées au réseau principal via HVDC. Par conséquent, cette thèse fournit des résultats qui contribuent au domaine du contrôle des convertisseurs ac MMC, ce qui pourrait permettre d'autres services auxiliaires.

Le chapitre 1 explique les caractéristiques actuelles du réseau électrique, en raison du système plus interconnecté et de l'augmentation de la production d'énergie renouvelable. De plus, il présente le contexte du développement de l'électronique de puissance et un aperçu des caractéristiques techniques atteintes par chaque type de dispositif de commutation. Le chapitre souligne la dernière réalisation dans ce domaine, comme la mise à niveau du VSC qui produit le MMC. Cette mise à niveau apporte des avantages tels que l'évolutivité et abaisse la fréquence de commutation au niveau des appareils, par rapport au VSC. Enfin, un bref aperçu du contrôle met en évidence les inconvénients du contrôleur MMCs et justifie le développement de la thèse.

Le chapitre 2 passe en revue les aspects techniques du convertisseur MMC. Ce chapitre comprend également un aperçu de la modélisation et indique les compromis sur la vitesse de simulation lors de l'utilisation de modèles d'ordre complet ou de modèles d'ordre réduit. En outre, la vue d'ensemble détaillée de la conception de commande pour MMC est présentée, où les réalisations obtenues par les contrôleurs non linéaires développés sont soulignées.

Le chapitre 3 montre la conception d'un contrôle linéaire qui est utilisé à des fins de comparaison. Les deux systèmes d'essais sont présentés, l'un en moyenne tension et l'autre en haute tension. De plus, une comparaison entre le modèle moyen et le modèle de commutation à l'aide du contrôleur PI est effectuée. Cette comparaison prouve la fidélité entre les modèles pour les variables d'état MMC. Ensuite, un système haute tension est simulé par un modèle de commutation et la dynamique interne est analysée. A partir de la dynamique interne, l'équilibrage d'énergie supérieur et inférieur est rapidement réalisé après les transitoires. Malgré ce fait, le fait que le contrôleur ne permet pas de contrôler directement l'énergie par demi-bras, ceci est réalisé en 400 ms. Enfin, l'équilibrage de tension des condensateurs est bien réalisé par l'algorithme de tri mis en œuvre.

Le chapitre 4 présente un contrôleur non linéaire pour un convertisseur MMC appliqué à des fins de transmission HVDC. La stratégie de contrôle est conçue pour contrôler non seulement les courants alternatifs et circulants, mais également l'énergie stockée et l'équilibre énergétique du convertisseur. La théorie de Lyapunov est la base pour développer le contrôle non linéaire présenté dans cette recherche, où une analyse de stabilité rigoureuse est effectuée pour assurer le bon fonctionnement de la grille.

Les performances de commande proposées sont testées dans un modèle moyen et dans un modèle MMC de commutation détaillé sur la plate-forme Matlab Simscape Electrical. Pour le contrôle proposé, il est à noter que les gains sont basés sur les performances de l'état souhaité et sont simples à régler. Les contrôles PI et non linéaires ont des performances similaires. De plus, le contrôleur non linéaire a un comportement approprié compte tenu d'une vaste région de fonctionnement pour la MMC limitée par les limitations physiques du système.

Les incertitudes de robustesse sur les paramètres sont analysées. Pour les changements dans R , R_c , L et L_c , les variables d'état du variateur de commande à leurs valeurs souhaitées à l'état fixe. Cependant, l'augmentation de la valeur des condensateurs SM C , les composantes dq du courant de circulation (i_{circdq}) et par conséquent l'équilibrage d'énergie W_v présentent une réponse oscillatoire.

Les fluctuations des tensions DC et AC affectent la vitesse de convergence de l'état du système. Pendant ce temps, le courant de circulation a une grande oscillation lorsque V_{ac} augmente, et oscille également pour les changements de V_{dc} .

Les simulations montrent que le contrôleur non linéaire présente des performances appropriées, avec un faible sur-signal dans les transitoires. Le contrôle

non linéaire pilote avec succès les variables contrôlées vers leurs références, ainsi que les états d'énergie. Ces derniers étant à dynamique libre, ils sont contrôlés par les entrées virtuelles conçues.

Le chapitre 5 présente un contrôle bilinéaire pour un convertisseur MMC, qui contrôle directement les courants alternatifs et circulants et l'énergie MMC. Une preuve mathématique rigoureuse est donnée pour sa stabilité, qui est basée sur la théorie de Lyapunov. Ce résultat fournit une stabilisation asymptotique pour les trois phases MMC, et l'utilisation d'une fonction de Lyapunov implique une vérification formelle de la stabilité et d'une région d'attraction spécifique pour le modèle considéré. De plus, des directives de réglage sont également présentées, en tenant compte du compromis entre la vitesse de réponse, l'effet de couplage et l'effort de contrôle. Une analyse de sensibilité est également présentée. Il présente de fortes propriétés de robustesse pour les erreurs de paramètres réalistes.

La technique de contrôle bilinéaire est simulée à l'aide d'un modèle moyen et d'un modèle de commutation dans l'environnement Simscape Electrical. Les résultats théoriques et de simulation montrent que le contrôleur proposé est adapté aux exigences MMC comme temps de réponse et de dépassement, et permet un compromis utile entre la commande de puissance et d'énergie dans le convertisseur. En outre, la gestion de l'énergie de la commande bilinéaire ouvre la voie à de nouveaux services auxiliaires pour la prise en charge du réseau, aussi bien pour les réseaux AC que DC, aussi vite que la réponse en fréquence ou l'inertie synthétique.

Le contrôle bilinéaire présente une preuve de stabilité rigoureuse et possède une zone de fonctionnement bien établie. Dans les simulations, le contrôle bilinéaire fonctionne bien.

Enfin, les contrôleurs proposés, non linéaires et bilinéaires, stabilisent bien les variables d'état MMC. De plus, l'implémentation non linéaire est simple une fois que la relation entre les performances des variables d'état et les gains est claire. Cependant, Bilinear a une solution simple par une loi de contrôle unique.

A.4.1 Résultats principaux

- Deux algorithmes de contrôle non linéaires, basés sur un modèle mathématique bilinéaire, sont conçus pour les convertisseurs MMC;
- Ces algorithmes sont capables de contrôler les flux d'alimentation CA et CC, l'énergie totale du convertisseur et l'équilibrage de l'énergie du convertisseur au modèle MMC de commutation;
- Il existe une analyse de stabilité formelle par la théorie de Lyapunov pour les deux contrôleurs;
- Une fois que les contrôles proposés ne sont pas basés sur un modèle linéarisé, une vaste zone d'opération est accessible;
- Pour le bilinéaire, par rapport aux autres techniques de contrôle des MMC, la stratégie de contrôle proposée permet de stabiliser toutes les variables d'état du convertisseur par une seule loi de contrôle. Le fait qu'il existe une

loi de contrôle unique rend le contrôleur beaucoup plus facile à régler que les contrôleurs PI en cascade standard de l'industrie.

A.4.2 Perspectives pour les recherches futures

À ce stade, la thèse a relevé certains défis liés au contrôleur d'énergie du convertisseur, et les futurs sujets à aborder sont:

- Utiliser le contrôle dans une grille MTDC, contrôlant également V_{DC} ;
- Étendre à une grille MTDC entièrement contrôlée par bilinéaire;
- Utiliser la commande MMC comme détecteur de défaut et protection;
- Pour certains points de fonctionnement MTDC, il sera défini la distance jusqu'à ce que la tension s'effondre dans chaque barre;
- Utiliser le stockage d'énergie SM pour fournir des services auxiliaires, tels que le support inertiel, de fréquence et de tension pour le réseau.